

Alternative solution to np.inf in the first greedy approach

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Let $a = \text{distance_matrix}[\text{city}]$, $b = \text{visited}$, c our 'mask'

a	b	c
T	T	F
T	F	T
F	T	F
F	F	F

This is the desired behavior

Easily we understand that $c = A \& (\text{not } B)$

a	b	$x=\text{not}(b)$	$c=a\&n(b)$
T	T	F	F
T	F	T	T
F	T	F	F
F	F	T	F

Actually, if $A=F$ means $B = T$, so last entry is not possible
The mask simply is $\text{not}(b)$

But what does mask actually do?

We use mask to filter `distance_matrix[city]`: we want to take a city not visited with distance > 0 and leave a city visited

Actually, we don't need to perform a `& not(b)`: mask can be defined with only `not(b)`, because when we visit a new city we put a True value in `visited[city]` (`a=F, b=F` not possible in our implementation)

So, mask is simply `np.logical_not(visited)`

How we find the minimum value?

When we compute `dist_matrix[city][mask]` we only check in the position marked as True in the mask: so, calculating the `argmin` gives us the index inside the masked array.

To get the cardinality of that true, we simply add 1 (if `argmin = 0` we refer to the first True value)

Let's use an example and suppose this is our final result:

- `a = np.array([0, 2, 4, 1, 5])`, `not(b) = False, True, False, True, True`

The `np.argmin(a[mask])` returns us 1

- we are looking for the 1+1 True value corispondance in the mask

The second True value has index = 3. `a[3] = 1`, which is the minimum value

Find k-occurrence

We define a function

```
def find_kth_occurrence(lst, element, k):  
    occurrences = (i for i, x in enumerate(lst) if x == element)  
    return next(islice(occurrences, k-1, k), -1)
```

to find the k-occurrence of true value in the vector, $k=\text{argmin}()+1$

So we finally get our index of the min in the dist_matrix, computing a not operation and using a find_kth_occurrence function

Bonus: China sample comparison

Trip to visit all cities:

```
Acheng -> Harbin (33.60)
Harbin -> Shuangcheng (53.02)
Shuangcheng -> Yushu (61.85)
Yushu -> Wuchang (47.68)
Wuchang -> Shulan (59.07)
Shulan -> Jishu (17.91)
Jishu -> Jilin city (50.81)
Jilin city -> Jiutai (65.06)
Jiutai -> Dehui (43.68)
Dehui -> Changchun (78.49)
Changchun -> Gongzhuling (59.12)
Gongzhuling -> Siping (54.24)
Siping -> Liaoyuan (71.76)
Liaoyuan -> Meihekou (60.38)
Meihekou -> Panshi (55.16)
Panshi -> Huadian (56.40)
Huadian -> Jiaohe (96.49)
Jiaohe -> Dunhua (82.15)
Dunhua -> Helong (110.22)
Helong -> Longjing (42.88)
Longjing -> Yanji (14.70)
Yanji -> Tumen (26.45)
Tumen -> Huichun (46.09)
...
Qiongsan -> Lasa (2215.54)
Lasa -> Xigaze (219.18)
```

Trip distance: 63962.52 with 727 cities visited

Using np.inf

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Lingao -> Lasa (2162.21)
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Trip distance: 63627.81 with 727 cities visited

Using mask

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Using np.inf

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Trip distance: 63627.81 with 727 cities visited

Using mask

improves the solution!

Code

```
# Initialization
```

```
def find_kth_occurrence(lst, element, k):  
    occurrences = (i for i, x in enumerate(lst) if x == element)  
    return next(islice(occurrences, k-1, k), -1)  
  
visited = np.full((cities.shape[0]), False)  
city = 0  
visited[city] = True  
trip = []  
trip.append(city)  
print("Trip to visit all cities:\n")
```

```
# Cycle
```

```
while not np.all(visited):  
    # visited = np.array(visited, dtype=bool)  
    # support = np.logical_and(distance_matrix[city], np.logical_not(visited))  
    support = np.logical_not(visited)  
    k = np.argmin(distance_matrix[city][support])  
    closest_city = find_kth_occurrence(support, 1, k+1)  
    print(f"{names[city]} -> {names[closest_city]}  
(distance_matrix[city][closest_city]:.2f)")  
    city = closest_city  
    visited[city] = True  
    trip.append(city)  
trip.append(0)
```


