YSC3248: Parallel, Concurrent and Distributed Programming

Concurrent Skip Lists

Set Object Interface

- Collection of elements
- No duplicates
- Methods
 - add() a new element
 - remove() an element
 - contains() if element is present

Many are Cold but Few are Frozen

- Typically high % of contains() calls
- Many fewer add() calls
- And even fewer remove() calls
 - 90% contains()
 - -9% add()
 - 1% remove()
- Folklore?
 - Yes but probably mostly true

Concurrent Sets

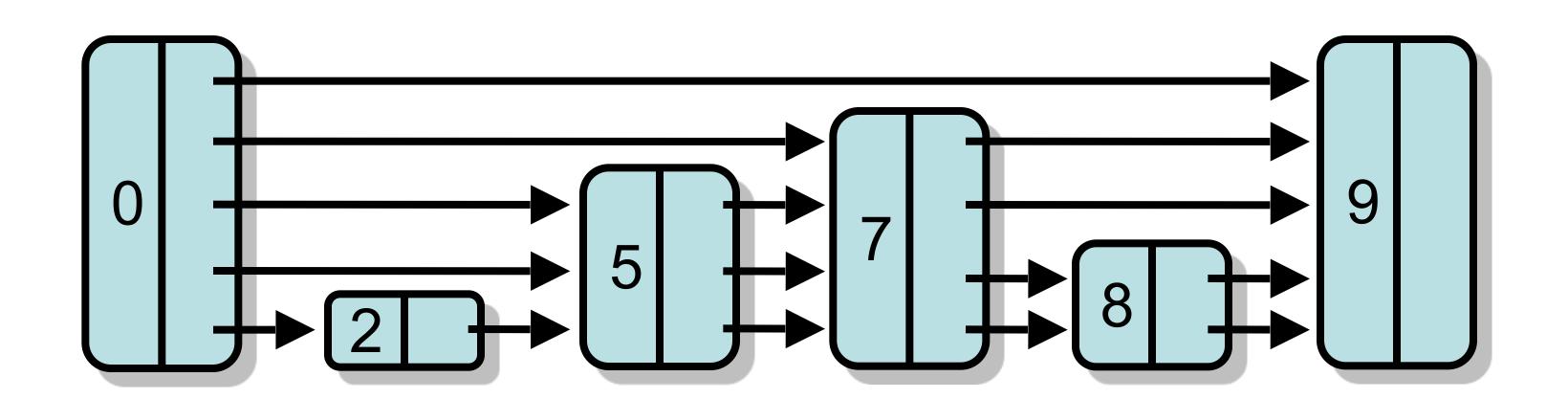
- Optimistic List, Lazy List
 - All have linear time (okay-ish)
- Any ideas on how we can do better?

Concurrent Sets

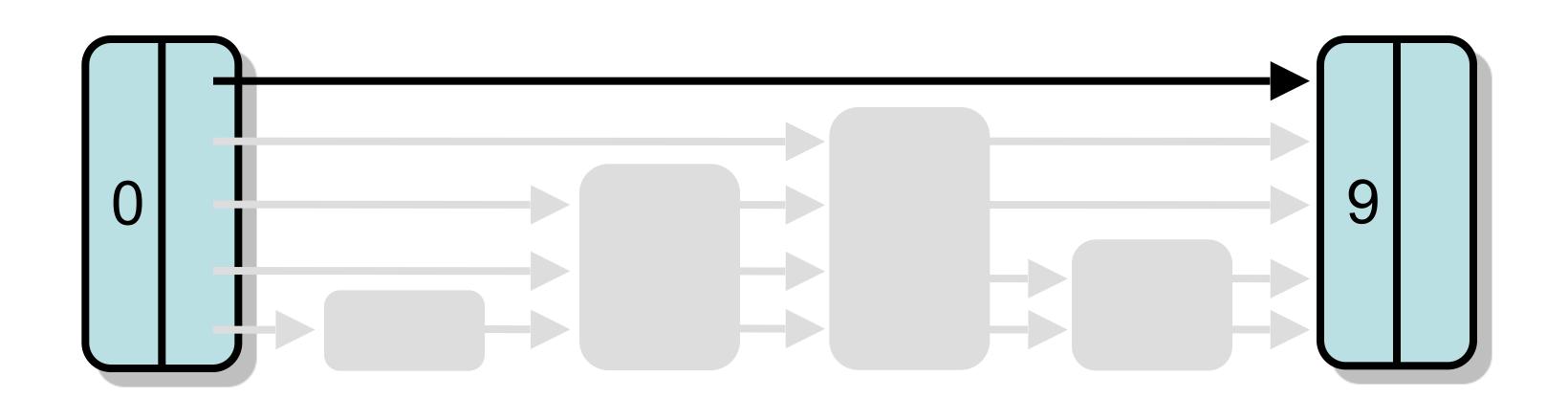
- Balanced Trees?
 - Red-Black trees, AVL trees, ...
- Problem: no one does this well ...
- ... because rebalancing after add() or remove() is a global operation

Skip Lists

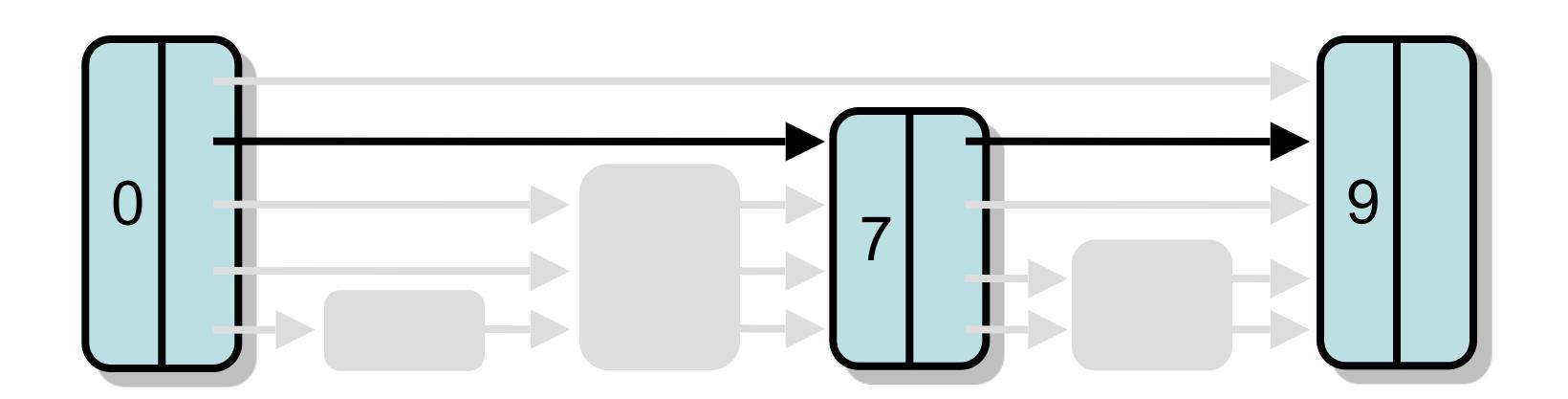
- Probabilistic Data Structure
- No global rebalancing
- Logarithmic-time search



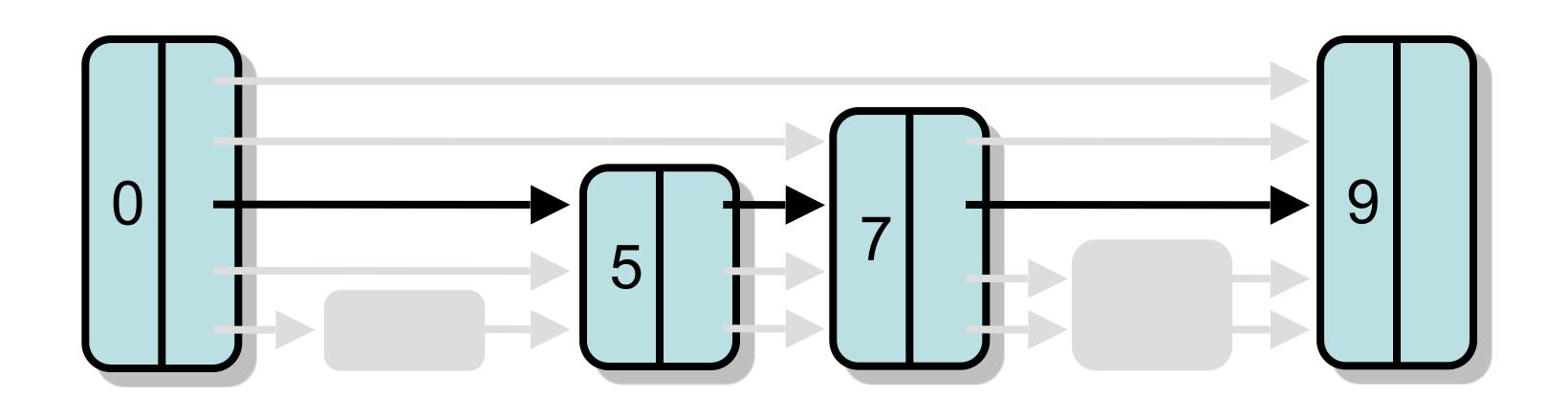
• Each layer is sub-list of lower levels



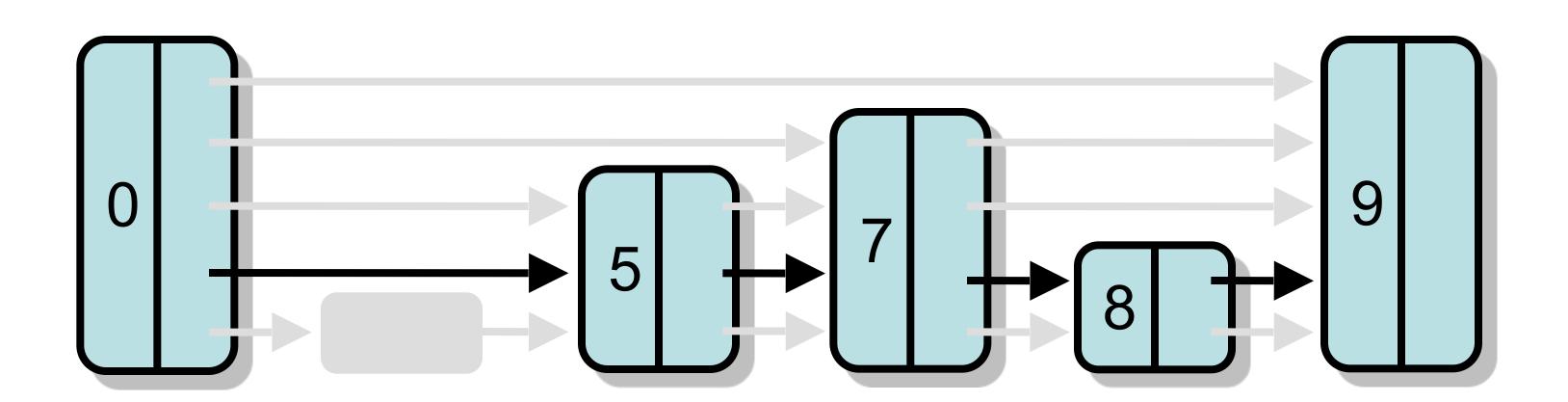
• Each layer is sub-list of lower-levels



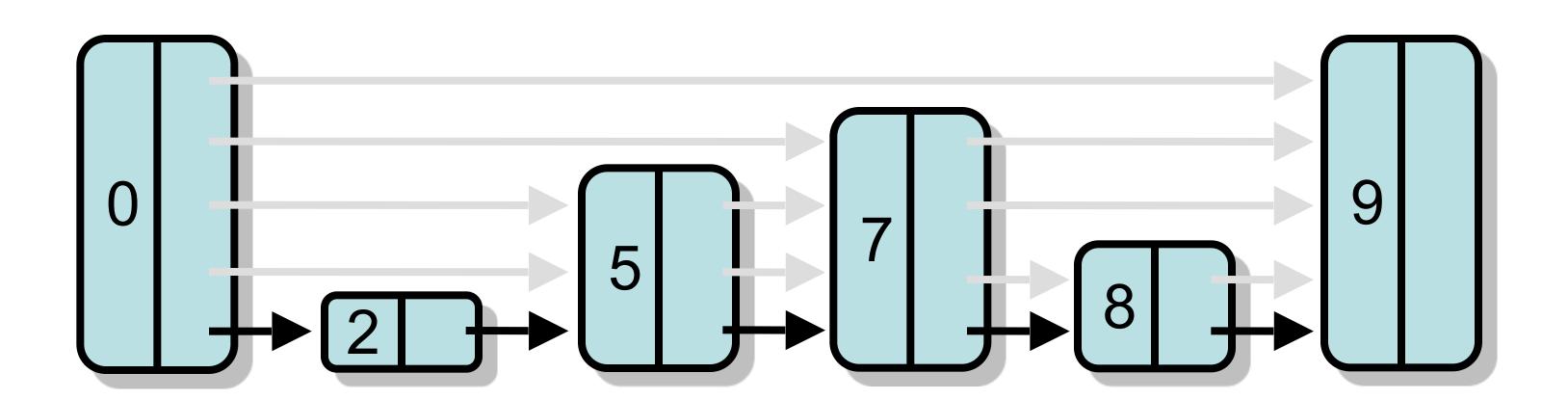
• Each layer is sub-list of lower levels



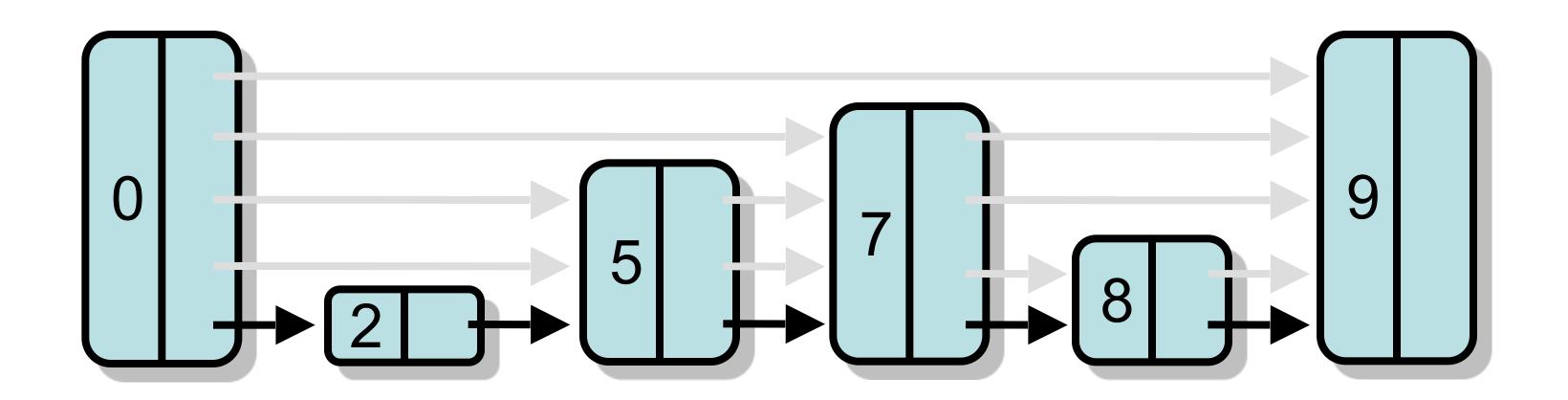
• Each layer is sub-list of lower levels

