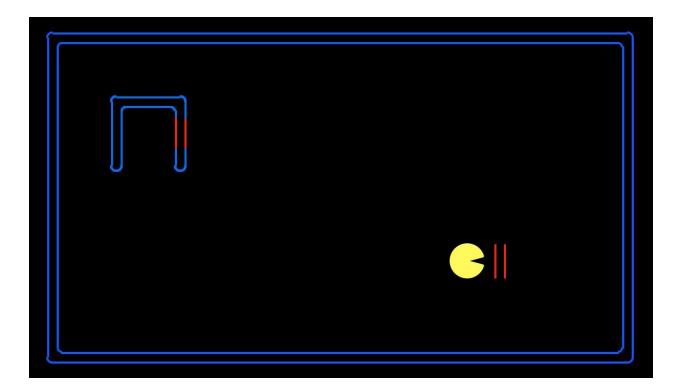
p4_bn_introduction

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Project 4: Bayes' Nets



Much truth is unseen.

How will Pacman become sure?

Bayes' Net Inference.

Introduction

In this project, you will implement inference algorithms for Bayes Nets, specifically variable elimination and value-of-perfect-information computations. These inference algorithms will allow you to reason about the existence of invisible pellets and ghosts.

This project includes an autograder for you to grade your answers on your machine. This can be run on all questions with the command:

python autograder.py

It can be run for one particular question, such as q2, by:

python autograder.py -q q2

It can be run for one particular test by commands of the form:

python autograder.py -t test_cases/q2/1-simple-eliminate

See the autograder tutorial in Project 0 for more information about using the autograder.

The code for this project contains the following files, available as a zip archive.

Files you'll edit:		
factorOperations.py	Operations on Factors (join, eliminate, normalize).	
inference.py	Inference algorithms (enumeration, variable elimination, likelihood weighting).	
bayesAgents.py	Pacman agents that reason under uncertainty.	

Files you should read but NOT edit:		
bayesNet.py	The BayesNet and Factor classes.	
Files you can ignore:		
graphicsDisplay.py	Graphics for Pacman	
graphicsUtils.py	Support for Pacman graphics	
textDisplay.py	ASCII graphics for Pacman	
ghostAgents.py	Agents to control ghosts	
keyboardAgents.py	Keyboard interfaces to control Pacman	
layout.py	Code for reading layout files and storing their contents	
autograder.py	Project autograder	
testParser.py	Parses autograder test and solution files	
testClasses.py	General autograding test classes	

test_cases/	Directory containing the test cases for each question
bayesNets2TestClass es.py	Project 4 specific autograding test classes

Files to Edit and Submit: You will fill in portions of factorOperations.py, inference.py, and bayesAgents.py during the assignment. You should submit these files with your code and comments. Please *do not* change the other files in this distribution or submit any of our original files other than these files.

Evaluation: Your code will be autograded for technical correctness. Please do not change the names of any provided functions or classes within the code, or you will wreak havoc on the autograder. However, the correctness of your implementation -- not the autograder's judgements -- will be the final judge of your score. If necessary, we will review and grade assignments individually to ensure that you receive due credit for your work.

Academic Dishonesty: We will be checking your code against other submissions in the class for logical redundancy. If you copy someone else's code and submit it with minor changes, we will know. These cheat detectors are quite hard to fool, so please don't try. We trust you all to submit your own work only; *please* don't let us down. If you do, we will pursue the strongest consequences available to us.

Getting Help: You are not alone! If you find yourself stuck on something, contact the course staff for help. Office hours, section, and the discussion forum are there for your support; please use them. If you can't make our office hours, let us know and we will schedule more. We want these projects

to be rewarding and instructional, not frustrating and demoralizing. But, we don't know when or how to help unless you ask.

Discussion: Please be careful not to post spoilers.

p4_bn_welcome

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TREASURE-HUNTING PACMAN

Pacman has entered a world of mystery. Initially, the entire map is invisible. As he explores it, he learns information about neighboring cells. The map contains two houses: a ghost house, which is probably mostly red, and a food house, which is probably mostly blue. Pacman's goal is to enter the food house while avoiding the ghost house.

Pacman will reason about which house is which based on his observations, and reason about the tradeoff between taking a chance or gathering more evidence. To enable this, you'll implement probabilistic inference using Bayes nets.

