

# A Group-Based Approach to Measuring Polarization

Isaac D. Mehlhaff\*

July 7, 2023

## Abstract

Despite polarization's growing importance in social science, its quantitative measurement has lagged behind its conceptual development. Political and social polarization are group-based phenomena characterized by intergroup heterogeneity and intragroup homogeneity, but existing measures capture only one of these features or make it difficult to compare across cases or over time. To bring the concept and measurement of polarization into closer alignment, I introduce the cluster-polarization coefficient (CPC), a measure of multimodality that allows scholars to incorporate multiple variables and compare across contexts with varying numbers of parties or social groups. Three applications to elite and mass polarization demonstrate that the CPC returns substantively sensible results, and an open-source software package implements the measure.

---

\*The University of North Carolina at Chapel Hill; mehlhaff@live.unc.edu; word count: 4,499.

Polarization is a key concept in the social sciences, playing a role in important political outcomes ranging from representation (Ahler and Broockman 2018) and party-building (Aldrich 2011) to policymaking (Binder 1999) and democracy (Mason 2018). Conceptually, polarization has two important features: intergroup heterogeneity and intragroup homogeneity. Yet the most common measures of polarization—difference-in-means and variance—are ill-suited to capture both features.

I offer an alternative. The cluster-polarization coefficient (CPC) explicitly models intergroup heterogeneity and intragroup homogeneity, placing polarization’s conceptual foundation front and center. I evaluate the CPC’s ability to discern polarization relative to difference-in-means and variance by applying them to three datasets of elite ideal points and mass party affect. One theoretical and two empirical advantages of the CPC emerge: It better captures the theoretical concept, displays greater flexibility when considering multiple variables, and facilitates measurement of and comparison across cases with more than two groups. Since most party systems have more than two parties and most political conflict occurs along more than one dimension, the CPC provides a very useful tool.

To make the measurement procedure widely accessible, I provide an open-source R package. In addition to calculating the CPC with researcher-specified group memberships, this package contains support for a variety of clustering methods to assign observations to groups, making the measure applicable to a variety of data structures.

## **Features of Polarization**

Polarization tends to manifest both between and within groups, emerging when group members disagree with members of other groups, agree with members of their own, or both. That understanding implies two conceptual features: distance from opponents (intergroup heterogeneity) and concentration within groups (intragroup homogeneity). When scholars conceptualize polarization,

they often reference both features (Aldrich 2011; DiMaggio, Evans, and Bryson 1996; Maoz and Somer-Topcu 2010; Rehm and Reilly 2010).

Yet when operationalizing polarization, the distance between groups tends to be the sole focus (Ahler and Broockman 2018; Layman and Carsey 2002). The emphasis on intergroup heterogeneity is not misplaced; polarization certainly increases as groups grow farther apart. However, the debate about whether polarization exists in the American mass public illustrates why one-feature measurement strategies may miss critical underlying forces. The early twenty-first century witnessed increases in both intergroup heterogeneity and intragroup homogeneity. Indeed, Fiorina (2005) conceded the parties had become farther apart, but dismissed this change as unimportant for polarization because the increase in distance between party means mostly resulted from partisans matching their issue preferences to their party, not necessarily becoming more extreme in their preferences. “Party sorting” as the primary contributor to diverging party ideal points in the American electorate suggests that whatever increase in intergroup heterogeneity that occurred in this case was mostly a function of increasing intragroup homogeneity.

In their critique of Fiorina (2005), Abramowitz and Saunders (2008) theorized polarization in terms of distance between parties (intergroup heterogeneity). Yet their most compelling evidence of polarization actually revealed increasing intragroup homogeneity. Specifically, they found Republicans were increasingly likely to adopt conservative positions on a wide range of issues, while Democrats were increasingly likely to take liberal positions on those same issues. This increase in what Converse (1964) labeled “constraint” reflects changing opinion patterns within parties, not between them. With the United States becoming qualitatively more polarized over the past twenty-five years, it is noteworthy that the foundational evidence from this debate better reflects the importance of intragroup homogeneity, even as the dialogue focused on the distance between parties.