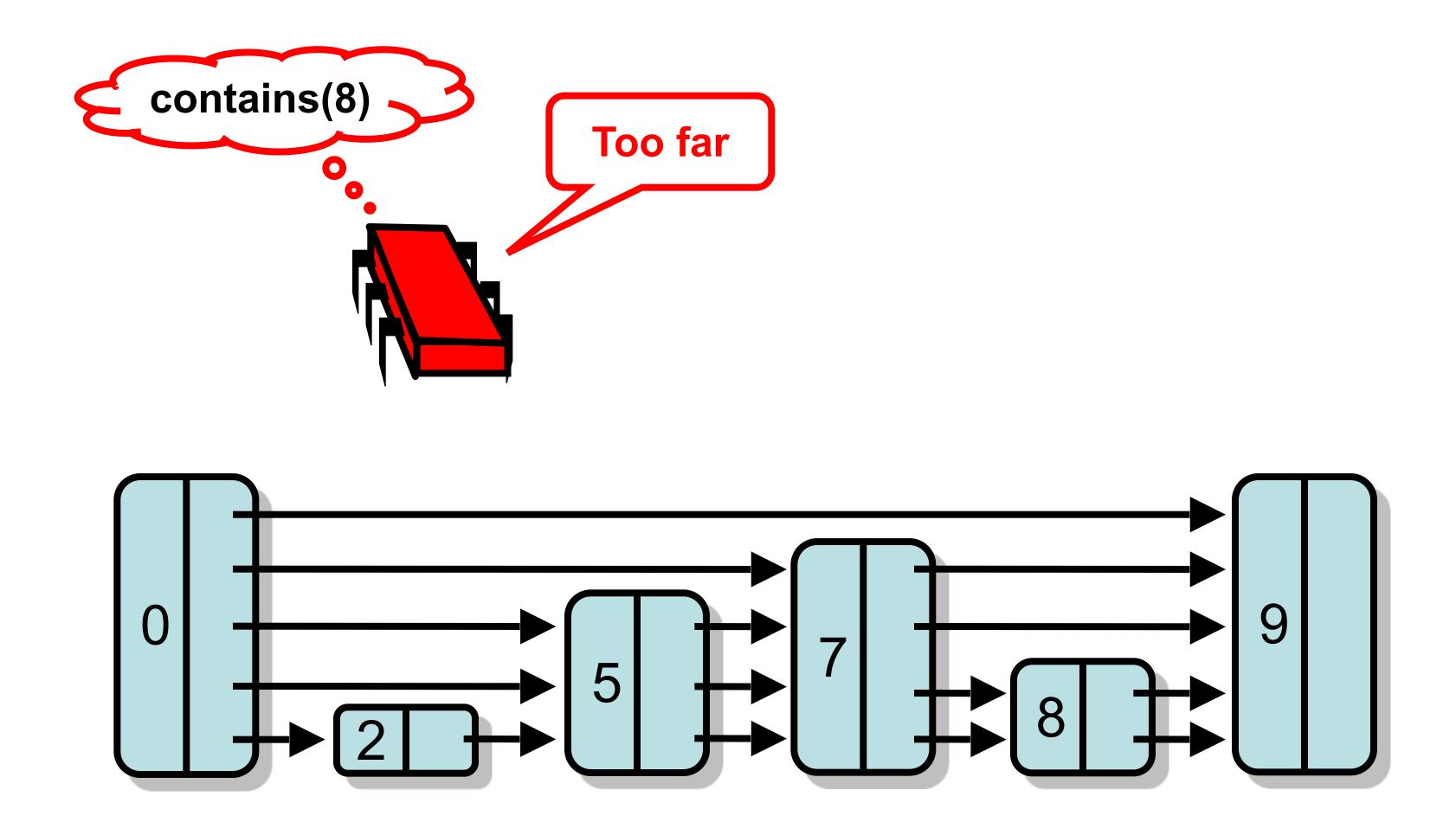


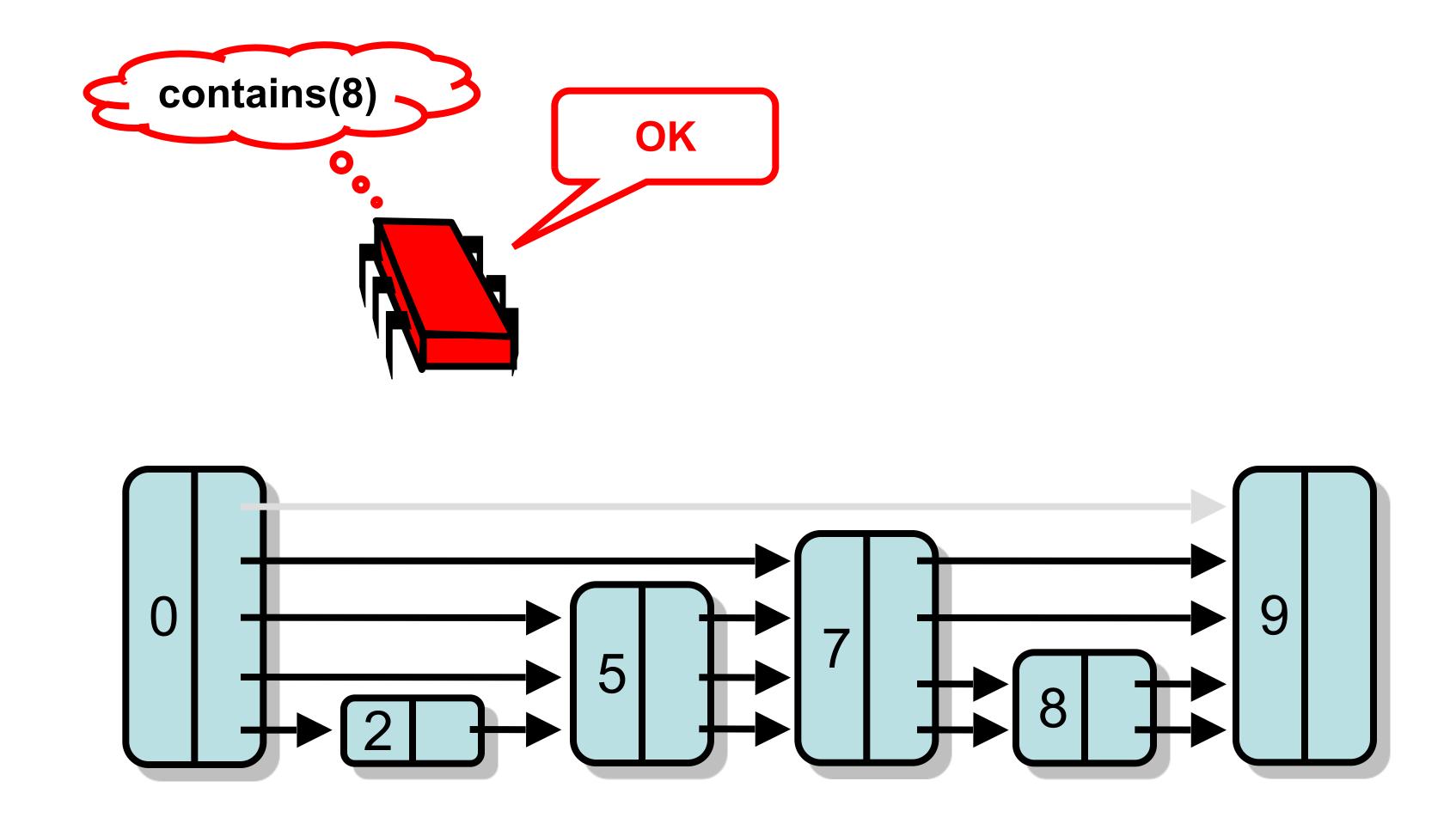
- Each layer is sub-list of lower levels
- Lowest level is entire list

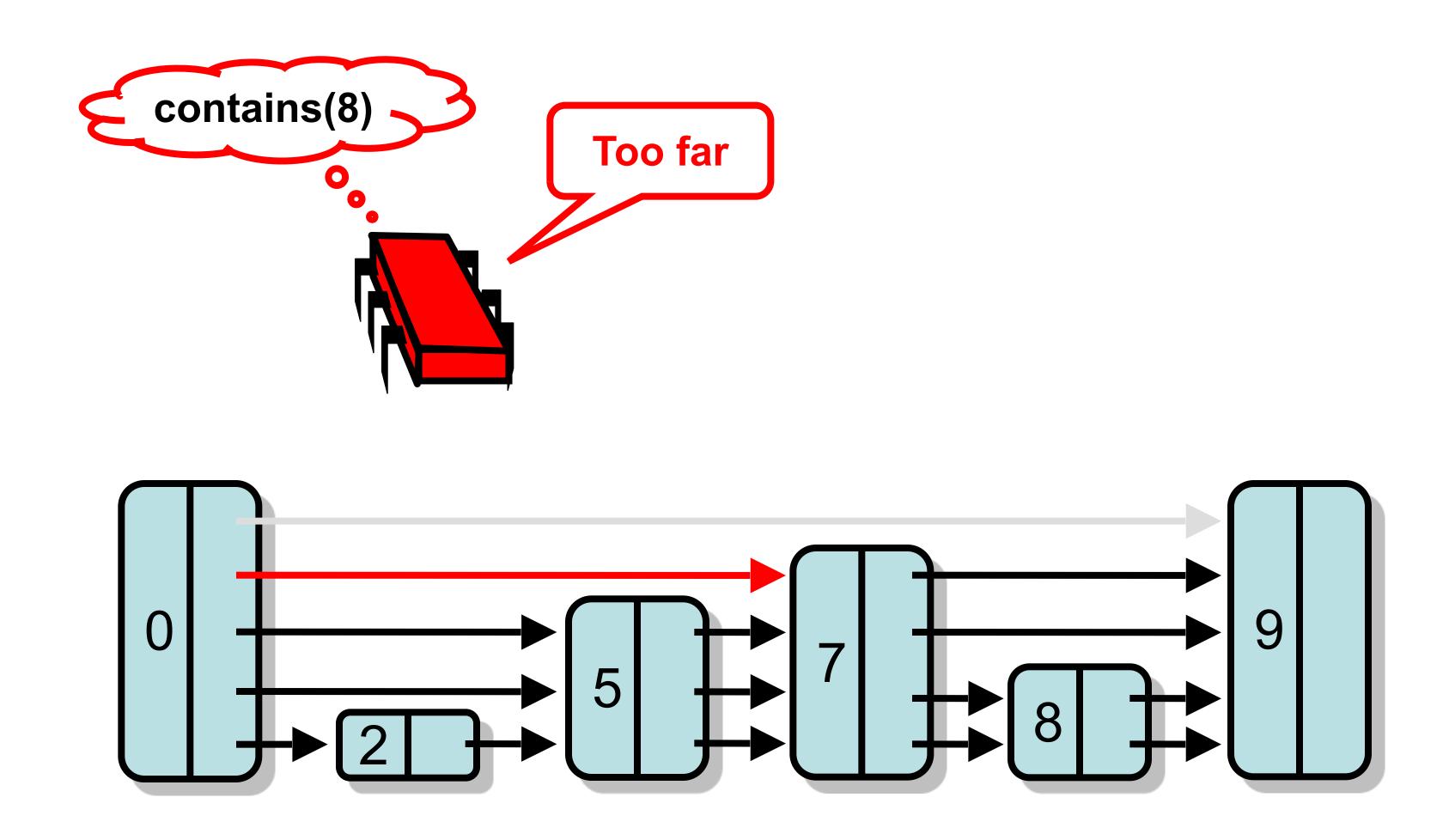


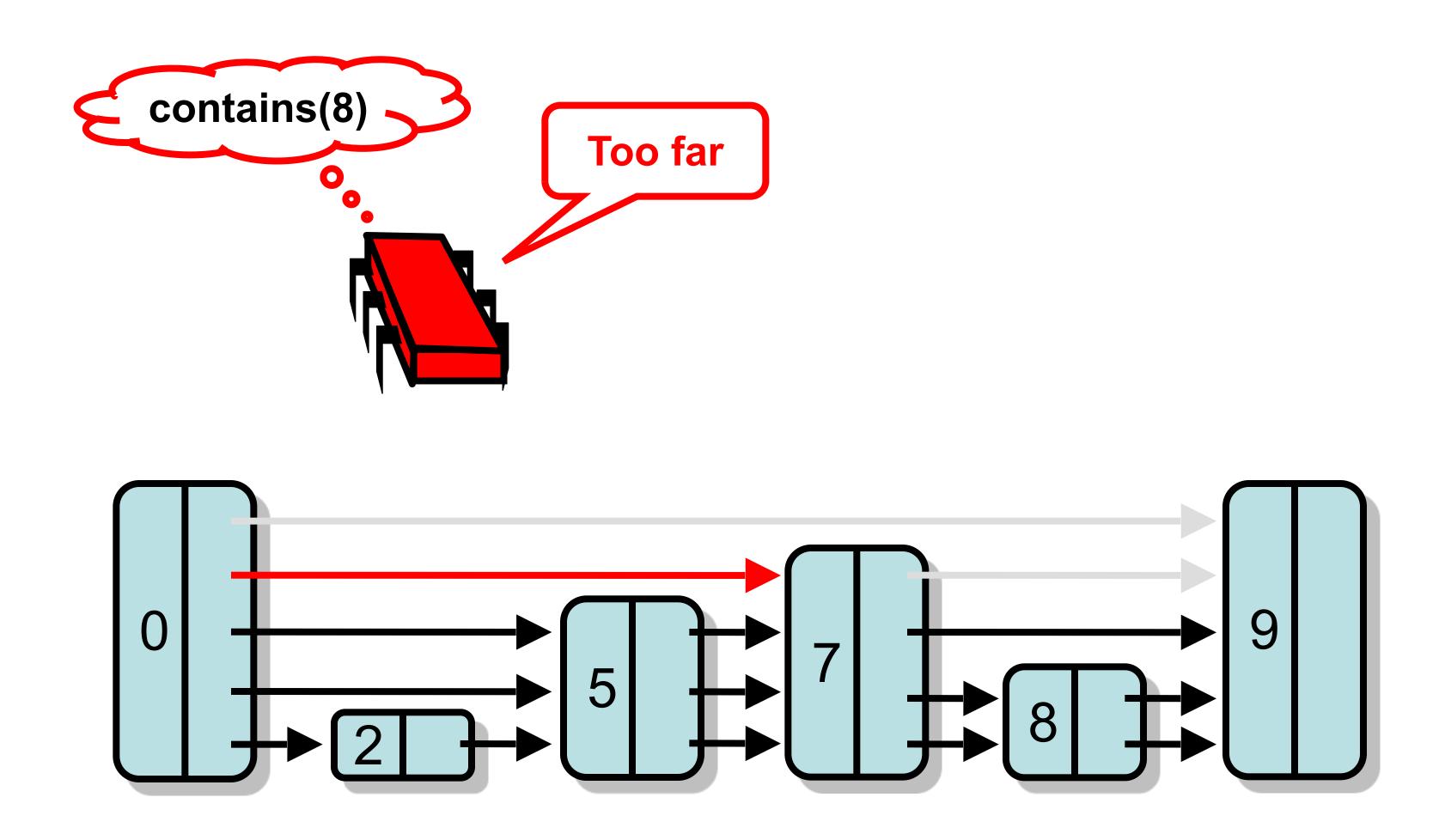
- Each layer is sub-list of lower levels
- Not easy to preserve in concurrent implementations ...

