



NATIONAL UNIVERSITY OF SCIENCE AND TECHNOLOGY

DEPARTMENT OF COMPUTER SCIENCE

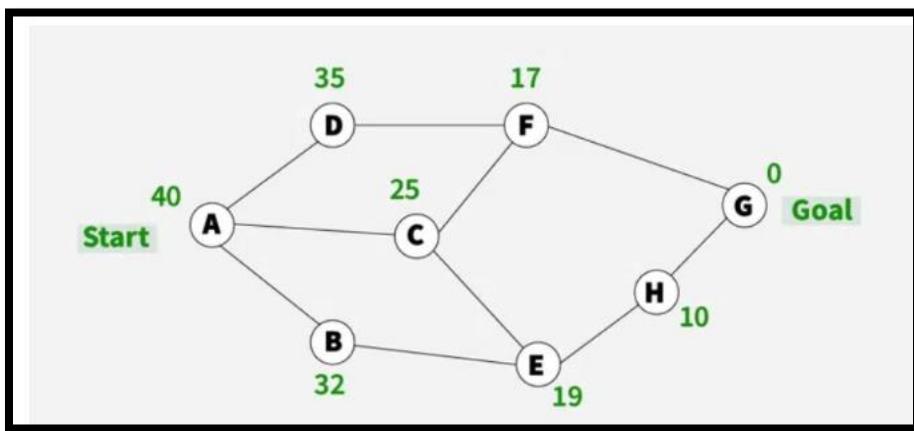
ARTIFICIAL INTELLIGENCE LAB

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| Submitted To | Lec. Ijlal Haider |

IN LAB TASKS

TASK 01:

Traverse the given graph with A as the starting and G as the Goal using greedy best first search. The heuristics value of reaching the goal G from current node is represented along each node.



SOLUTION:

Traverse the given graph with A as the starting and G as the Goal using greedy best first search. The heuristics value of reaching the goal G from current node is represented along each node.

To perform **Greedy Best-First Search (GBFS)** on the graph you provided, we'll use the heuristic values ($h(n)$) at each node to guide the traversal. GBFS always chooses the node with the **lowest heuristic value**—it's greedy because it tries to get to the goal as quickly as possible based on estimated cost, not actual path cost.

Assumptions:

Since the image shows edge weights but not heuristic values, I'll assume you meant that each node is labeled with a heuristic value ($h(n)$) estimating the cost to reach **G**. If you have specific heuristic values, feel free to share them. For now, I'll walk you through a **generic GBFS traversal strategy** using placeholder heuristics.

🔍 Greedy Best-First Search Steps (Example)

Let's assume the following **heuristic values (h)** for each node:

| Node | $h(n)$ |
|------|--------|
| A | 40 |
| B | 35 |
| C | 30 |
| D | 25 |
| E | 20 |
| F | 15 |
| H | 5 |
| G | 0 |

🚀 Traversal from A to G

1. **Start at A** Neighbors: B, C, D, F Heuristic values:
 - B: 35
 - C: 30
 - D: 25
 - F: 15 → **Choose F**
2. **Move to F** Neighbors: D, C Heuristic values:
 - D: 25
 - C: 30 → **Choose D**
3. **Move to D** Neighbors: (already visited F), no new lower-h nodes → backtrack or explore other options from F
4. **Backtrack to F**, try other unexplored neighbor: **C**

5. **Move to C** Neighbors: E Heuristic:
○ E: 20 → **Choose E**
6. **Move to E** Neighbors: H Heuristic:
○ H: 5 → **Choose H**
7. **Move to H** Neighbor: G Heuristic:
○ G: 0 → **Choose G**
8. **Goal reached at G**

Final Path (based on heuristic values):

A → F → C → E → H → G

Note: GBFS does **not** guarantee the shortest path it only follows the lowest heuristic estimate at each step. If you want optimal paths, you'd use A* instead.