More important than the fact that greater intragroup homogeneity can mechanically produce more intergroup heterogeneity through a process like party sorting is the theoretical importance of intragroup homogeneity in understanding group identity and conflict. Group members tend to

be able to perceive increases in the homogeneity of their ingroup (Park and Judd 1990), which leads group members to surmise they have more in common with each other. Such perceptions can strengthen ingroup identities and produce more intergroup conflict, including in networks of political partisans (Parsons 2015). Perceptions of homogeneity within opposing groups is also important. Because group members tend to exaggerate the homogeneity of outgroups, anti-outgroup bias often results (Wilder 1978). For example, when partisans misperceive other parties as being mostly comprised of negatively valenced constituent groups, they tend to see those out-partisans as more extreme, view them negatively, and express stronger allegiance to their own party (Ahler and Sood 2018). Taken together, measures of polarization would be well-served to account for both intergroup heterogeneity and intragroup homogeneity.

## Cluster-Polarization Coefficient

Recognizing that a measure of polarization should account for both intergroup heterogeneity and intragroup homogeneity does not point to an obvious solution. A survey of eight political science journals reveals 322 articles published about polarization since 2000,<sup>1</sup> employing at least twenty distinct operationalizations. Two approaches account for most uses: Measures of difference-in-means and variance are used in 57% and 14% of articles, respectively.<sup>2</sup> While both indicate movement toward the extremes, neither provides much information about the degree to which that movement is organized as group conflict.

I present a measure—the cluster-polarization coefficient (CPC)—that accounts for both features, beginning from the premise that social scientific data are often comprised of distinct clusters of observations. In politics, clusters are typically represented by parties or social groups. To derive the CPC, I decompose the total variance of this clustered data ( $TSS$ ) in (1) into components

---

<sup>1</sup>See Supplementary Information (SI) section S1 for details.

<sup>2</sup>“Variance” refers to total variance, as opposed to within-group variance.

corresponding to the two features of polarization: the variance accounted for between the clusters ( $BSS$ ; intergroup heterogeneity) and the variance accounted for within all clusters ( $WSS$ ; intra-group homogeneity). Dividing by  $TSS$  and solving for the  $BSS$  term in (1) gives an expression for the proportion of the total variance accounted for by the between-cluster variance—what I call the cluster-polarization coefficient. As it is a proportion, the value produced by this expression varies on the domain  $[0, 1]$ .

$$\begin{aligned} TSS &= BSS + WSS, \\ \rightarrow CPC &= 1 - \frac{WSS}{TSS} = \frac{BSS}{TSS}. \end{aligned} \tag{1}$$

More formally, the CPC takes the expression in (2), where each individual  $i$  in cluster  $k$  holds a position on dimension  $j$ .<sup>3</sup> This construction in terms of  $k$  and  $j$  shows how the CPC facilitates the incorporation of multiple groups and variables, respectively. Expressed in this way, the CPC appears related to a one-way ANOVA  $F$ -statistic and the coefficient of determination ( $R^2$ ). These are useful similarities for deriving properties of the measure (SI sections S2.2-S2.5).

$$CPC = 1 - \frac{\sum_{k=1}^{n_k} \sum_{i=1}^{n_i} \sum_{j=1}^{n_j} (x_{ikj} - \mu_{kj})^2}{\sum_{i=1}^{n_i} \sum_{j=1}^{n_j} (x_{ij} - \mu_j)^2} = \frac{\sum_{k=1}^{n_k} \sum_{j=1}^{n_j} (\mu_{kj} - \mu_j)^2}{\sum_{i=1}^{n_i} \sum_{j=1}^{n_j} (x_{ij} - \mu_j)^2}. \tag{2}$$

Because intra-state political dynamics, the number and nature of sociopolitical cleavages, and the size and number of political coalitions typically vary across countries or within countries over time, one additional modification is needed to make the CPC appropriate for comparison across contexts with varying numbers of observations, variables, and clusters. The expression in (2) will be biased