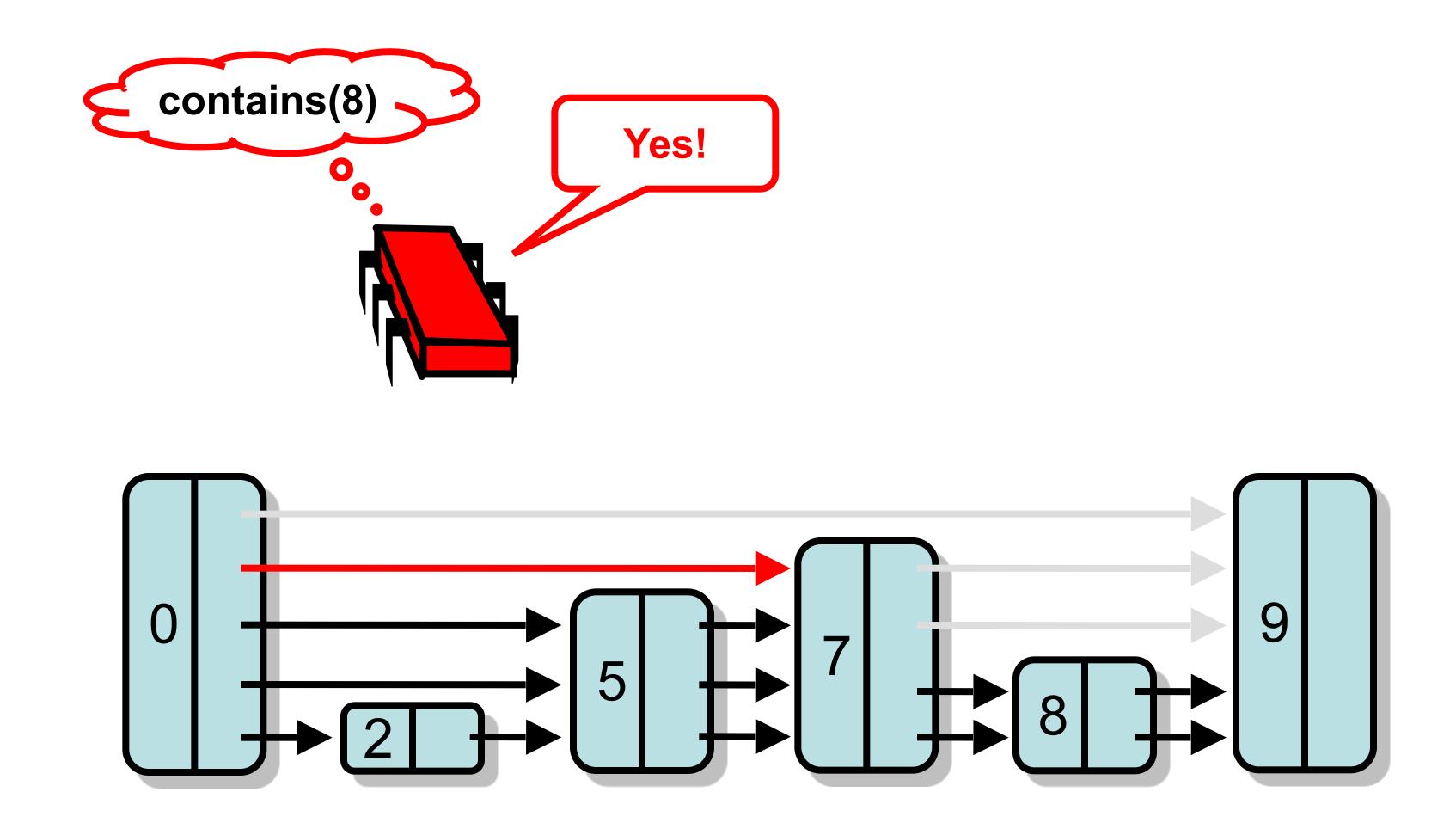


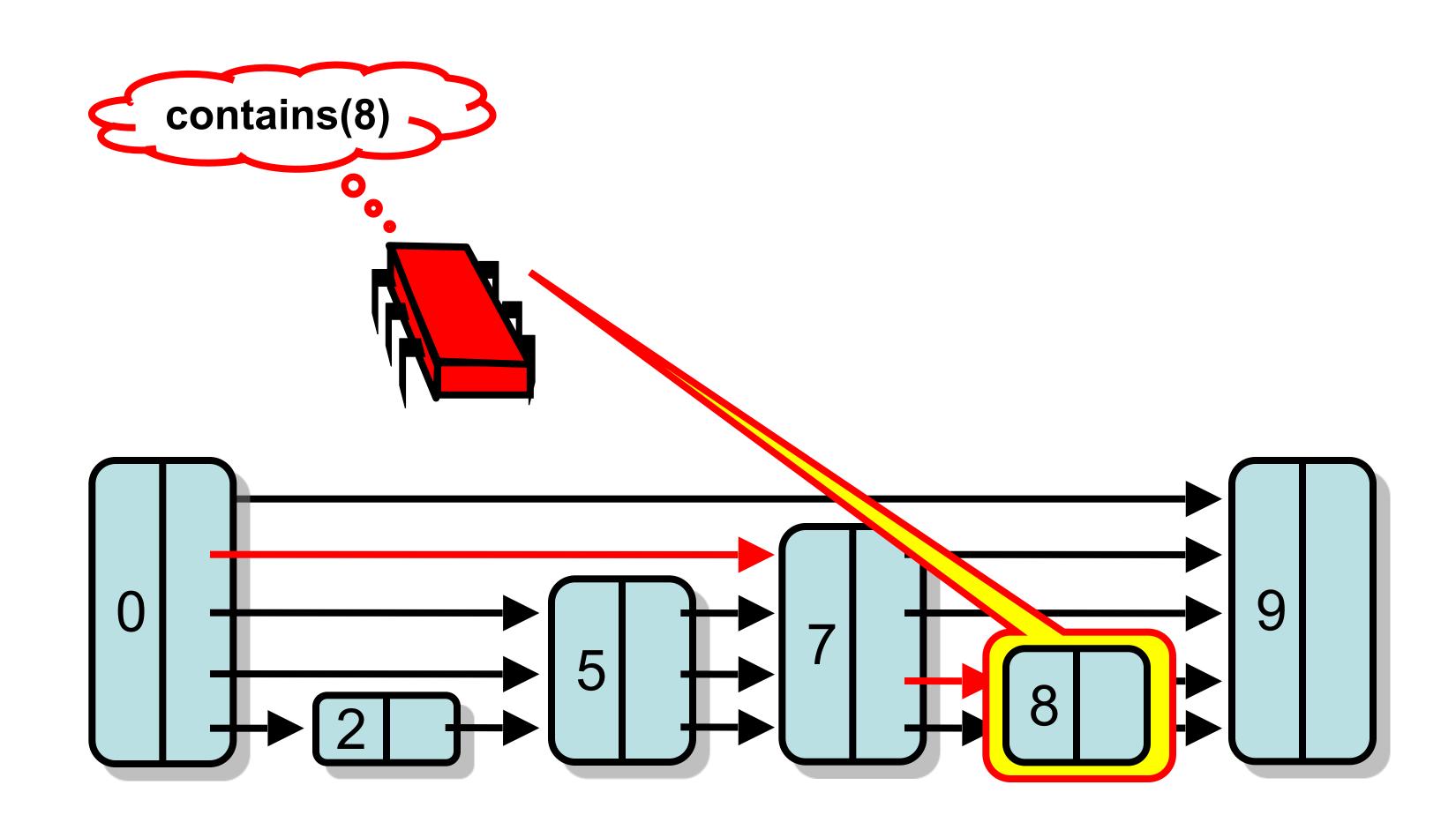




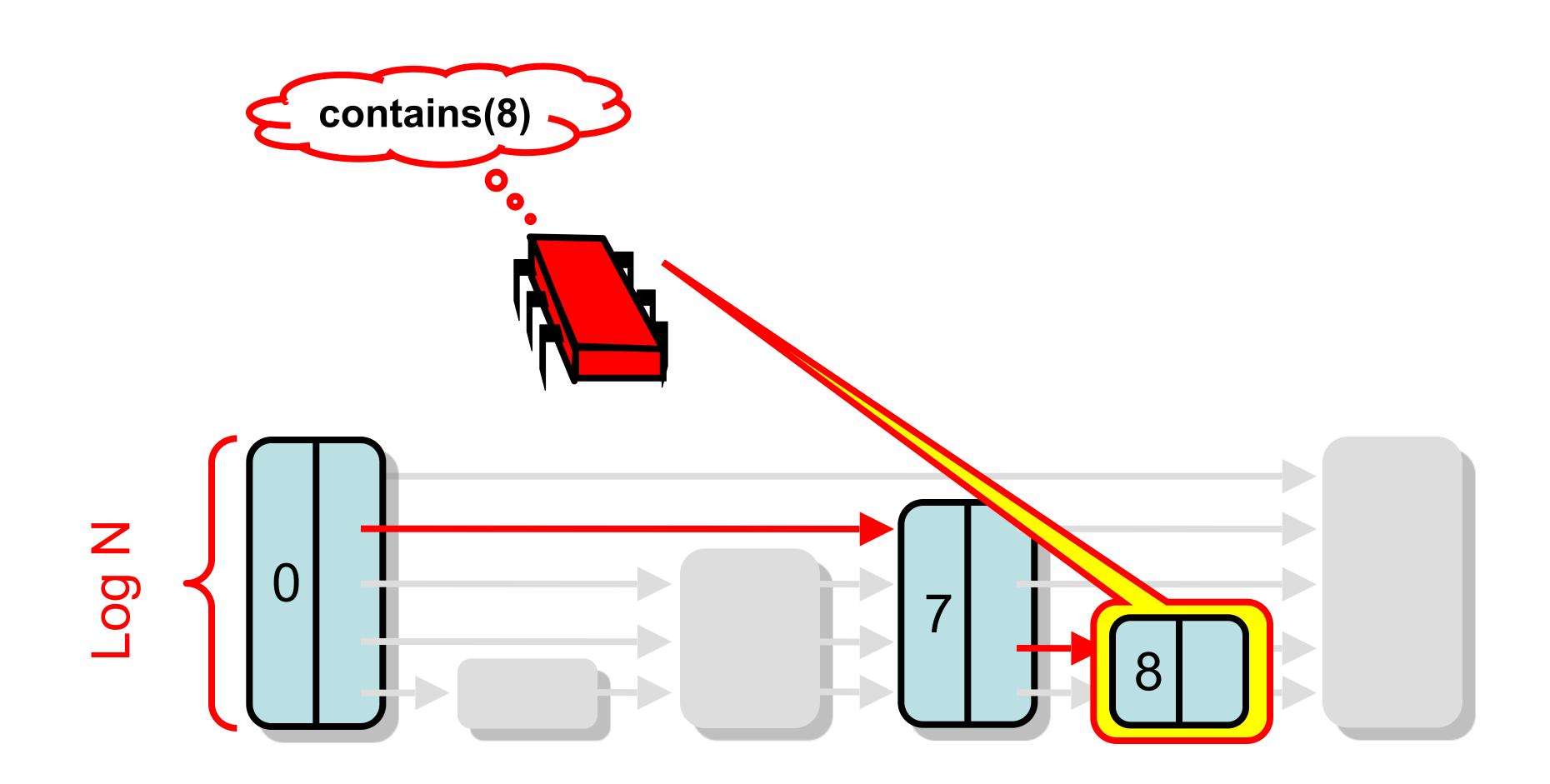






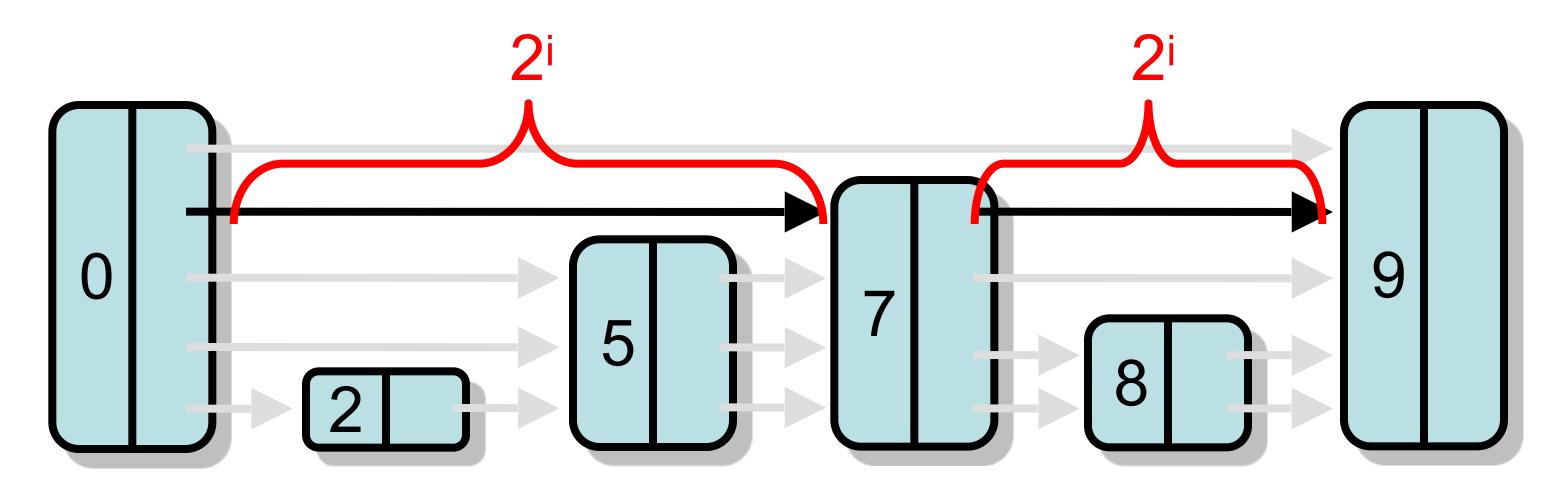


Logarithmic



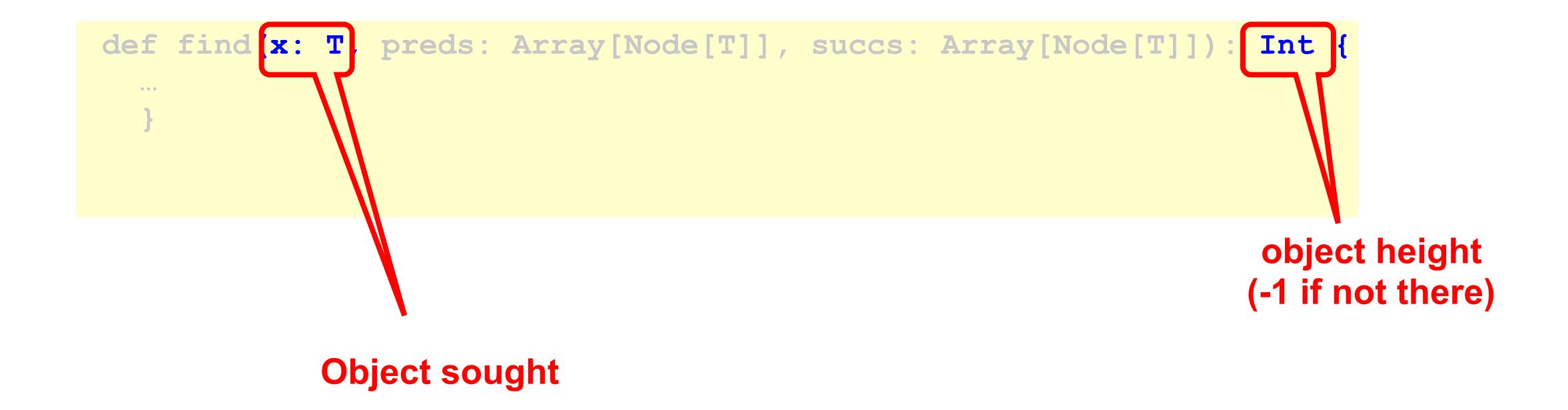
Why Logarthimic

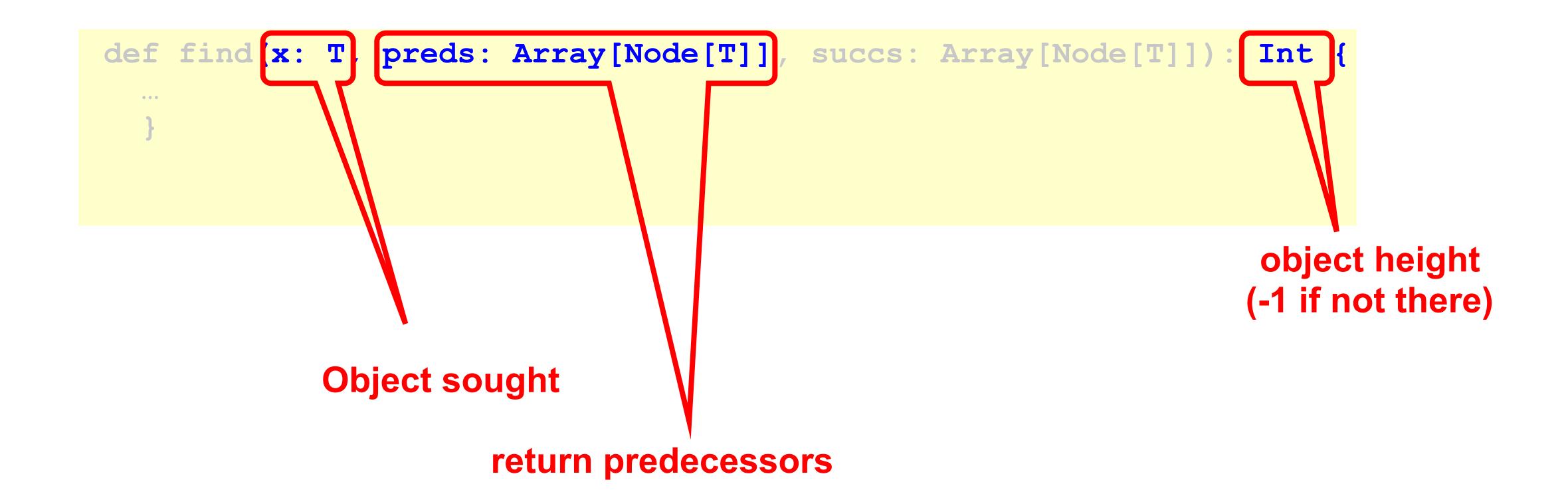
- Property: Each pointer at layer i jumps over roughly 2ⁱ nodes
- Pick node heights randomly so property guaranteed probabilistically

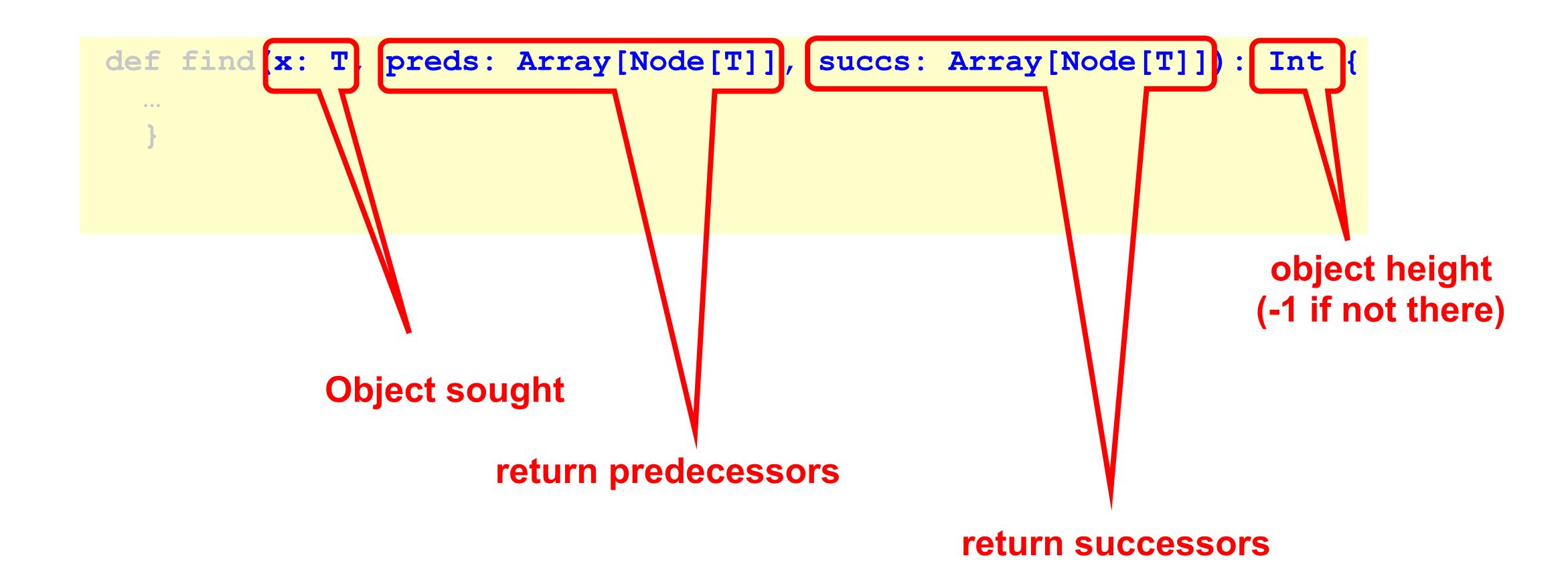


```
def find(x: T, preds: Array[Node[T]], succs: Array[Node[T]]): Int {
    ...
}
```

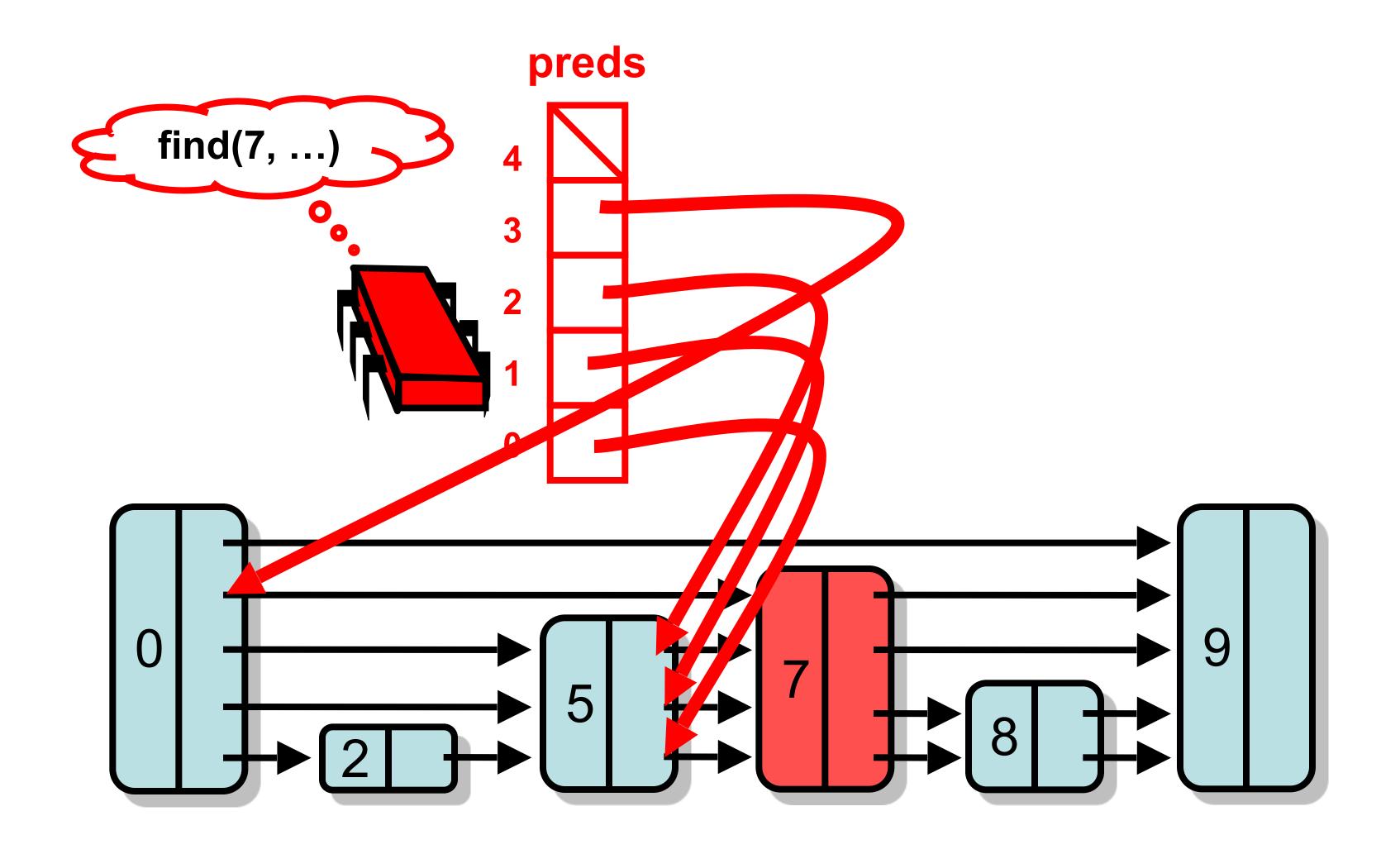
```
def find(x: T, preds: Array[Node[T]], succs: Array[Node[T]]): Int {
    ...
  }
    object height
    (-1 if not there)
```