CODE:

```
import heapq

# Define the graph as an adjacency list with edge weights
graph = {
    'A': {'D': 35, 'C': 25, 'B': 32, 'F': 17},
    'B': {},
    'C': {'F': 25, 'E': 19},
    'D': {'F': 17},
    'E': {'H': 10},
    'F': {},
    'H': {'G': 0},
    'G': {}
}

# Heuristic values for each node (example values)
heuristics = {
    'A': 40,
    'B': 35,
    'C': 30,
    'D': 25,
```

```

        'E': 20,
        'F': 15,
        'H': 5,
        'G': 0
    }

def greedy_best_first_search(start, goal):
    visited = set()
    priority_queue = []
    heapq.heappush(priority_queue, (heuristics[start],
start))
    came_from = {start: None}

    while priority_queue:
        _, current = heapq.heappop(priority_queue)

        if current == goal:
            break

        visited.add(current)

        for neighbor in graph[current]:
            if neighbor not in visited:
                heapq.heappush(priority_queue,
(heuristics[neighbor], neighbor))
                    if neighbor not in came_from:
                        came_from[neighbor] = current

    # Reconstruct path
    path = []
    node = goal
    while node:
        path.append(node)
        node = came_from.get(node)
    path.reverse()

    return path

# Run the search

```

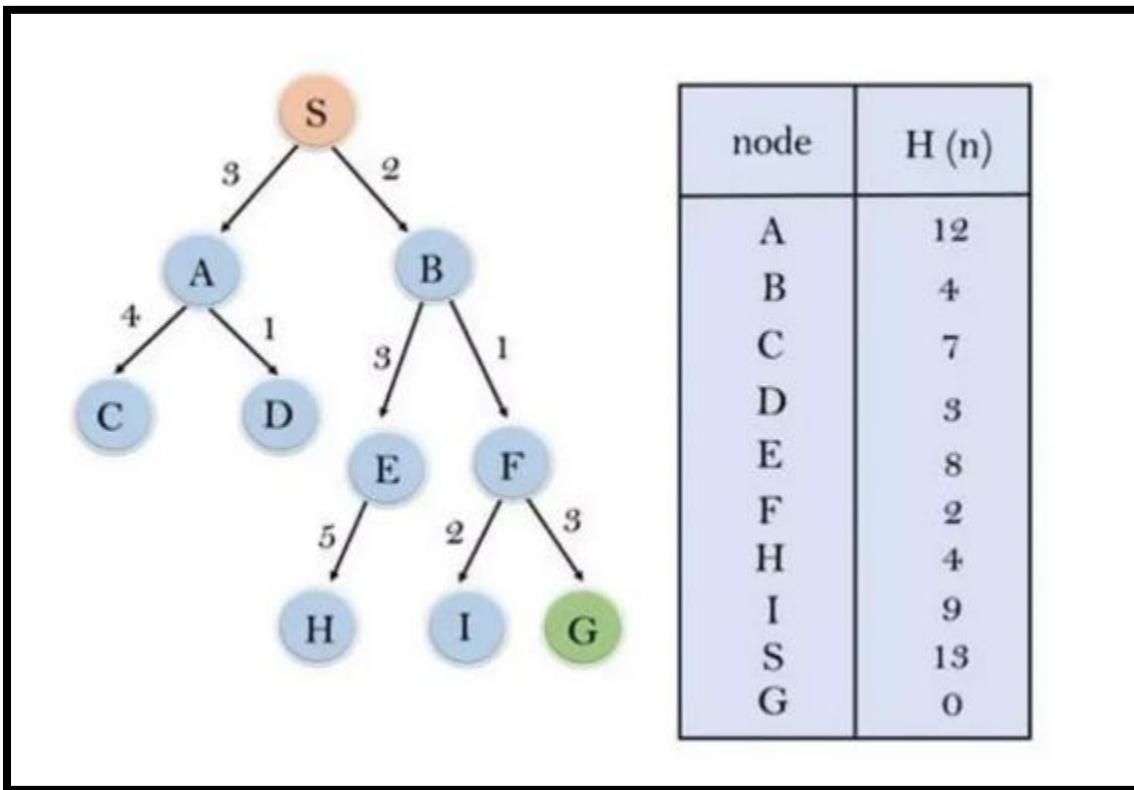
```
path = greedy_best_first_search('A', 'G')
print("Greedy Best-First Search Path:", " → ".join(path))
```

OUTPUT:

Greedy Best-First Search Path: A → C → E → H → G

Task 2

Traverse the given tree with S as the root node and G as the Goal using greedy best first search. The heuristics value of reaching the goal G from current node is represented in the table.



