# YSC4231: Parallel, Concurrent and Distributed Programming

Concurrent Skip Lists

#### Set Object Interface

- Collection of elements
- No duplicates
- Methods
  - add() a new element
  - remove() an element
  - contains() if element is present

#### Many are Cold but Few are Frozen

- Typically high % of contains() calls
- Many fewer add() calls
- And even fewer remove() calls
  - 90% contains()
  - -9% add()
  - 1% remove()
- Folklore?
  - Yes but probably mostly true

#### Concurrent Sets

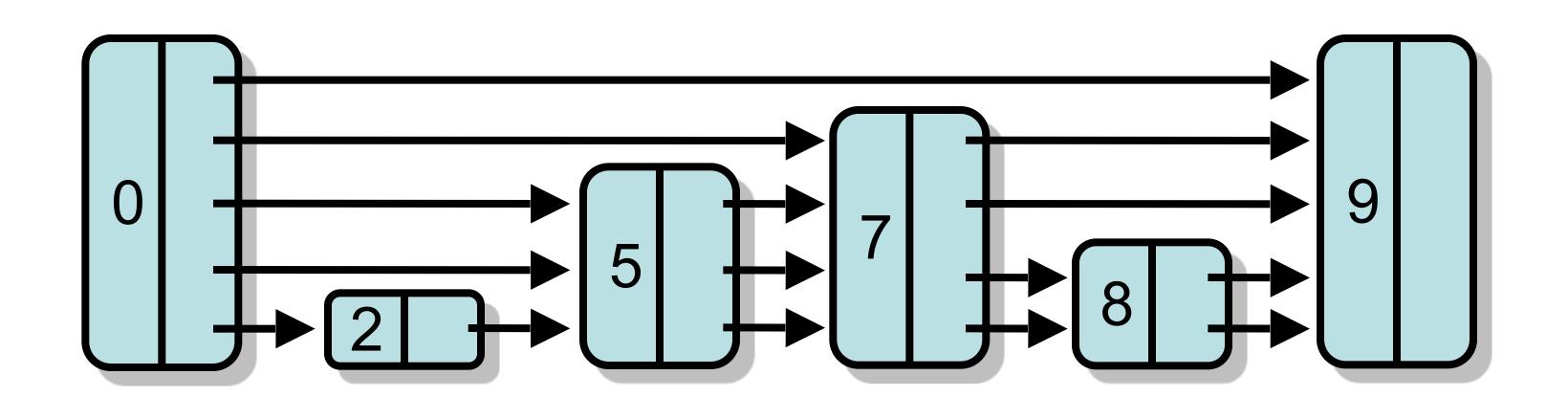
- Optimistic List, Lazy List
  - All have linear time (okay-ish)
- Any ideas on how we can do better?

#### Concurrent Sets

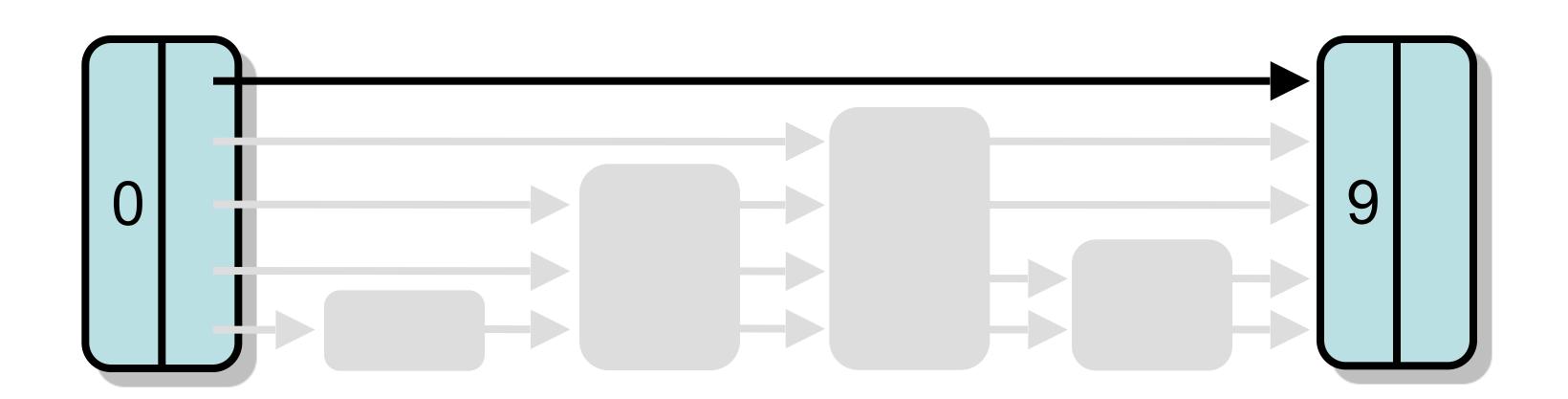
- Balanced Trees?
  - Red-Black trees, AVL trees, ...
- Problem: no one does this well ...
- ... because rebalancing after add() or remove() is a global operation

### Skip Lists

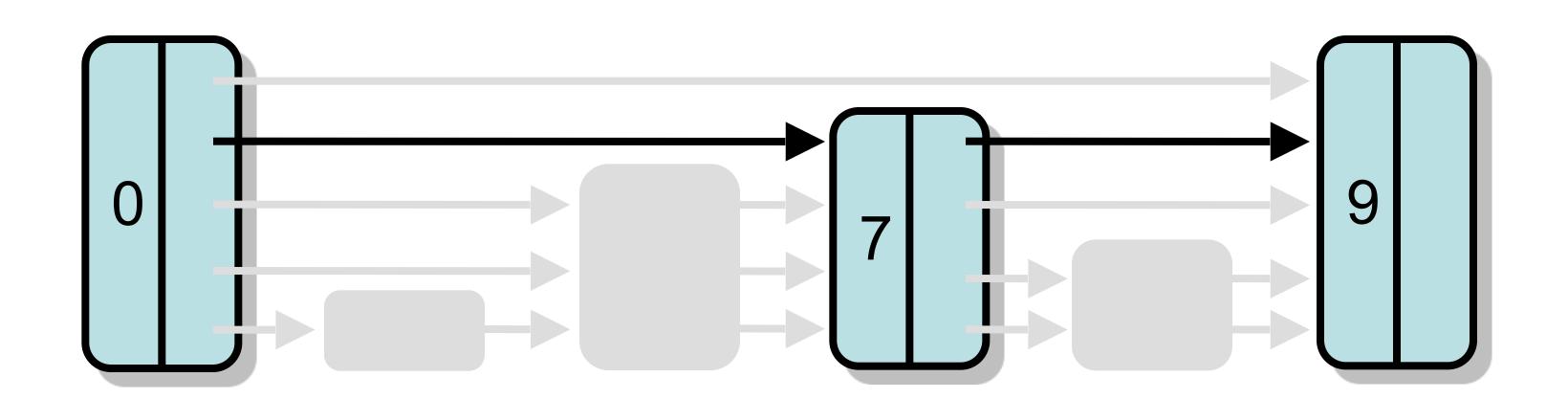
- Probabilistic Data Structure
- No global rebalancing
- Logarithmic-time search



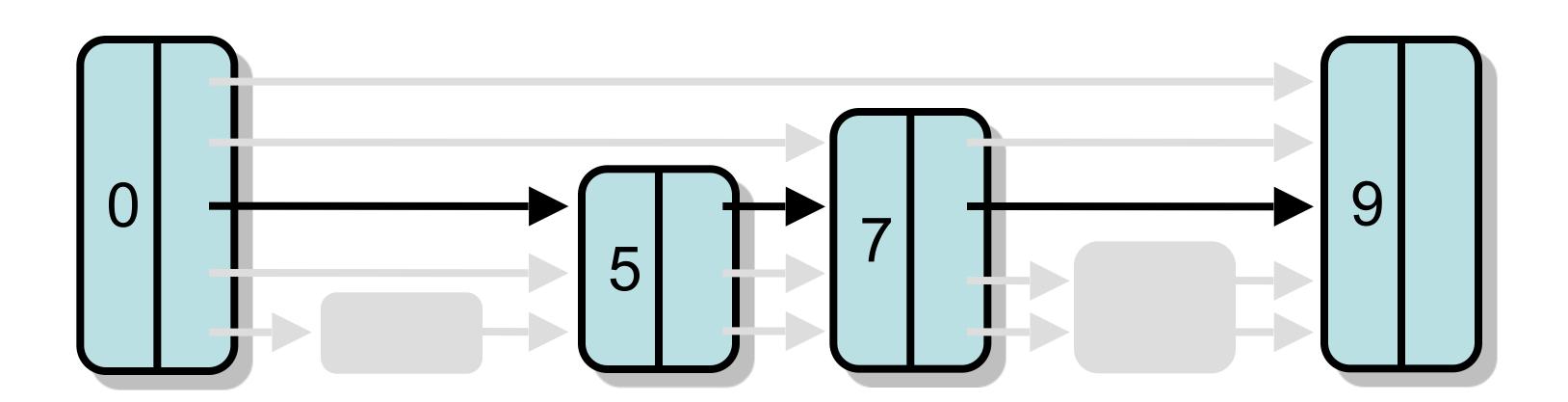
• Each layer is sub-list of lower levels



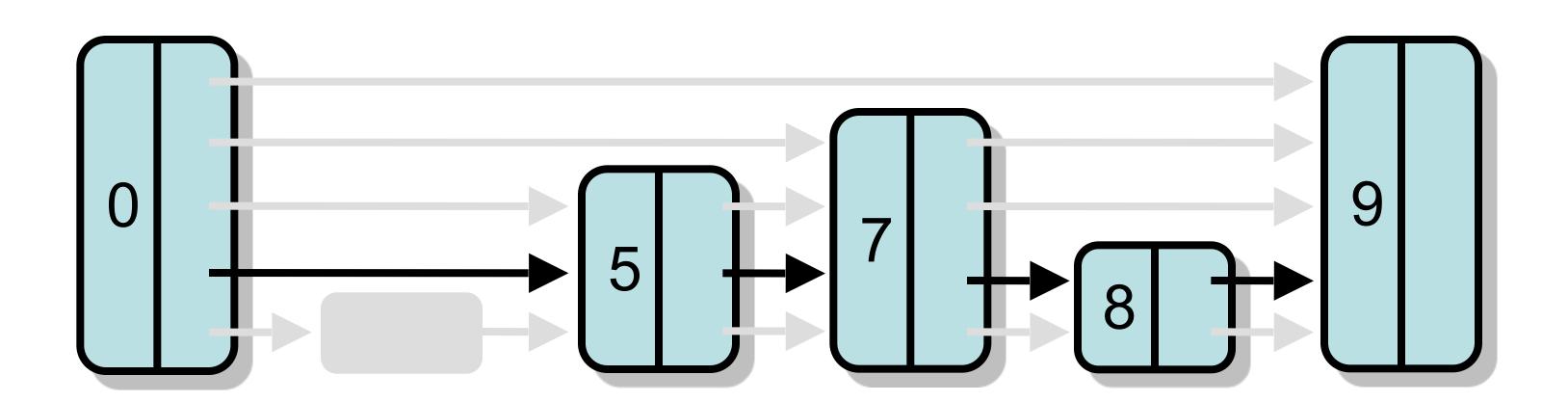
• Each layer is sub-list of lower-levels



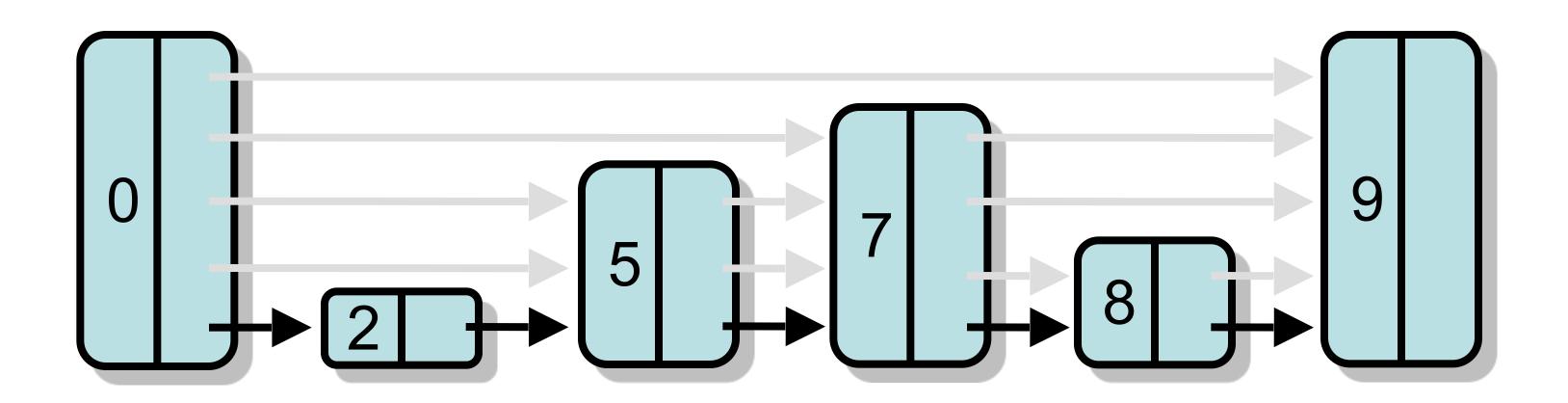
• Each layer is sub-list of lower levels



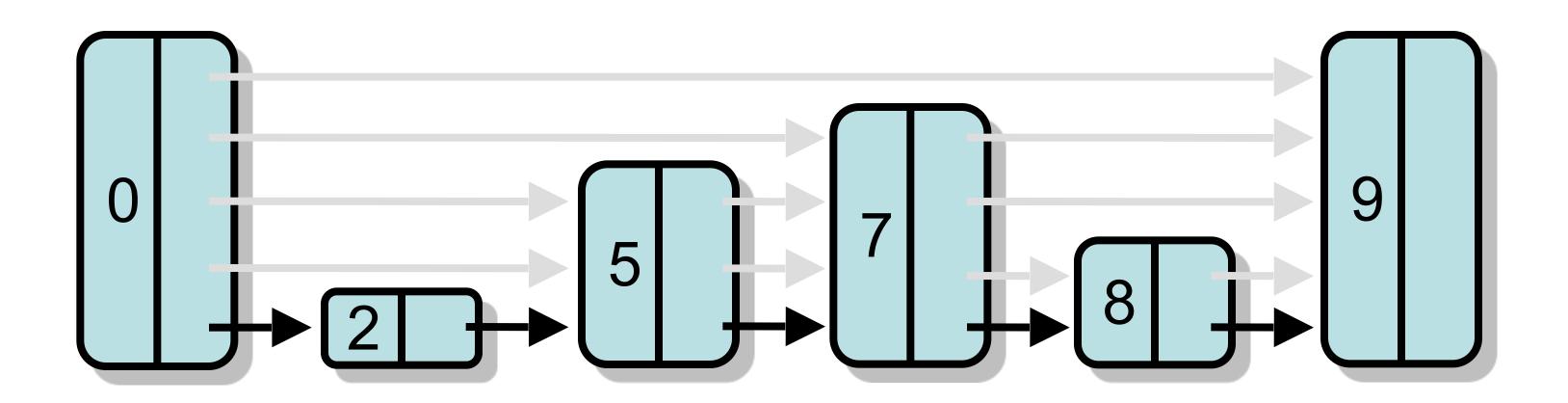
• Each layer is sub-list of lower levels