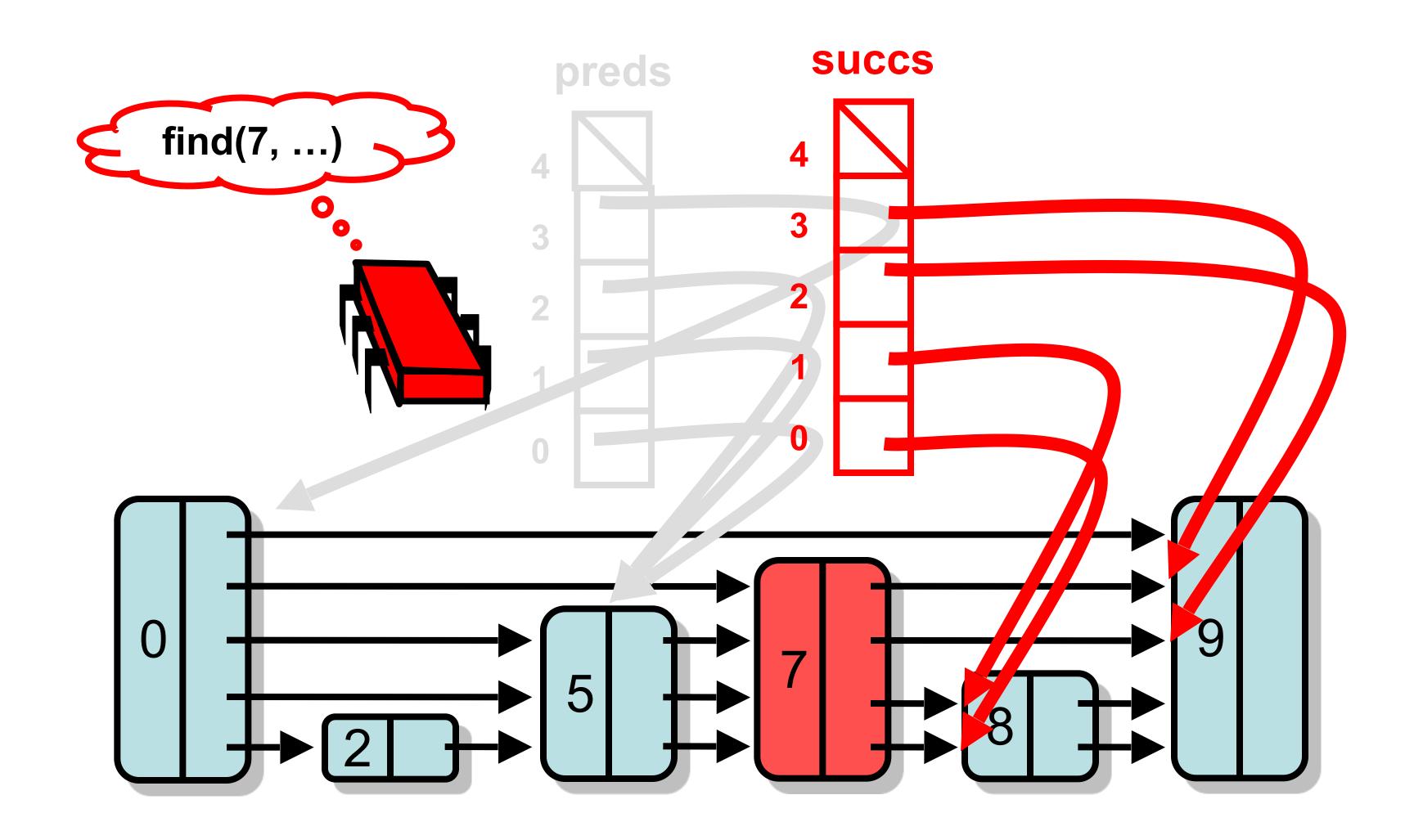




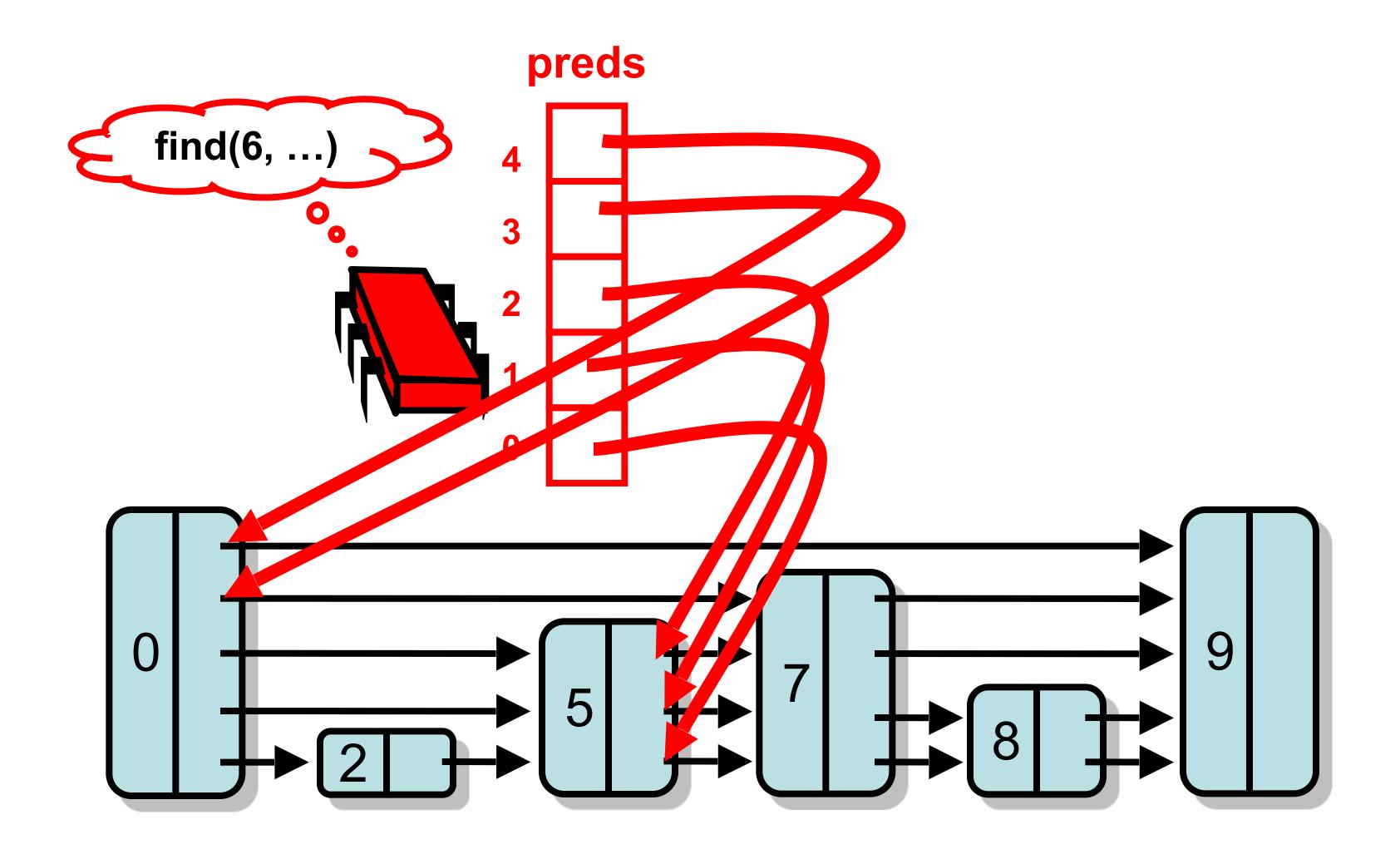
Successful Search



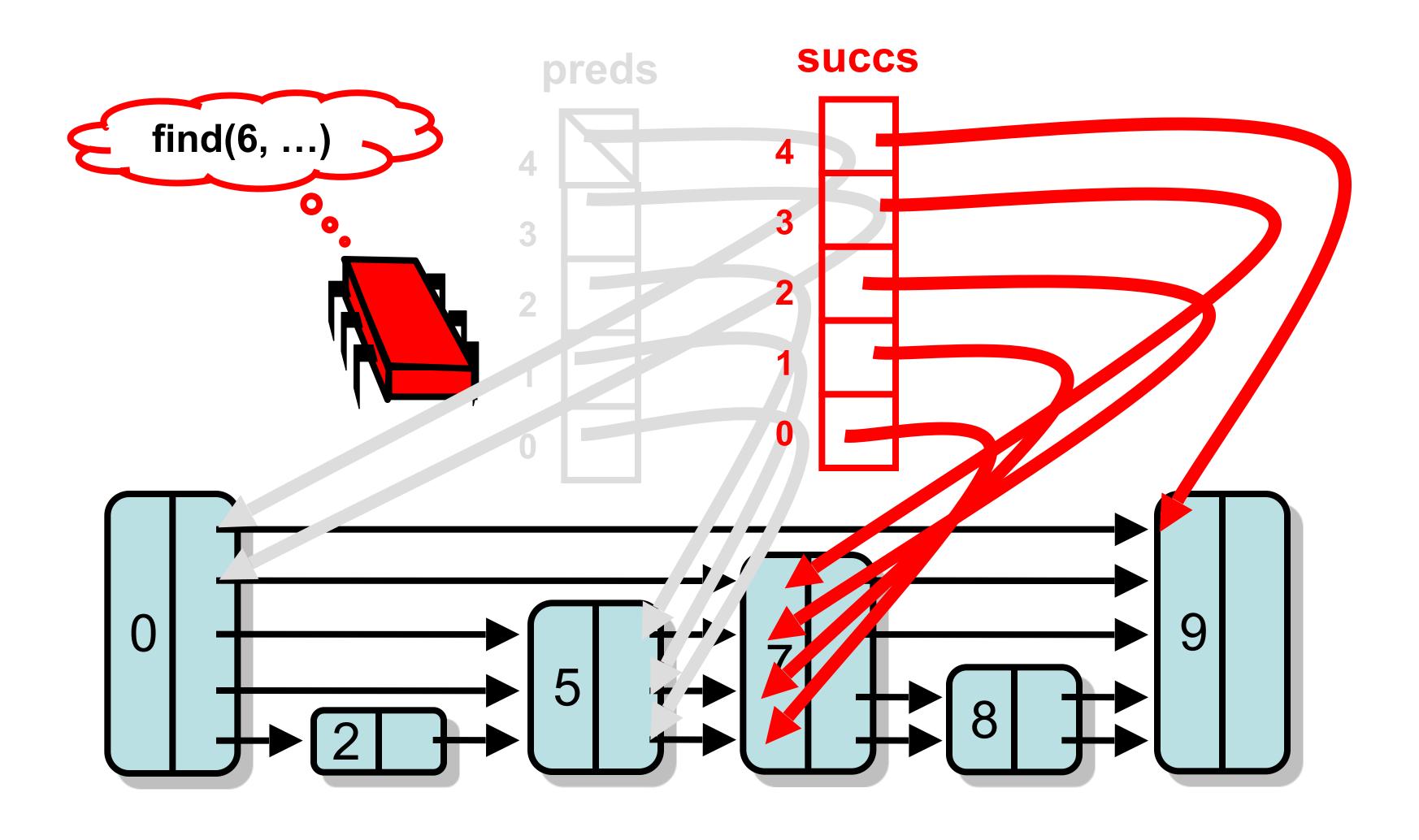
Successful Search



Unsuccessful Search



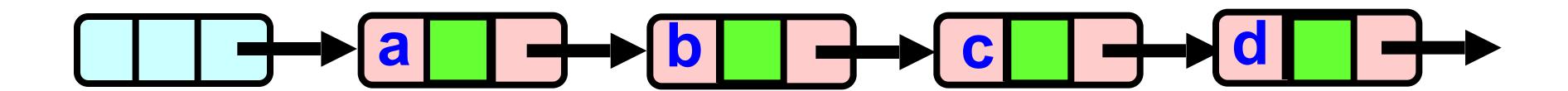
Unsuccessful Search

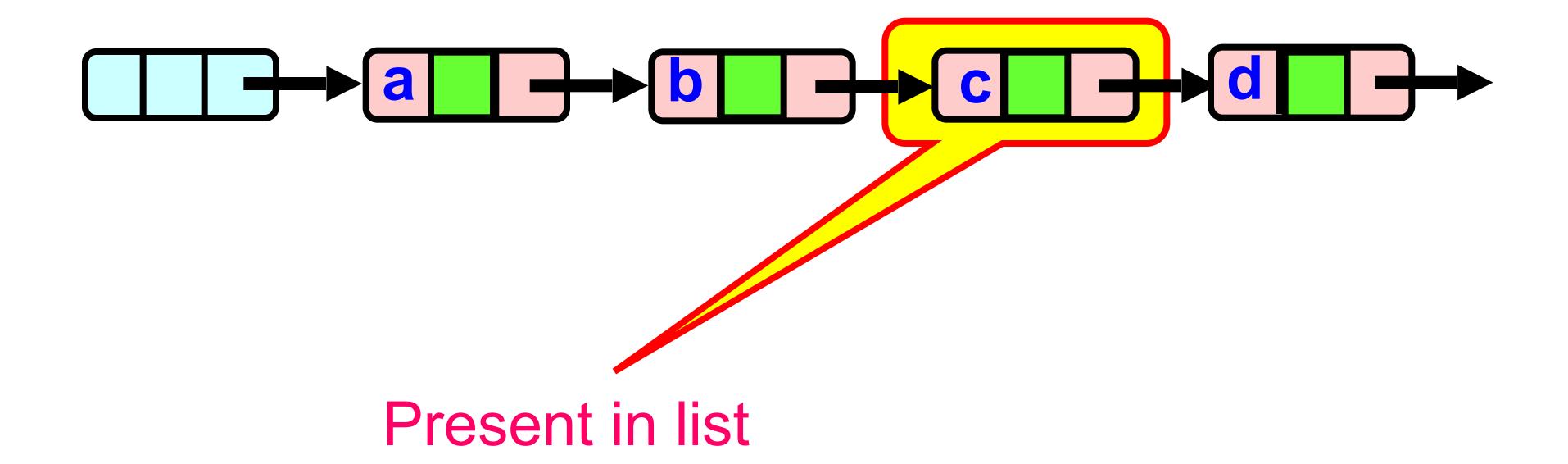


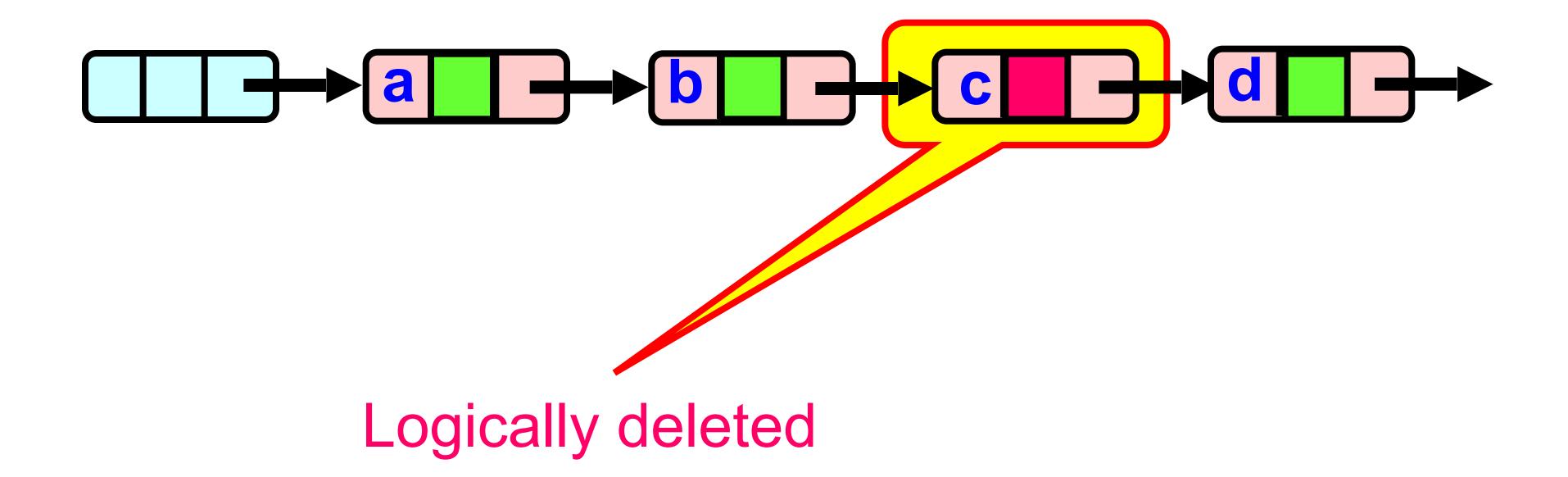
An Example (Sequential)

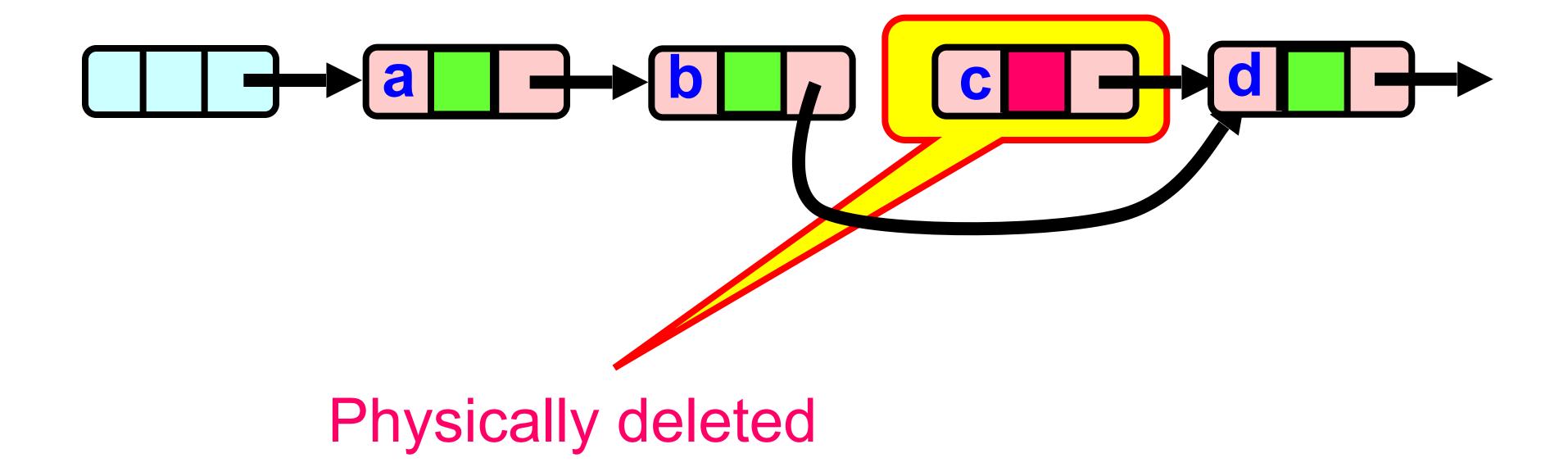
Lazy Skip List

- Mix blocking and non-blocking techniques:
 - Use optimistic-lazy locking for add() and remove()
 - Wait-free contains()
- Remember: typically lots of contains() calls but few add() and remove()



