Fingerprint Recognition

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Figure 1: Source Image

1. Preprocessing

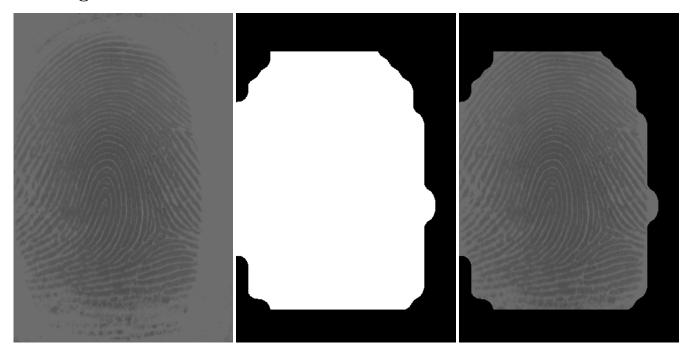
1.1. Normalization



Figure 2: Normalization

$$\begin{split} A(M) &= \frac{\sum M_{ij}}{Size(M)} \\ S &= Std(M) = \sqrt{\frac{\sum ((M_{ij} - A(M))^2)}{Size(M)}} \\ \delta &= \frac{\sqrt{S_0 \times (M_{ij} - A(M))^2}}{S} \\ M_{ij} &= \begin{cases} A_0 - \delta, & \text{if } M_{ij} \geq A(M) \\ A_0 + \delta, & \text{if } M_{ij} < A(M) \end{cases} \end{split}$$

1.2. Segmentation



A block K in image M is background if:

$$Std(K) \leq Std(M) \times {\rm threshold}$$

Dilation, followed by Erosion are performed to unify the blocks.

Then, erosion followed by dilation are performed to exclude insignificant blocks.

1.3. Orientation



(The third image is only used for visualization only. It does not take part in any computing process.) Sobel Operator is used for detect gradient along Ox and Oy.

Then, for each pixel in image, we can calculate the gradient angle:

$$\theta = \tan^{-1} \frac{|\overrightarrow{Gx}|}{|\overrightarrow{Gy}|}$$

Then we can calculate the gradient angle for each block.

1.4. Ridges' Frequency

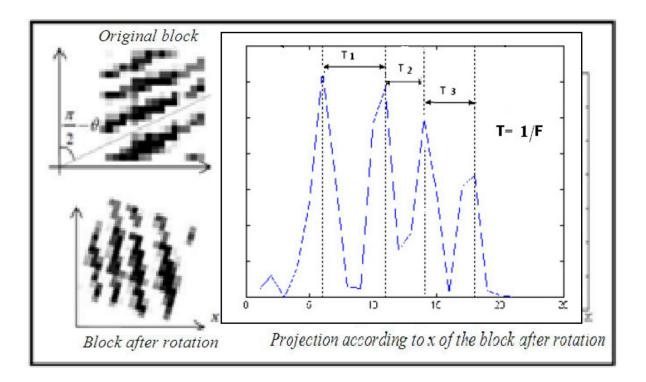
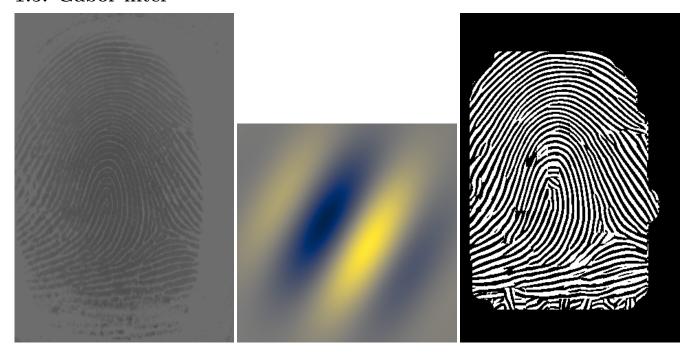


Figure 3: Calculating Ridges' Frequency

 θ is calculated in the Orientation step.

1.5. Gabor filter



The size of the filter is determined by $ridge\ frequency$.

The Rotation of the filter is determined by block orientation.

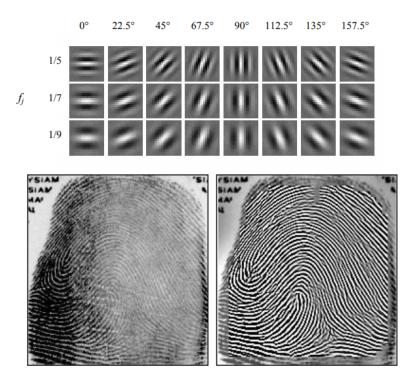


Figure 4: Another Example

1.6. Skeletonization

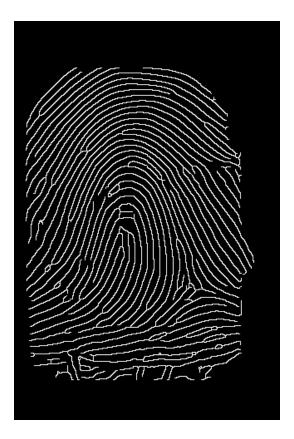


Figure 5: Skeletonization

1.7. Singularities and Keypoints

$$P_{\mathbf{G},C}(i,j) = \sum_{k=0...7} angle(\mathbf{d}_k, \mathbf{d}_{(k+1) \mod 8}).$$

