

ДЗ по мат. анализу на 1.12.2021

Кожевников Илья 2112-1

28 ноября 2021 г.

a)

$$\bar{o}(x^2) + \bar{o}(x) = \bar{o}(x)$$

$$h_1(x) \cdot x^2 + h_2(x) \cdot x = \bar{o}(x)$$

$$x(h_1(x) \cdot x + h_2(x)) = \bar{o}(x)$$

$$\bar{o}(x) = \bar{o}(x)$$

Значит, $\bar{o}(x^2) + \bar{o}(x) = \bar{o}(x)$ справедливо

b)

$$\bar{o}(x) + x^2 = \bar{o}(x)$$

$$\bar{o}(x) + \bar{o}(x) \cdot x = \bar{o}(x)$$

$$\bar{o}(x) + \bar{o}(x^2) = \bar{o}(x)$$

$$\bar{o}(x) = \bar{o}(x)$$

Значит, $\bar{o}(x) + x^2 = \bar{o}(x)$ справедливо

c)

$$(x + \bar{o}(x))(2x^2 + \bar{o}(x^2)) = 2x^3 + \bar{o}(x^3)$$

$$2x^3 + x \cdot \bar{o}(x^2) + 2x^2 \cdot \bar{o}(x) + \bar{o}(x) \cdot \bar{o}(x^2) = 2x^3 + \bar{o}(x^3)$$

$$2x^3 + 4\bar{o}(x^3) = 2x^3 + \bar{o}(x^3)$$

$$2x^3 + \bar{o}(x^3) = 2x^3 + \bar{o}(x^3)$$

Значит, $(x + \bar{o}(x))(2x^2 + \bar{o}(x^2)) = 2x^3 + \bar{o}(x^3)$ справедливо.

d)

$$\bar{o}(1) - \bar{o}(1) = 0$$

$$h_1(1) \cdot 1 - h_2(1) \cdot 1 = 0$$

$$h_1(1) - h_2(1) = 0.$$

$$0 - 0 = 0$$

$$0 = 0$$

Значит, $\bar{o}(1) - \bar{o}(1) = 0$ справедливо.