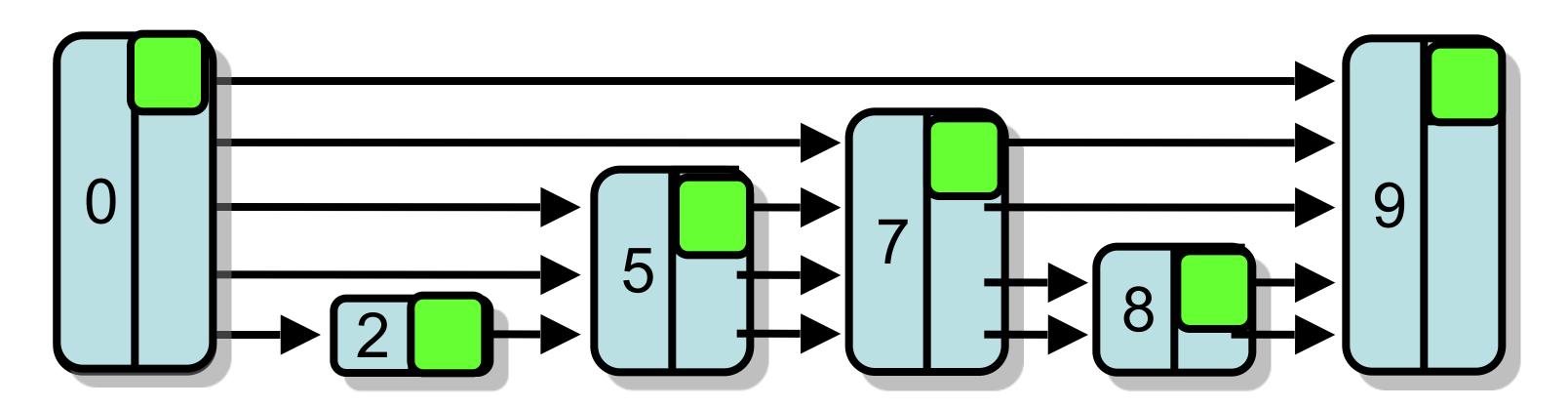




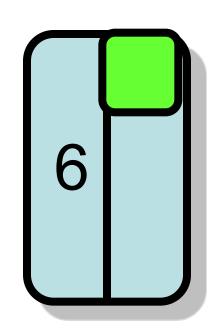


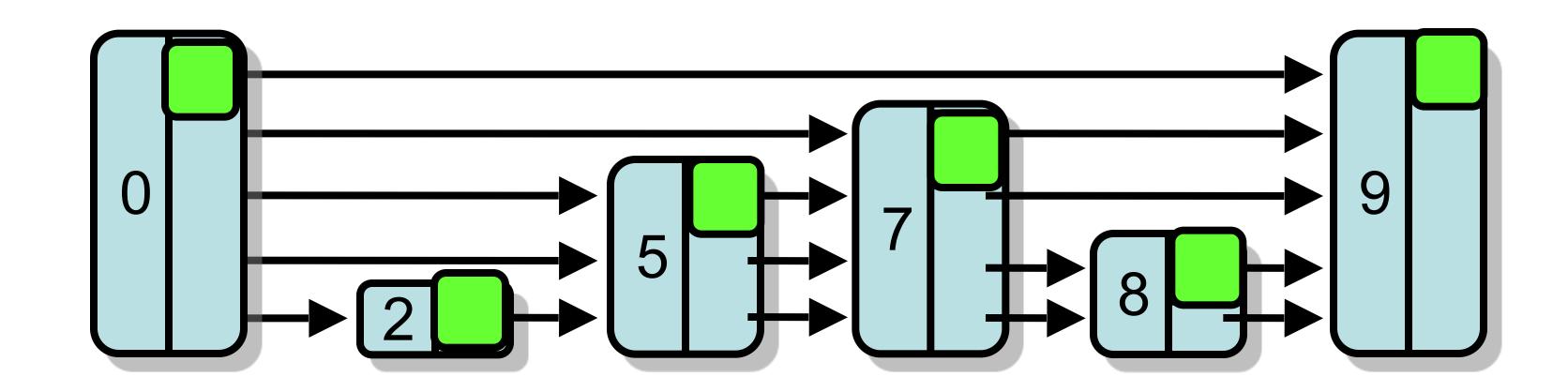
Lazy Skip Lists

Use a mark bit for logical deletion

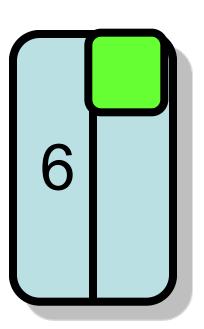


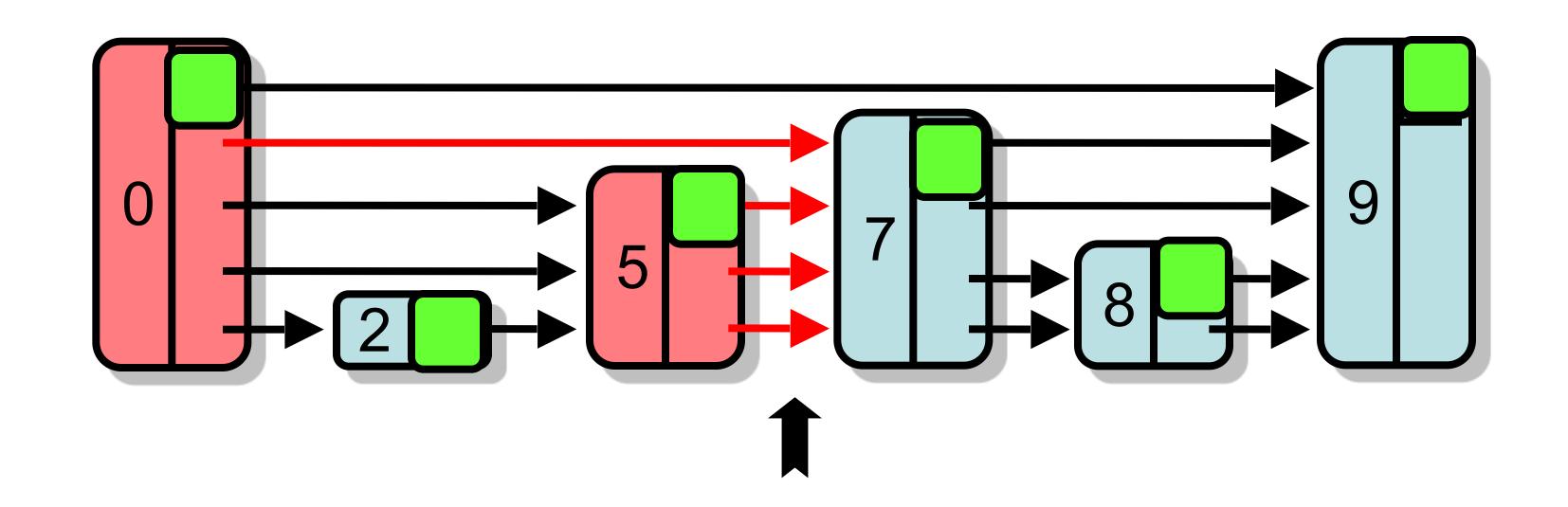
Create node of (random) height 4



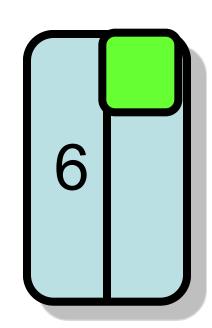


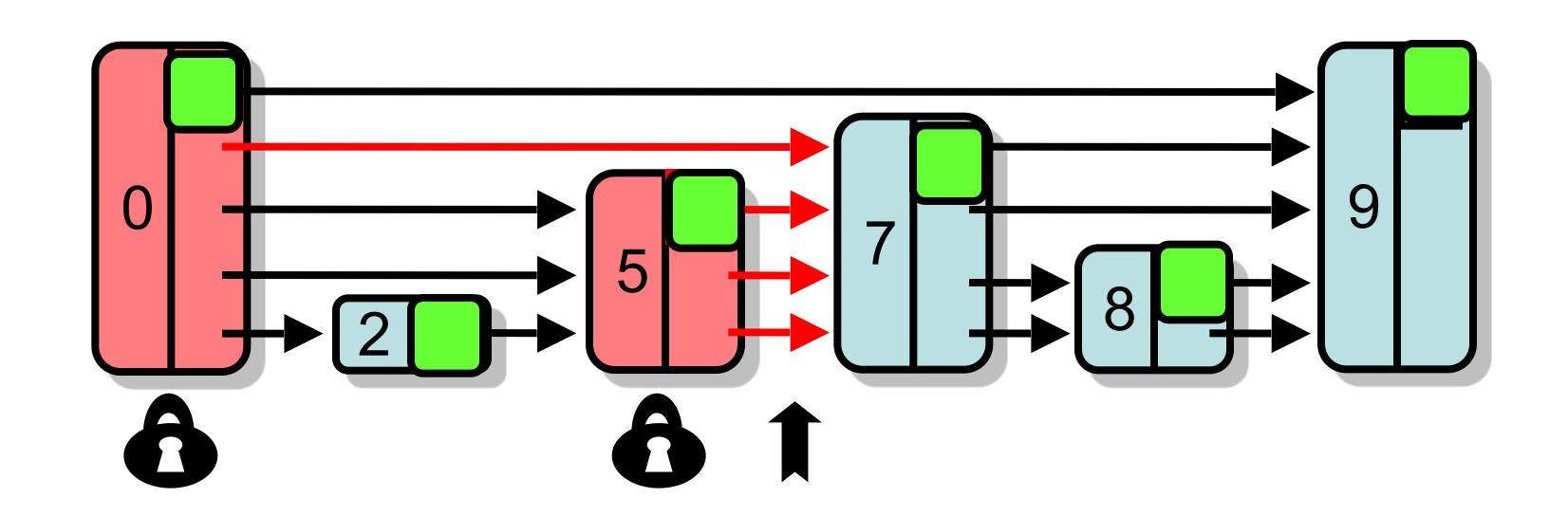
• find() predecessors



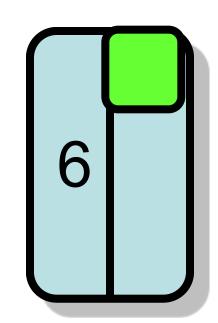


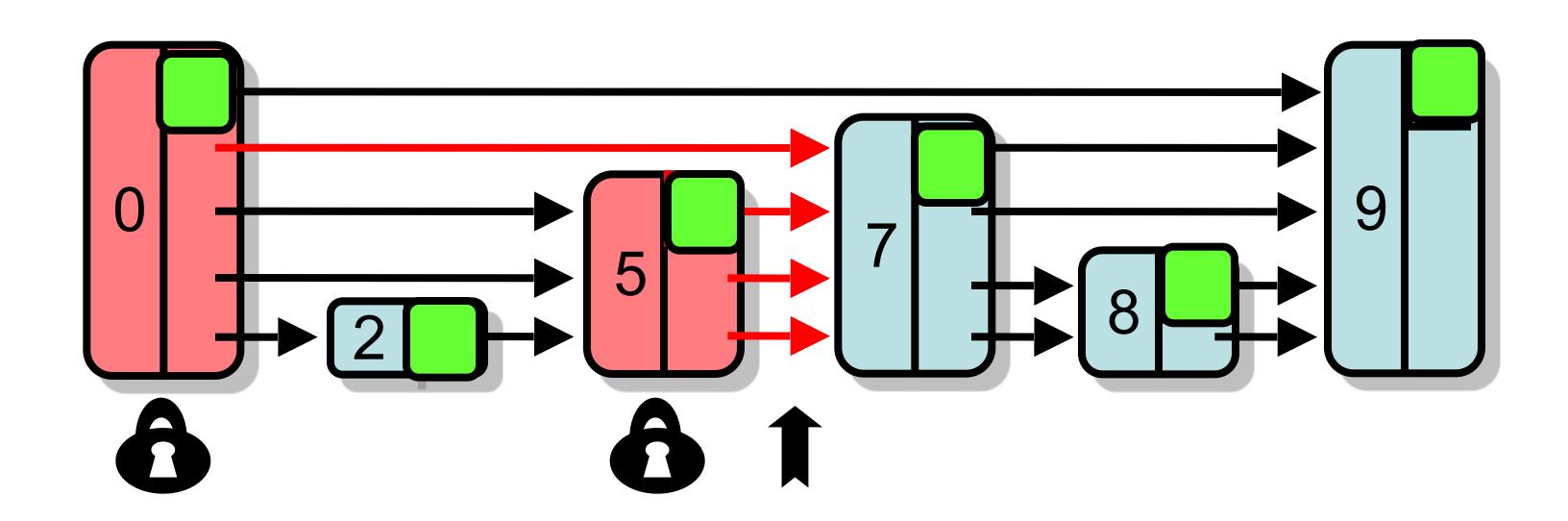
- find() predecessors
- Lock them



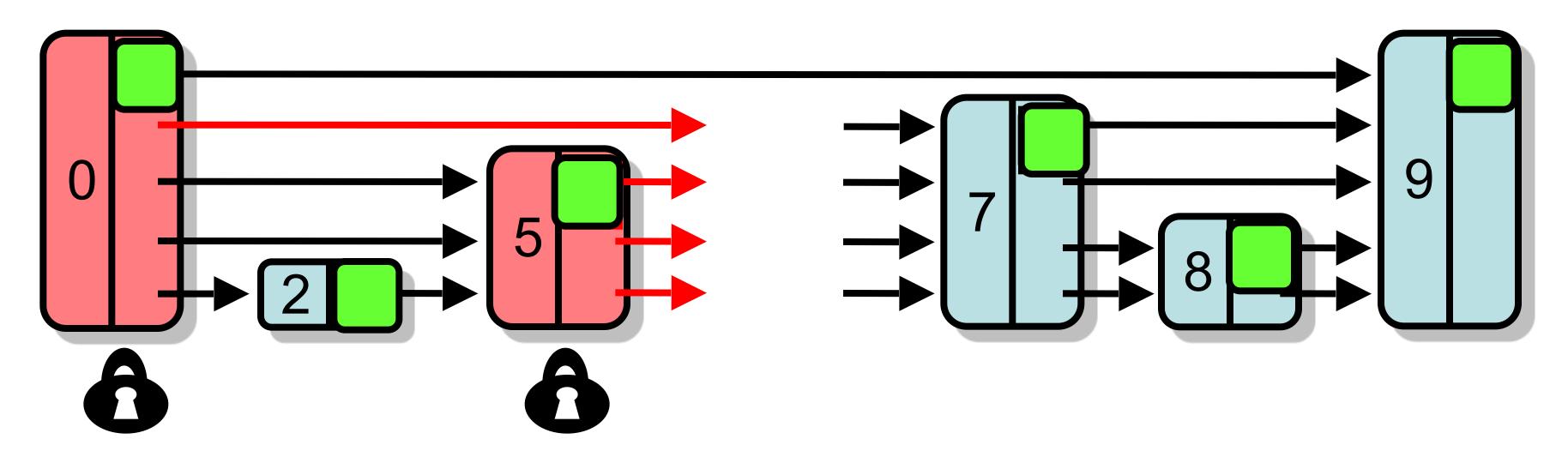


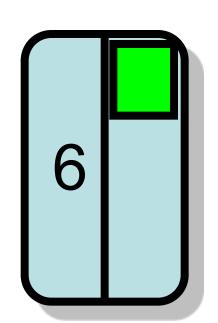
- find() predecessors
- Lock them Optimistic approach
- Validate



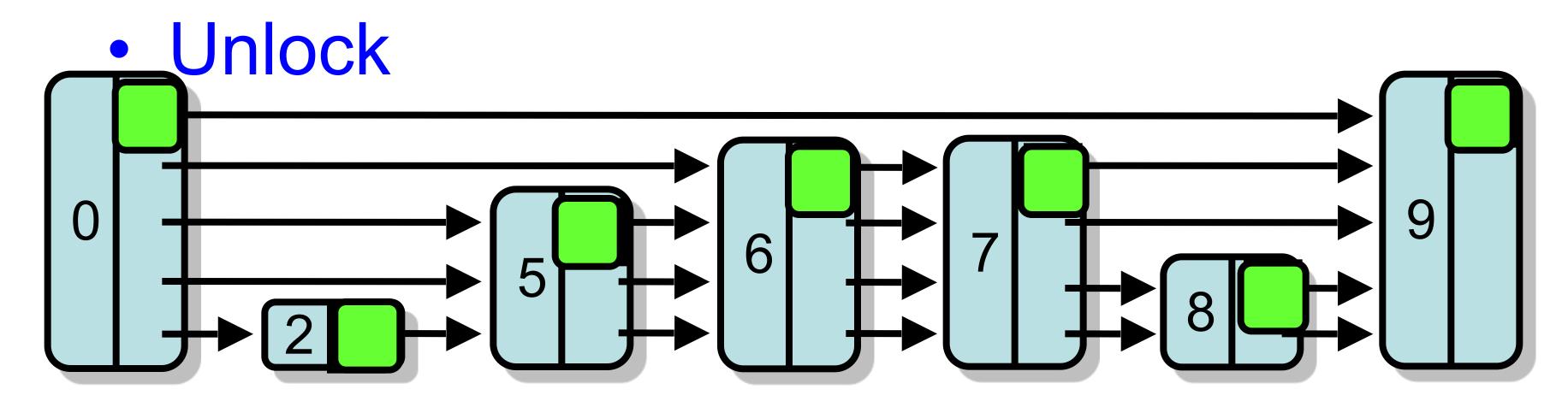


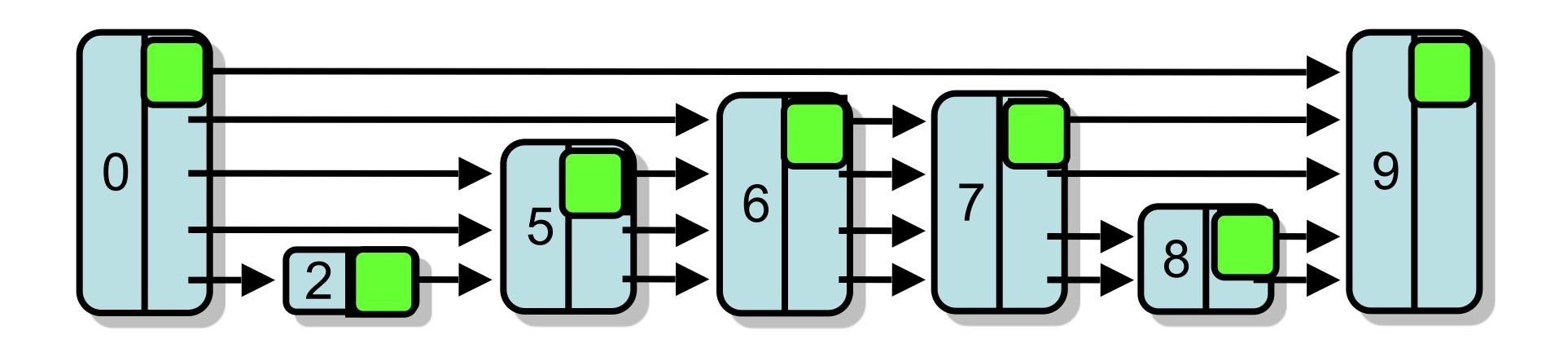
- find() predecessors
- Lock them
- Validate
- Splice