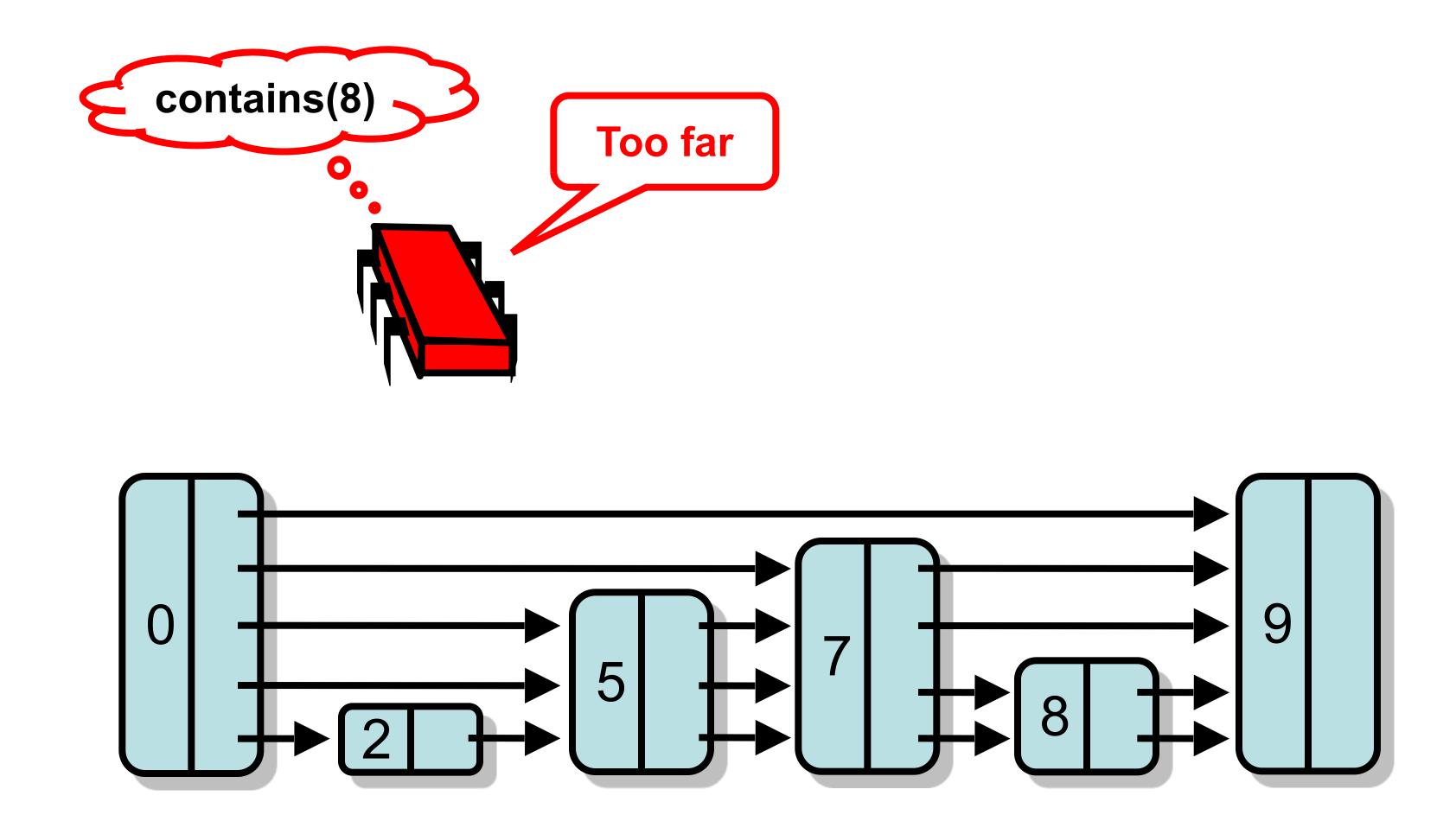


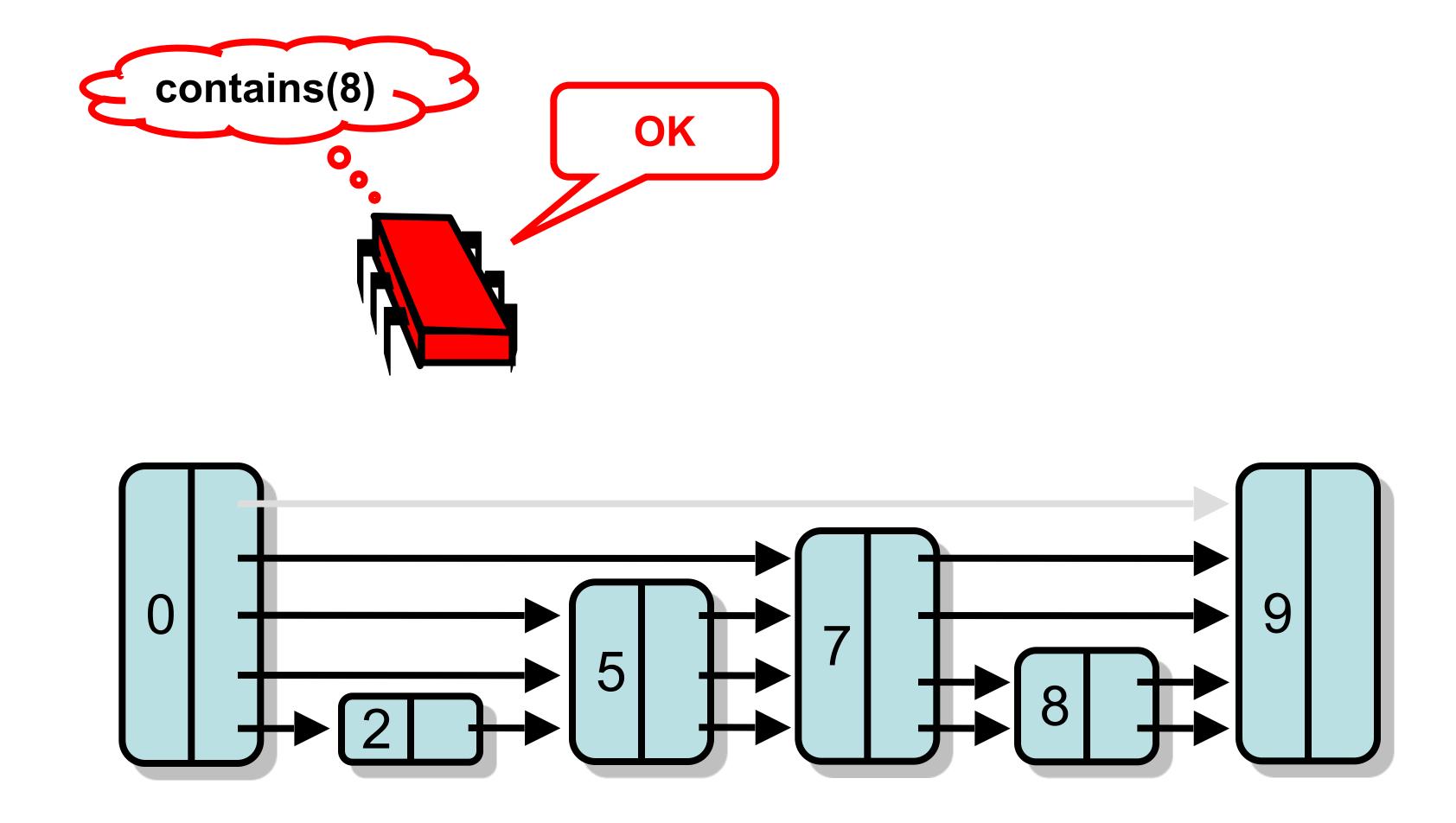
- Each layer is sub-list of lower levels
- Lowest level is entire list

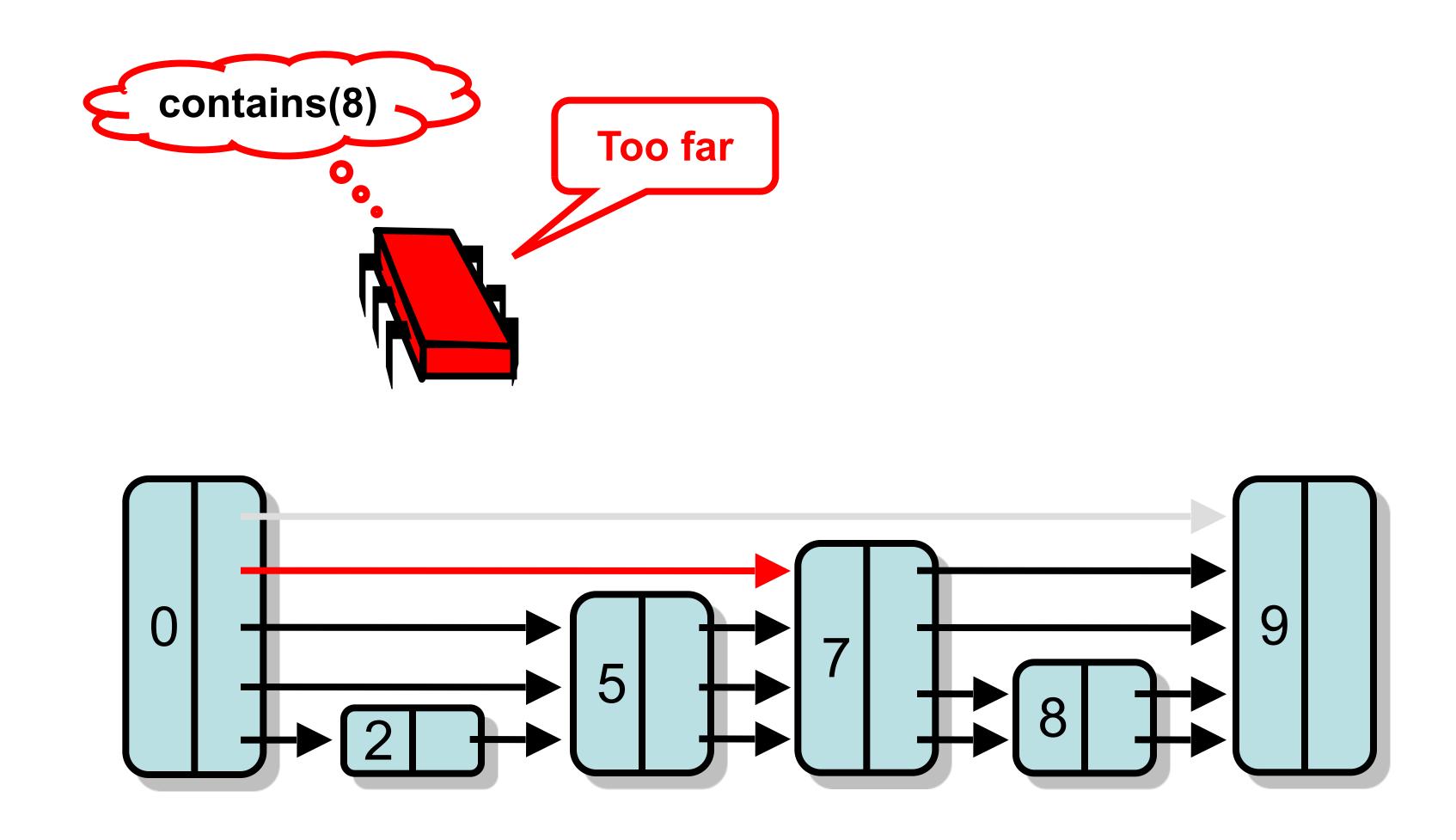


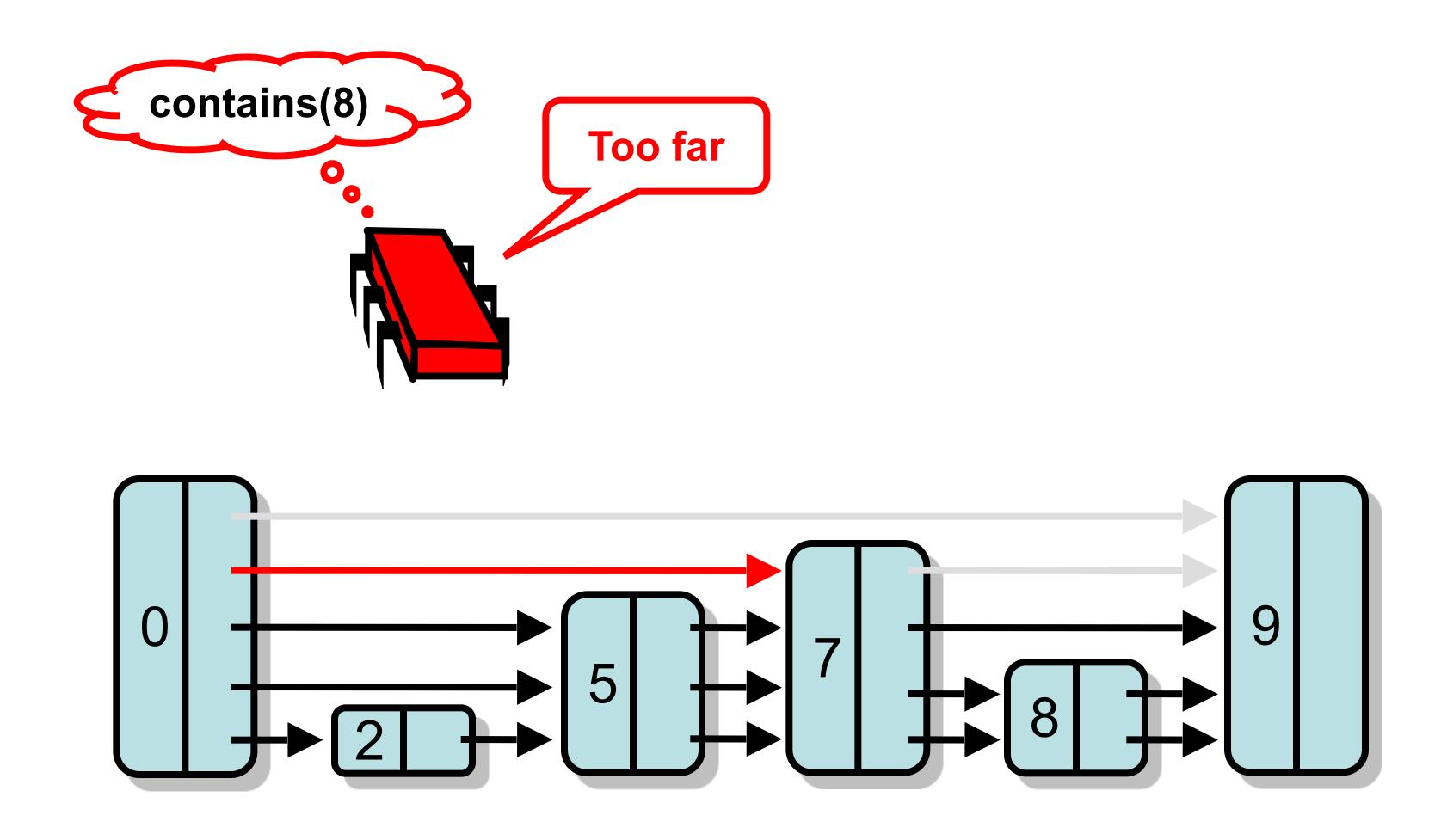
- Each layer is sub-list of lower levels
- Not easy to preserve in concurrent implementations ...