To play for yourself, run:

python hunters.py -p KeyboardAgent -r

p4_bn_data_types

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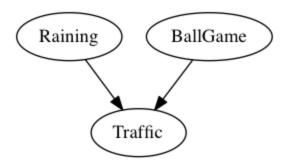
Bayes' Nets and Factors

First, take a look at bayesNet.py to see the classes you'll be working with - BayesNet and Factor. You can also run this file to see an example BayesNet and associated Factors:

python bayesNet.py

You should look at the printStarterBayesNet function - there are helpful comments that can make your life *much* easier later on.

The Bayes' Net created in this function is shown below:



A summary of the terminology is given below:

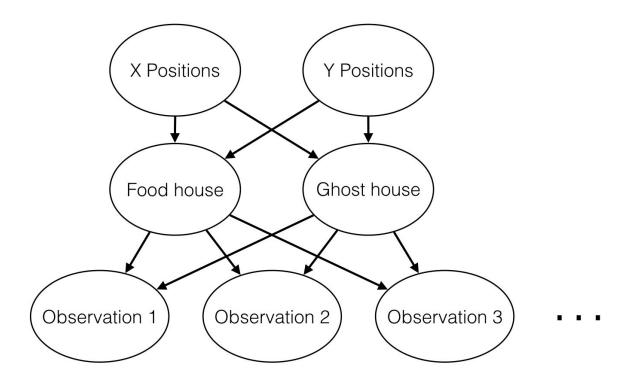
- Bayes' Net: This is a representation of a probabilistic model as a directed acyclic graph and a set of conditional probability tables, one for each variable, as shown in lecture. The Traffic Bayes' Net above is an example.
- Factor: This stores a table of probabilities, although the sum of the entries in the table is not necessarily 1. A factor is of the general form P(X1,...,Xm,y1,...,yn | Z1,...,Zp,w1,...,wq). Recall that lower case variables have already been assigned. For each possible assignment of values to the Xi and Zj variables, the factor stores a single number. The Zj,wk variables are said to be conditioned while the Xi,yl variables are unconditioned.
- Conditional Probability Table (CPT): This is a factor satisfying two properties:

- 1. Its entries must sum to 1 for each assignment of the conditional variables.
- 2. There is exactly one unconditioned variable.
- The Traffic Bayes' Net stores the following CPTs:

QUESTION 1 (3 POINTS): BAYES NET STRUCTURE

Implement the constructBayesNet function in bayesAgents.py. It constructs an empty Bayes net with the structure described below. (We'll specify the actual factors in the next question.)

The treasure hunting world is generated according to the following Bayes net:



Don't worry if this looks complicated! We'll take it step by step. As described in the code for constructBayesNet, we build the empty structure by listing all of the variables, their values, and the edges between them. This figure shows the variables and the edges, but what about their values?

- X positions determines which house goes on which side of the board.
 It is either food-left or ghost-left.
- **Y positions** determines how the houses are vertically oriented. It models the vertical positions of both houses simultaneously, and has one of four values: **both-top**, **both-bottom**, **left-top**, and **left-bottom**. "left-top" is as the name suggests: the house on the left side of the board is on top, and the house on the right side of the board is on the bottom.
- Food house and ghost house specify the actual positions of the two houses. They are both deterministic functions of "X positions" and "Y positions"
- The observations are measurements that Pacman makes while traveling around the board. Note that there are many of these nodes---one for every board position that might be the wall of a house. If there is no house in a given location, the corresponding observation is none; otherwise it is either red or blue, with the precise distribution of colors depending on the kind of house.

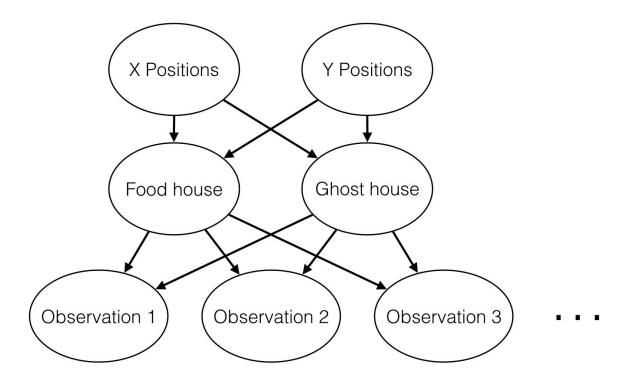
p4_bn_q2_probabilities

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QUESTION 2 (3 POINTS): BAYES NET PROBABILITIES

Implement the fillYCPT and fillObsCPT functions in bayesAgents.py. These take the Bayes net you constructed in the previous problem, and specify the factors governing the **Y position** and **observation** variables. (We've already filled in the **X position** and **house** factors for you.)

