

3.3.

$$(a) \sum_z P(Z=z | B_1, \dots, B_n) = 1$$

$$\therefore \sum_{z=-\infty}^{+\infty} \left(\frac{1-\alpha}{1+\alpha} \right) \alpha^{|z-f(B)|}$$

$$\because z = -\infty \text{ to } +\infty$$

$$\therefore z + f(B) \text{ still from } -\infty \text{ to } +\infty$$

$$\therefore \sum_{z=-\infty+f(B)}^{+\infty+f(B)} \left(\frac{1-\alpha}{1+\alpha} \right) \alpha^{|z+f(B)-f(B)|}$$

$$= \sum_{z=-\infty}^{+\infty} \left(\frac{1-\alpha}{1+\alpha} \right) \alpha^{|z|} = \left(\frac{1-\alpha}{1+\alpha} \right) \sum_{z=-\infty}^{+\infty} \alpha^{|z|}$$

$$= \left(\frac{1-\alpha}{1+\alpha} \right) \left(\alpha^0 + 2 \sum_{z=1}^{+\infty} \alpha^z \right) = \left(\frac{1-\alpha}{1+\alpha} \right) \left(1 + 2 \left(\frac{\alpha}{1-\alpha} \right) \right)$$

$$= \left(\frac{1-\alpha}{1+\alpha} \right) \left(\frac{1+\alpha}{1-\alpha} \right) = 1$$

\therefore the conversion is normalized when $z \in [-\infty, +\infty]$

(b)