---

<sup>3</sup>SI section S2.1 shows full derivations.

upward in small samples, so I incorporate corrections for lost degrees of freedom and express the adjusted CPC in (3):<sup>4</sup>

$$CPC_{adj} = 1 - \frac{\frac{\sum_{k=1}^{n_k} \sum_{i=1}^{n_i} \sum_{j=1}^{n_j} (x_{ikj} - \mu_{kj})^2}{n_i - n_j n_k}}{\frac{\sum_{i=1}^{n_i} \sum_{j=1}^{n_j} (x_{ij} - \mu_j)^2}{n_i - n_j}} = 1 - (1 - CPC) \frac{n_i - n_j}{n_i - n_j n_k}. \quad (3)$$

By explicitly modeling both *BSS* and *WSS*, the CPC accounts for both features of polarization. It increases when the distance between groups increases or when groups become more tightly concentrated around their collective ideal point, with the rate of those increases depending on the relative levels of *BSS* and *WSS*.

To illustrate the importance of both features and how the CPC produces more accurate estimates than existing measures, consider the stylized distributions in Figure 1. They imitate four possible combinations of intergroup heterogeneity and intragroup homogeneity. The distribution in plot A has neither feature—two clusters are faintly apparent, but they are close together and display little cohesion. Plot B has high intragroup homogeneity and low intergroup heterogeneity, and plot C has the reverse. The group means are the same in plot B as in plot A, but the groups are more concentrated. Intragroup homogeneity is the same in plot C as in plot A, but group means are further apart. Finally, plot D has high levels of both characteristics.

A measure accurately capturing polarization should indicate more polarization in plots B, C, and D relative to A and less polarization in plots A, B, and C, relative to D. Plot labels display the polarization estimate for each distribution based on difference-in-means, variance, and the CPC. In all cases, higher numbers indicate greater polarization.

Difference-in-means successfully distinguishes between plots A and C and between plots B and D, assigning a higher polarization estimate to the latter plot in each pairing, but it cannot distinguish plot A from B nor plot C from D. It assigns identical polarization estimates to each

---

<sup>4</sup>The expression in (3) is unbiased and consistent (SI sections S2.2-S2.5). All calculations in this paper use the adjusted CPC.