Here's the structure of the Bayes net again:



For an example of how to construct factors, look at the implementation of the factor for **X positions** in fillXCPT.

The **Y positions** are given by values BOTH_TOP, BOTH_BOTTOM, LEFT_TOP and LEFT_BOTTOM. These variables, and their associated probabilities, are provided by constants at the top of the file.

If you're interested, you can look at the computation for **house positions**. All you need to remember is that each house can be in one of four positions: **top-left**, **top-right**, **bottom-left**, or **bottom-right**.

Observations are more interesting. Every possible observation position is adjacent to a possible center for a house. Pacman might observe that position to contain a **red** wall, a **blue** wall, or **no wall**. These outcomes occur with the following probabilities (again defined in terms of constants at the top of the file):

- If the adjacent house center is occupied by neither the ghost house or the food house, an observation is **none** with certainty (probability 1).
- If the adjacent house center is occupied by the **ghost house**, it is red with probability PROB GHOST RED and blue otherwise.
- If the adjacent house center is occupied by the food house, it is red with probability PROB_FOOD_RED and blue otherwise.

IMPORTANT NOTE: the structure of the Bayes Net means that the food house and ghost house might be assigned to the same position. This will never occur in practice. But the observation CPT needs to be a proper distribution for every possible set of parents. In this case, you should use the **food house distribution**.

Hints

There are only four entries in the Y position factor, so you can specify each of those by hand. You'll have to be cleverer for the observation variables. You'll find it easiest to first loop over possible house positions, then over possible walls for each house, and finally over assignments to (wall color, ghost house position, food house position) triples. Remember to create a separate factor for *every one* of the 4*7=28 possible observation positions.

p4_bn_q3_join

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Question 3 (5 points): Join Factors

Implement the joinFactors function in factorOperations.py. It takes in a list of Factors and returns a new Factor whose probability entries are the product of the corresponding rows of the input Factors.

joinFactors can be used as the product rule, for example, if we have a factor of the form P(X|Y) and another factor of the form P(Y), then joining these factors will yield P(X,Y). So, joinFactors allows us to incorporate probabilities for conditioned variables (in this case, Y). However, you should not assume that joinFactors is called on probability tables - it is possible to call joinFactors on Factors whose rows do not sum to 1.

Grading: To test and debug your code, run

python autograder.py -q q1

It may be useful to run specific tests during debugging, to see only one set of factors print out. For example, to only run the first test, run:

python autograder.py -t test_cases/q1/1-product-rule

Hints and Observations

- Your joinFactors should return a *new* Factor.
- Here are some examples of what joinFactors can do:
 - joinFactors(P(X|Y), P(Y)) = P(X,Y)
 - \blacksquare joinFactors(P(V,W|X,Y,Z), P(X,Y|Z)) = P(V,W,X,Y|Z)
 - joinFactors(P(X|Y,Z), P(Y)) = P(X,Y|Z)
 - joinFactors(P(V|W), P(X|Y), P(Z)) = P(V,X,Z|W,Y)

- For a general joinFactors operation, which variables are unconditioned in the returned Factor? Which variables are conditioned?
- Factors store a variableDomainsDict, which maps each variable to a list of values that it can take on (its domain). A Factorgets its variableDomainsDict from the BayesNet from which it was instantiated. As a result, it contains all the variables of the BayesNet, not only the unconditioned and conditioned variables used in the Factor. For this problem, you may assume that all the input Factors have come from the same BayesNet, and so their variableDomainsDicts are all the same.

p4_bn_q4_eliminate

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Question 4 (4 points): Eliminate

Implement the eliminate function in factorOperations.py. It takes a Factor and a variable to eliminate and returns a new Factor that does not contain that variable. This corresponds to summing all of the entries in the Factor which only differ in the value of the variable being eliminated.

Grading: To test and debug your code, run

python autograder.py -q q4

It may be useful to run specific tests during debugging, to see only one set of factors print out. For example, to only run the first test, run:

python autograder.py -t test_cases/q4/1-simple-eliminate

Hints and Observations

- Your eliminate should return a *new* Factor.
- eliminate can be used to marginalize variables from probability tables.
 For example:
 - \circ eliminate(P(X,Y|Z), Y) = P(X|Z)
 - \circ eliminate(P(X,Y|Z), X) = P(Y|Z)
- For a general eliminate operation, which variables are unconditioned in the returned Factor? Which variables are conditioned?
- Remember that Factors store the variableDomainsDict of the original BayesNet, and *not* only the unconditioned and conditioned variables that they use. As a result, the returned Factor should have the same variableDomainsDict as the input Factor.

p4_bn_q5_normalize

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Question 5 (4 points): Normalize

Implement the normalize function in factorOperations.py. It takes a Factor as input and normalizes it, that is, it scales all of the entries in the Factor such that the sum of the entries in the Factor is 1.

