## Proof of Step 2.3

2.3. Assume:  $j \in \{0, 1\}$ 

Prove:  $InCS(j)' \lor (pc'[j] = \text{``e2''}) \Rightarrow x'[j]$ 

Remember that  $Inv, i \in \{0,1\}$ , and e2(i) hold by the step 2 assumption.

2.3.1. Case:  $j \neq i$ 

PROOF: The third conjunct of Inv and the 2.3 assumption imply  $InCS(j) \lor (pc[j] = \text{``e2''}) \Rightarrow x[j]$ ; and e2(i) and the case assumption imply that InCS(j), pc[j], and x[j] are unchanged.

2.3.2. Case: j = i

2.3.2.1. pc[i] = ``e2''

PROOF: By e2(i), since pc[i] = ``e2'' is the enabling condition of action e2(i).

2.3.2.2. x[i]

PROOF: By 2.3.2.1, the third conjunct of Inv, and  $i \in \{0,1\}$ .

2.3.2.3. x'[i]

PROOF: By 2.3.2.2 and e2(i), which implies x[i] is unchanged.

2.3.2.4. Q.E.D.

PROOF: 2.3.2.3 and the 2.3.2 case assumption imply x'[j] (which implies  $P \Rightarrow x'[j]$  for any P).

2.3.3. Q.E.D.

PROOF: By 2.3.1 and 2.3.2.