

$$X_1, \dots, X_n \sim \text{Pois}(\lambda), \quad \mathbb{E}[X_i] = \text{var}[X_i] = \lambda$$

$$\hat{\lambda} = \bar{X} \sim N\left(\lambda, \frac{\lambda}{n}\right)$$

$$\lambda \in \left[\hat{\lambda} \pm z_{1-\frac{\alpha}{2}} \cdot \sqrt{\frac{\hat{\lambda}}{n}} \right]$$

$$X_1, \dots, X_{n_x} \sim \text{Pois}(\lambda_x)$$

$$Y_1, \dots, Y_{n_y} \sim \text{Pois}(\lambda_y)$$

$$\hat{\lambda}_x - \hat{\lambda}_y = \bar{X} - \bar{Y} \sim N\left(\lambda_x - \lambda_y, \frac{\lambda_x}{n_x} + \frac{\lambda_y}{n_y}\right)$$

$$P(X=x) = \frac{e^{-\lambda} \cdot \lambda^x}{x!}$$

$$P(X=x) \Big|_{\lambda} = \frac{1}{x!} \left(-e^{-\lambda} \cdot \lambda^{x-1} + e^{-\lambda} \cdot x \cdot \lambda^{x-1} \right) =$$

$$= \frac{1}{x!} e^{-\lambda} \cdot \lambda^{x-1} \cdot (x - \lambda)$$

$$\hat{\lambda} = \bar{X}$$

$$\widehat{P(X=x)} = \frac{1}{x!} e^{-\hat{\lambda}} \cdot \hat{\lambda}^{(x-1)} \cdot (x - \hat{\lambda}) \sim N\left(\frac{\lambda}{n}, \left(\frac{\lambda}{n} \right)^2 \right)$$

$$g(\hat{\lambda}) \sim N\left(g(\lambda), \frac{\lambda}{n} \cdot [g'_{\lambda}(\lambda)]^2\right)$$