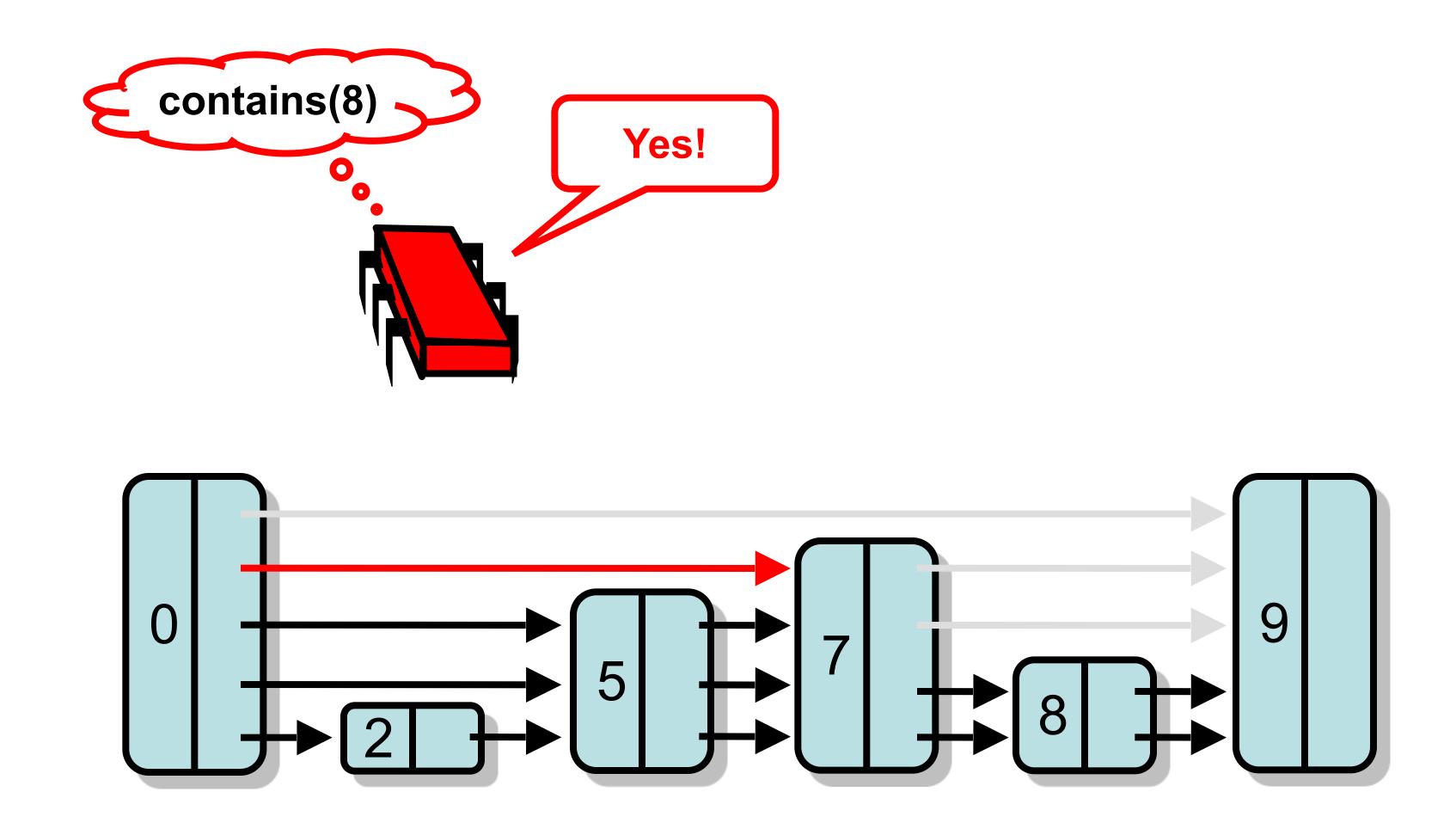


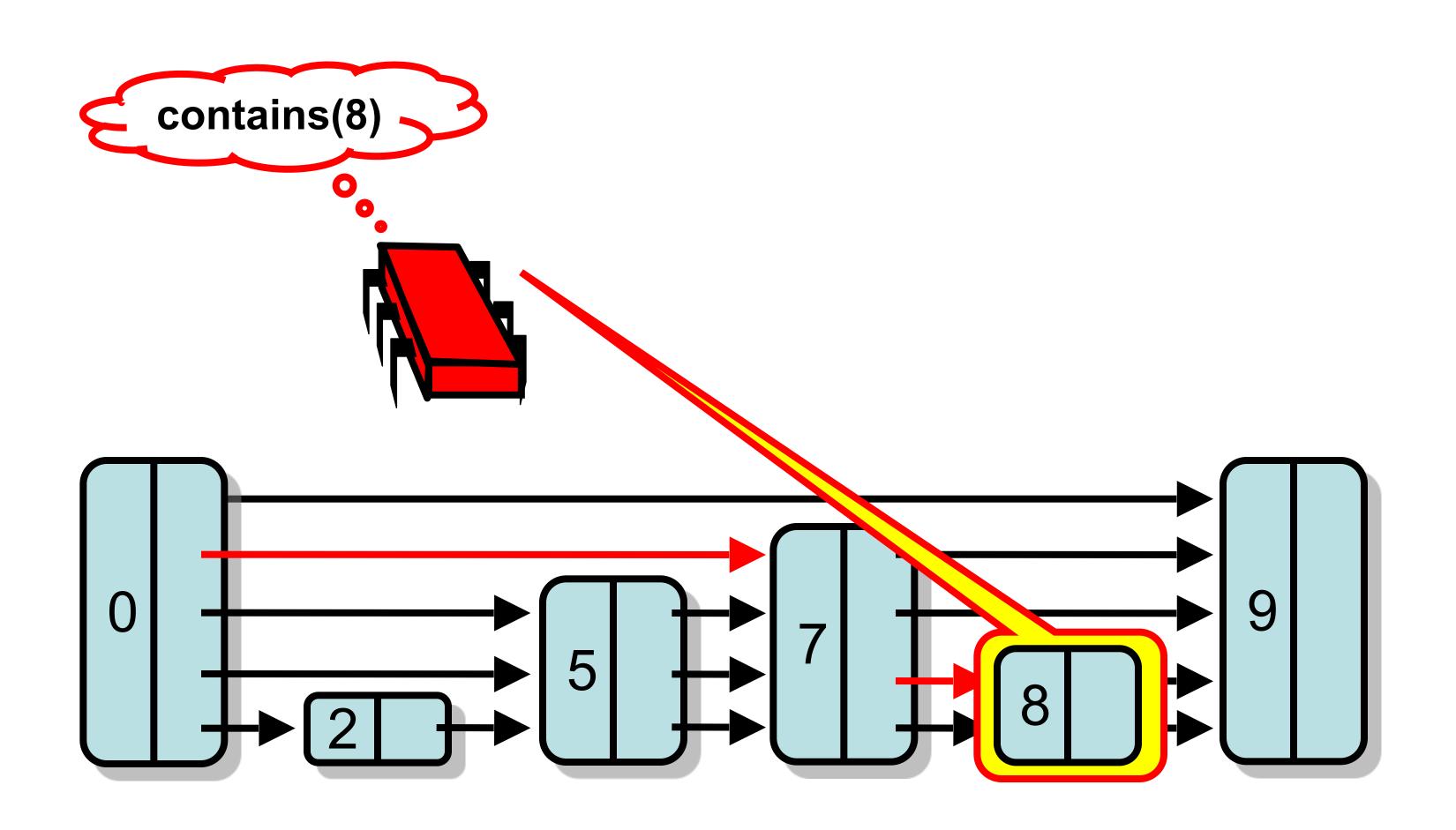




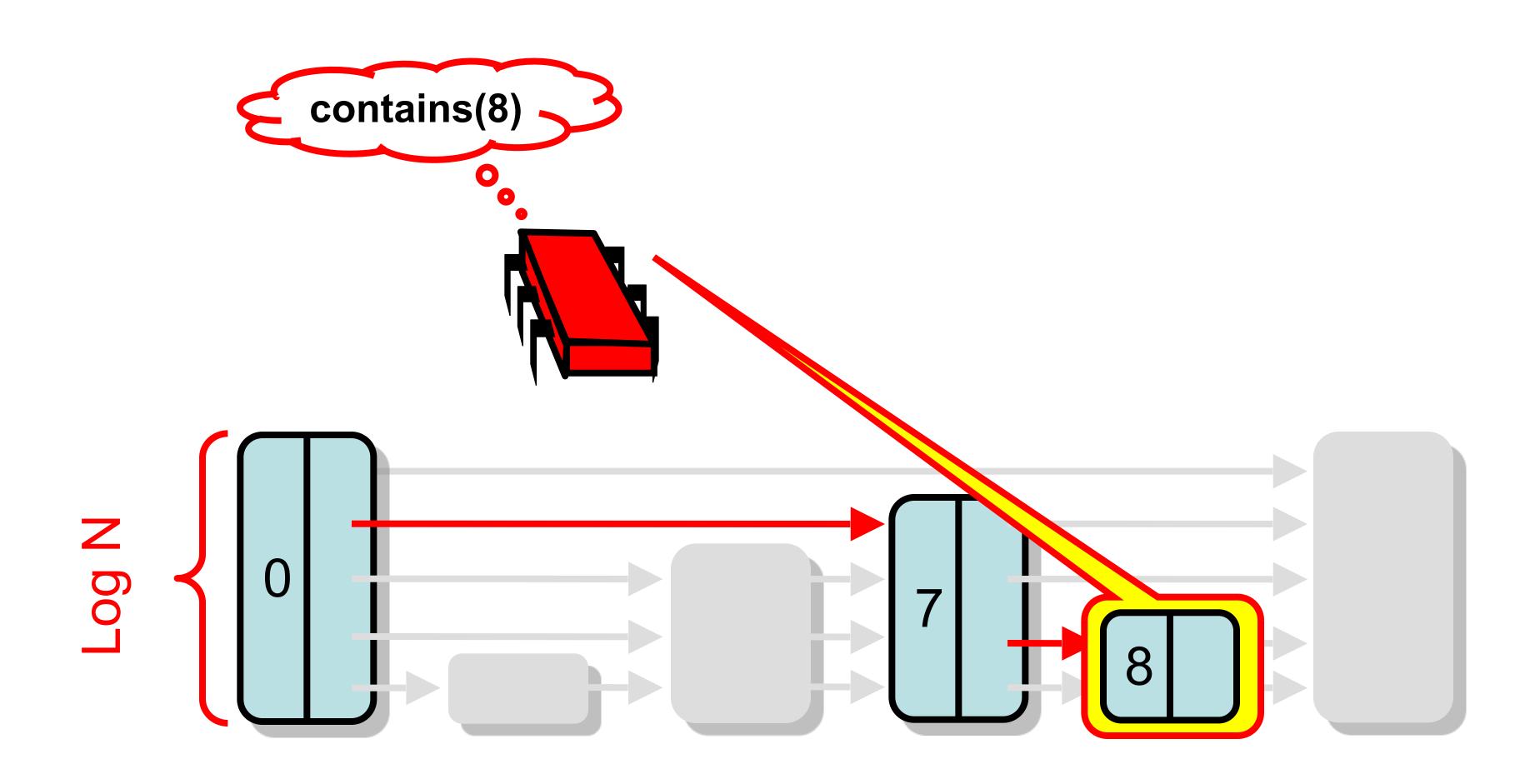






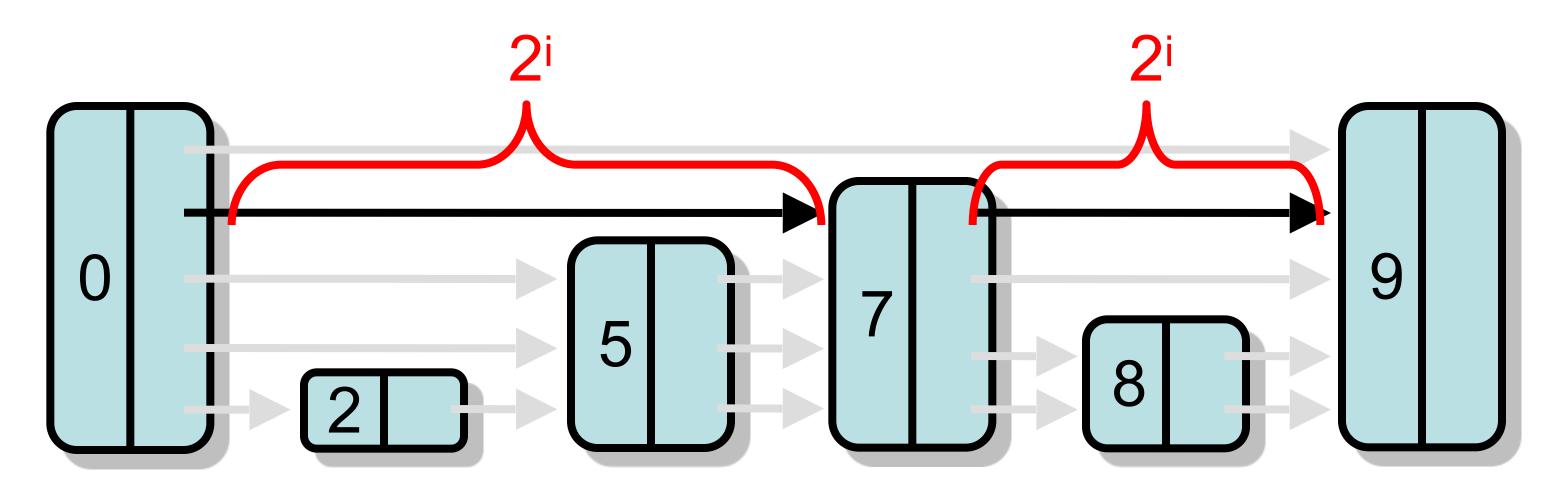


# Logarithmic



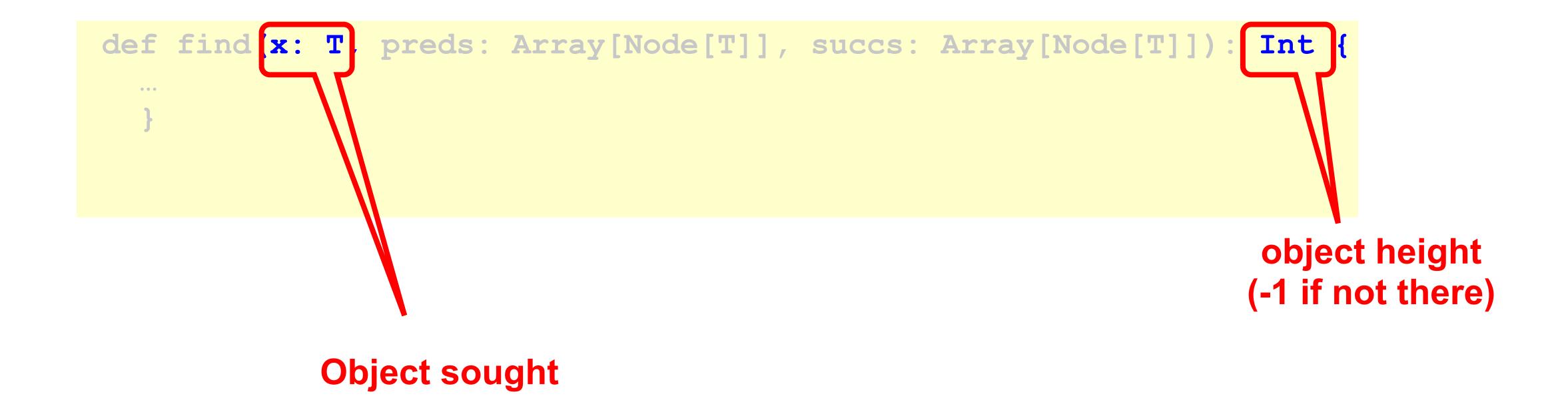
# Why Logarthimic

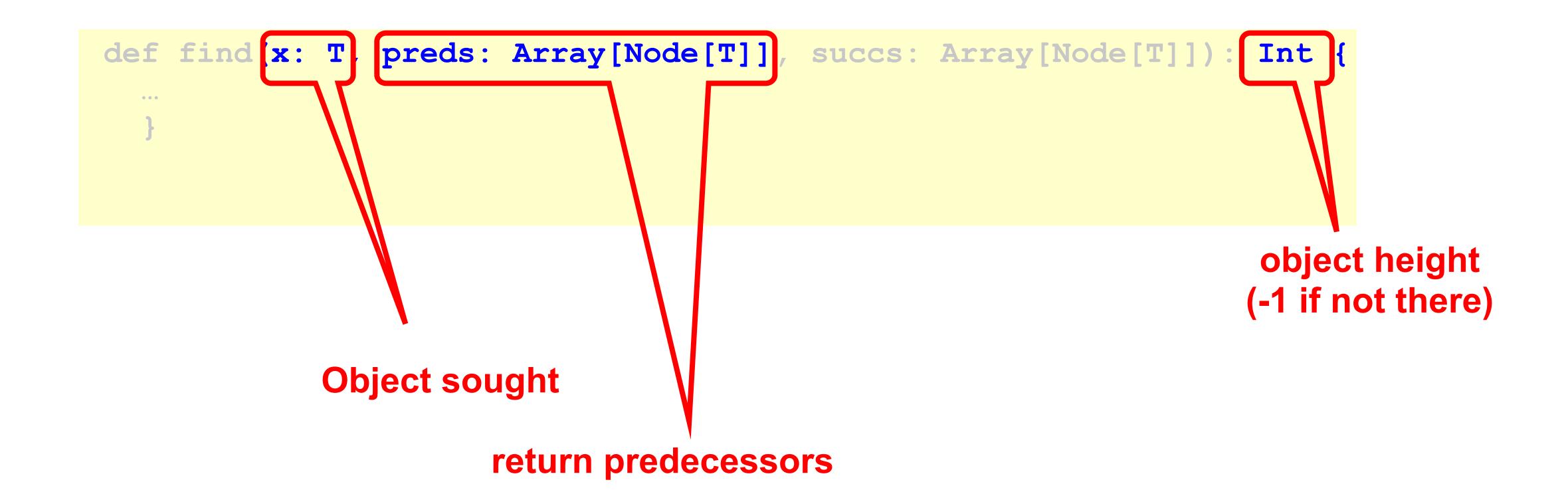
- Property: Each pointer at layer i jumps over roughly 2<sup>i</sup> nodes
- Pick node heights randomly so property guaranteed probabilistically

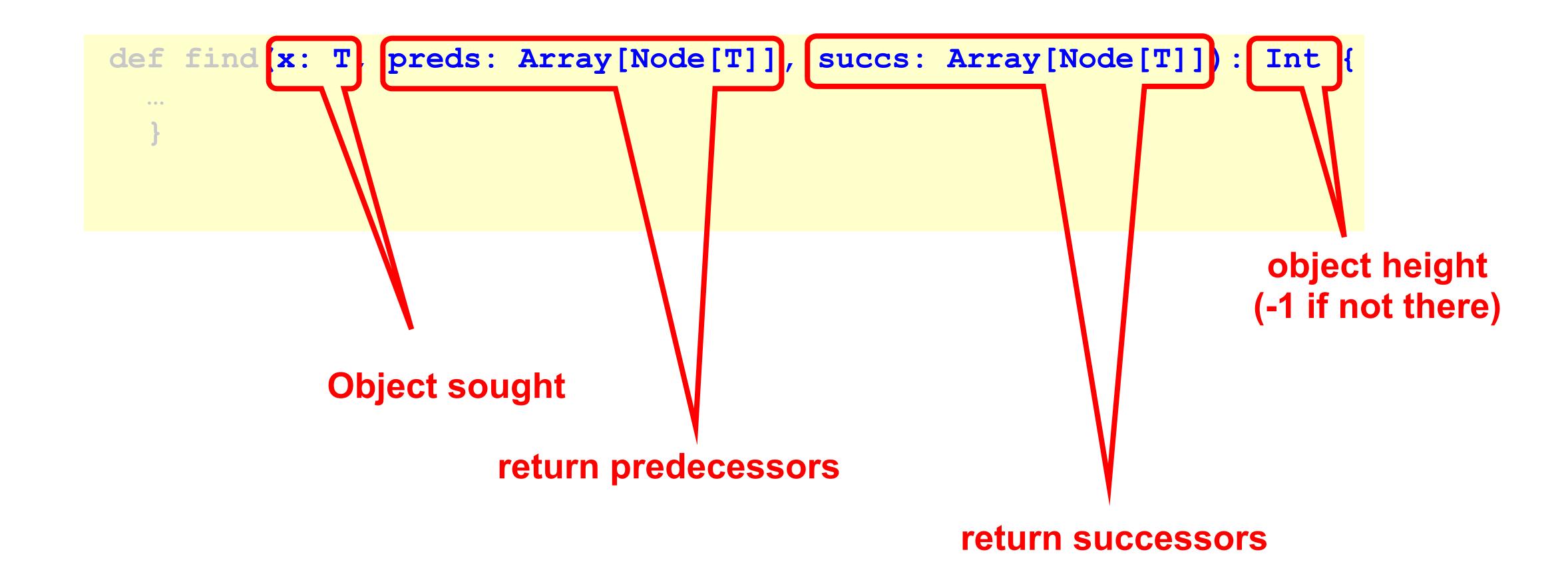


```
def find(x: T, preds: Array[Node[T]], succs: Array[Node[T]]): Int {
    ...
}
```

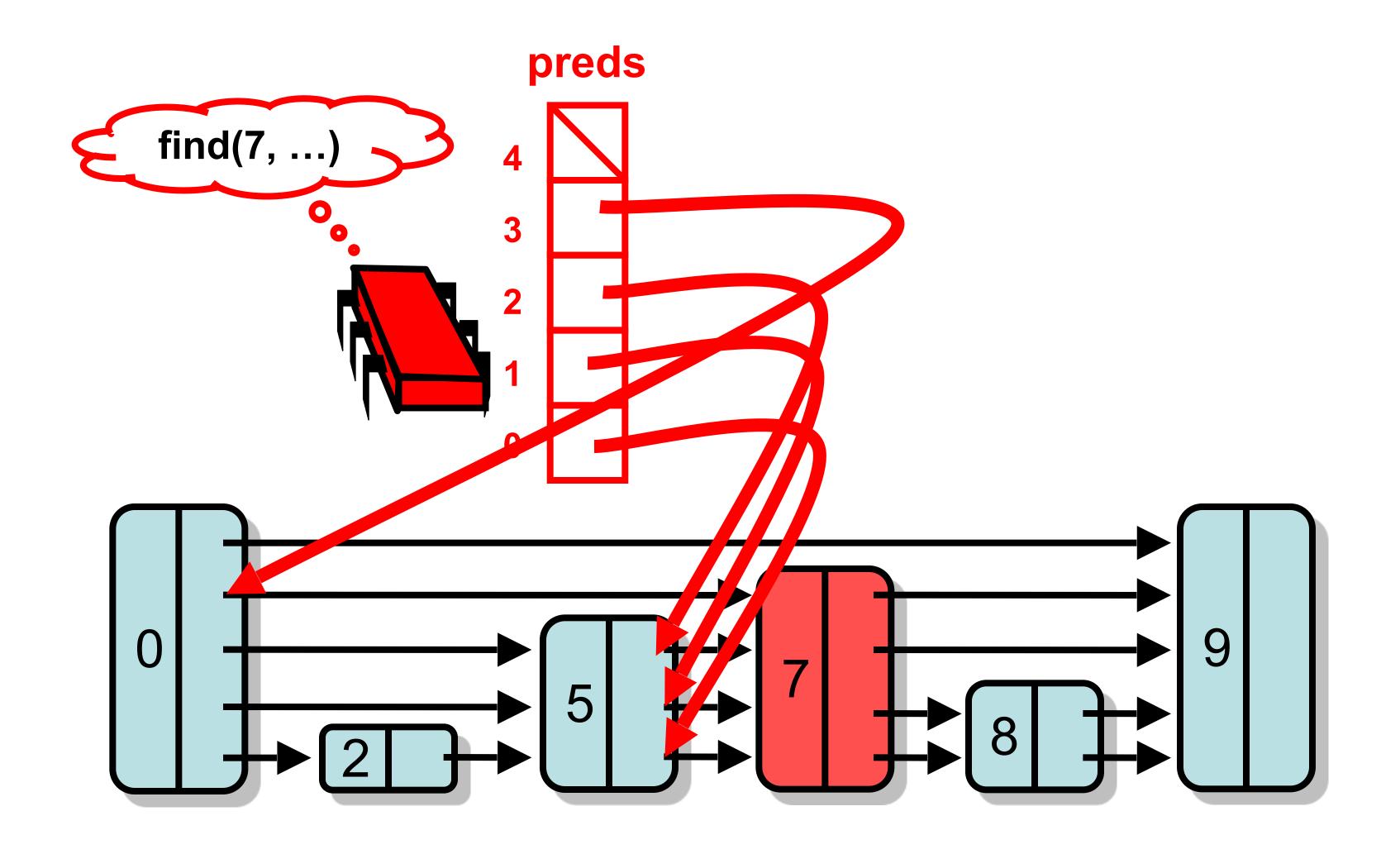
```
def find(x: T, preds: Array[Node[T]], succs: Array[Node[T]]): Int {
    ...
  }
  object height
  (-1 if not there)
```