♣ Tree Structure Summary

Edges:

- $S \rightarrow A$ (3), $S \rightarrow B$ (2)
- $A \rightarrow C$ (4), $A \rightarrow D$ (1)
- $B \rightarrow E$ (3), $B \rightarrow F$ (1)
- $E \rightarrow H$ (5), $F \rightarrow I$ (2), $I \rightarrow G$ (3)

Heuristic values ($H(n)$):

| Node | $H(n)$ |
|------|--------|
| A | 12 |
| B | 4 |
| C | 7 |
| D | 3 |
| E | 8 |
| F | 2 |
| H | 9 |
| I | 13 |
| G | 0 |

📌 Greedy Best-First Search Steps

GBFS chooses the next node based **only on the lowest heuristic value**, ignoring actual path cost.

1. **Start at S Children:** A ($h=12$), B ($h=4$) → **Choose B**
2. **Move to B Children:** E ($h=8$), F ($h=2$) → **Choose F**
3. **Move to F Child:** I ($h=13$) → **Choose I**
4. **Move to I Child:** G ($h=0$) → **Choose G**
5. **Goal reached at G**

Final GBFS Path:

S → B → F → I → G

Note: GBFS ignores edge costs and may not find the optimal path—it's fast but not always efficient.

CODE:

```

import heapq

# Tree structure with edge costs
tree = {
    'S': {'A': 3, 'B': 2},
    'A': {'C': 4, 'D': 1},
    'B': {'E': 3, 'F': 1},
    'E': {'H': 5},
    'F': {'I': 2},
    'I': {'G': 3},
    'C': {}, 'D': {}, 'H': {}, 'G': {}
}

# Heuristic values from the table
heuristics = {
    'A': 12,
    'B': 4,
    'C': 7,
    'D': 3,
    'E': 8,
    'F': 2,
    'H': 9,
    'I': 13,
    'G': 0
}

def greedy_best_first_search(start, goal):
    visited = set()
    priority_queue = []
    heapq.heappush(priority_queue,
    (heuristics.get(start, 0), start))
    came_from = {start: None}

    while priority_queue:

```

```

_, current = heapq.heappop(priority_queue)

if current == goal:
    break

visited.add(current)

for neighbor in tree.get(current, {}):
    if neighbor not in visited:
        heapq.heappush(priority_queue,
        (heuristics[neighbor], neighbor))
        if neighbor not in came_from:
            came_from[neighbor] = current

# Reconstruct path
path = []
node = goal
while node:
    path.append(node)
    node = came_from.get(node)
path.reverse()

return path

# Run the search
path = greedy_best_first_search('S', 'G')
print("Greedy Best-First Search Path:", " → ".join(path))

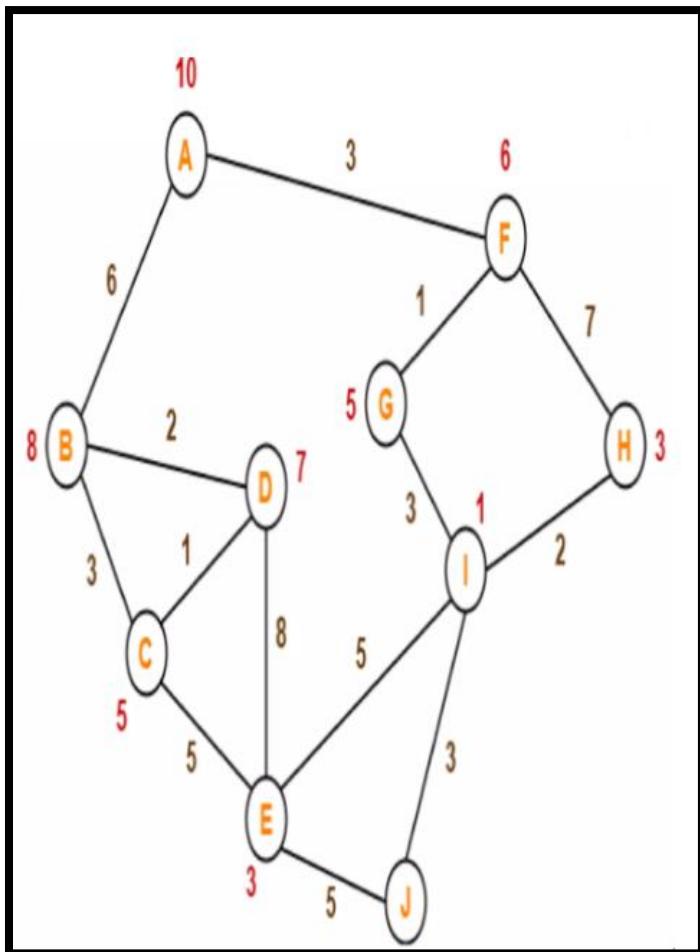
```