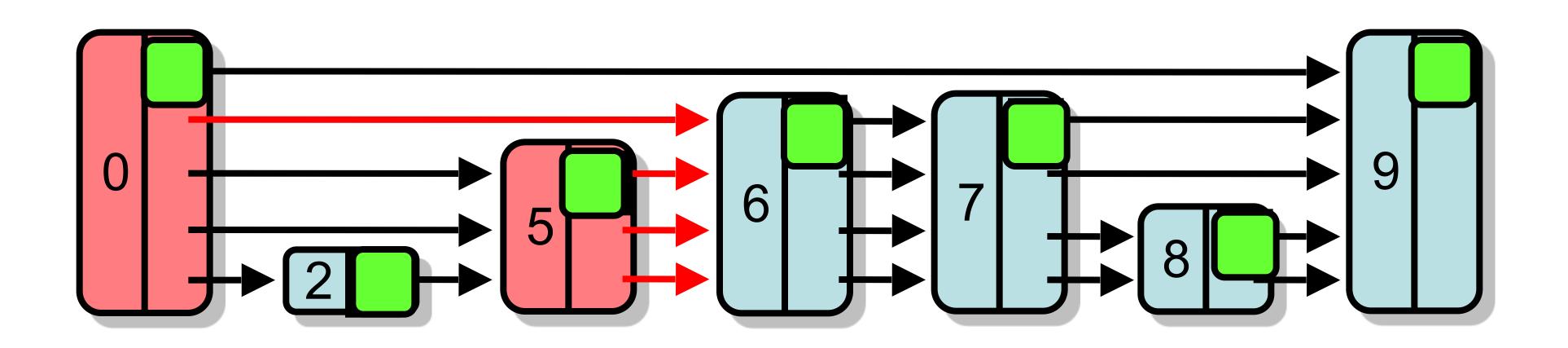


- find() predecessors
- Lock them
- Validate
- Splice

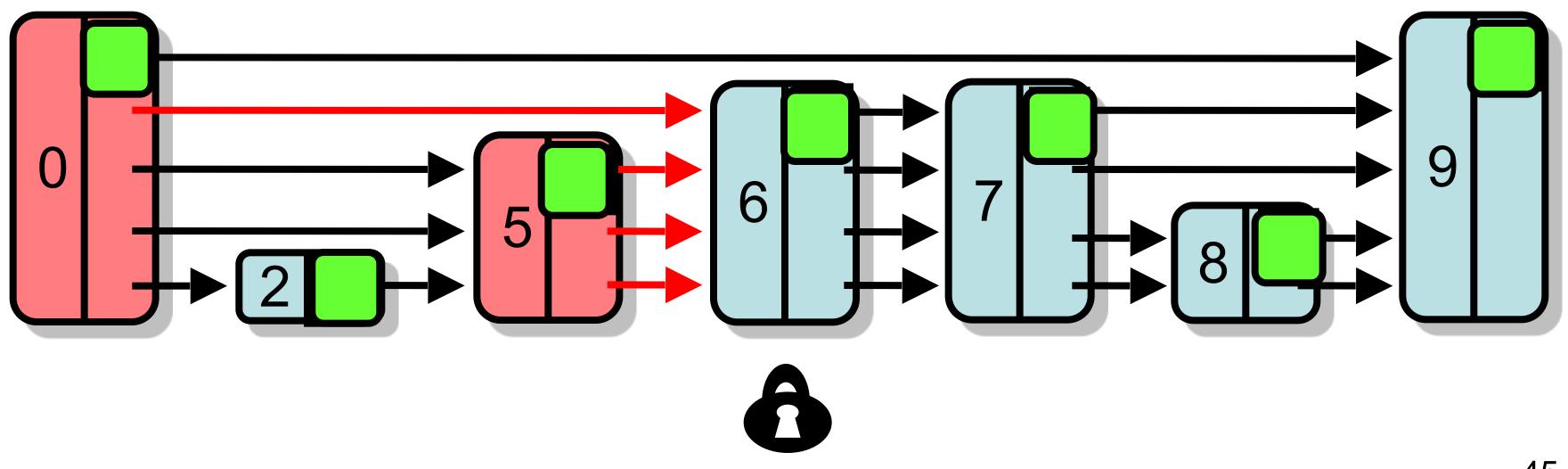




• find() predecessors

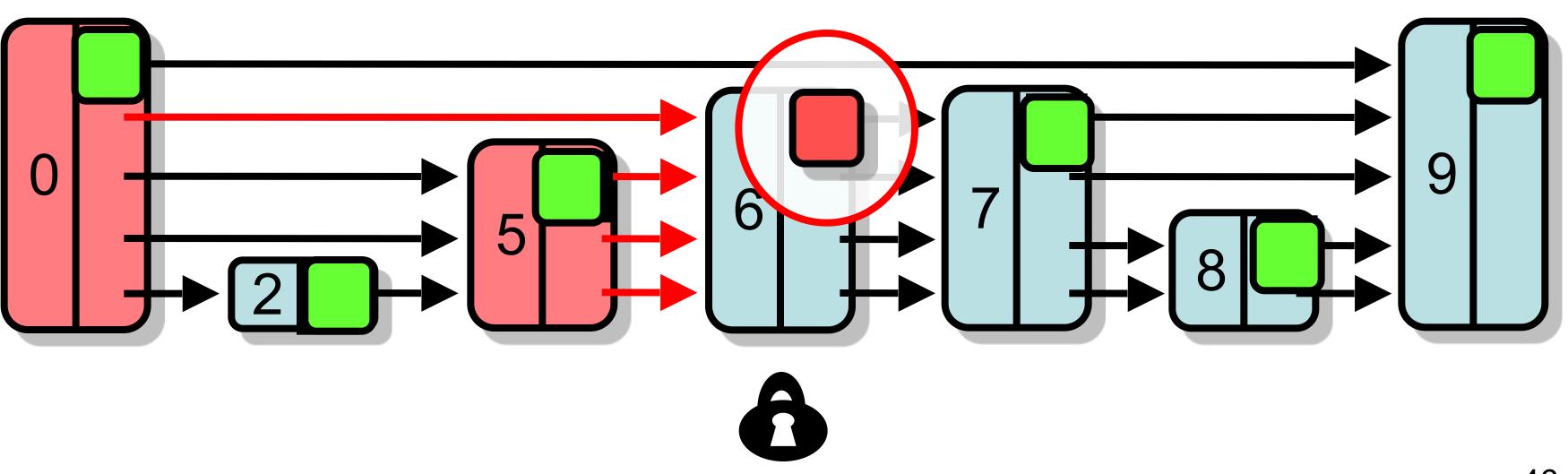


- find() predecessors
- Lock victim

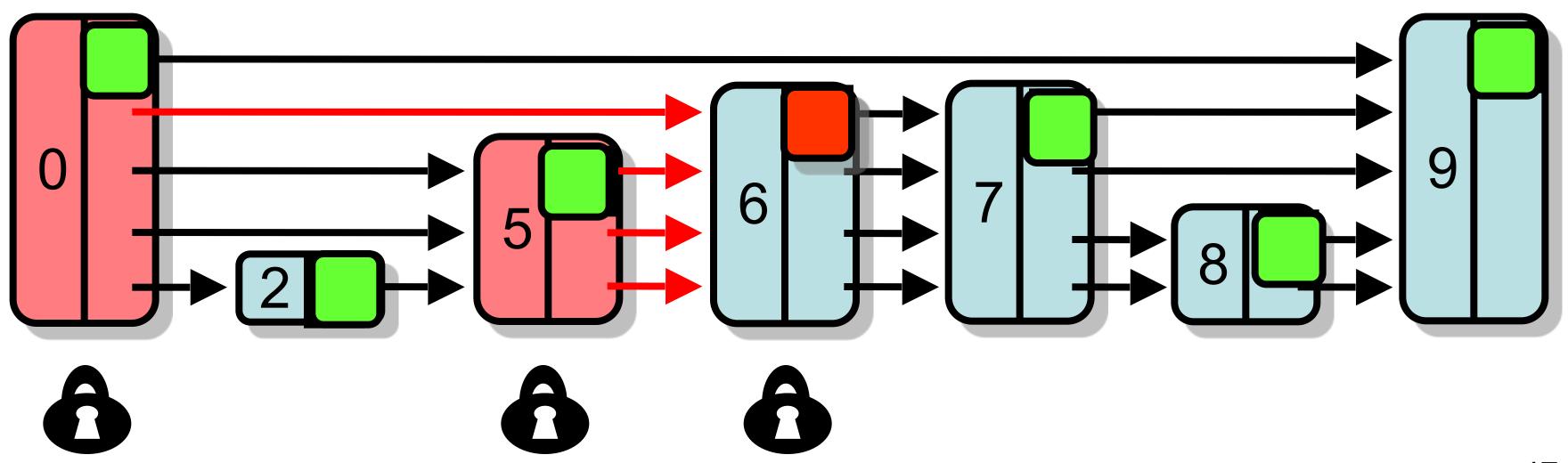


- find() predecessors
- Lock victim
- Set mark (if not already set)

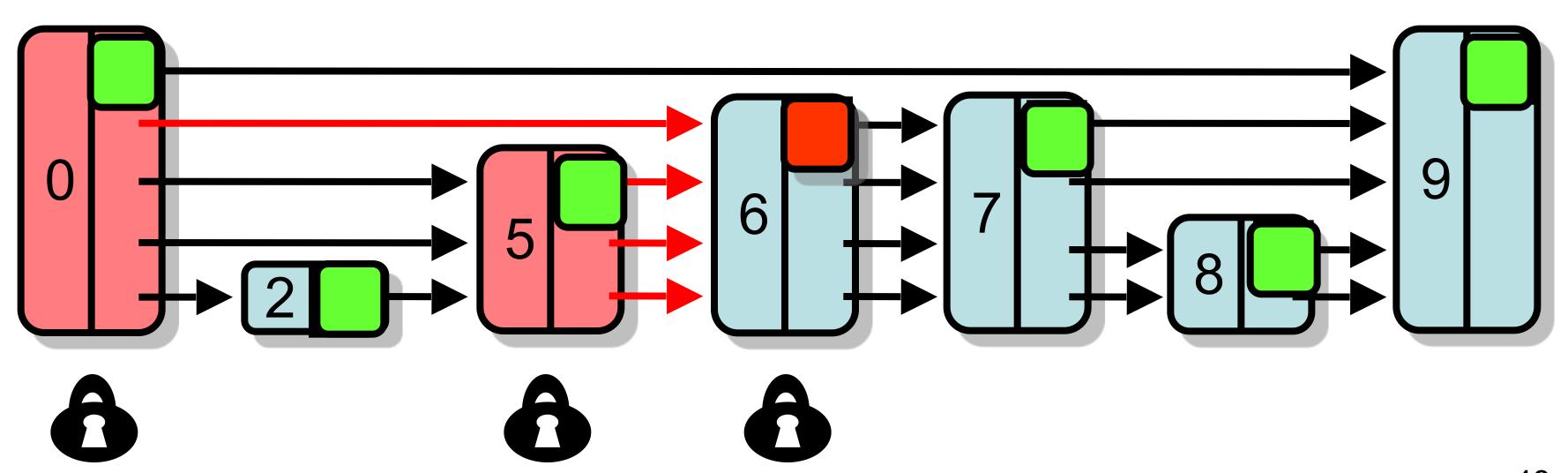
Logical remove...



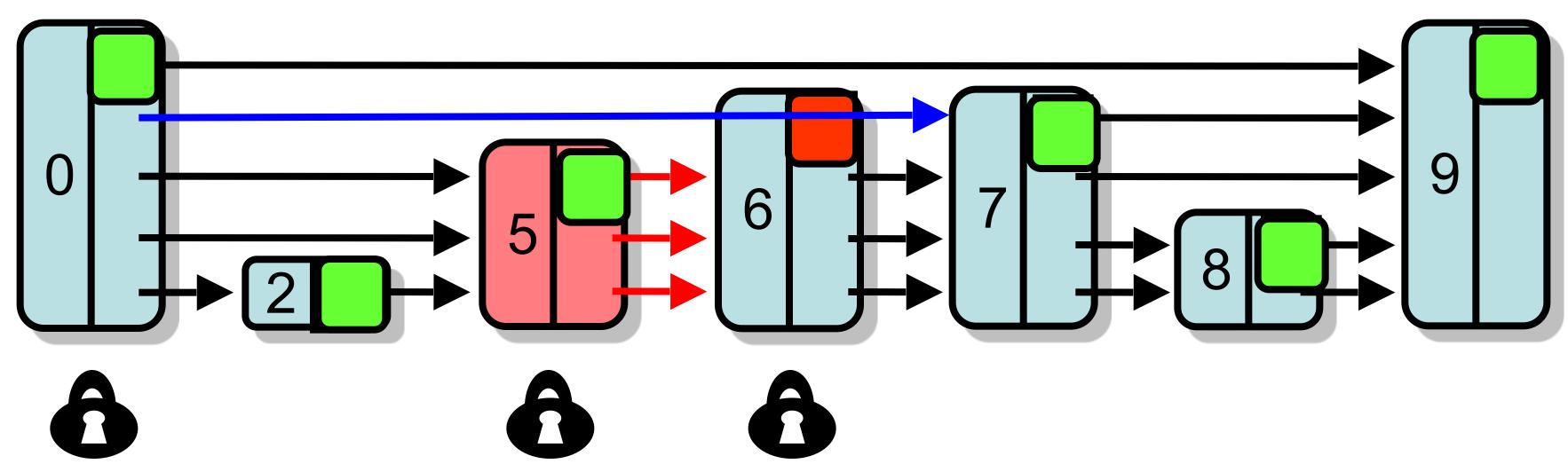
- find() predecessors
- Lock victim
- Set mark (if not already set)
- Lock predecessors (ascending order) & validate



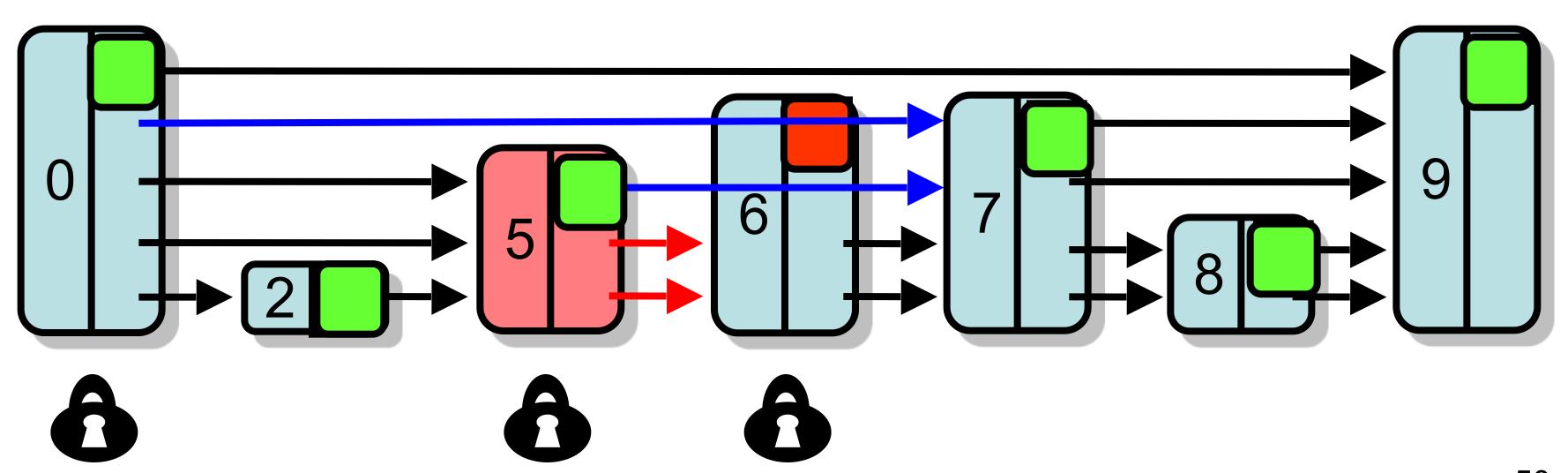
- find() predecessors
- Lock victim
- Set mark (if not already set)
- Lock predecessors (ascending order) & validate
- Physically remove



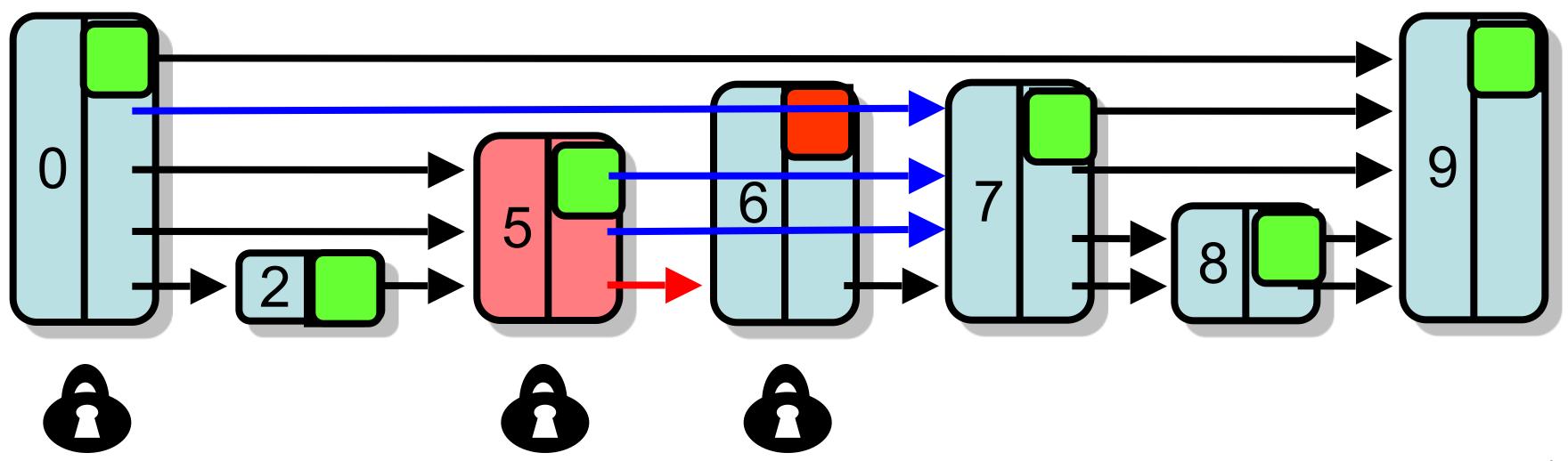
- find() predecessors
- Lock victim
- Set mark (if not already set)
- Lock predecessors (ascending order) & validate
- Physically remove



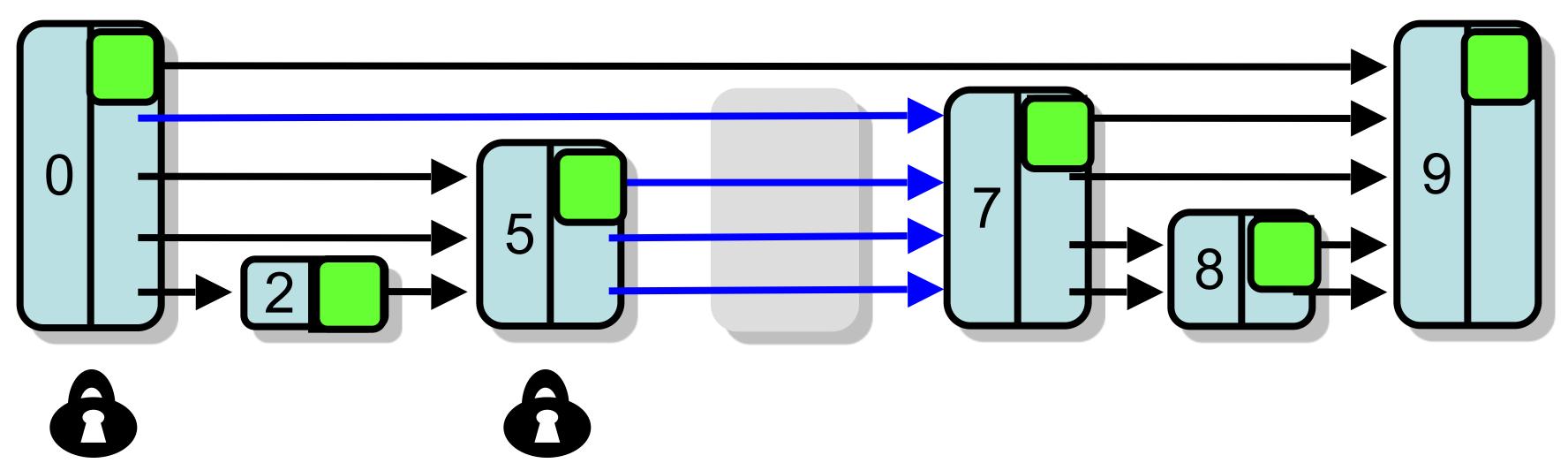
- find() predecessors
- Lock victim
- Set mark (if not already set)
- Lock predecessors (ascending order) & validate
- Physically remove



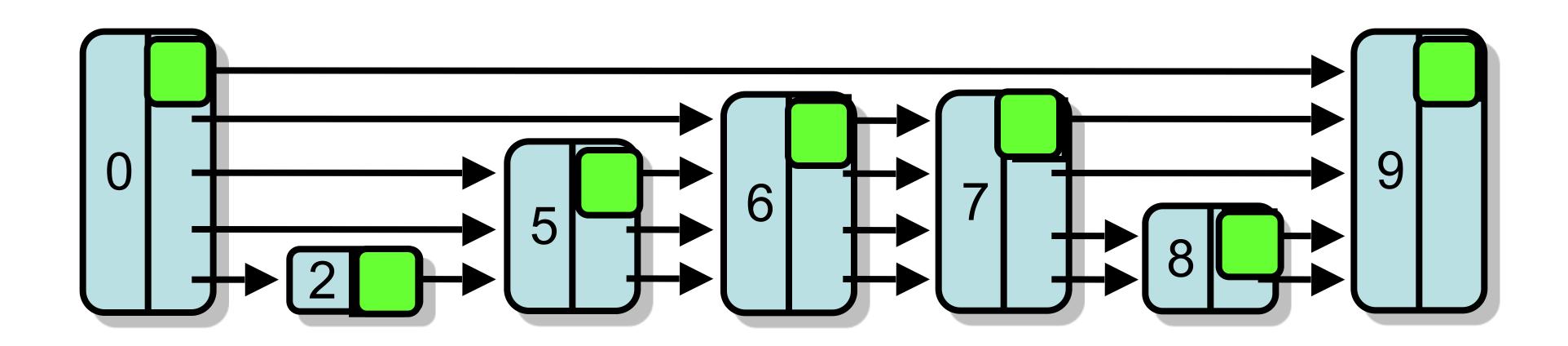
- find() predecessors
- Lock victim
- Set mark (if not already set)
- Lock predecessors (ascending order) & validate
- Physically remove