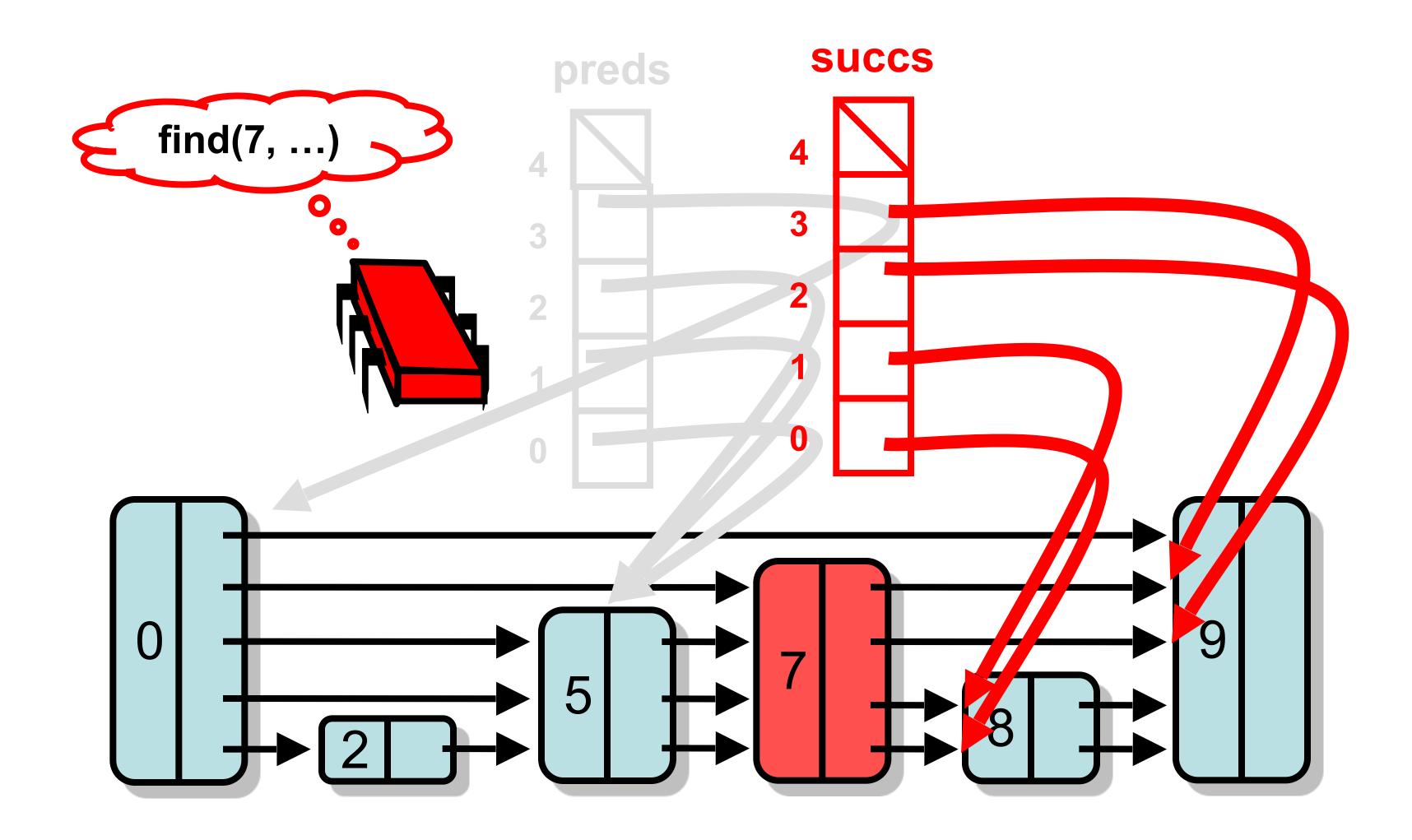




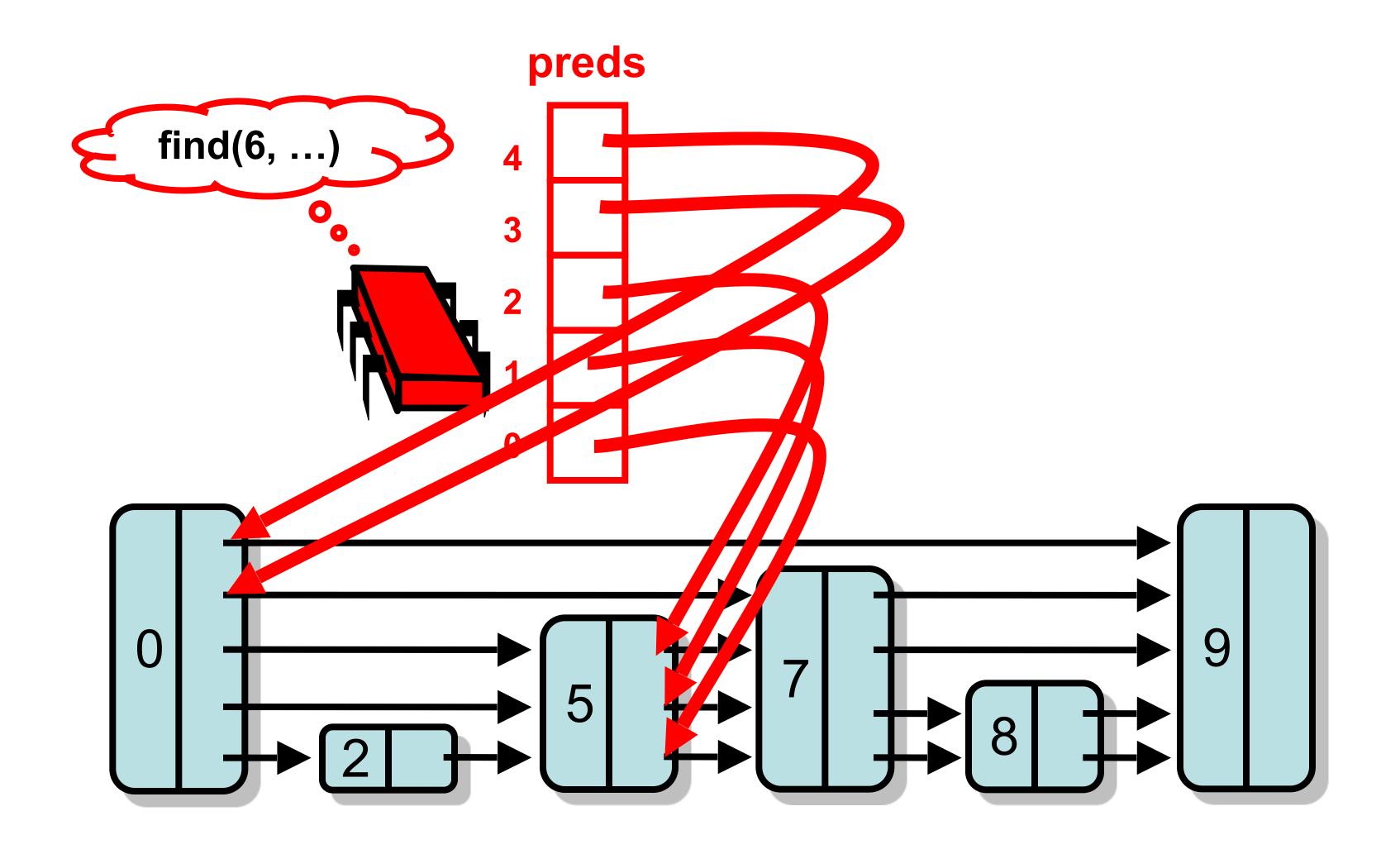
#### Successful Search



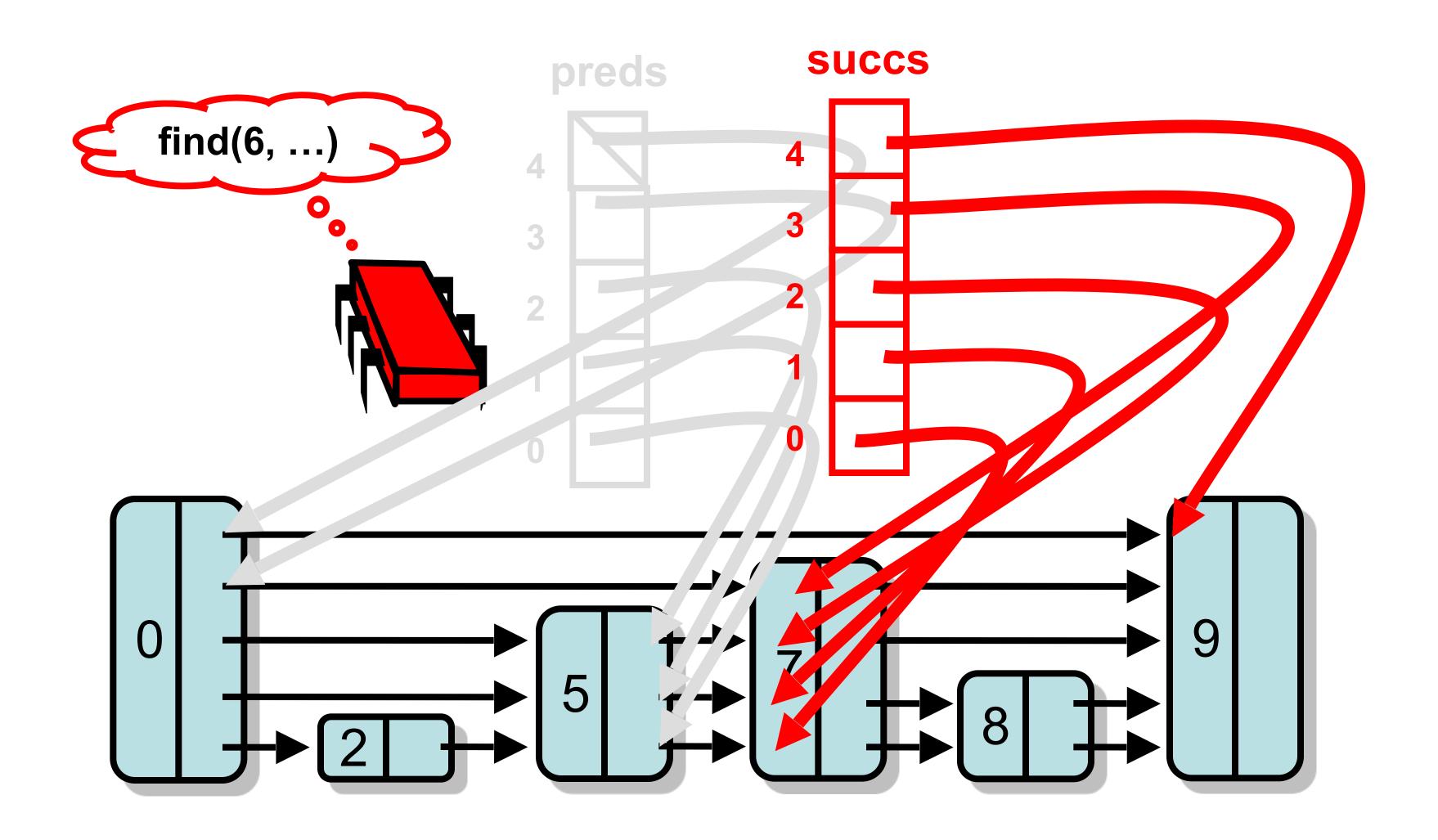
#### Successful Search



#### Unsuccessful Search



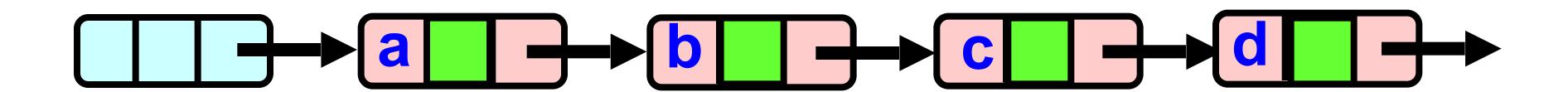
#### Unsuccessful Search

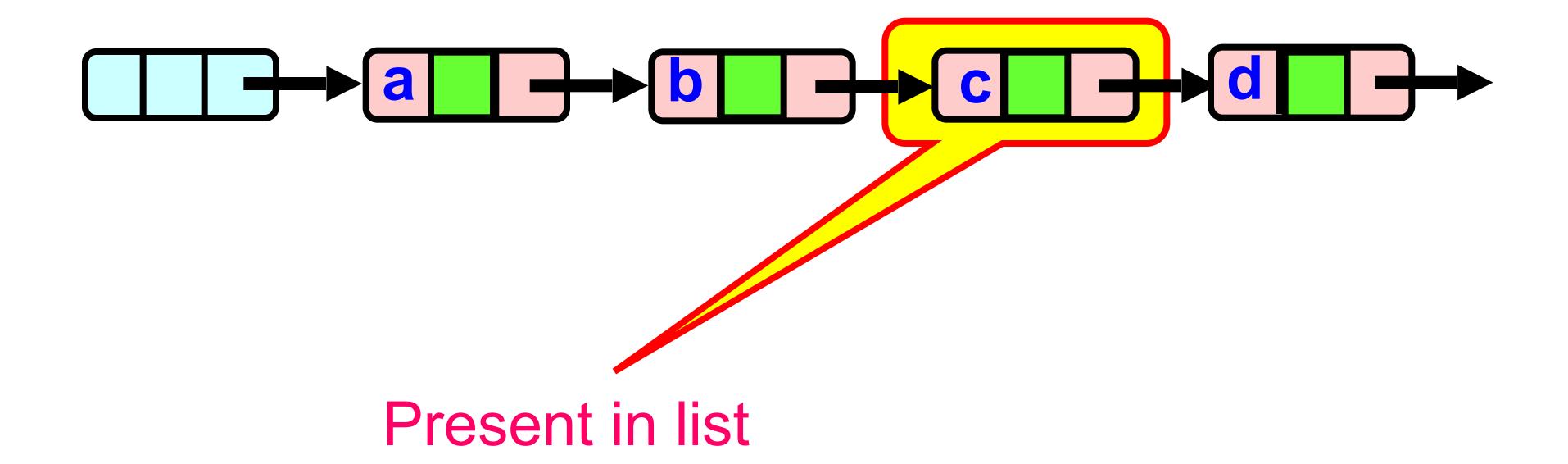


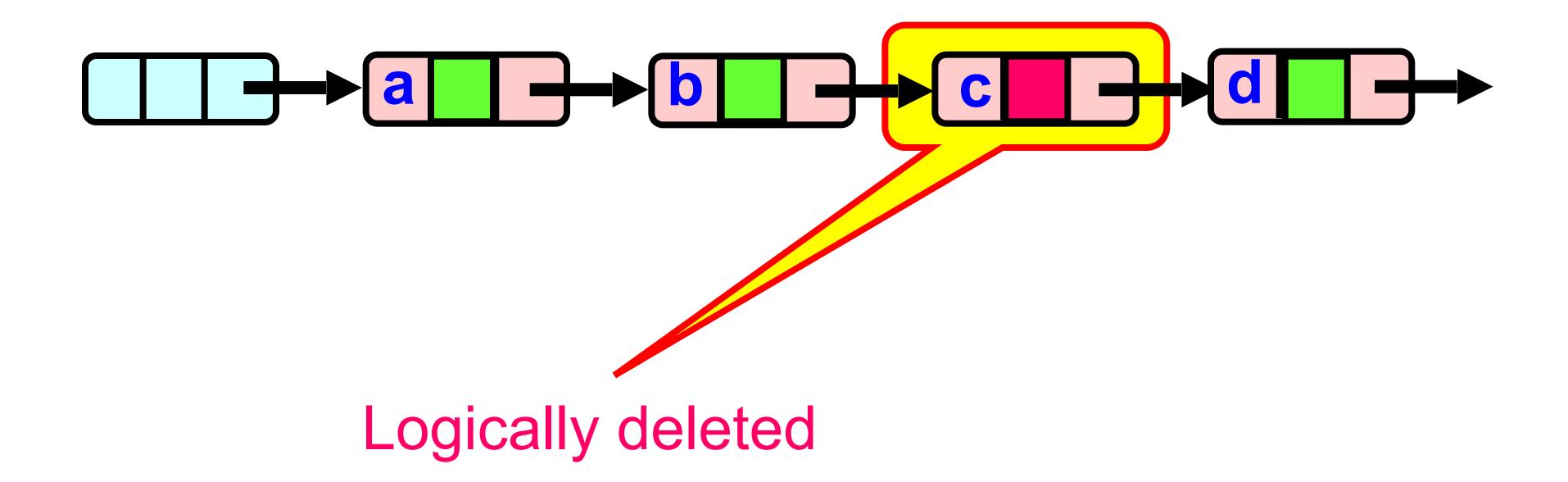
# An Example (Sequential)

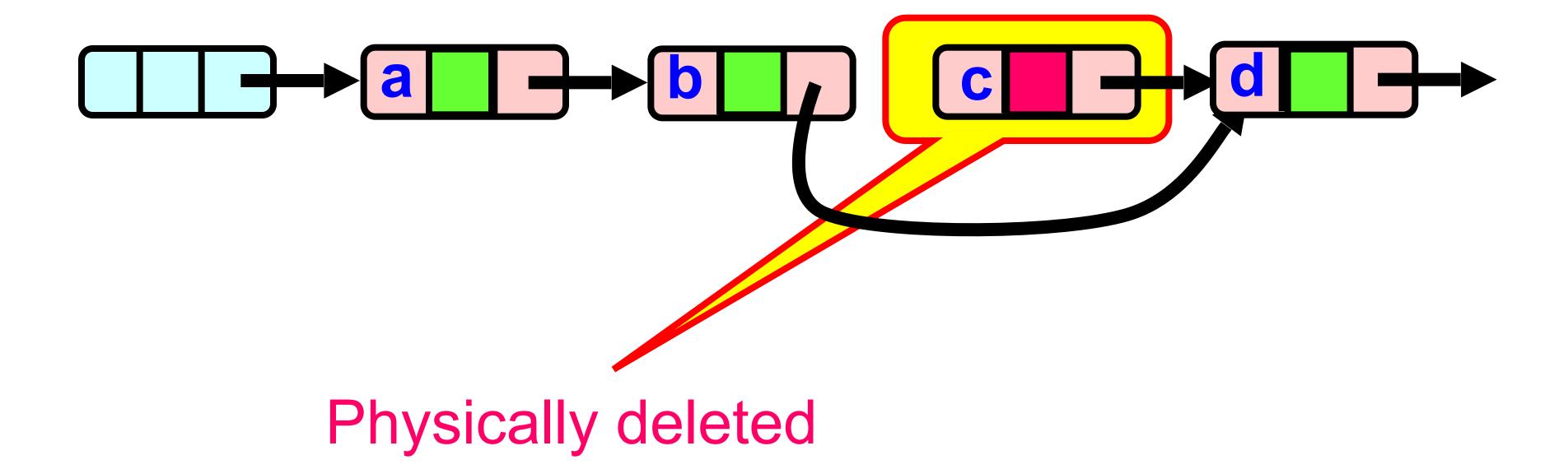
# Lazy Skip List

- Mix blocking and non-blocking techniques:
  - Use optimistic-lazy locking for add() and remove()
  - Wait-free contains()
- Remember: typically lots of contains() calls but few add() and remove()