OUTPUT:

Greedy Best-First Search Path: S → B → F → I → G

Task 3:

Traverse the given graph with A as the starting node and J as the goal using A* search. The heuristics value of reaching the goal J from current node is represented on the nodes. The cost of each reaching from current node to next node is represented along the edges.



Step-by-Step A* Traversal Strategy

We'll use a **priority queue** to always expand the node with the lowest $f(n)$ value.

Heuristic Values (from red numbers on nodes)

| Node | $h(n)$ |
|------|--------|
| A | 10 |
| B | 8 |
| C | 3 |
| D | 2 |
| E | 3 |
| F | 6 |
| G | 5 |
| H | 7 |
| I | 1 |
| J | 3 |

CODE:

```
import heapq

# Graph with edge weights
graph = {
    'A': {'B': 6, 'D': 3, 'F': 6, 'G': 1},
    'B': {'A': 6, 'C': 3, 'D': 2},
    'C': {'B': 3, 'D': 1, 'E': 7},
    'D': {'A': 3, 'B': 2, 'C': 1, 'E': 8, 'G': 5},
    'E': {'C': 7, 'D': 8, 'I': 5, 'J': 5},
    'F': {'A': 6, 'G': 1, 'H': 7},
    'G': {'A': 1, 'D': 5, 'F': 1, 'I': 3},
    'H': {'F': 7, 'I': 2},
    'I': {'G': 3, 'H': 2, 'E': 5, 'J': 1},
    'J': {'E': 5, 'I': 1}
```

```

}

# Heuristic values
heuristics = {
    'A': 10, 'B': 8, 'C': 3, 'D': 2, 'E': 3,
    'F': 6, 'G': 5, 'H': 7, 'I': 1, 'J': 3
}

def a_star_search(start, goal):
    open_set = []
    heapq.heappush(open_set, (heuristics[start], 0,
start))
    came_from = {start: None}
    g_score = {start: 0}

    while open_set:
        _, current_g, current =
heapq.heappop(open_set)

        if current == goal:
            break

        for neighbor, cost in graph[current].items():
            tentative_g = current_g + cost
            if neighbor not in g_score or tentative_g
< g_score[neighbor]:
                g_score[neighbor] = tentative_g
                f_score = tentative_g +
heuristics[neighbor]
                heapq.heappush(open_set, (f_score,
tentative_g, neighbor))
                came_from[neighbor] = current

# Reconstruct path

```

```
path = []
node = goal
while node:
    path.append(node)
    node = came_from.get(node)
path.reverse()

return path

# Run the search
path = a_star_search('A', 'J')
print("A* Search Path:", " → ".join(path))
```

OUTPUT:

A* Search Path: A → G → I → J

POST LAB TASKS

Task 1

Write a Python program that implements the Greedy Best-First Search algorithm using a graph representation created with a Node class. Each node in the graph should represent a point in the environment and can be connected to other nodes via edges. Your implementation should be able to find a path from a specified start node to a goal node. Implement the algorithm using both Euclidean distance and Manhattan distance as heuristics to estimate the cost from the current node to the goal node.

