

# Proving R2 for the Handshake Algorithm

THEOREM  $Inv_H \wedge Inv_H' \wedge Next_H \Rightarrow \overline{[Next_A]_{vars_A}}$

1.  $p1_H \Rightarrow \text{UNCHANGED } \overline{vars_A}$

PROOF: Obvious, since  $p1_H$  implies that  $p$ ,  $c$ , and  $box$  are unchanged.

2. ASSUME:  $Inv_H \wedge p2_H$

PROVE:  $\overline{Producer_A}$

2.1.  $p \oplus c = 0$

PROOF:  $p2_H$  implies  $p = c$ , which by the first two conjuncts of  $Inv_H$  imply  $p \oplus c = 0$ .

2.2.  $box' = \overline{Put_A}(box)$

PROOF: Follows from the definition of  $p2_H$ , since  $\overline{Put_A}(box)$  equals  $Put_H(box)$ .

2.3.  $(p \oplus c)' = 1$

PROOF:  $p2_H$  implies  $(p \oplus c)' = (p \oplus 1) \oplus c$ , which by 2.1 and the first two conjuncts of  $Inv_H$  implies  $(p \oplus c)' = 1$ .

2.4. Q.E.D.

PROOF: By 2.1–2.3, which prove the three conjuncts of  $\overline{Producer_A}$ .

3.  $c1_H \Rightarrow \text{UNCHANGED } \overline{vars_A}$

PROOF: Obvious, since  $c1_H$  implies that  $p$ ,  $c$ , and  $box$  are unchanged.

4. ASSUME:  $Inv \wedge c2_H$

PROVE:  $\overline{Consumer_A}$

PROOF: Similar to the proof of step 2.

5. Q.E.D.

PROOF: By 1–4 and simple logic, because  $Next_H$  equals

$$p1_H \vee p2_H \vee c1_H \vee c2_H$$

and  $\overline{[Next_A]_{vars_A}}$  equals

$$\overline{Producer_A} \vee \overline{Consumer_A} \vee \text{UNCHANGED } \overline{vars_A}$$