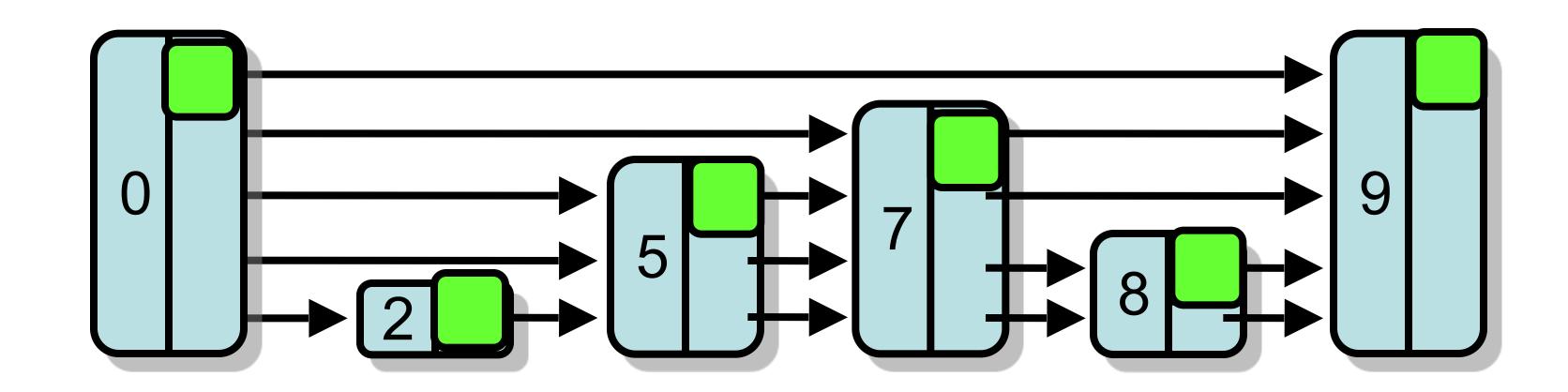




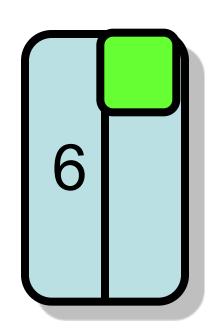


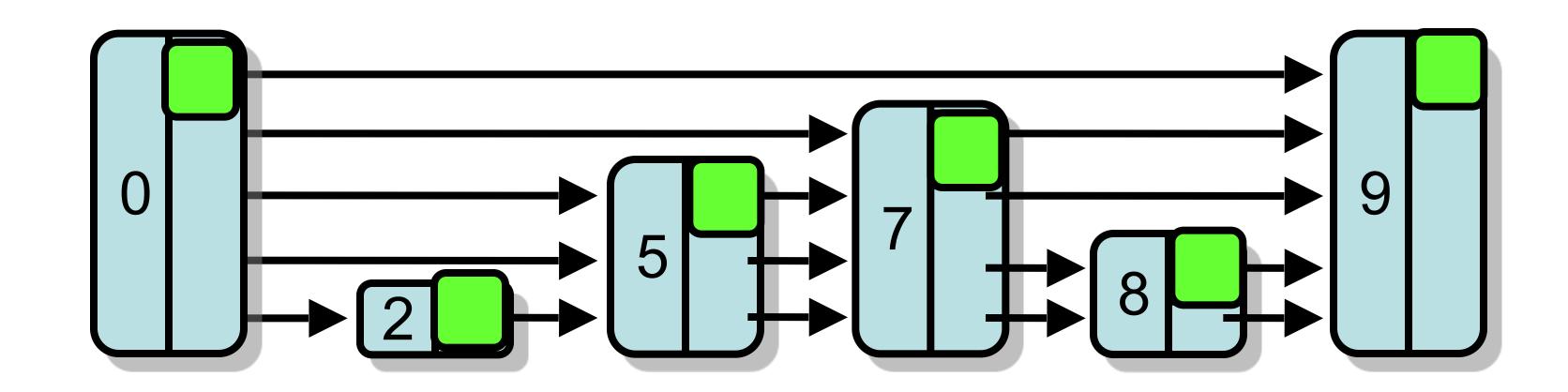
# Lazy Skip Lists

Use a mark bit for logical deletion

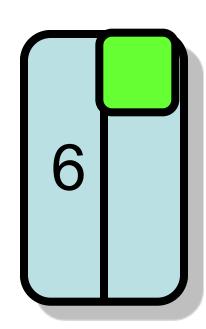


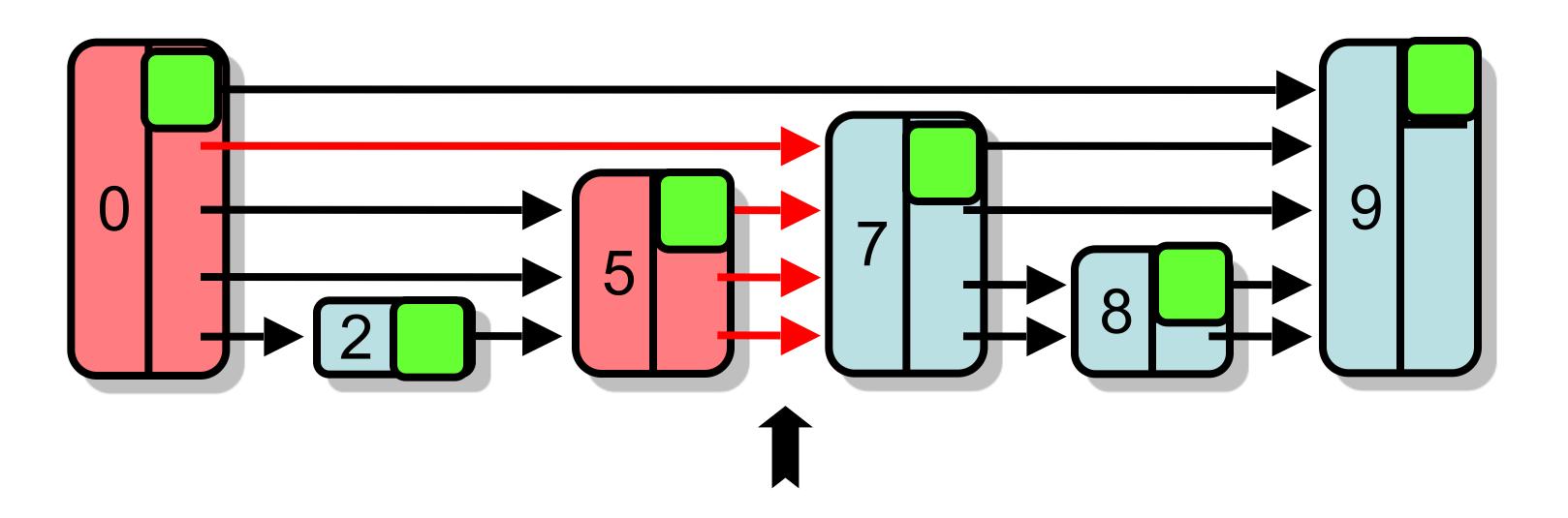
Create node of (random) height 4



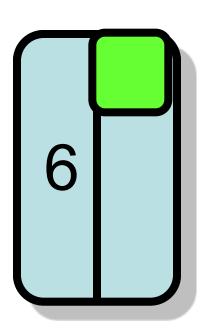


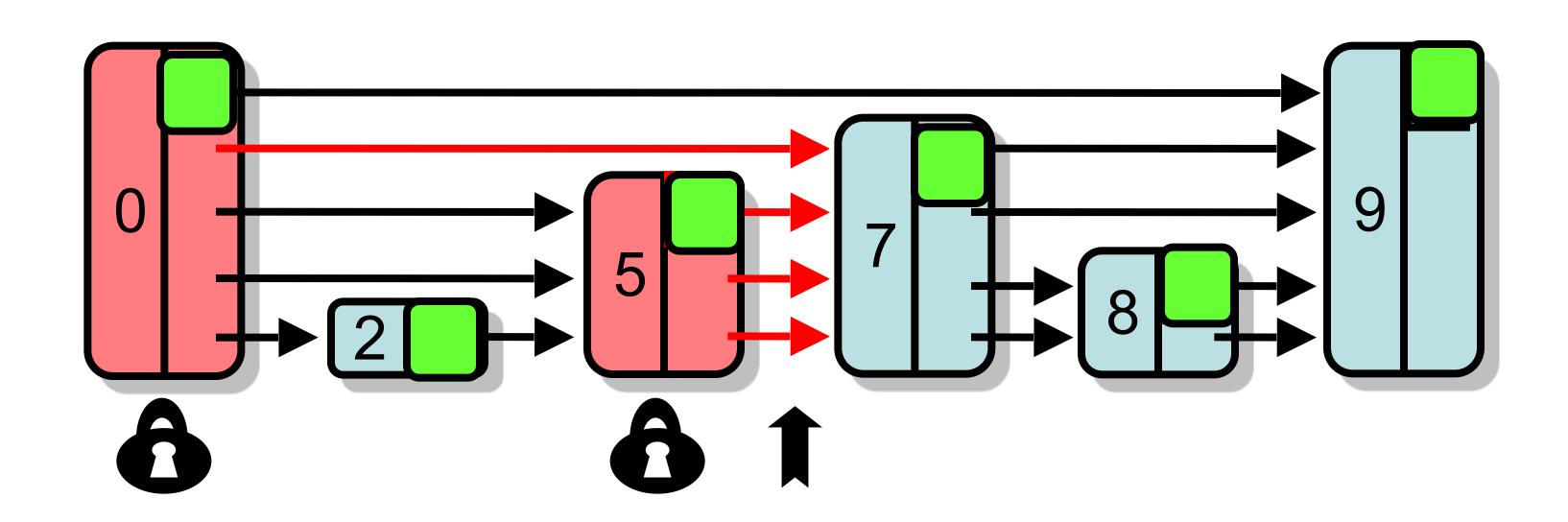
• find() predecessors





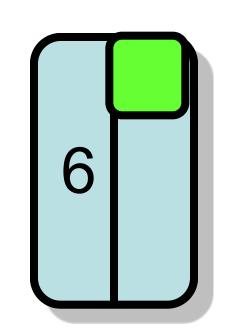
- find() predecessors
- Lock them

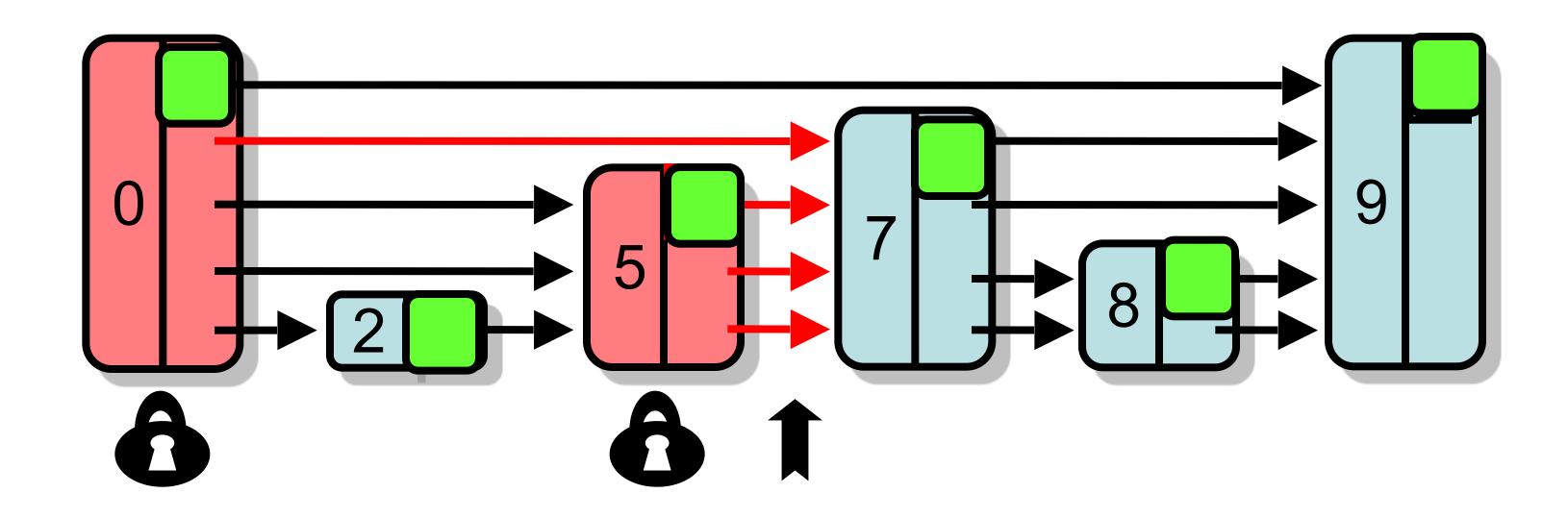




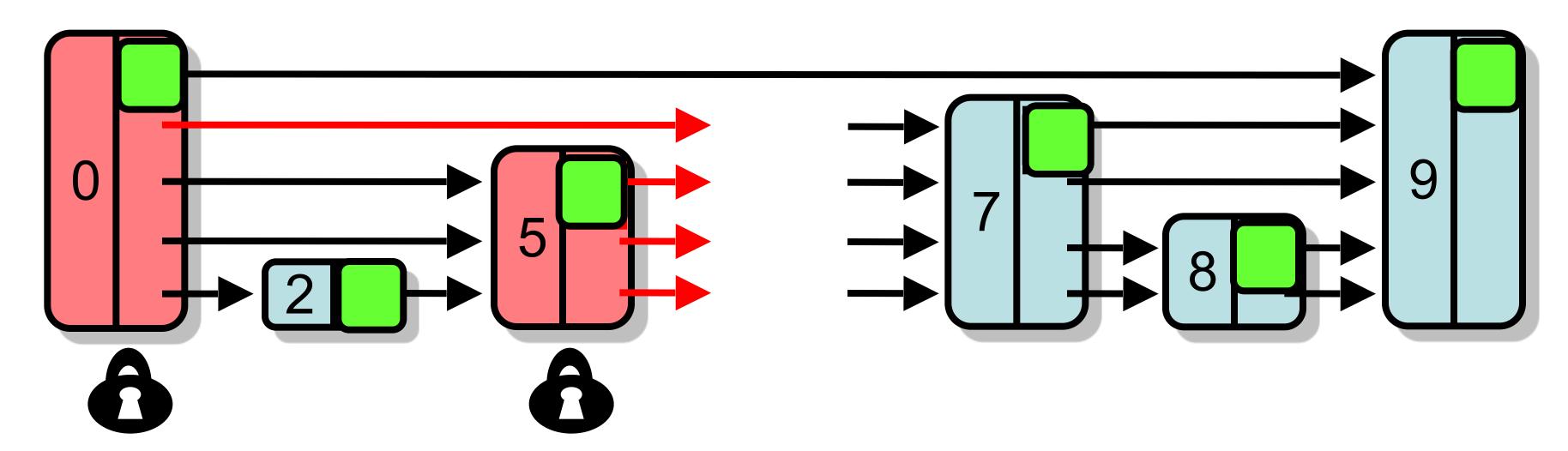
- find() predecessors
- Lock them
- Validate

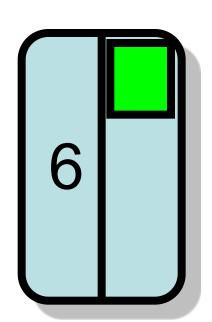
- Optimistic approach



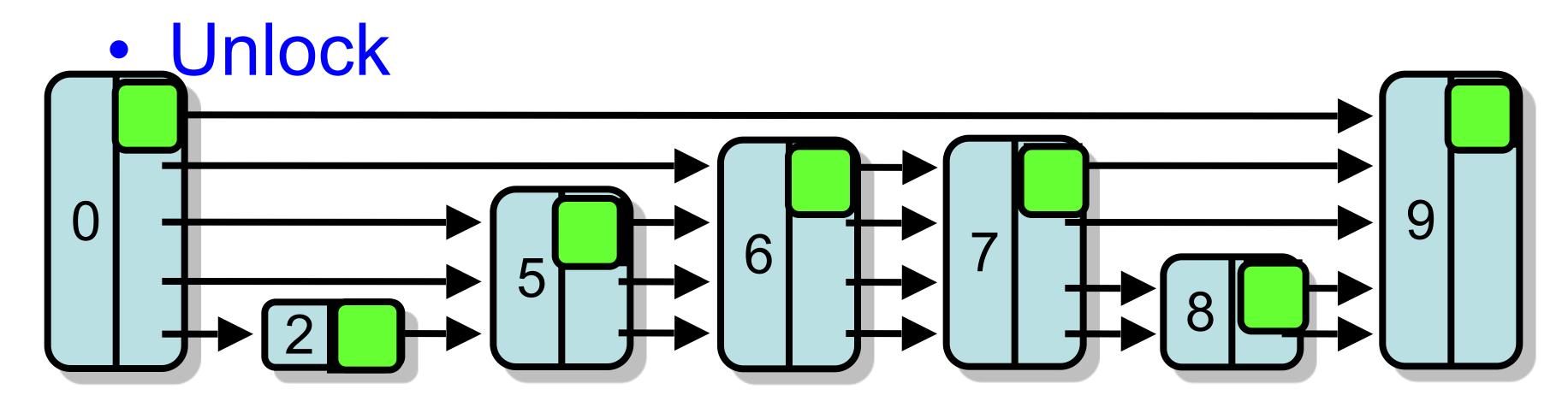


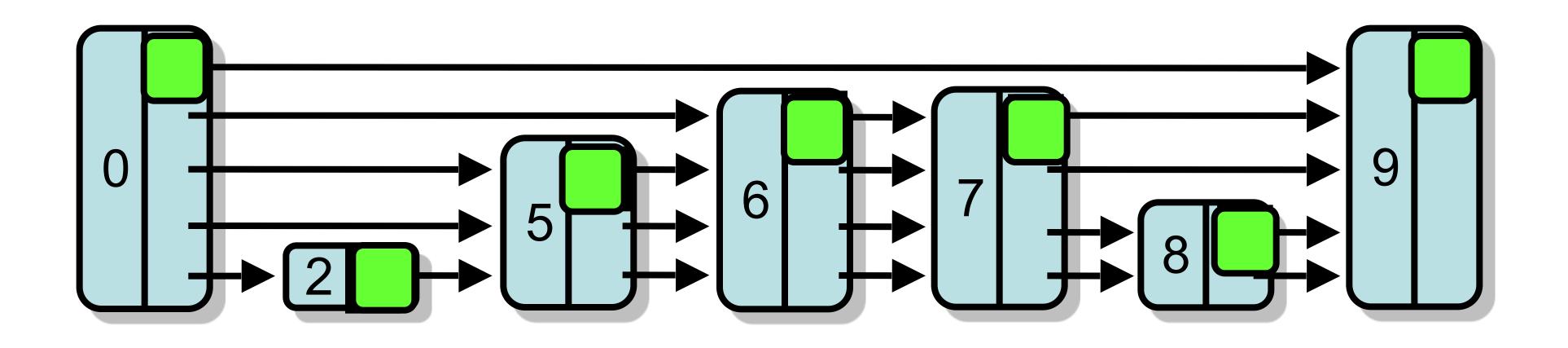
- find() predecessors
- Lock them
- Validate
- Splice



