8.
$$\int_0^\pi \sin^{\nu-1} x \cos ax \, dx = \frac{\pi \cos \frac{a\pi}{2}}{2^{\nu-1} \nu B\left(\frac{\nu+a+1}{2}, \frac{\nu-a+1}{2}\right)}$$
 [Re $\nu > 0$] Лб V 121(68)и, Вт 337и

9.
$$\int_{0}^{\pi/2} \sin^{v-1} x \cos ax \, dx = \frac{\pi}{2^{\nu} \nu B\left(\frac{\nu + a + 1}{2}, \frac{\nu - a + 1}{2}\right)}$$

$$[Re \ \nu > 0]$$

10.
$$\int_0^{\pi/2} \sin^{\nu-2} x \cos \nu x \, dx = \frac{1}{\nu - 1} \sin \frac{\nu \pi}{2}$$
 [Re $\nu > 1$] X2 (332)(9c)

11.
$$\int_0^\pi \sin^\nu x \cos \nu x \, dx = \frac{\pi}{2^\nu} \cos \frac{\nu \pi}{2}$$
 [Re $\nu > -1$] Лб V 121(70)и

12.
$$\int_0^\pi \sin^{2n} x \cos 2mx \, dx = 2 \int_0^{\pi/2} \sin^{2n} x \cos 2mx \, dx = \frac{(-1)^m}{2^{2n}} \binom{2n}{n-m} \pi \qquad [n \geqslant m]$$
$$= 0 \qquad \qquad [n < m]$$
Bu (40)(16), \Gamma X2 (332)(12b)

13.⁷
$$\int_0^{\pi} \sin^{2n+1} x \cos 2mx \, dx =$$

$$= 2 \int_0^{\pi/2} \sin^{2n+1} x \cos 2mx \, dx = \frac{(-1)^m 2^{n+1} n! (2n+1)!!}{(2m-2n-3)!! (2m+2n+1)!!} \qquad [n \le m-1]$$

$$= \frac{(-1)^{n+1} 2^{n+1} n! (2m-2n+3)!! (2n+1)!!}{(2m+2n+1)!!} \qquad [n < m-1]$$

$$= \frac{(-1)^{n+1} 2^{n+1} n! (2m-2n+3)!! (2n+1)!!}{(2m+2n+1)!!} \qquad [n < m-1]$$

$$= \frac{(-1)^{n+1} 2^{n+1} n! (2m-2n+3)!! (2n+1)!!}{(2m+2n+1)!!} \qquad [n < m-1]$$