

1.3

1.3 $\text{erka}(504, 160)$

$$504 = 3 \cdot 160 + 54$$

$$160 = 2 \cdot 54 + 42$$

$$54 = 1 \cdot 42 + 12$$

$$42 = 3 \cdot 12 + 6$$

$$12 = 2 \cdot 6 + 0$$

2.4

$$11 = 8(3)$$

$$11a - 8b$$

$$3 \mid 11 - 8$$

$$3 \mid 3$$

☺

19en

3.3

$$16x \equiv 36 \pmod{28}$$

$$28 \mid 16x - 36$$

$$28 \mid 4(4x - 9)$$

$$7 \mid 4$$

$$7 \mid 4x - 9$$

☺

$$4x - 9 = 7$$

$$x = 4 \checkmark$$

1. van mogeliken

4.5.6.

$$x \cdot 3 + y \cdot 4 = 40$$

1. $\text{erka}(3, 4) \mid 40 = 1 \mid 40 \checkmark$

$$2. 3x = 40 - 4y \pmod{4}$$

$$3x \pmod{4} = (40 - 4y) \pmod{4}$$

$$3x \pmod{4} = 40 \pmod{4} \quad -4y \pmod{4} = 0$$

$$3x \equiv 40 \pmod{4}$$

$$3. 3x \equiv 40(4) + 4 + 4$$

$$3x \equiv 48(4) \quad / 3$$

$$x \equiv 12 \pmod{4}$$

$$x \equiv 12(4)$$

$$x \in \{12 + 4k \mid k \in \mathbb{Z}\}$$

erka(16, 28) | 36

$$28 = 1 \cdot 16 + 12$$

$$16 = 1 \cdot 12 + 4$$

$$12 = 4 \cdot 4 + 0$$

$$4 \mid 36 \checkmark \text{ van mogeliken}$$

$$16x \equiv 36 \pmod{28} = 29 \pmod{28}$$

$$16x \equiv 64 \pmod{28} \quad / 16$$

$$x \equiv 4 \pmod{28}$$

$$x \equiv 4(7)$$

$$x \in \{4 + 7k \mid k \in \mathbb{Z}\}$$

$$\{4 + 7k_1 \mid k_1 \in \mathbb{Z}\} \cup \{-10 + 7k_2 \mid k_2 \in \mathbb{Z}\}$$

$$\{25 + 28k_3\} \cup \{11 + 7k_4 \mid k_4 \in \mathbb{Z}\}$$

$$\{-17, -10, -3, 4, 11, 18, 25, 32\}$$

$$3x + 4y = 40$$

$$3 \cdot (4k + 4y) = 10$$

$$y = 10 - 3k \quad (k \in \mathbb{Z})$$

$$x, y \geq 0 \in \mathbb{Z}$$

$$4k \geq 0 \Leftrightarrow \underline{k \geq 0} = k_1$$

$$10 - 3k \geq 0 \Leftrightarrow \underline{k \leq \frac{10}{3}} = k_2$$

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$$k \in k_1 \wedge k_2 \Rightarrow 0 \leq k \leq \frac{10}{3} =$$

$$\Rightarrow \underline{k \in \{0, 1, 2, 3\}}$$

7.3

$$9x \equiv 3 \pmod{6}$$

$$5x \equiv -1 \pmod{3} \quad \left(\begin{array}{l} \text{helyett 7 helyett} \\ \text{leghelyesebb} \end{array} \right)$$

$$-x \equiv 4 \pmod{5}$$

① Kiválasztás

$$\text{LCM}(6, 3) = 1 \Rightarrow \text{nem teljesül}$$

$$\text{LCM}(6, 5) = 1 \text{ helyes}$$

$$\text{LCM}(5, 3) = 1$$

$$\textcircled{5} \quad X \equiv C_1 \cdot m_1 \cdot y_1 \pmod{M}$$

$$X \equiv 3 \cdot 35 \cdot 1 + (-1) \cdot 30 \cdot 4 + 4 \cdot 42 \cdot 3 \pmod{210}$$

$$X \equiv 279 \pmod{210}$$

$$\boxed{X \equiv 69 \pmod{210}}$$

$$\textcircled{2} \quad C_1 = 3 \quad m_1 = 6$$

$$C_2 = -1 \quad m_2 = 7$$

$$C_3 = 4 \quad m_3 = 5$$

$$\textcircled{3} \quad M = m_1 \cdot m_2 \cdot m_3 = 6 \cdot 7 \cdot 5 = 210$$

$$M_1 = \frac{M}{m_1} = 210/6 = 35 = 7 \cdot 5$$

$$M_2 = \frac{M}{m_2} = 210/7 = 30$$

$$M_3 = \frac{M}{m_3} = 210/5 = 42$$

$$\textcircled{4} \quad \boxed{M_i \cdot y_i \equiv 1 \pmod{m_i}}$$

$$35y \equiv 1 \pmod{6} \Rightarrow y_1 \equiv 1 \pmod{6}$$

$$30y \equiv 1 \pmod{7} \Rightarrow y_2 \equiv 4 \pmod{7}$$

$$42y \equiv 1 \pmod{5} \Rightarrow y_3 \equiv 3 \pmod{5}$$