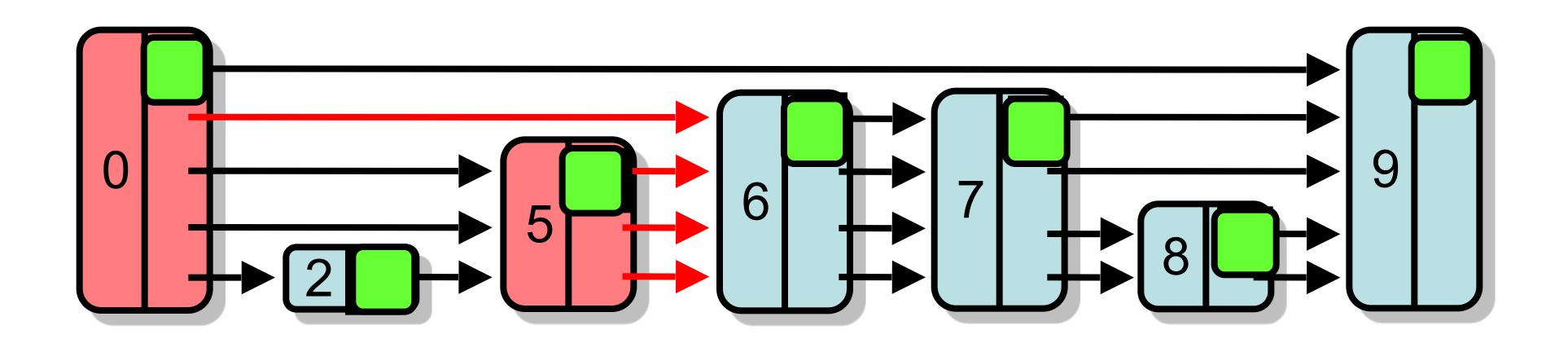


- find() predecessors
- Lock them
- Validate
- Splice

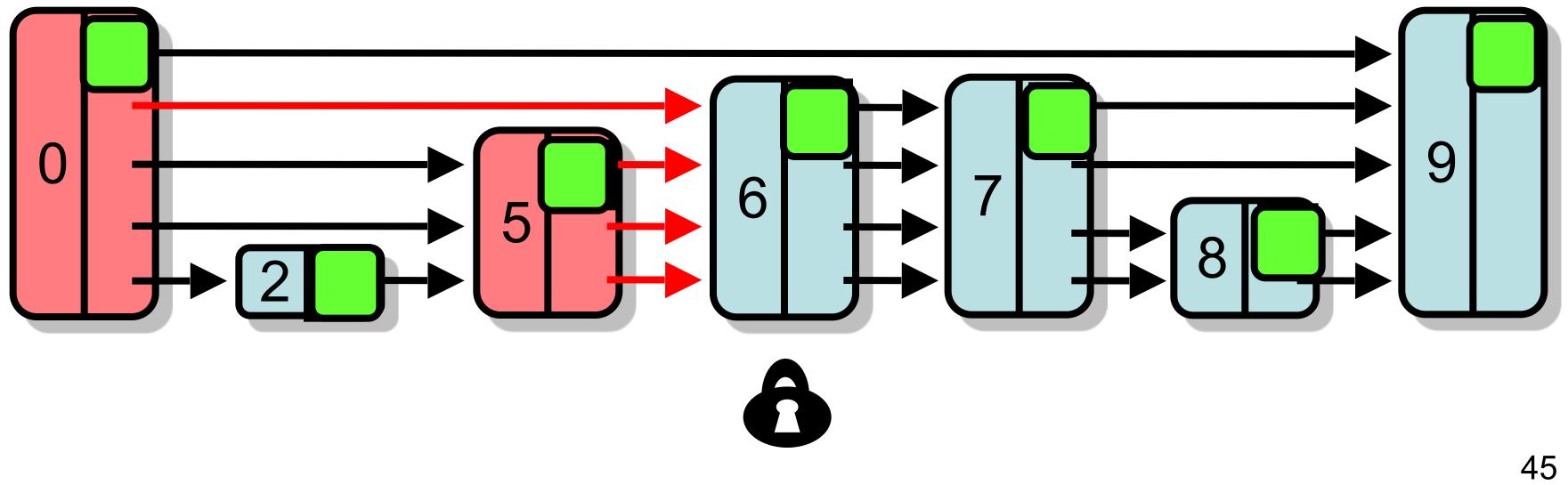




• find() predecessors

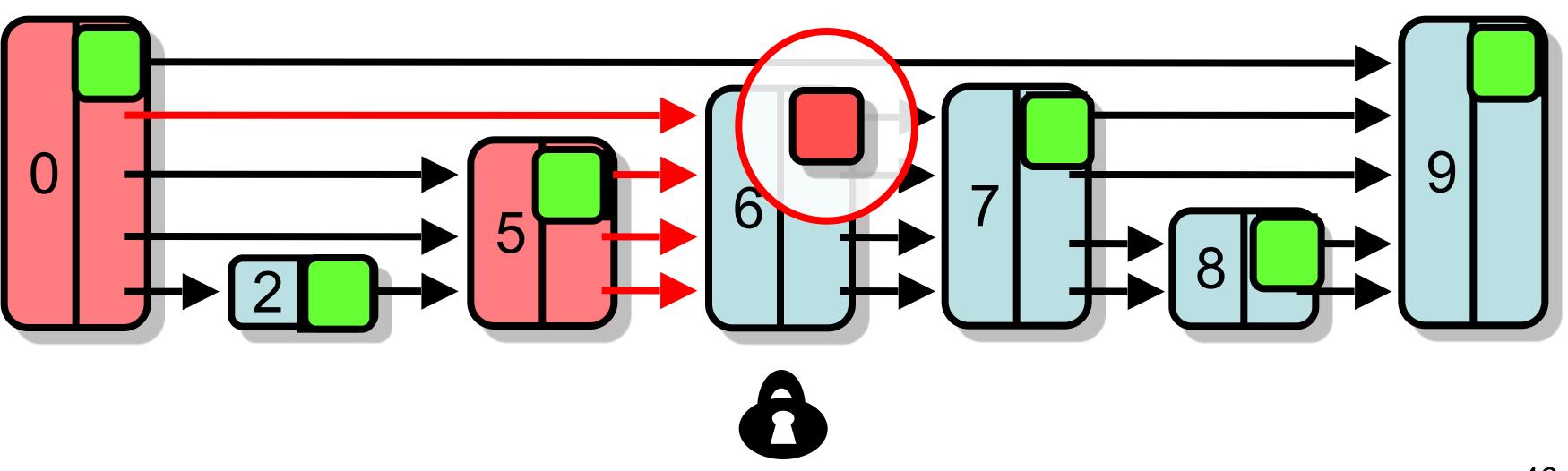


- find() predecessors
- Lock victim

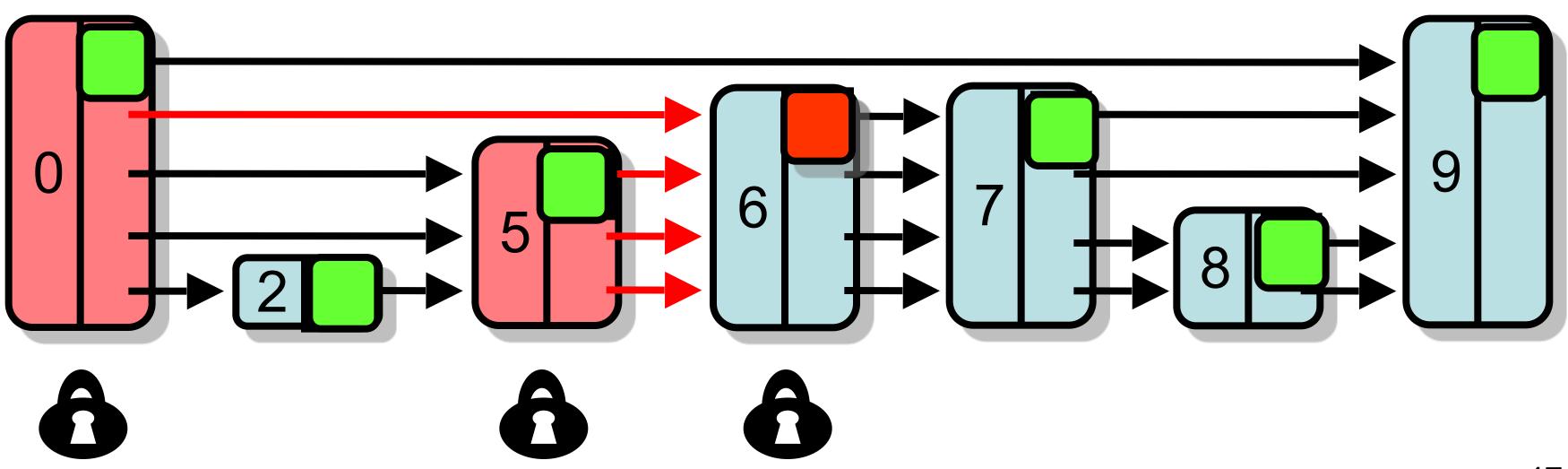


- find() predecessors
- Lock victim
- Set mark (if not already set)

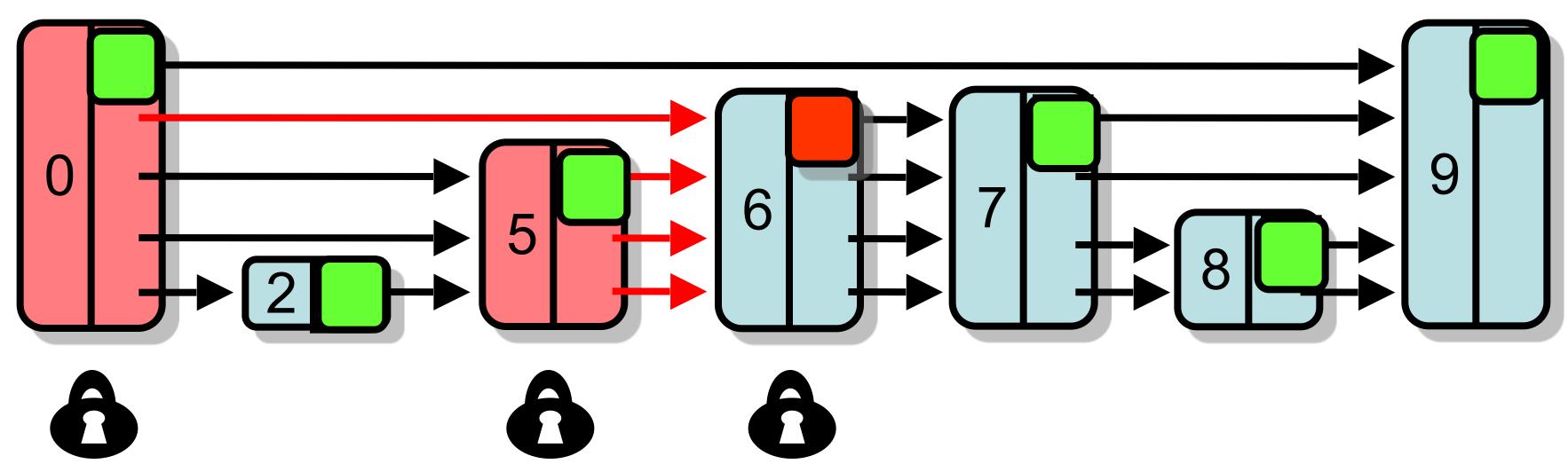
#### Logical remove...



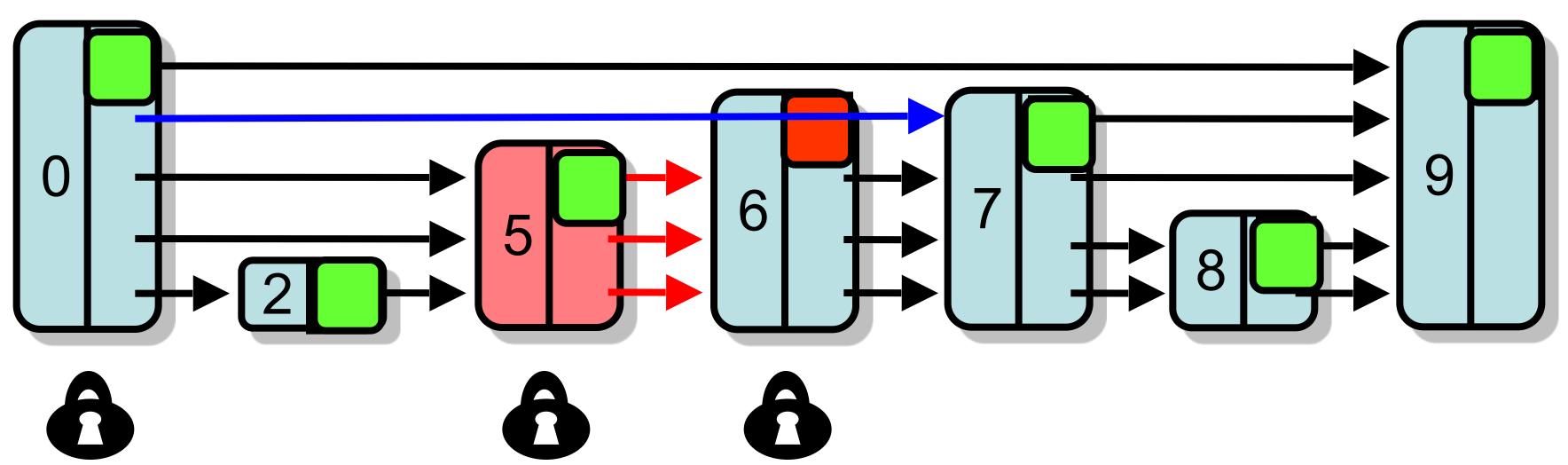
- find() predecessors
- Lock victim
- Set mark (if not already set)
- Lock predecessors (ascending order) & validate



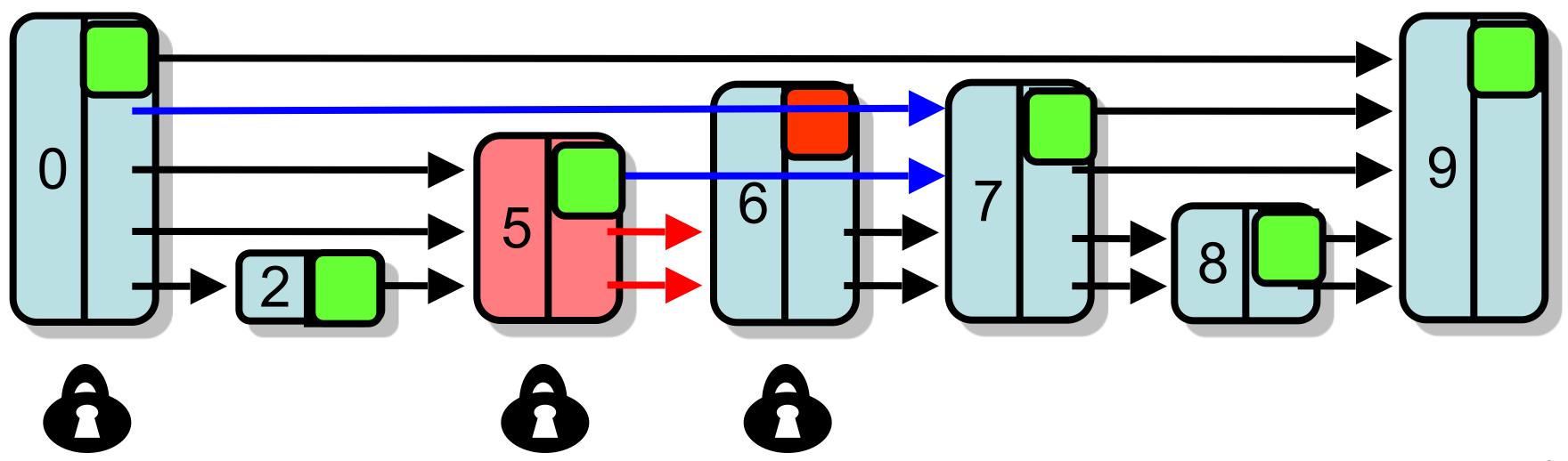
- find() predecessors
- Lock victim
- Set mark (if not already set)
- Lock predecessors (ascending order) & validate
- Physically remove



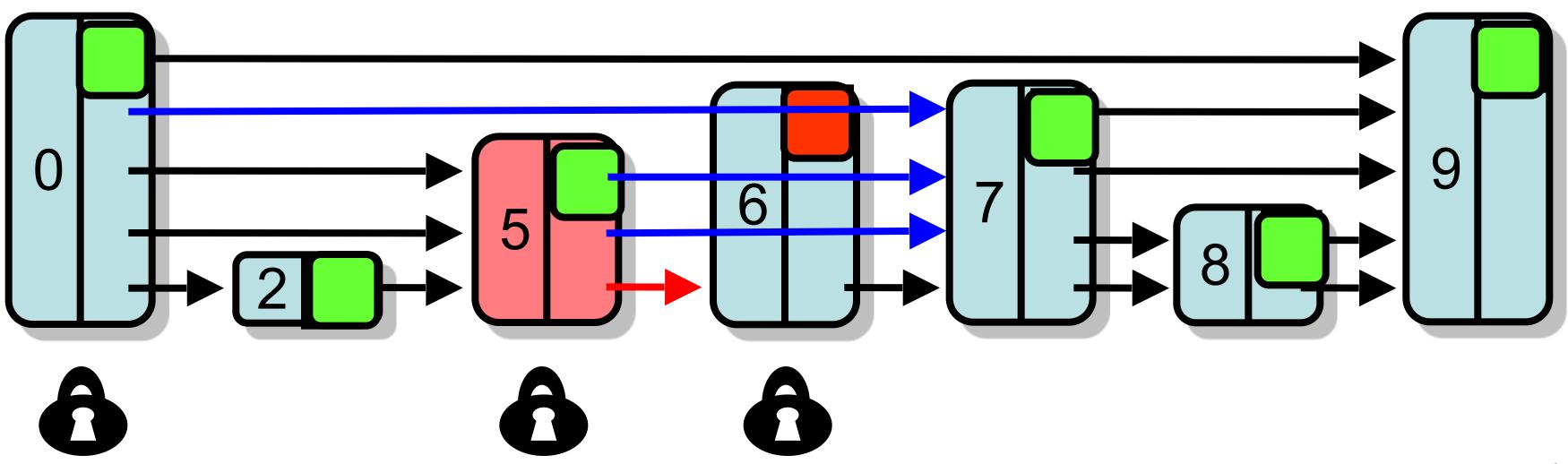
- find() predecessors
- Lock victim
- Set mark (if not already set)
- Lock predecessors (ascending order) & validate
- Physically remove



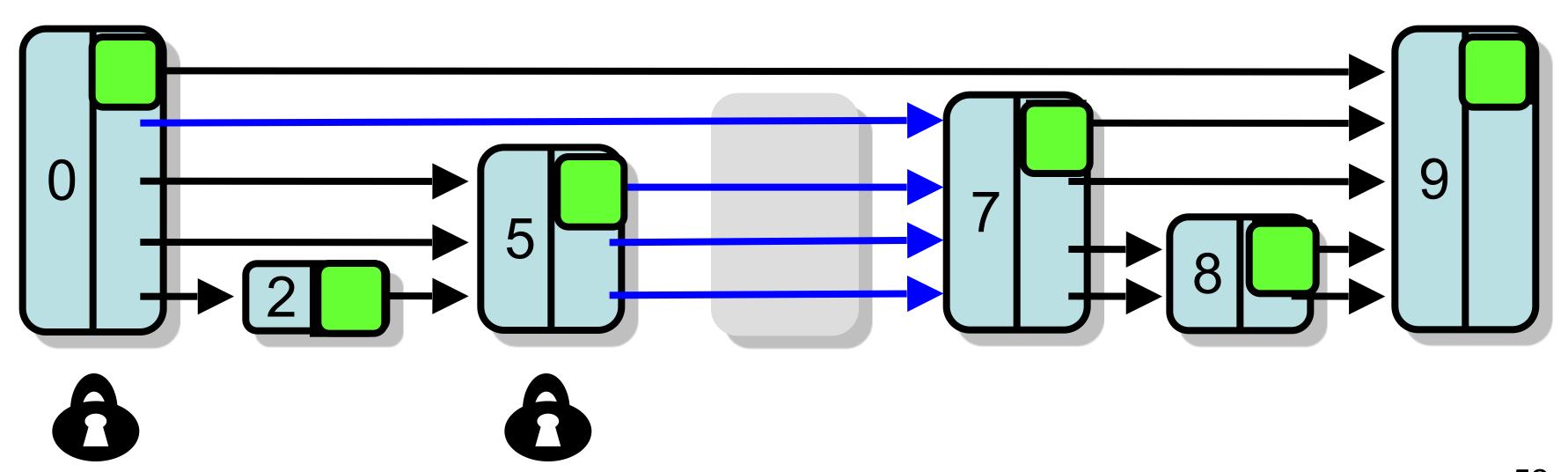
- find() predecessors
- Lock victim
- Set mark (if not already set)
- Lock predecessors (ascending order) & validate
- Physically remove



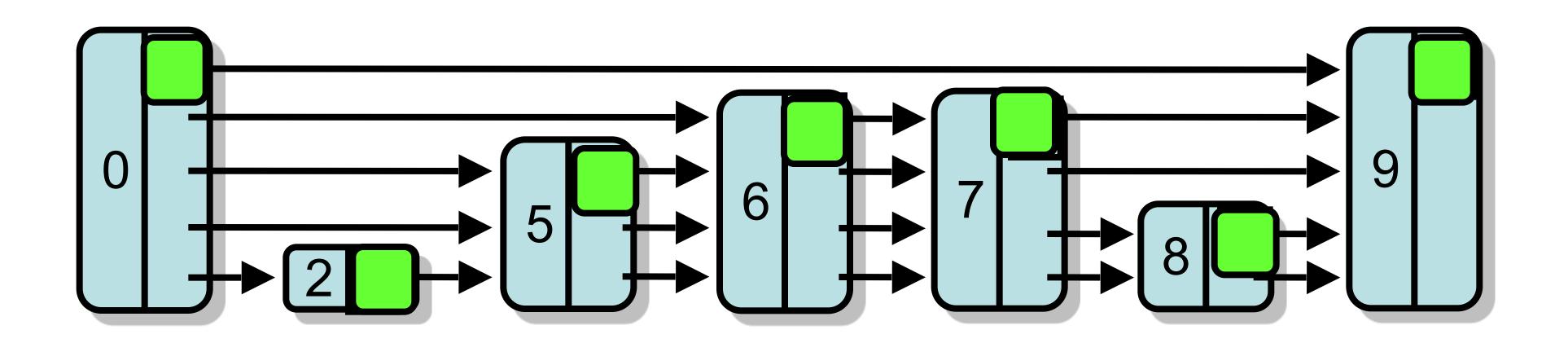
- find() predecessors
- Lock victim
- Set mark (if not already set)
- Lock predecessors (ascending order) & validate
- Physically remove