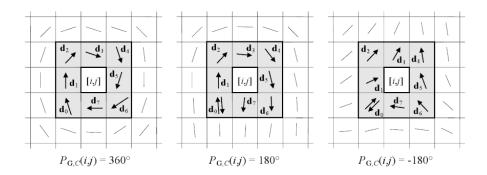
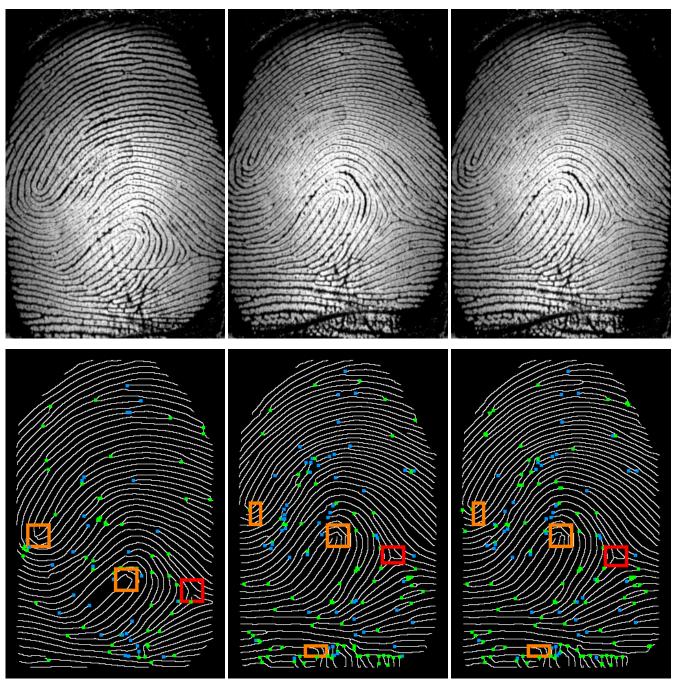


Figure 6: Detect Singularities



2. Comparing

Verdict: Match



Comparing 1 and 9: MMScore = 0.02355706937779257 [True]
Comparing 1 and 10: MMScore = 0.03147042916615236 [True]

MMScore's Calculation



Compare respective spans:

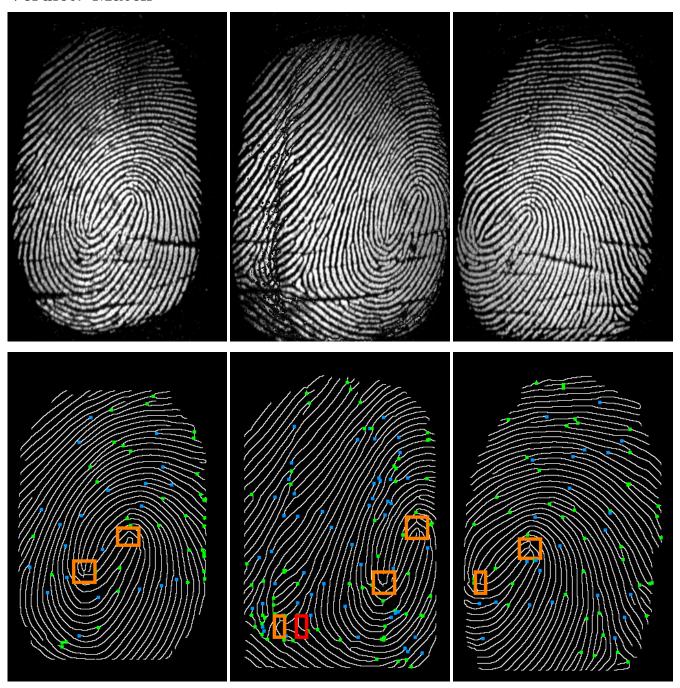


$$\text{Ridges Mismatch Score} = \frac{|A-B|}{\max(A,B)}$$

$$\text{Keypoints Mismatch Score} = \frac{|f(A) - f(B)|}{\max(f(A), f(B))}$$

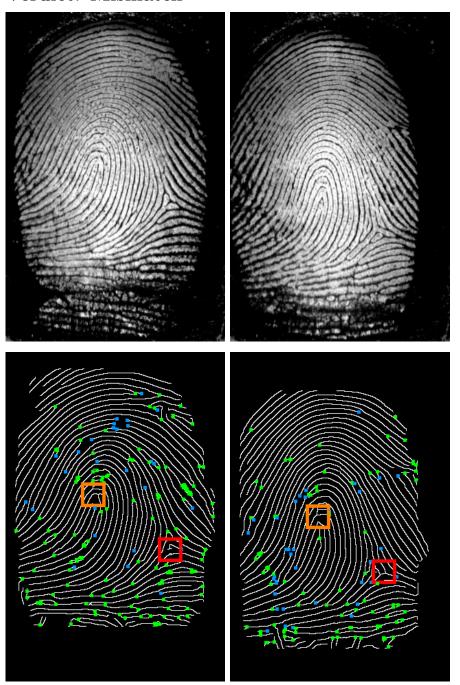
where f(X) is a keypoints segmentation function.

Verdict: Match



Comparing 11 and 13: MMScore = 0.06850775829491 [True] Comparing 11 and 14: MMScore = 0.057465974475778385 [True]

Verdict: Mismatch



Comparing 0 and 4: Ridge MMScore = 0.11450558858066591 [False]

Verdict: Mismatch



Comparing 16 and 21:
CA = (268, 155), CB = (259, 183);
Ridge MMScore = 0.2133995812504585;
Singu MMScore = 0.5;
MMScore = 0.7133995812504585 [False]