## **Proof of Condition 1**

 $Init \Rightarrow Inv$ 

1.  $Init \Rightarrow TypeOK$ 

PROOF: By Init1.

2.  $Init \Rightarrow MutualExclusion$ 

PROOF: By the definition of MutualExclusion and Init2, which implies InCS(i) is false for both processes i.

3.  $Init \Rightarrow \forall i \in \{0,1\} : InCS(i) \lor (pc[i] = \text{``e2"}]) \Rightarrow x[i]$ PROOF: By Init2, which implies InCS(i) is false and  $pc[i] \neq \text{``e2"}$ , for each i. (Of course, we are using the fact that FALSE  $\Rightarrow P$  is true for any formula P.)

4. Q.E.D.

Proof: By steps 1–3 and the definition of Inv