First Order Nonsmooth Optimization: Catalyst Acceleration and Unifying Nesterov's Acceleration

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Overview

This talks will be based on the content of our draft paper and selected content of the Catalyst Meta Acceleration Framework. Our preprint:

• X. Wang and H. Li, A Parameter Free Accelerated Proximal Gradient Method Without Restarting, preprint, (2025).

Catalyst Meta Acceleration:

- H. Lin, J. Mairal and Z. Harchaoui, A universal catalyst for first-order optimization, in NISP, vol. 28, (2015).
- Catalyst acceleration for first-order convex optimization: from theory to practice, JMLR, 18 (2018), pp. 1–54.

ToC

- Introduction
 - Notations and preliminaries
- Content of the draft paper
 - Direction of future works
- Selected contents from Catalyst Meta Accelerations
 - Direction of future works
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Notations and preliminaries

Throughout this talk, let \mathbb{R}^n be the ambient space equiped with Euclidean inner product and norm. We consider

$$\min_{x \in \mathbb{R}^n} \left\{ F(x) := f(x) + g(x) \right\}. \tag{1}$$

Unless specified, assume:

- **1** $f: \mathbb{R}^n \to \mathbb{R}$ is L-Lipschiz smooth $\mu \geq 0$ strongly convex,
- ② $g: \mathbb{R}^n \to \overline{\mathbb{R}}$ is closed convex proper.

Our works on R-WAPG

Introduction to Catalyst Acceleration

Citation examples

Citation examples [1]

References I



A. Chambolle and C. Dossal, "On the convergence of the iterates of the "Fast iterative shrinkage/thresholding algorithm"," *Journal of Optimization Theory and Applications*, vol. 166, no. 3, pp. 968–982, Sep. 2015. [Online]. Available: https://doi.org/10.1007/s10957-015-0746-4