Proof of Step 2.2

2.2. MutualExclusion'

- 2.2.1. It suffices to assume InCS(i)' and prove $\neg InCS(1-i)'$. PROOF: By definition of MutualExclusion.
- 2.2.2. $\neg x[1-i]$

PROOF: By the 2.2.1 assumption and e2(i) (which holds by the step 2 assumption), since an e2(i) step puts process i in its critical section only if $\neg x[1-i]$ equals TRUE.

2.2.3. $\neg InCS(1-i)$

PROOF: By 2.2.2 and $Inv \wedge (i \in \{0,1\})$ (which holds by the step 2 assumption), since the third conjunct of Inv together with $i \in \{0,1\}$ imply $InCS(1-i) \Rightarrow x[1-i]$.

2.2.4. Q.E.D.

PROOF: By 2.2.1, 2.2.3, and e2(i), which implies that pc[1-i] is unchanged and hence InCS(1-i) equals InCS(1-i)'.