Hints:

Euclidean Distance:

Manhattan Distance:

Solution:

What We're Building

We'll create a graph where each **node**:

- Has a **name** (like 'A', 'B', etc.)
- Has **coordinates** (x, y) so we can calculate distances
- Can connect to other nodes with **edges** that have costs

Then we'll implement **Greedy Best-First Search**, which:

- Always picks the node with the **lowest heuristic estimate** to the goal
- Doesn't care about actual path cost—just wants to get to the goal fast

► Heuristics We'll Use

| Heuristic | Formula | Description |
|--------------------|--|--|
| Euclidean Distance | $\sqrt{((x_2 - x_1)^2 + (y_2 - y_1)^2)}$ | Measures the straight-line distance between two points. |
| Manhattan Distance | $ x_2 - x_1 + y_2 - y_1 $ | Measures distance along grid lines (horizontal and vertical movement only), like navigating city blocks. |

We'll be able to switch between them by passing the desired function into the search.

Structure Overview

1. **Node class**: Stores name, coordinates, and neighbors
2. **Graph setup**: You manually connect nodes with edge costs
3. **Heuristic functions**: Euclidean and Manhattan
4. **GBFS function**: Uses a priority queue to pick the lowest heuristic node
5. **Path reconstruction**: Traces back from goal to start

CODE:

```
import heapq
import math

# Node class with coordinates and neighbors
class Node:
    def __init__(self, name, x, y):
        self.name = name
        self.x = x # X-coordinate
        self.y = y # Y-coordinate
        self.neighbors = [] # List of tuples:
    (neighbor_node, edge_cost)
    def add_neighbor(self, neighbor, cost):
        self.neighbors.append((neighbor, cost))

# Heuristic: Euclidean distance
def euclidean_distance(node, goal):
    return math.sqrt((goal.x - node.x)**2 + (goal.y - node.y)**2)

# Heuristic: Manhattan distance
def manhattan_distance(node, goal):
    return abs(goal.x - node.x) + abs(goal.y - node.y)

# Greedy Best-First Search algorithm
def greedy_best_first_search(start, goal,
heuristic_func):
    visited = set()
    priority_queue = []
    heapq.heappush(priority_queue,
    (heuristic_func(start, goal), start))
    came_from = {start.name: None}
```

```

while priority_queue:
    _, current = heapq.heappop(priority_queue)

    if current.name == goal.name:
        break

    visited.add(current.name)

    for neighbor, _ in current.neighbors:
        if neighbor.name not in visited:
            heapq.heappush(priority_queue,
            (heuristic_func(neighbor, goal), neighbor))
            if neighbor.name not in came_from:
                came_from[neighbor.name] =
current.name

# Reconstruct path
path = []
node_name = goal.name
while node_name:
    path.append(node_name)
    node_name = came_from.get(node_name)
path.reverse()

return path

# Example usage
if __name__ == "__main__":
    # Create nodes with coordinates
    A = Node('A', 0, 0)
    B = Node('B', 2, 1)
    C = Node('C', 4, 2)
    D = Node('D', 1, 3)

```

```

E = Node('E', 3, 4)
F = Node('F', 5, 5)

# Define edges
A.add_neighbor(B, 2)
A.add_neighbor(D, 3)
B.add_neighbor(C, 2)
B.add_neighbor(E, 4)
D.add_neighbor(E, 2)
E.add_neighbor(F, 3)
C.add_neighbor(F, 2)

# Run GBFS with Euclidean
path_euclidean = greedy_best_first_search(A, F,
euclidean_distance)
print("Path using Euclidean heuristic:", " →
".join(path_euclidean))

# Run GBFS with Manhattan
path_manhattan = greedy_best_first_search(A, F,
manhattan_distance)
print("Path using Manhattan heuristic:", " → ".join(path_manhattan))

```

OUTPUT:

Path using Euclidean heuristic: A → D → E → F

Path using Manhattan heuristic: A → D → E → FS

Task 2

Write a Python program that implements the A* Search algorithm using a graph representation created with a Node class. Each node in the graph should represent a point in the environment and can be connected to other nodes via edges. Your implementation should be able to find a path from a specified start node to a goal node. Implement the algorithm using both Euclidean distance and Manhattan distance as heuristics to estimate the cost from the current node to the goal node.

Solution:

What Is A* Search?

A* is a pathfinding algorithm that finds the **shortest path** from a start node to a goal node using:

- $g(n)$: actual cost from start to current node
- $h(n)$: estimated cost from current node to goal (heuristic)
- $f(n) = g(n) + h(n)$: total estimated cost

It chooses the node with the **lowest $f(n)$** from a priority queue.