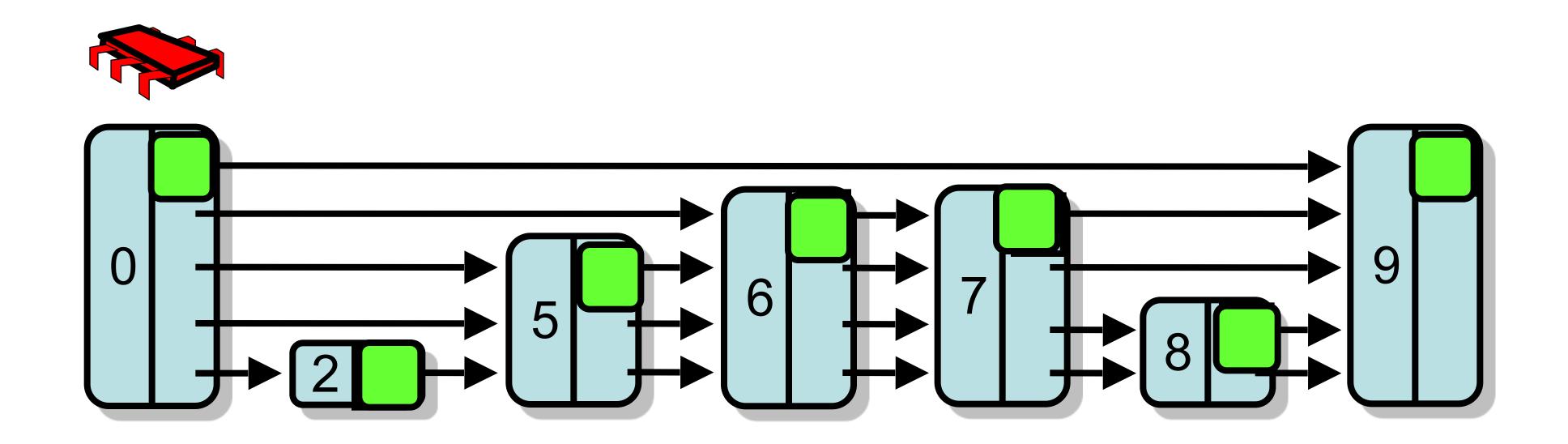
- find() predecessors
- Lock victim
- Set mark (if not already set)
- Lock predecessors (ascending order) & validate
- Physically remove

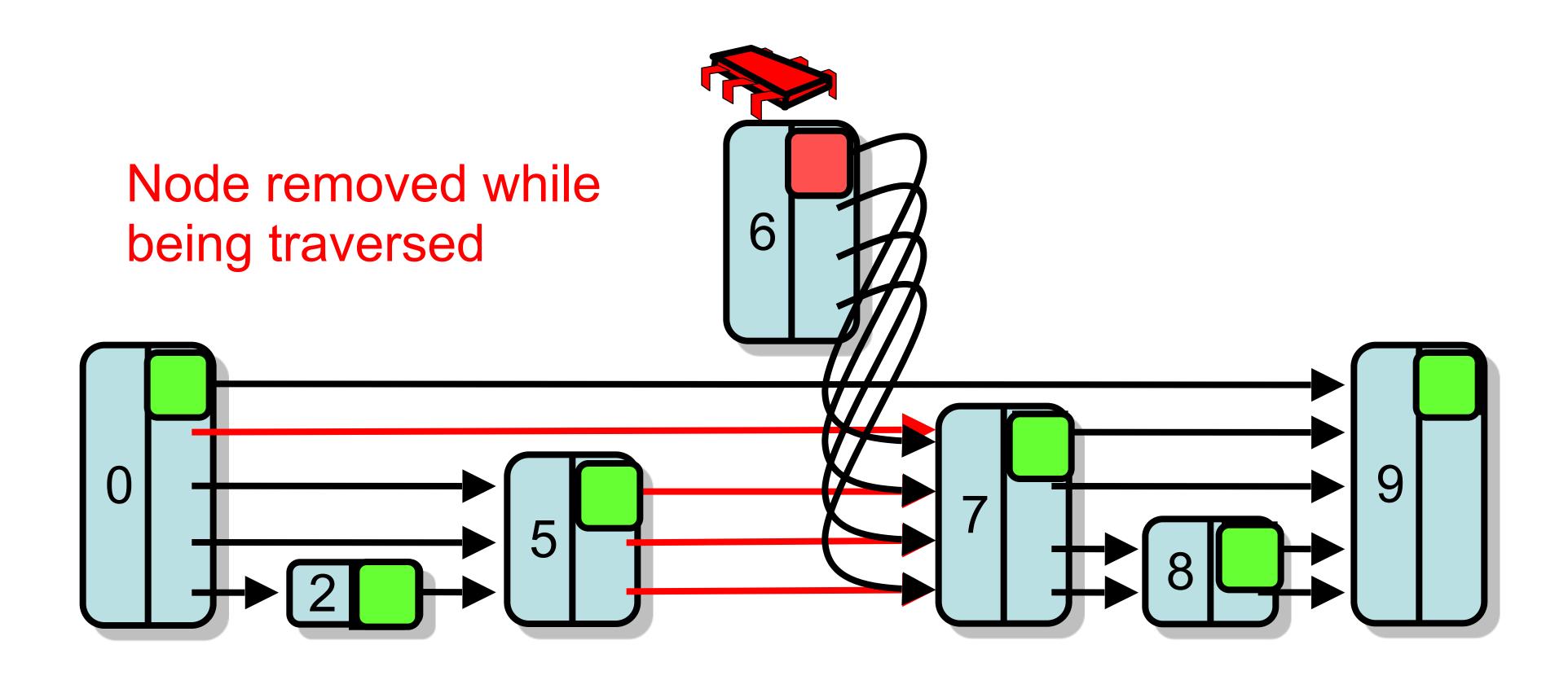


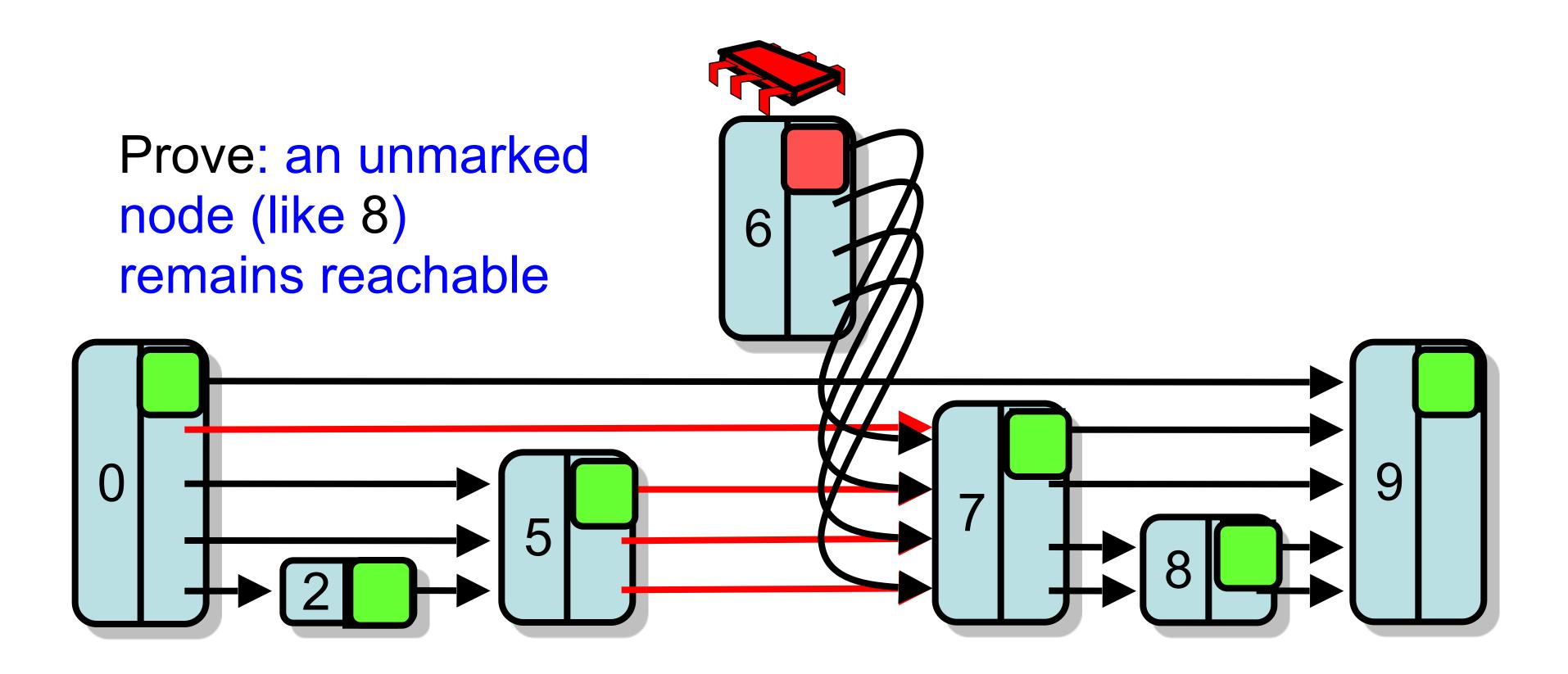
• find() & not marked



#### Node 6 removed while traversed



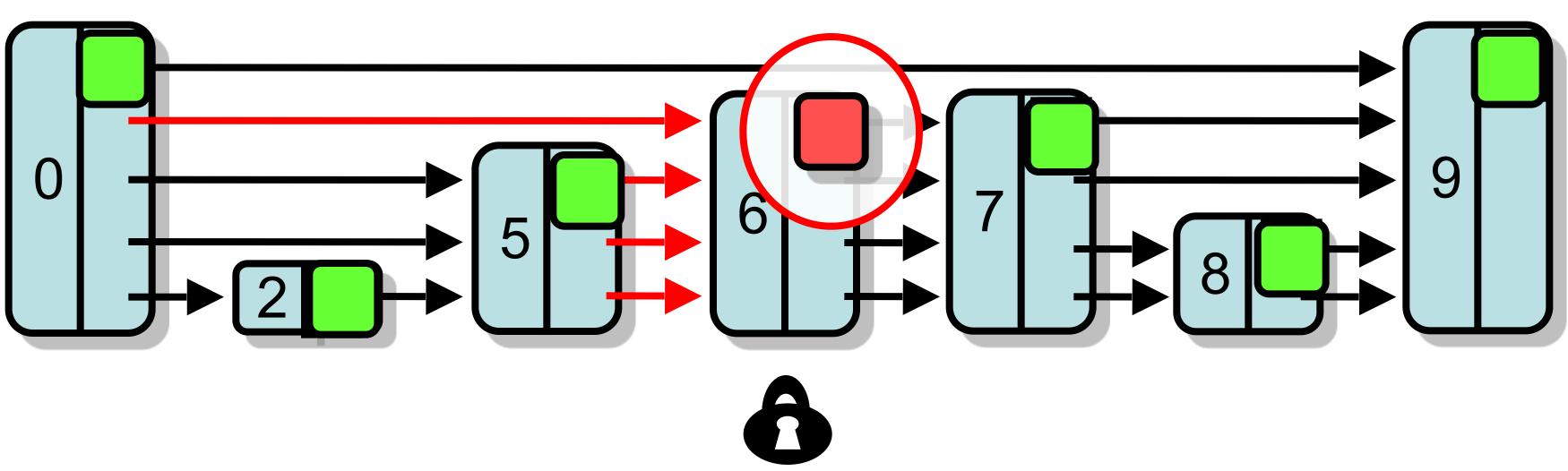




# remove(6): Linearization

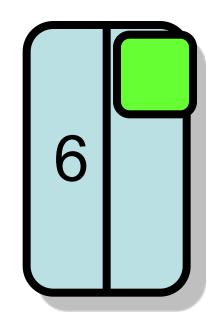
Successful remove happens when bit is set

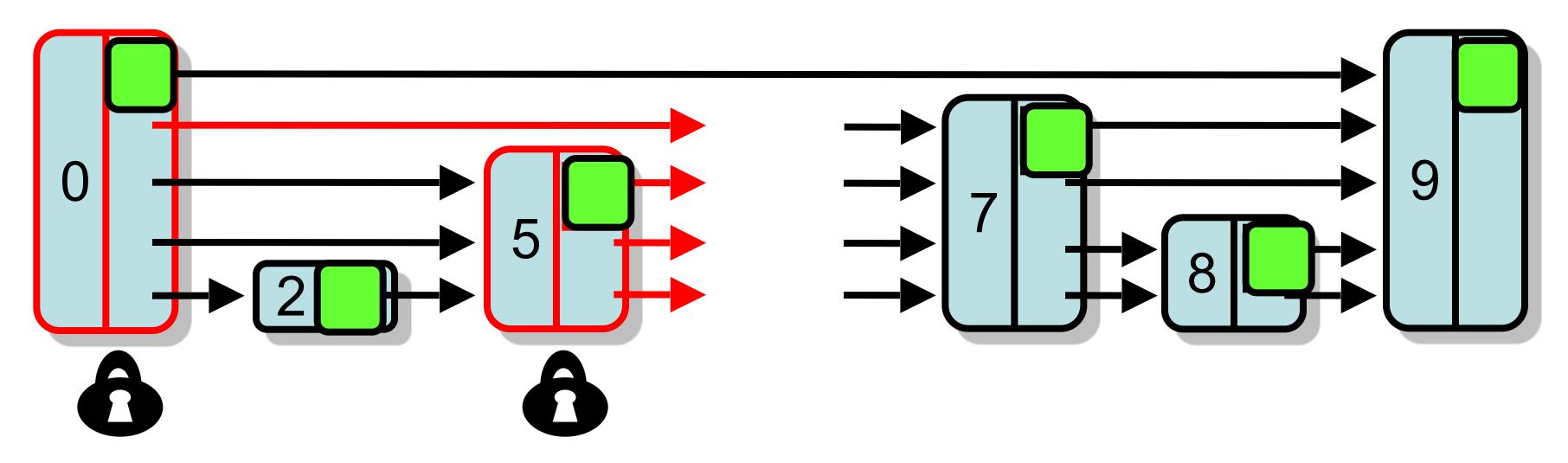
#### Logical remove...



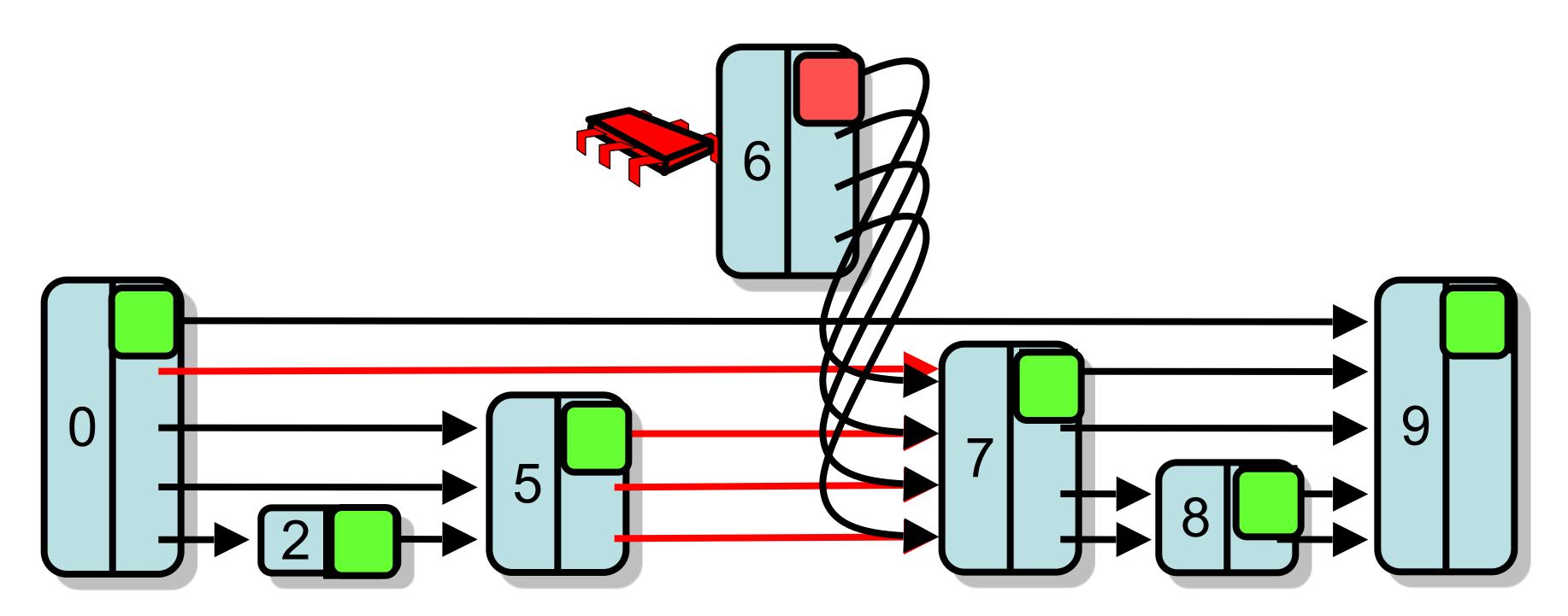
#### Add: Linearization

- Successful add() at point when fully linked
- Add fullyLinked bit to indicate this
- Bit tested by contains()

