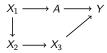
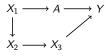
Find adjustment sets that identify the effect of A on Y



Find adjustment sets that identify the effect of A on Y



Find adjustment sets that identify the effect of A on Y

$$X_1 \longrightarrow A \longrightarrow Y$$

$$\downarrow \qquad \qquad \downarrow$$

$$X_2 \longrightarrow X_3$$

We can block the backdoor path in several ways:

▶ Condition on  $X_1$ :  $A \leftarrow \boxed{X_1} \rightarrow X_2 \rightarrow X_3 \rightarrow Y$ 

Find adjustment sets that identify the effect of A on Y

$$X_1 \longrightarrow A \longrightarrow Y$$

$$\downarrow \qquad \qquad \downarrow$$

$$X_2 \longrightarrow X_3$$

- ▶ Condition on  $X_1$ :  $A \leftarrow \boxed{X_1} \rightarrow X_2 \rightarrow X_3 \rightarrow Y$
- ▶ Condition on  $X_2$ :  $A \leftarrow X_1 \rightarrow \boxed{X_2} \rightarrow X_3 \rightarrow Y$

Find adjustment sets that identify the effect of A on Y

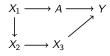
$$X_1 \longrightarrow A \longrightarrow Y$$

$$\downarrow$$

$$X_2 \longrightarrow X_3$$

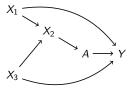
- ▶ Condition on  $X_1$ :  $A \leftarrow X_1 \rightarrow X_2 \rightarrow X_3 \rightarrow Y$
- ▶ Condition on  $X_2$ :  $A \leftarrow X_1 \rightarrow \boxed{X_2} \rightarrow X_3 \rightarrow Y$
- ▶ Condition on  $X_3$ :  $A \leftarrow X_1 \rightarrow X_2 \rightarrow \boxed{X_3} \rightarrow Y$

Find adjustment sets that identify the effect of A on Y

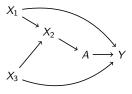


- ► Condition on  $X_1$ :  $A \leftarrow X_1 \rightarrow X_2 \rightarrow X_3 \rightarrow Y$
- ▶ Condition on  $X_2$ :  $A \leftarrow X_1 \rightarrow \boxed{X_2} \rightarrow X_3 \rightarrow Y$
- ▶ Condition on  $X_3$ :  $A \leftarrow X_1 \rightarrow X_2 \rightarrow \boxed{X_3} \rightarrow Y$
- ► Any combination of the above

Find 3 sufficient adjustment sets to identify  $A \to Y$ 

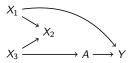


Find 3 sufficient adjustment sets to identify  $A \to Y$ 

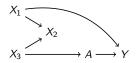


Answer:  $\{X_2\}, \{X_1, X_3\}, \{X_1, X_2, X_3\}$ 

What is the smallest adjustment set that identifies  $A \rightarrow Y$ ?



What is the smallest adjustment set that identifies  $A \rightarrow Y$ ?



Answer: The empty set! Don't condition on anything. The collider  $X_2$  already blocks the path.