Step-by-Step Dry Run

Let's say we have a graph with nodes A → B → C → Goal (F), and each node has coordinates so we can calculate distances.

1. Node Class

Each node has:

- A name (e.g., 'A')
- Coordinates (x, y)
- A list of neighbors with edge costs

```

python
class Node:
    def __init__(self, name, x, y):
        self.name = name
        self.x = x
        self.y = y
        self.neighbors = [] # (neighbor_node, cost)

```

2. Heuristic Functions

We use coordinates to estimate how far each node is from the goal:

- **Euclidean**: straight-line distance

$$h(n) = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

- **Manhattan**: grid-based movement

$$h(n) = |x_2 - x_1| + |y_2 - y_1|$$

These are passed into the A* function so you can switch between them.

3. Priority Queue

We use a min-heap (heappq) to always pick the node with the lowest f(n).

Each entry in the queue is:

python

(f_score, g_score, node)

4. Tracking Costs

We use:

- g_score: actual cost from start to each node
- came_from: to reconstruct the path later

5. Main Loop

- Pop the node with the lowest $f(n)$
- If it's the goal, stop
- For each neighbor:
 - Calculate $\text{tentative_g} = \text{current_g} + \text{edge_cost}$
 - If it's better than previous g, update it
 - Push $(f\text{-score}, g\text{-score}, \text{neighbor})$ into the queue

6. Reconstruct Path

We trace back from goal to start using `came_from`.

CODE:

```
import heapq
import math

# Node class with coordinates and neighbors
class Node:
    def __init__(self, name, x, y):
        self.name = name
        self.x = x # X-coordinate
        self.y = y # Y-coordinate
        self.neighbors = [] # List of tuples:
    (neighbor_node, edge_cost)
    def add_neighbor(self, neighbor, cost):
        self.neighbors.append((neighbor, cost))

# Heuristic: Euclidean distance
def euclidean_distance(node, goal):
    return math.sqrt((goal.x - node.x)**2 + (goal.y - node.y)**2)

# Heuristic: Manhattan distance
def manhattan_distance(node, goal):
```

```

        return abs(goal.x - node.x) + abs(goal.y -
node.y)

# A* Search algorithm
def a_star_search(start, goal, heuristic_func):
    open_set = []
    heapq.heappush(open_set, (heuristic_func(start,
goal), 0, start))
    came_from = {start.name: None}
    g_score = {start.name: 0}

    while open_set:
        _, current_g, current =
heapq.heappop(open_set)

        if current.name == goal.name:
            break

        for neighbor, cost in current.neighbors:
            tentative_g = current_g + cost
            if neighbor.name not in g_score or
tentative_g < g_score[neighbor.name]:
                g_score[neighbor.name] = tentative_g
                f_score = tentative_g +
heuristic_func(neighbor, goal)
                heapq.heappush(open_set, (f_score,
tentative_g, neighbor))
                came_from[neighbor.name] =
current.name

# Reconstruct path
path = []
node_name = goal.name
while node_name:

```

```

        path.append(node_name)
        node_name = came_from.get(node_name)
path.reverse()

return path

# Example usage
if __name__ == "__main__":
    # Create nodes with coordinates
    A = Node('A', 0, 0)
    B = Node('B', 2, 1)
    C = Node('C', 4, 2)
    D = Node('D', 1, 3)
    E = Node('E', 3, 4)
    F = Node('F', 5, 5)

    # Define edges
    A.add_neighbor(B, 2)
    A.add_neighbor(D, 3)
    B.add_neighbor(C, 2)
    B.add_neighbor(E, 4)
    D.add_neighbor(E, 2)
    E.add_neighbor(F, 3)
    C.add_neighbor(F, 2)

    # Run A* with Euclidean
    path_euclidean = a_star_search(A, F,
euclidean_distance)
    print("A* Path using Euclidean heuristic:", " →
".join(path_euclidean))

    # Run A* with Manhattan
    path_manhattan = a_star_search(A, F,
manhattan_distance)

```

```
    print("A* Path using Manhattan heuristic:", " →  
".join(path_manhattan))
```

OUTPUT:

A* Path using Euclidean heuristic: A → B → C → F

A* Path using Manhattan heuristic: A → B → C → F