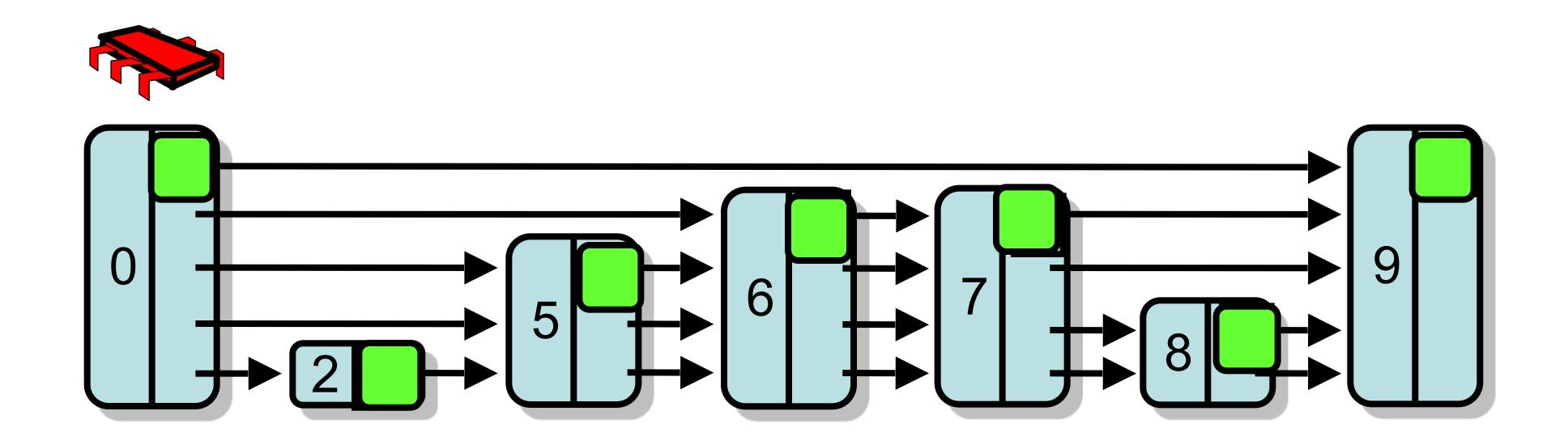
- find() predecessors
- Lock victim
- Set mark (if not already set)
- Lock predecessors (ascending order) & validate
- Physically remove

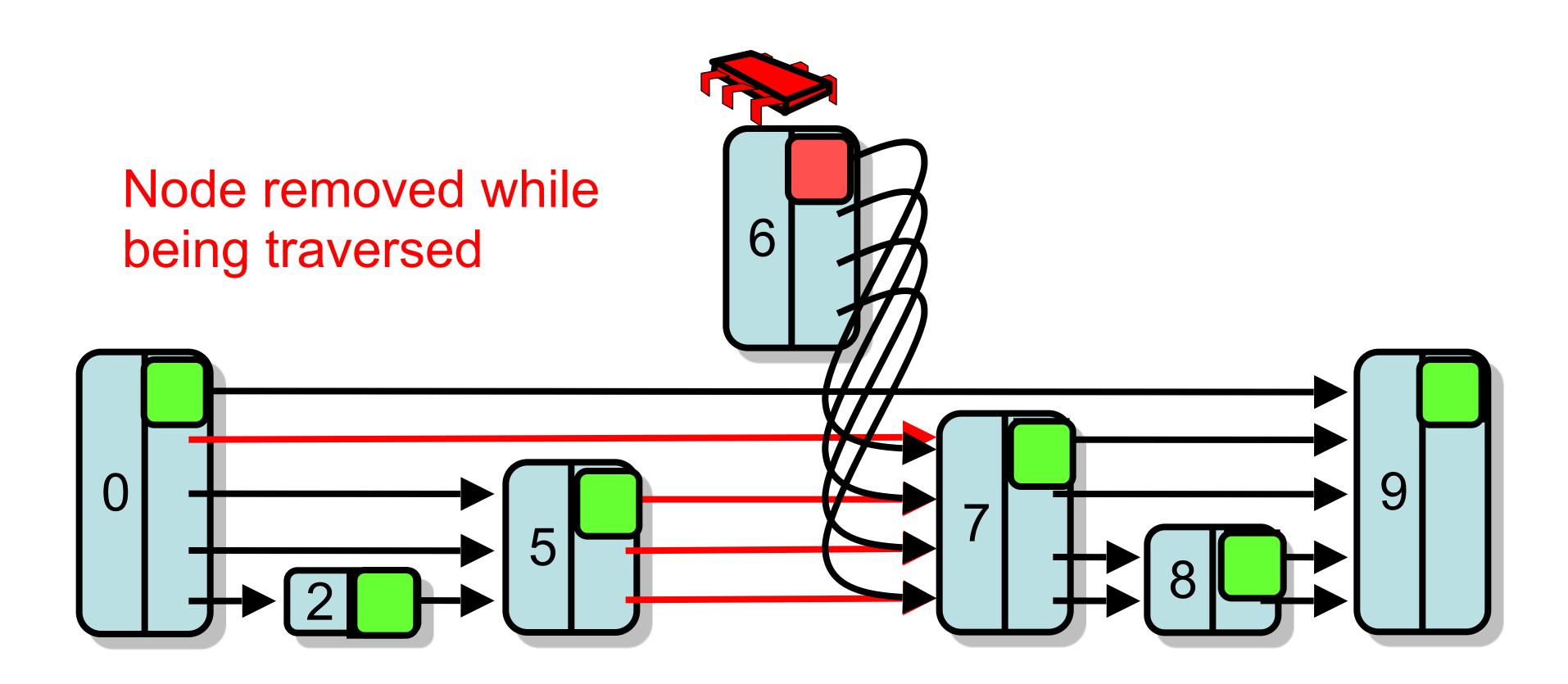


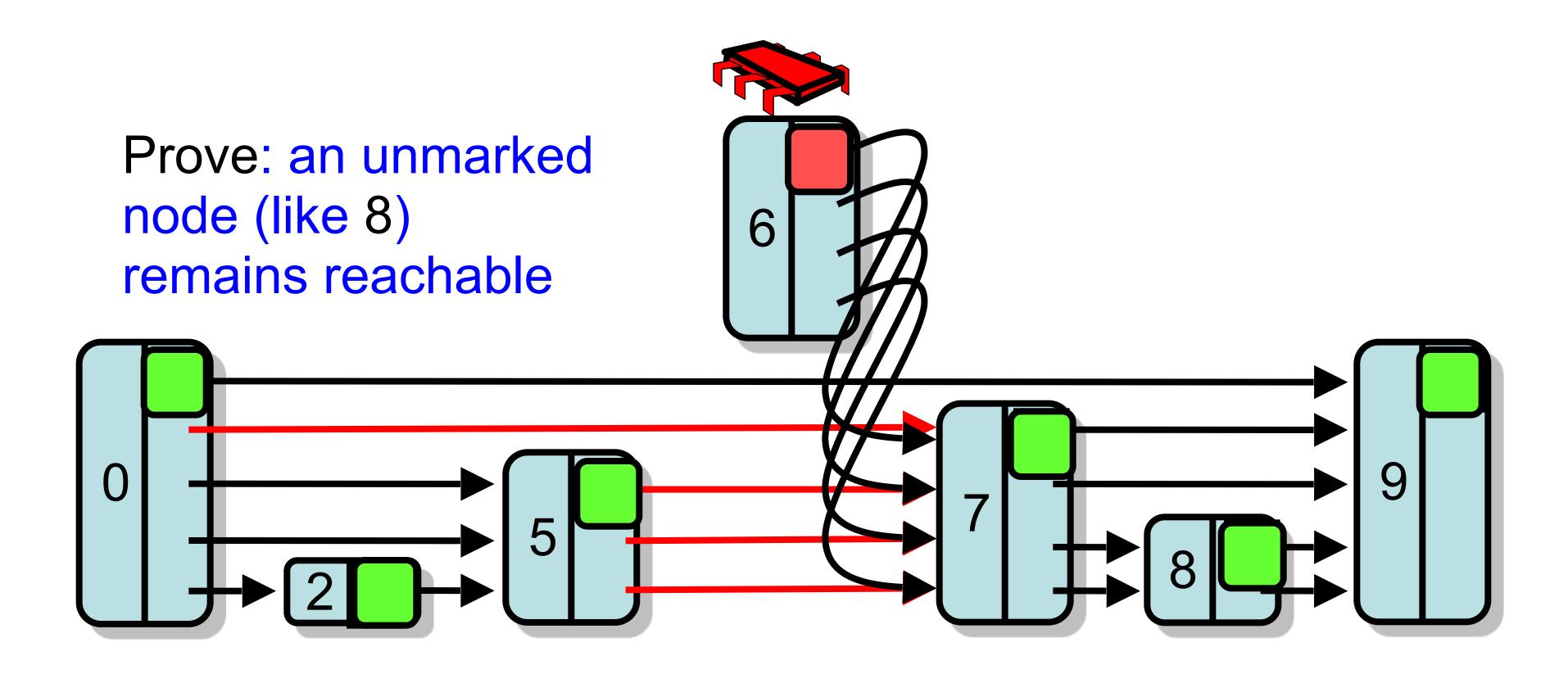
• find() & not marked



Node 6 removed while traversed



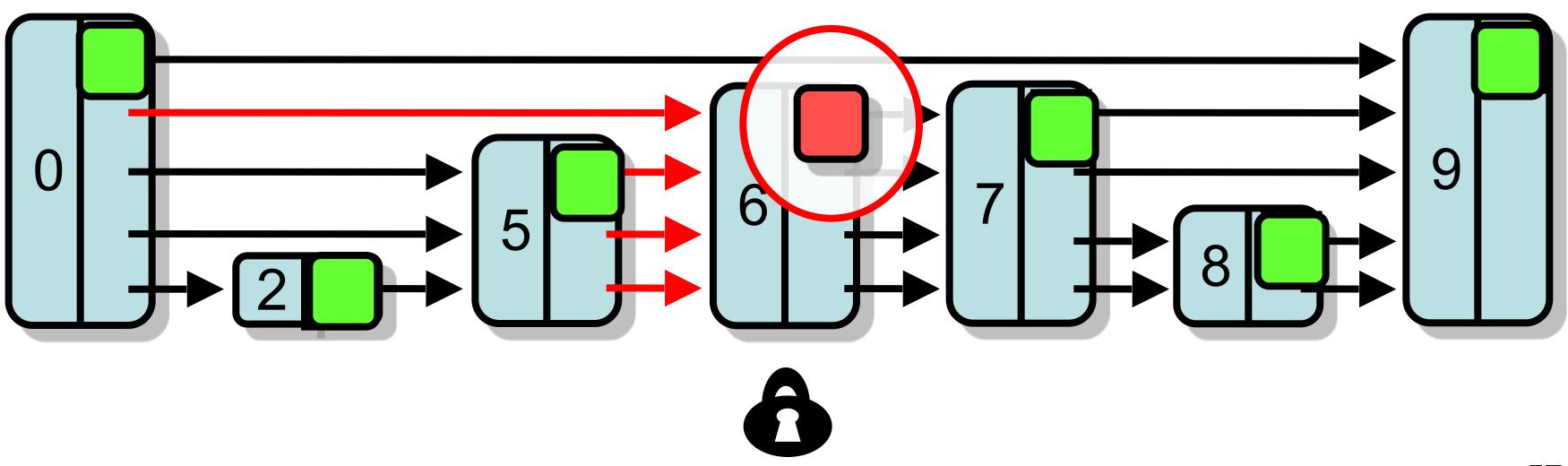




remove(6): Linearization

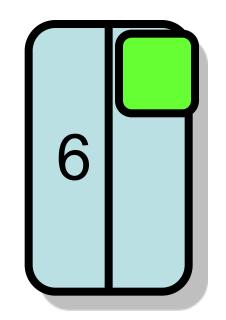
Successful remove happens when bit is set

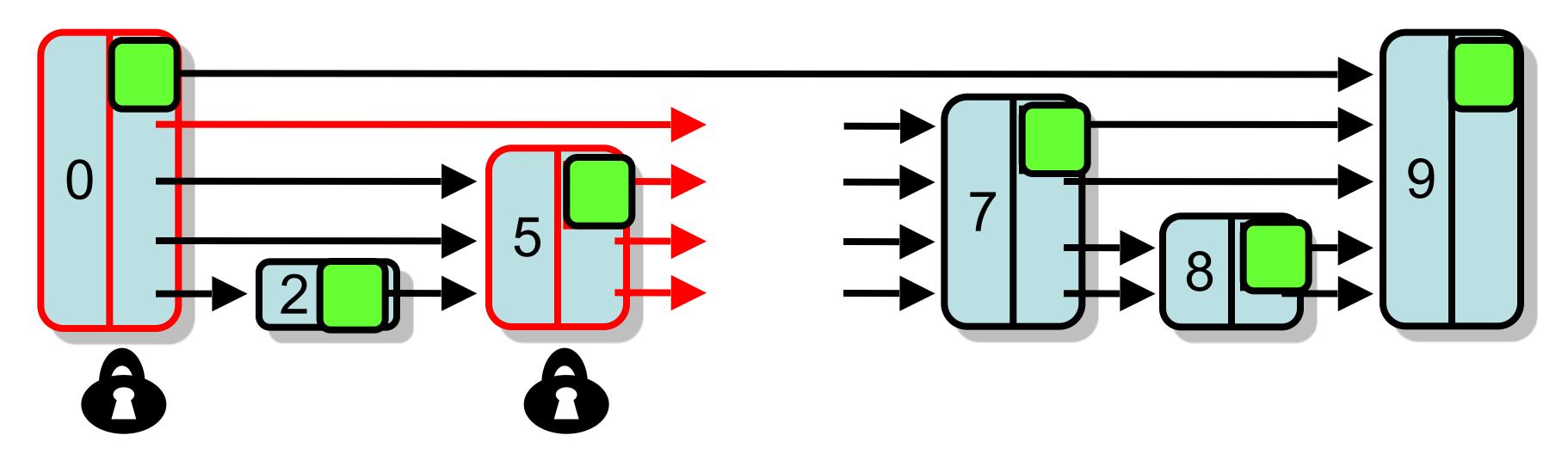
Logical remove...



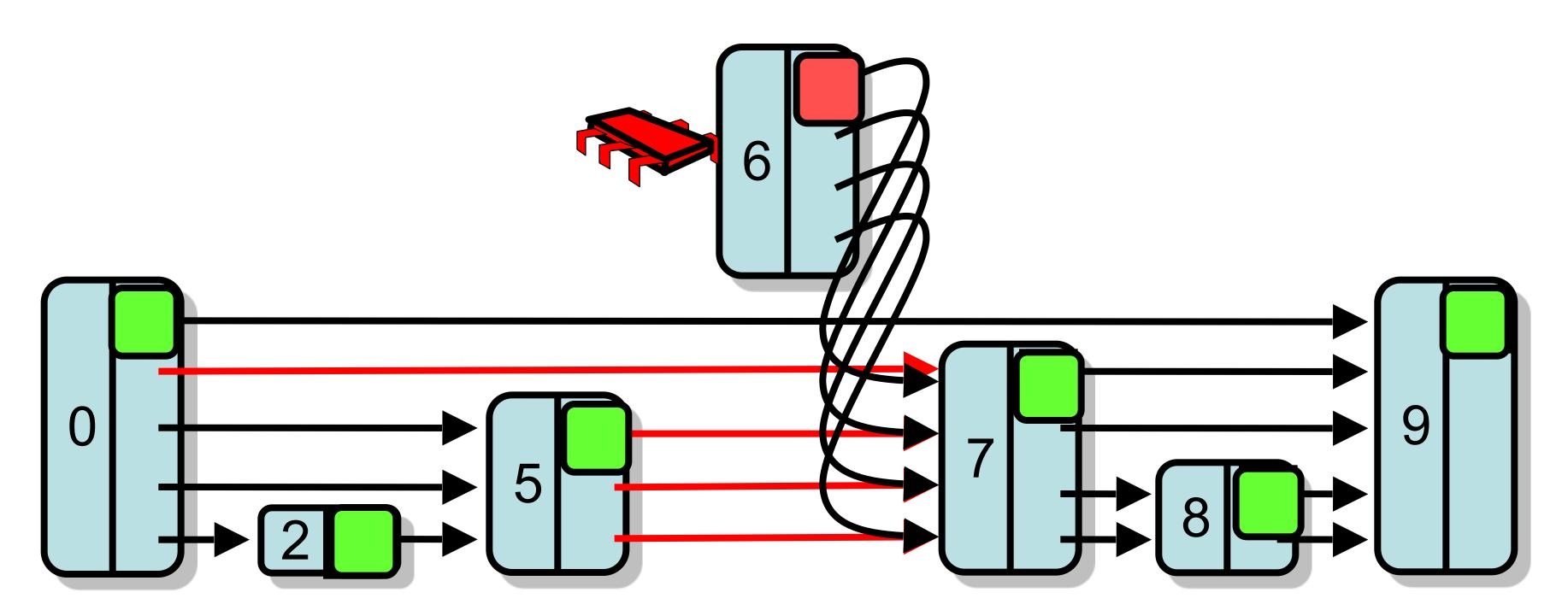
Add: Linearization

- Successful add() at point when fully linked
- Add fullyLinked bit to indicate this
- Bit tested by contains()