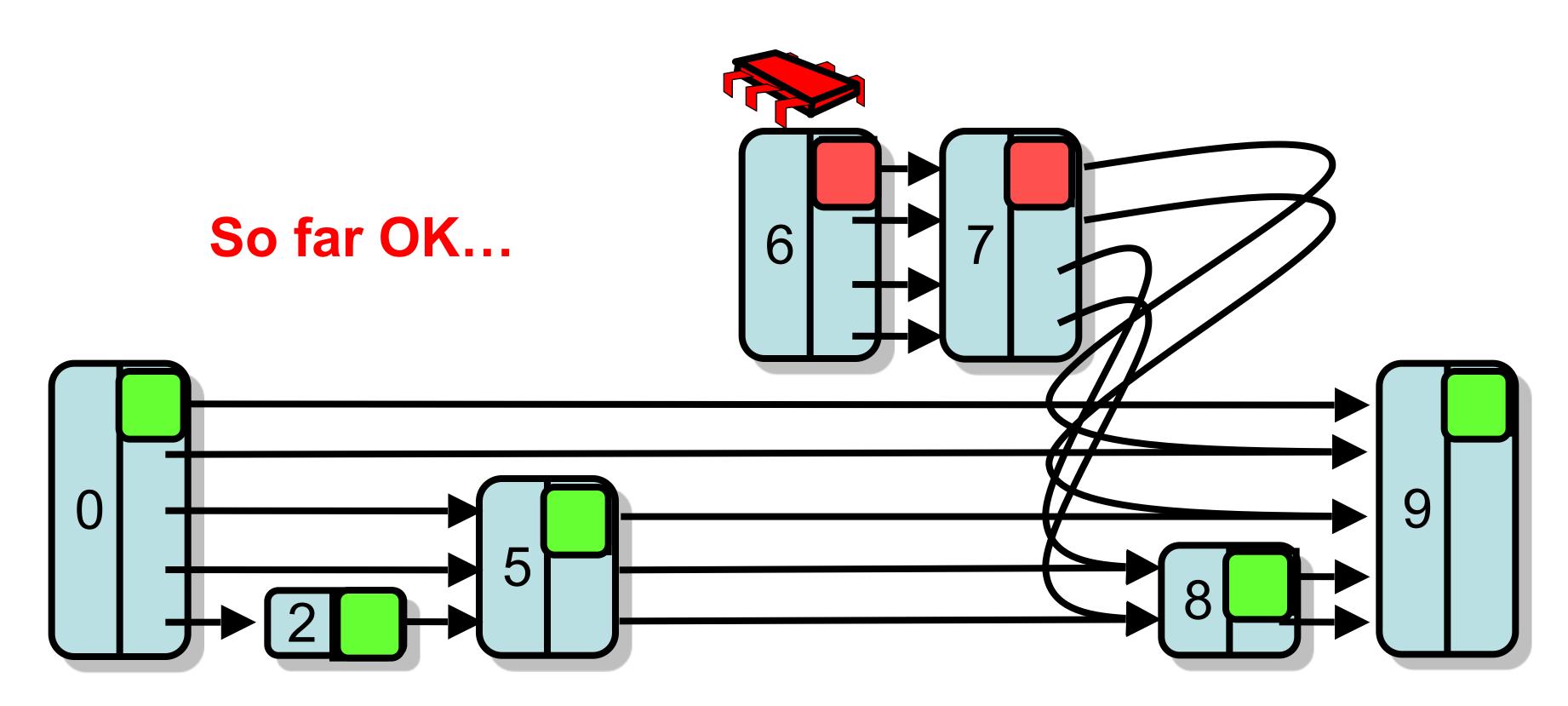




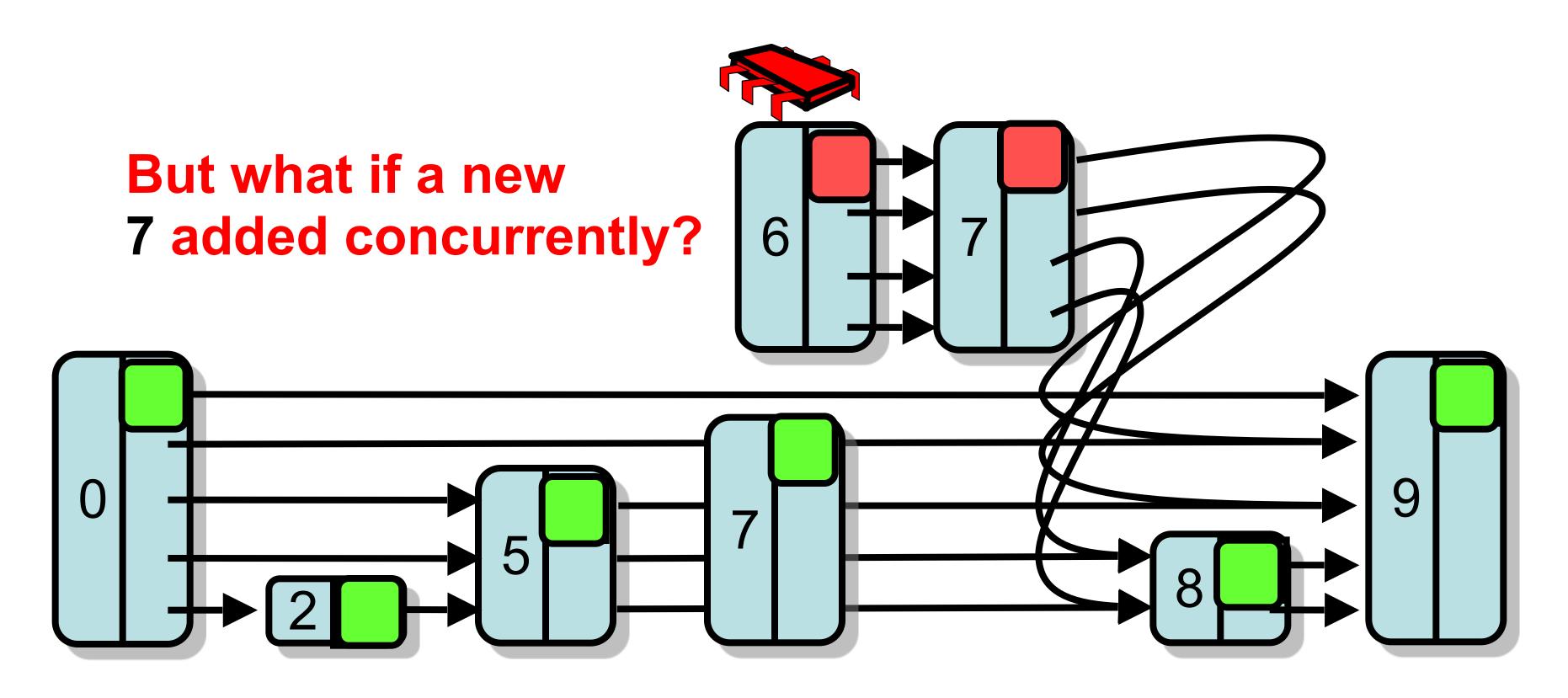
- When fully-linked unmarked node found
- Pause while fullyLinked bit unset



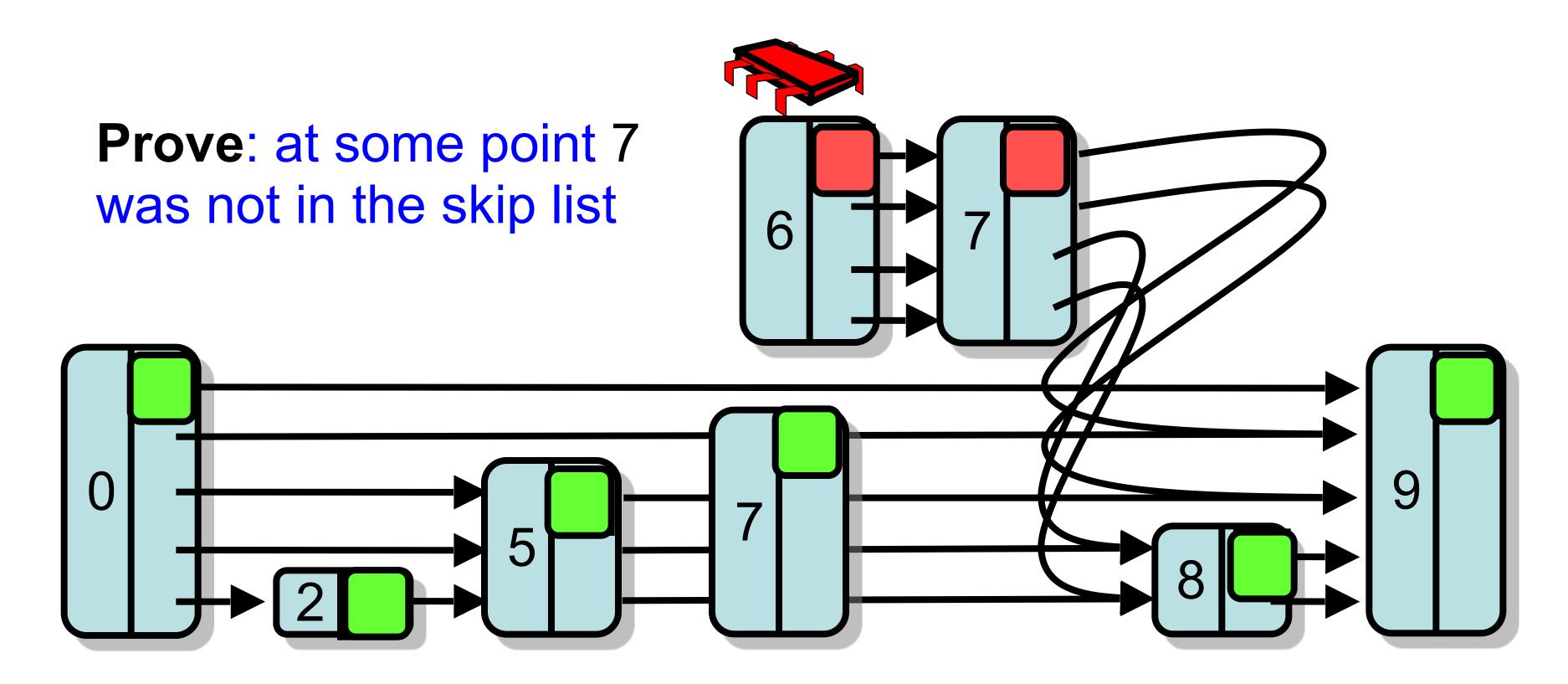
When do we linearize unsuccessful Search?



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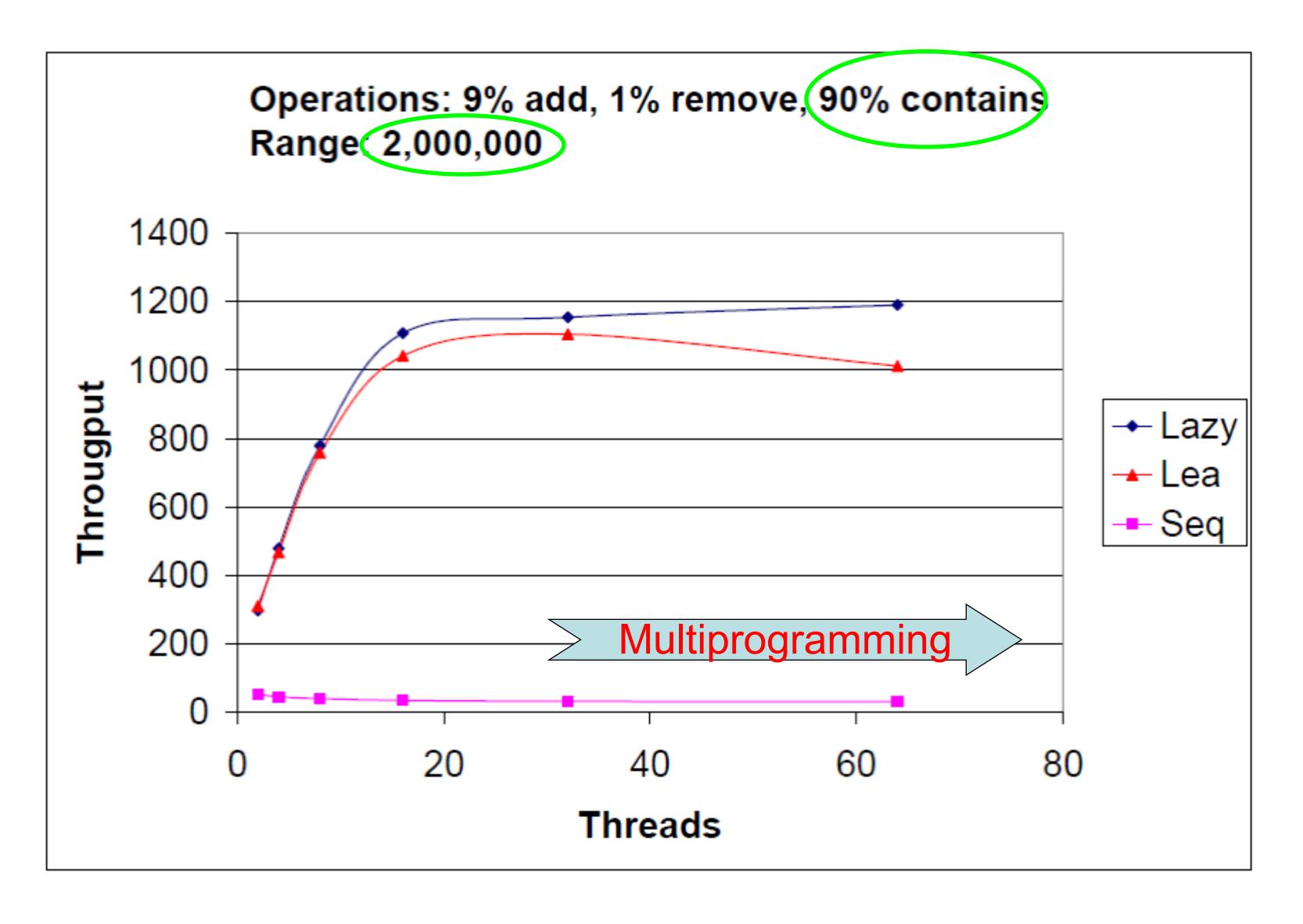
When do we linearize unsuccessful Search?



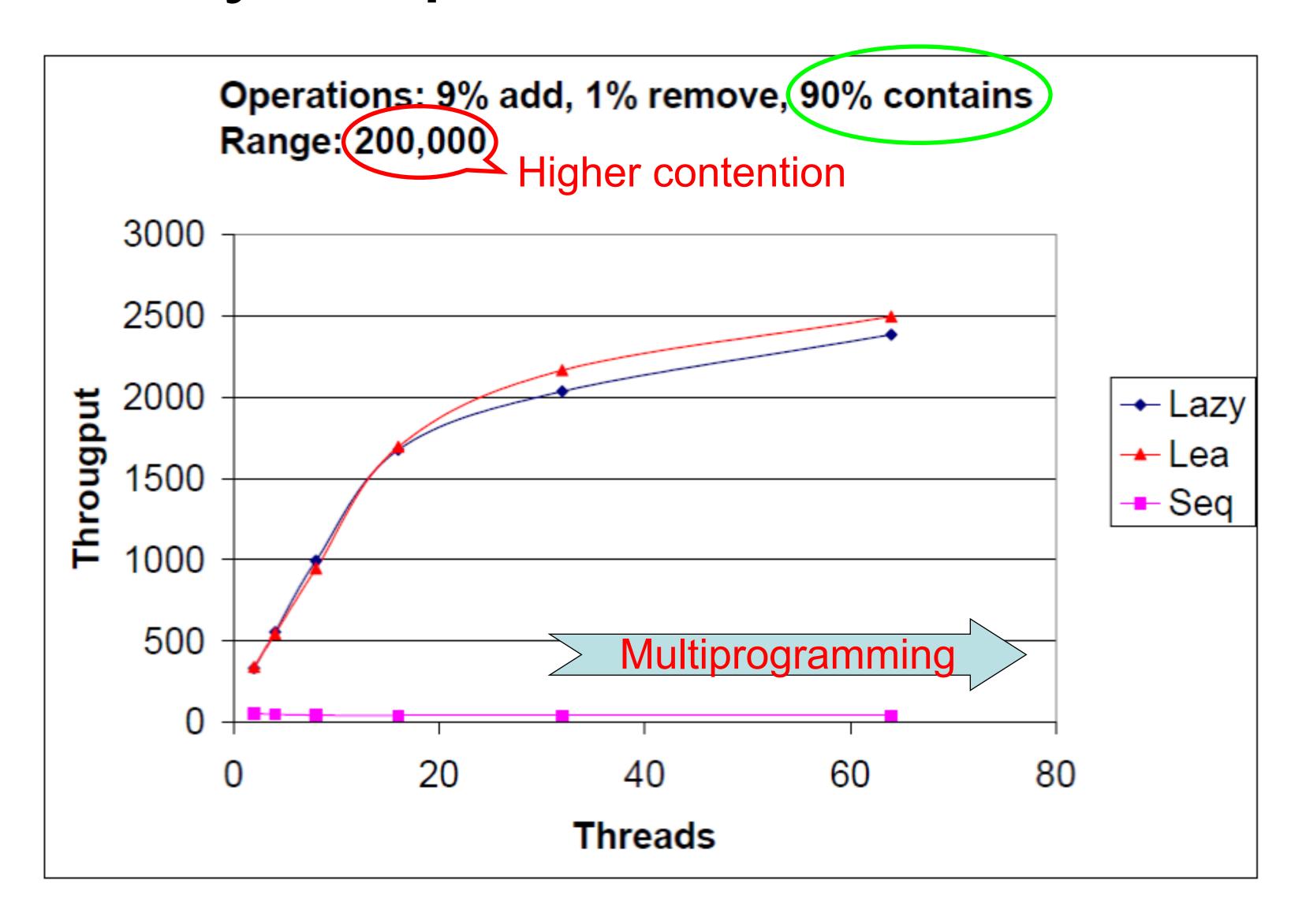
## Coding Time!

- Design a benchmark suite for concurrent set implementations allowing arbitrary numbers of threads and operations.
- Use the ideas from the previous lectures.
- Implement it for optimistic lists, lazy lists and lazy skip-lists and determine the winner!
- Also, let's add Java's concurrent set implementation (by Doug Lea) into the mix

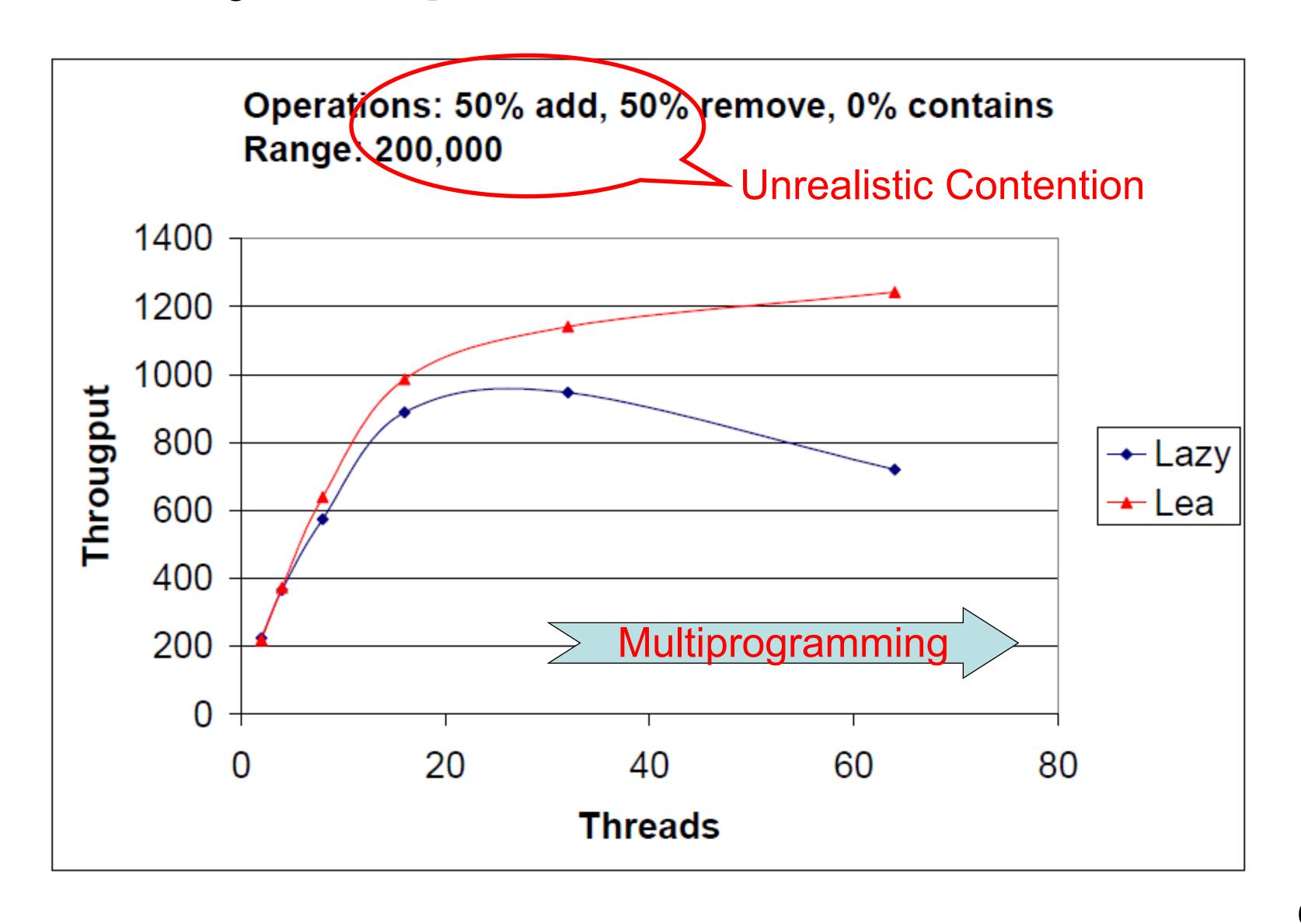
## Lazy Skip List: Performance



## Lazy Skip List: Performance



#### Lazy Skip List: Performance



## Summary

- Lazy Skip List
  - Optimistic fine-grained Locking
- Performs as well as the lock-free solution in "common" cases

This is how you implement a concurrent set.



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