

MonteCarlo Markov Chain and Simulated Annealing with Applications and Implementations

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Abstract

In this report, we prove the fundamentals for the convergence of the Metropolis Hastings Chain under the discrete case; then introduce some ideas from the continuous case. We discuss the Simulated Annealing algorithm as a particular case of the Metropolis Hastings and use both algorithms to construct several numerical experiments in Julia. The first experiment is sampling from complicated distribution functions on 2D, the second is applying Simulated Annealing for the knapsack problem, and in the third experiment, we test simulated Annealing on the Rastrigin function using different base chains. We collect data and illustrate the behaviors of these algorithms.

1 Introduction

2 Preliminaries

3 Metropolis Hasting and Its Convergence

3.1 The Discrete Case

3.2 The Continuous Case

3.3 Numerical Experiments

4 Simulated Annealing

4.1 The Limit of Temperature

4.2 Solving the Knapsack Problem

4.3 Best Base Chain to Avoid Curse of Dimensionality

4.4 Numerical Experiments

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References