等用計 雪谷 弘州 1 引登

1. (1) 
$$L(\lambda;y) = f(y;\lambda) = \frac{\lambda^4 e^{-\lambda}}{y!}$$

(3) 
$$S(\lambda) = \frac{3}{3\lambda} l(\lambda; y) = \frac{y}{\lambda} - 1$$

(4) 
$$J(\lambda) = -\frac{\partial^2}{\partial \lambda^2} \varrho(\lambda; Y) = \frac{4}{3} / \lambda^2$$

(台) 
$$I(\lambda) = E[J(\lambda)] = \frac{1}{\lambda^2}E(y) = \frac{1}{\lambda}$$

2 (1) 
$$L_n(\lambda; y) = \prod_{i=1}^n f(y_i; \lambda) = \prod_{i=1}^n \frac{\lambda^{y_i} e^{-\lambda}}{y_i!}$$

= 
$$\lambda^{\Sigma yi}e^{-n\lambda}\frac{n}{n}\frac{1}{yi!}$$

(2) 
$$l_n(\lambda; \underline{y}) = \sum y_i \log \lambda - n\lambda + \log \left[ \frac{\hat{\eta}}{3_i}, \frac{\hat{\eta}}{3_i} \right]$$

(3) 
$$S_n(\lambda) = \frac{\sum y_i^2 - n}{\lambda}$$

$$(4) \quad J_n(\lambda) = \frac{\Sigma g_i}{\lambda^2}$$

(b) 
$$I_n(\lambda) = \frac{n}{\lambda}$$

$$(6) \quad \stackrel{\wedge}{\lambda} = \frac{\sum yi}{n}$$

편의는 의하여 6<sup>2</sup>= 도로 들은 원 벡터 면 = (μ, τ)<sup>†</sup> 가고하자

$$L(\theta; y) = \pi (2\pi\tau)^{-1/2} \exp\left\{-\frac{(3i-\mu)^2}{2\tau}\right\}$$

= 
$$[2\pi 7]$$
 exp $[-\frac{1}{2}]$   $[y;-\mu]^2$ 

$$ln(\underline{\theta}:\underline{4}) = -\frac{n}{2}\log(2\pi) - \frac{n}{2}\log \tau - \frac{1}{2\tau}\sum_{i=1}^{N}(y_i - \mu)^2$$

MIZ는 가음의 방정식은 반복하는 
$$\hat{\theta} = (\hat{\mu}, \hat{\tau})^{\dagger}$$
이각.

$$Sn(\theta; \Psi) = \begin{bmatrix} \frac{\partial}{\partial \mu} ln(\theta; \Psi) \\ \frac{\partial}{\partial \tau} ln(\theta; \Psi) \end{bmatrix} \approx 0$$

(a) 
$$\frac{\partial}{\partial z} \ln(0; \underline{y}) = -\frac{n}{2T} + \frac{1}{2T^2} \sum_{z=0}^{2} (y_i - \mu)^2 = 0$$

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$$\hat{\mu} = \frac{\sum y \hat{\epsilon}}{n} = y \qquad \hat{\tau} = \hat{\delta}^2 = \frac{\sum [y \hat{\epsilon} - \hat{y}]^2}{n}$$

$$J_{n}(\underline{\theta}) = \begin{bmatrix} \frac{\partial^{2}}{\partial \mu^{2}} l_{n}(\underline{\theta}) & \frac{\partial^{2}}{\partial \mu^{2}} l_{n}(\underline{\theta}) \\ \frac{\partial^{2}}{\partial \tau^{2}} l_{n}(\underline{\theta}) & \frac{\partial^{2}}{\partial \tau^{2}} l_{n}(\underline{\theta}) \end{bmatrix}$$

$$-2\tau$$

$$\frac{1}{\tau} \sum_{i=1}^{n} \frac{1}{\tau_{i}} \sum_{i=1}^{n} \frac{1}{\tau_{i}} \sum_{i=1}^{n} \frac{1}{\tau_{i}} \sum_{i=1}^{n} \frac{1}{\tau_{i}} \sum_{i=1}^{n} \frac{1}{\tau_{i}} \frac{1}{\tau_{$$

$$I_n(\theta) = E[J_n(\theta)]$$

$$= \left(\begin{array}{cc} \frac{N}{T} & O \\ \hline 0 & -\frac{N}{2T^2} + \frac{N}{T^2} \end{array}\right)$$

$$= \begin{bmatrix} \frac{h}{T} & 0 \\ 0 & \frac{N}{2T^2} \end{bmatrix} \Rightarrow$$

$$J_{n}^{-1}(\theta) = \begin{bmatrix} T/n & 0 \\ 0 & 2T^{2}/n \end{bmatrix}$$

地是 中의 社能。12十三計型

$$\widehat{\theta} = \left[ \widehat{\mathcal{I}}_{1} \right] \sim \mathbb{N} \left( \underline{\theta}_{0}, \underline{\mathsf{I}}_{n}^{-1} (\underline{\theta}_{0}) \right)$$

4. 
$$y_i \sim \text{exp(h)} f(y_i h) = \frac{1}{h} e^{-\frac{h}{2}h}$$

$$ln(\lambda) = -n \log \lambda - \frac{\sum yi}{\lambda}$$

$$S_{nL}\lambda) = -\frac{n}{\lambda} + \frac{\Sigma y_i}{\lambda^2}$$

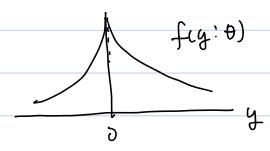
$$J_n(\lambda) = -\frac{n}{\lambda^2} + \frac{2 \sum y_i}{\lambda^3}$$

$$I_{n}(\lambda) = -\frac{n}{\lambda^{2}} + \frac{2n}{\lambda^{2}} = \frac{n}{\lambda^{2}}$$

$$\hat{\lambda} \sim N(\lambda_0, \frac{\lambda_0}{n})$$

5 
$$y_i \stackrel{\text{fid}}{\sim} f(y_i|\theta) = \frac{1}{10} \exp\left(-\frac{y_i}{\theta}\right)$$

f(ylf) 의 학원 번조 합수는 다음과 같다.



하지만 두(일(日) 현 수의 감수인 보면 의원가능한 한수이다.

$$L_n(\theta; y) = (2\theta)^{-n} exp \left(-\frac{1}{\theta} \sum_{i=1}^{n} |y_i|\right)$$

$$ln(\theta) \underline{y} = -n \log_2 - n \log_{\theta} - \frac{1}{\theta} \sum_{i=1}^{n} |y_i|$$

$$S_n(\theta;\underline{q}) = -\frac{h}{\hbar} + \frac{1}{\theta^2} \sum_{i=1}^{n} |y_i|$$

Su(b) y) 는 한국하는 MLE 는

$$\hat{\theta} = \frac{\sum |y|}{n}$$

$$J_{n}(\theta;\underline{y}) = -\frac{\eta}{\theta^{2}} + \frac{2}{\theta^{3}} \sum |y_{i}|$$

$$I_n(\theta)(y) = -\frac{n}{\theta^2} + \frac{2n}{\theta^2} = \frac{n}{\theta^2}$$

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$$= \int_{-\infty}^{\infty} |y| \cdot \frac{1}{2\theta} e^{-\frac{|y|}{\theta}} dy \qquad 2 \qquad \text{with}$$

 $\hat{\theta} \sim N(\theta_0, \frac{\theta_0}{n})$