Grading: To test and debug your code, run

python autograder.py -q q5

It may be useful to run specific tests during debugging, to see only one set of factors print out. For example, to only run the first test, run:

python autograder.py -t test_cases/q5/1-preNormalized

Hints and Observations

- Your normalize should return a *new* Factor.
- normalize does not affect probability distributions (since probability distributions must already sum to 1).
- For a general normalize operation, which variables are unconditioned in the returned Factor? Which variables are conditioned? Make sure to read the docstring of normalize for more instructions.
- Remember that Factors store the variableDomainsDict of the original BayesNet, and *not* only the unconditioned and conditioned variables that they use. As a result, the returned Factor should have the same variableDomainsDict as the input Factor.

p4_bn_q6_variable_elimination

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Question 6 (4 points): Variable Elimination

Implement the inferenceByVariableElimination function in inference.py. It answers a probabilistic query, which is represented using a BayesNet, a list of query variables, and the evidence.

Grading: To test and debug your code, run

python autograder.py -q q6

It may be useful to run specific tests during debugging, to see only one set of factors print out. For example, to only run the first test, run:

python autograder.py -t test_cases/q6/1-disconnected-eliminate

Hints and Observations

- The algorithm should iterate over hidden variables in elimination order, performing joining over and eliminating that variable, until the only the query and evidence variables remain.
- The sum of the probabilities in your output factor should sum to one (so that it is a true conditional probability, conditioned on the evidence).
- Look at the inferenceByEnumeration function in inference.py for an example on how to use the desired functions. (Reminder: Inference by enumeration first joins over all the variables and then eliminates all the hidden variables. In contrast, variable elimination interleaves join and eliminate by iterating over all the hidden variables and perform a join and eliminate on a single hidden variable before moving on to the next hidden variable.)

p4_bn_q7_agent

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QUESTION 7 (1 POINTS): MARGINAL INFERENCE

Inside bayesAgents.py, use the inferenceByVariableElimination function you just wrote to compute the marginal distribution over positions of the food house, then return the most likely position. This information is used by **Bayesian Pacman**, who wanders around randomly collecting information for a fixed number of timesteps, then heads directly to the house most likely to contain food.

p4_bn_q8_vpi

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QUESTION 8 (4 POINTS): VALUE OF PERFECT INFORMATION

Bayesian Pacman spends a lot of time wandering around randomly, even when further exploration doesn't provide any additional value. Can we do something smarter?

We'll evaluate **VPI Pacman** in a more restricted setting: everything in the world has been observed, except for the colors of one of the houses' walls. VPI Pacman has three choices:

- 1. immediately enter the already-explored house
- 2. immediately enter the hidden house
- 3. explore the outside of the hidden house, and then make a decision about where to go

You'll implement code to reason about the expected value of each of these actions.

First look at computeEnterValues. This function computes the expected value of entering the left and right houses. Again, you can use the inference code you already wrote to do all the heavy lifting here. First compute $p(foodHouse = topLeft \ and \ ghostHouse = topRight \ evidence)$ and $p(foodHouse = topRight \ and \ ghostHouse = topLeft \ evidence)$. Then use these two probabilities to compute expected values for rushing left and rushing right.

Next look at computeExploreRightValue. This function computes the expected value of exploring all of the hidden cells, and then making a decision. To do this, you'll need to think about all of the things that might

happen as a result of your exploration. Maybe you'll find 1 red wall and 6 blue ones; maybe you'll find 2 red walls and 5 blue ones; and so on. We've provided a helper method, getExplorationProbsAndOutcomes, which returns a list of future observations Pacman might make, and the probability of each. To calculate the value of the extra information Pacman will gain, you can use the following formula:

 $E[value \ of \ exploration] = \sum p(new \ evidence) \ max_{actions} \ E[action \ | \ old \ evidence]$

Note that *E[action | evidence]* is exactly the quantity computed by computeEnterVals, so to compute the value of exploration, you can call computeEnterValues again with the hypothetical evidence provided by getExplorationProbsAndOutcomes.

Hints

After exploring, Pacman will again need to compute the expected value of entering the left and right houses. Fortunately, you've already written a function to do this! Your solution to computeExploreRightValue can rely on your solution to computeEnterValues to determine the value of future observations.