

In[]:= (*Сложение двух точек эллиптической кривой*)

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EllipticAdd[p_, a_, b_, c_, P_List, Q_List] := Module[{lam, x3, y3, P3},  
  Which[  
    |условный оператор с множественными ветвями  
    P == {0}, Q,  
      |О большое  
    Q == {0}, P,  
      |О большое  
    P[[1]] != Q[[1]],  
      lam = Mod[(Q[[2]] - P[[2]]) PowerMod[Q[[1]] - P[[1]], p - 2, p], p];  
      |остаток от деления |степень по модулю  
      x3 = Mod[lam^2 - a - P[[1]] - Q[[1]], p];  
      |остаток от деления  
      y3 = Mod[-(lam (x3 - P[[1])) + P[[2]]], p];  
      |остаток от деления  
      {x3, y3},  
    (P == Q) & (P[[2]] == 0), {0},  
      |О большое  
    (P == Q) & (P != {0}),  
      |О большое  
      lam = Mod[(3 * P[[1]]^2 + 2 a * P[[1]] + b) PowerMod[2 P[[2]], p - 2, p], p];  
      |остаток от деления |степень по модулю  
      x3 = Mod[lam^2 - a - P[[1]] - Q[[1]], p];  
      |остаток от деления  
      y3 = Mod[-(lam (x3 - P[[1])) + P[[2]]], p];  
      |остаток от деления  
      {x3, y3},  
    (P[[1]] == Q[[1]]) & (P[[2]] != Q[[2]]), {0}  
      |О большое  
  ]  
]
```

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In[ ]:= (*Умножение точки эллиптической кривой на константу*)
EllipticMultSlow[p0_, a0_, b0_, c0_, pointP0_, n0_] := Module[
    {p = p0, a = a0, b = b0, c = c0, pointP = pointP0, n = n0, pointQ = pointP0},
    Do[pointQ = EllipticAdd[p, a, b, c, pointP, pointQ], {i, 2, n}];
    pointQ
]
EllipticMult[p0_, a0_, b0_, c0_, pointP0_, n0_] := Module[
    {pointP = pointP0, n = n0, p = p0, a = a0, b = b0, c = c0, pointQ = {0, 0}, binN},
    binN = IntegerDigits[n, 2];
    Do[
        If[binN[[i]] == 0,
            pointQ = EllipticAdd[p, a, b, c, pointQ, pointQ]
            , pointQ = EllipticAdd[p, a, b, c, EllipticAdd[
                p, a, b, c, pointQ, pointQ
            ], pointP]
        ]
    , {i, 1, Length[binN]}}];
    pointQ
]

In[ ]:= (*Нахождение порядка эллиптической кривой*)
EllipticRank[p0_, a0_, b0_, c0_, pointP0_] := Module[
    {p = p0, a = a0, b = b0, c = c0, pointP = pointP0, pointQ = pointP0, i = 1},
    While[pointQ != {0}, pointQ = EllipticAdd[p, a, b, c, pointP, pointQ];
        i++];
    i
]

```