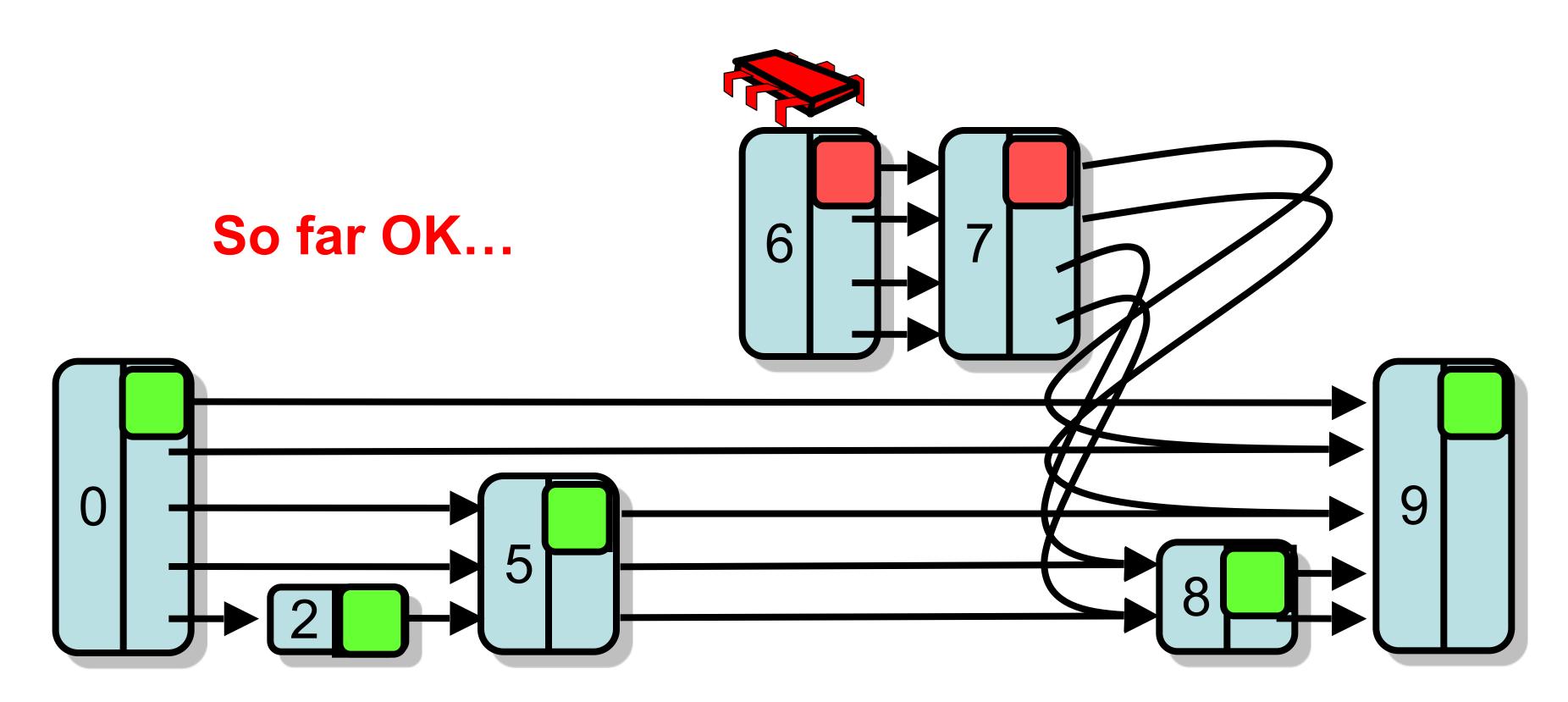




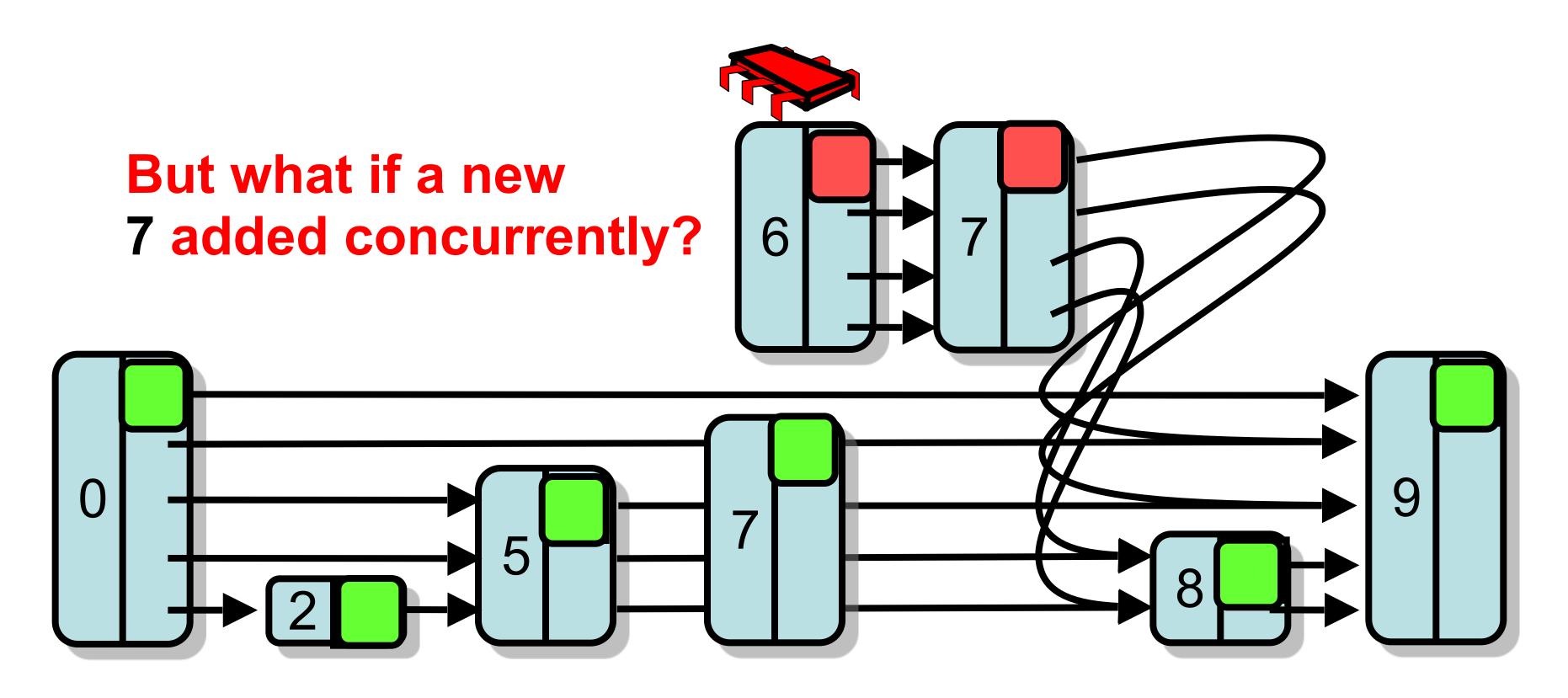
- When fully-linked unmarked node found
- Pause while fullyLinked bit unset



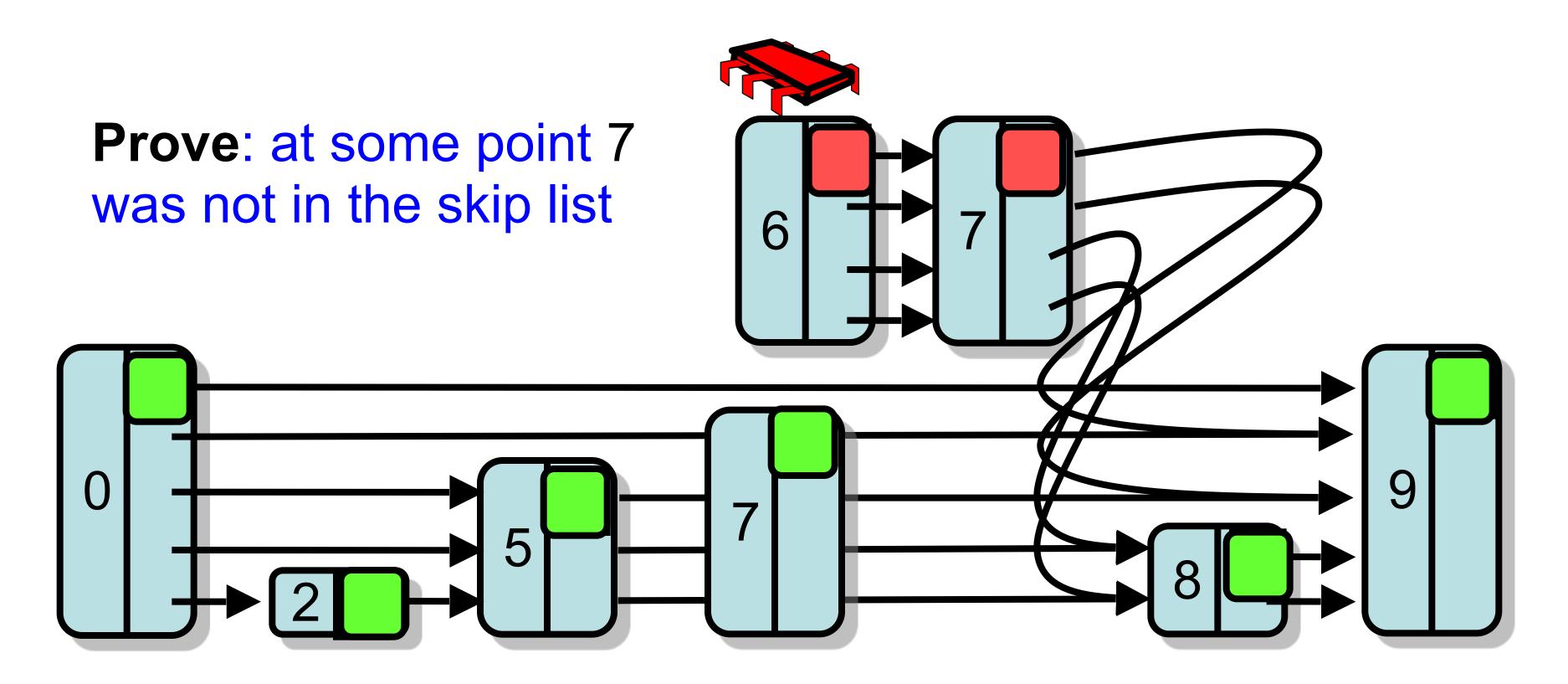
When do we linearize unsuccessful Search?



When do we linearize unsuccessful Search?



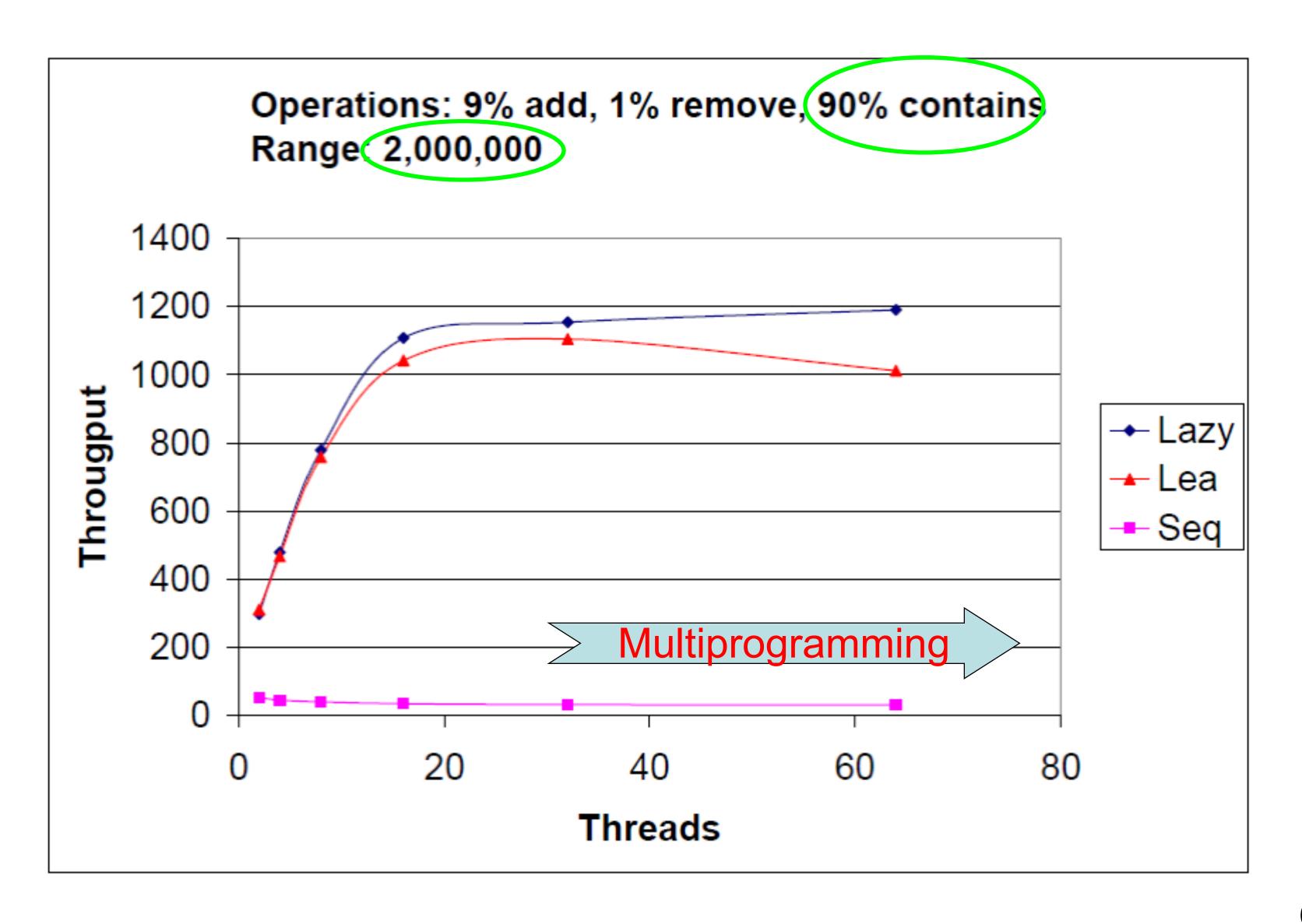
When do we linearize unsuccessful Search?



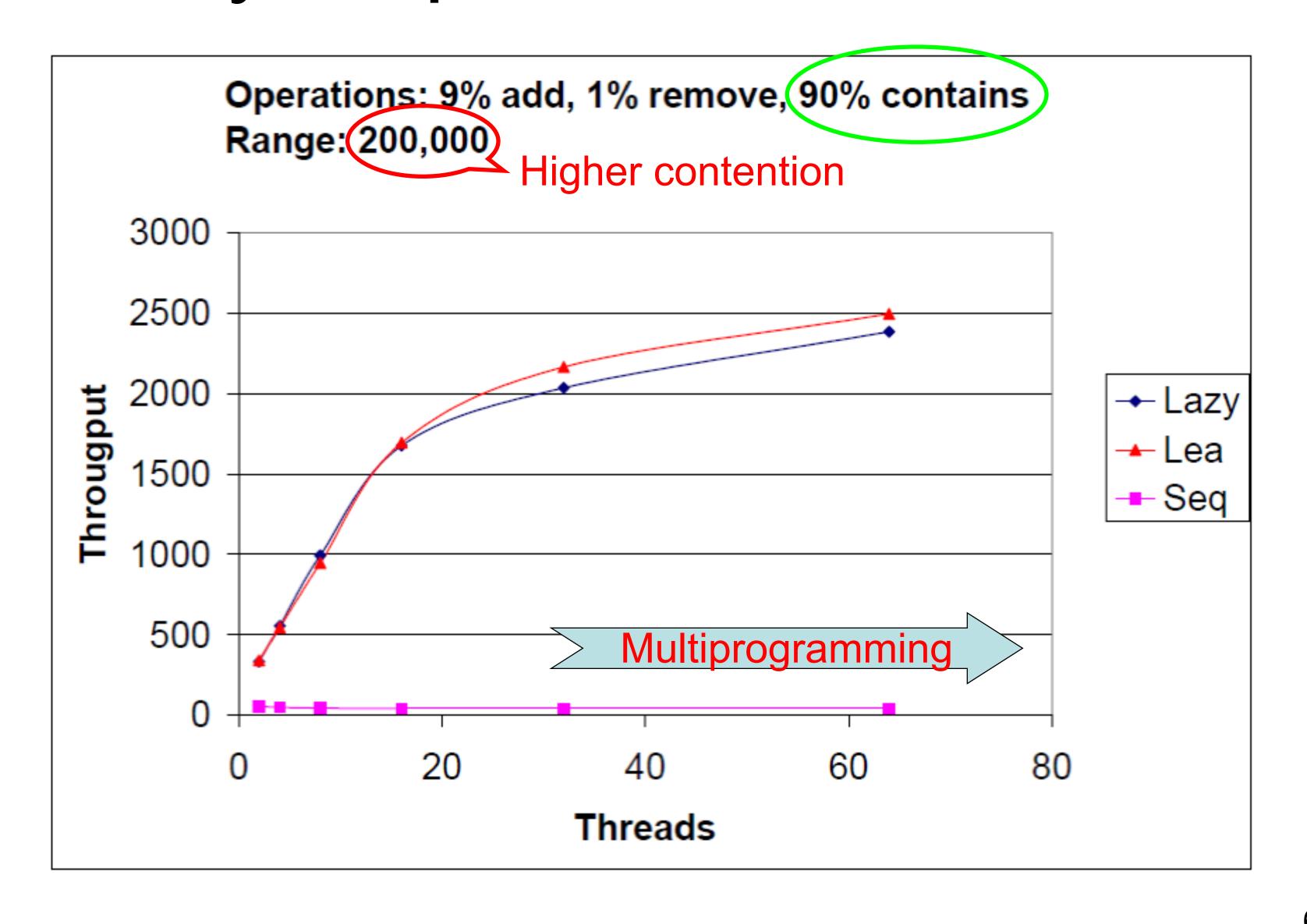
Coding Time!

- Design a benchmark suite for concurrent set implementations allowing arbitrary numbers of threads and operations.
- Use the ideas from the previous lectures.
- Implement it for *optimistic lists*, *lazy lists* and *lazy skip-lists* and determine the winner!
- Also, let's add Java's concurrent set implementation (by Doug Lea) into the mix

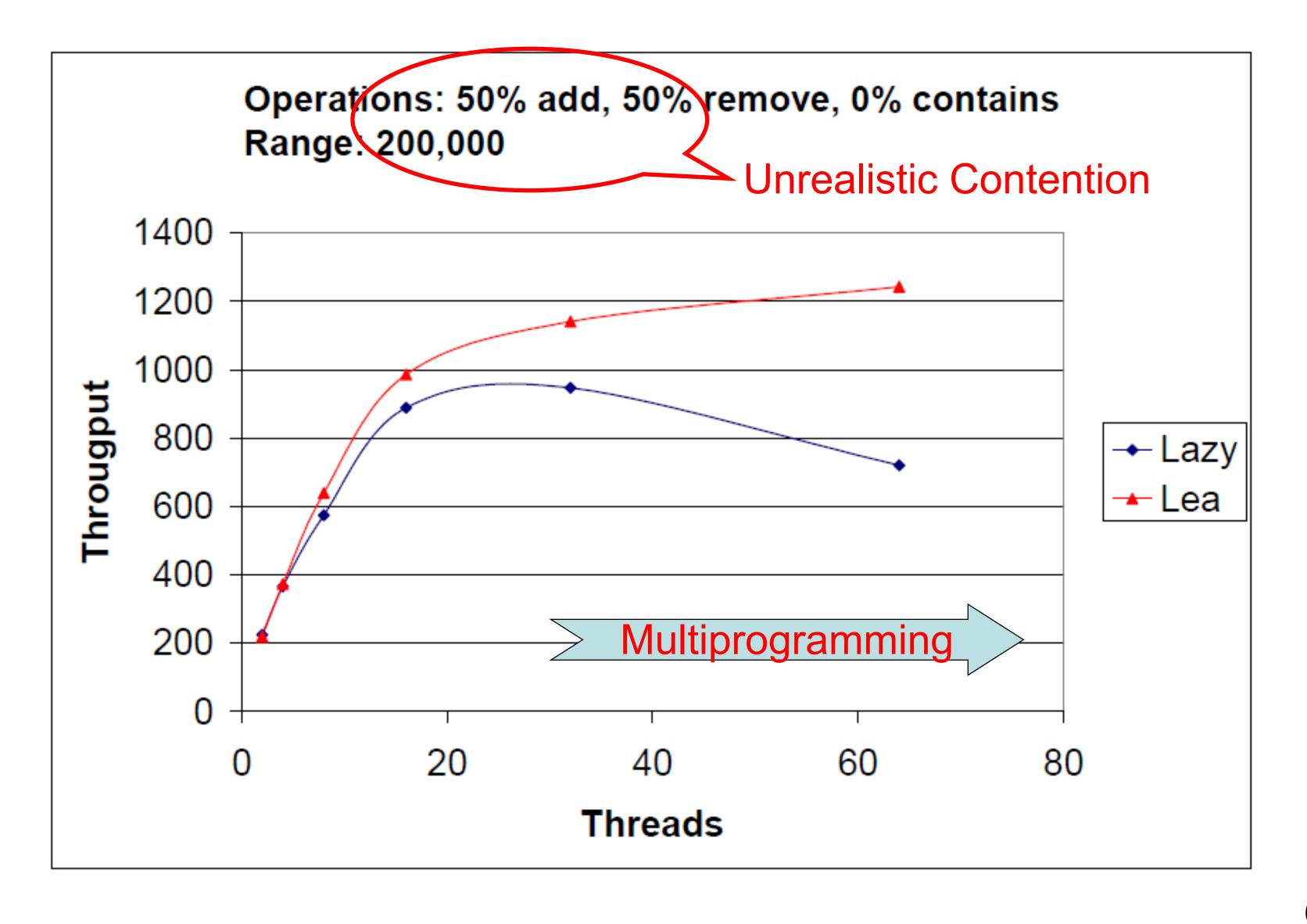
Lazy Skip List: Performance



Lazy Skip List: Performance



Lazy Skip List: Performance



Summary

- Lazy Skip List
 - Optimistic fine-grained Locking

 Performs as well as the lock-free solution in "common" cases

Simple

Next Week: Concurrent Functional Programming



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