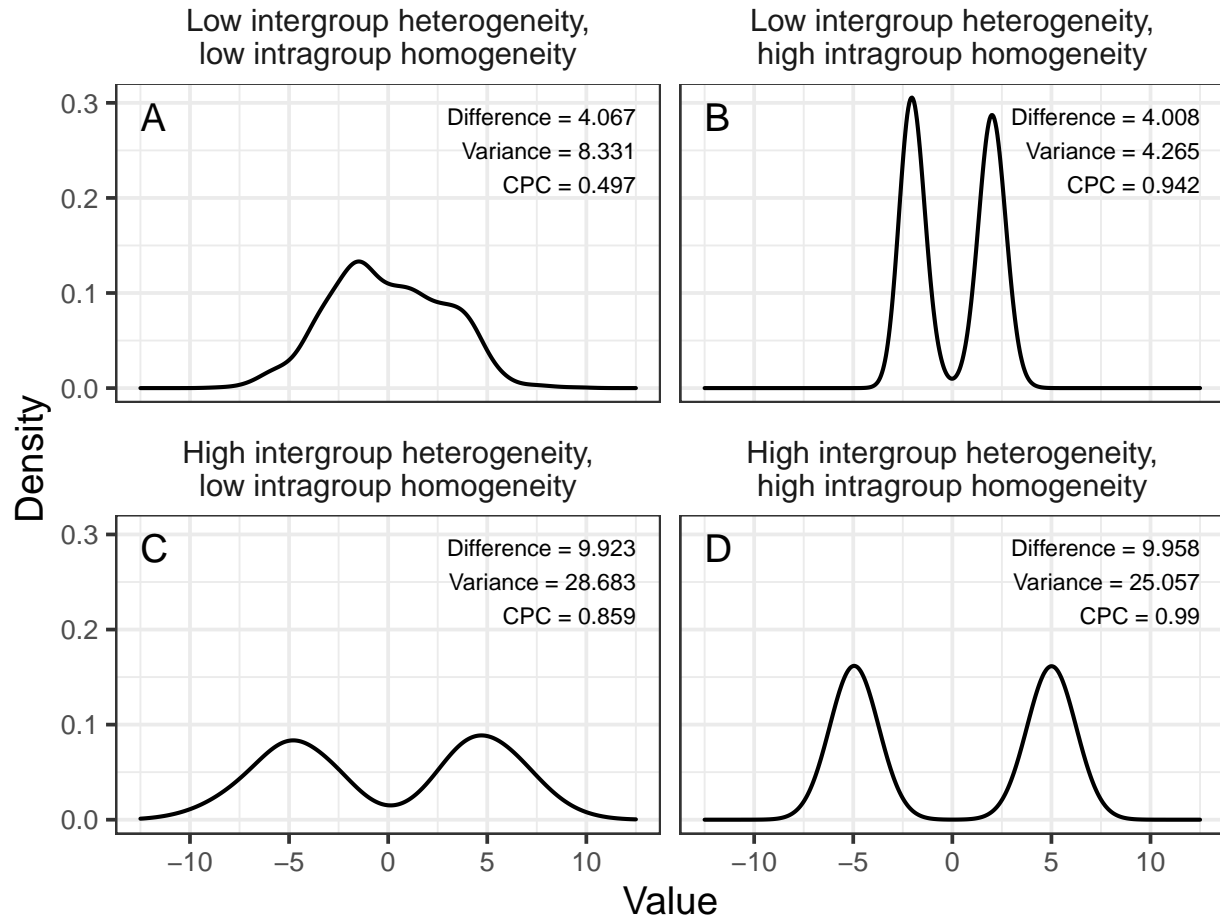


Figure 1: Stylized Distributions of Polarization Features. Simulated bimodal Gaussian mixture distributions with  $\mu_{global} = 0$ . Labels show polarization levels according to each measure.

distribution even though plots B and D are qualitatively more polarized than plots A and C, respectively, reflecting why Levendusky and Pope (2011) urge scholars to “go beyond the mean” when measuring polarization. Variance is frequently offered as one way of doing that, but it performs even worse here. It, too, distinguishes between plots A and C and between plots B and D, but it assigns *lower* polarization estimates to plots B and D relative to plots A and C, opposite the conceptual understanding of polarization. This simple exercise suggests that the most common measures may allow polarization to go undetected in some cases and, in others, identify it where it does not exist. The CPC is the only measure of the three that accurately captures the qualitative differences between all four distributions.

The SI includes several validation exercises. Sections S3.1-S3.3 show that, compared to difference-in-means and variance, the CPC more consistently captures both features of polarization in univariate and bivariate contexts and in distributions with two, three, and four groups. Sections S3.4-S3.5 show the CPC can be sensitive to outliers and large differences in group size, though it still outperforms existing measures and scaling the input data ameliorates outlier sensitivity. Section S4 benchmarks each measure’s performance against “ground-truth” data gathered from human annotators.

## Polarization in Congress: A Multidimensional Test

I investigate the well-established rise in congressional polarization in the United States, showing that the CPC recovers this increase in multidimensional data. I calculate congressional polarization using DW-NOMINATE (Lewis et al. 2021), which uses a scaling procedure to estimate the ideal points of legislators in a two-dimensional latent space. The first dimension is said to capture economic issues and the second racial and other social issues. Because the CPC is expressed in terms of  $j$  in (2) and (3), it can incorporate both variables without needing to average over them or create an index.

A steady increase in party polarization has been one of the defining features of congressional politics in the late twentieth and early twenty-first centuries, occurring in economic, racial, and cultural issue domains (Layman and Carsey 2002). Focusing on the period from 1975 to the present, each measure of polarization should therefore indicate increases whether they examine only the first NOMINATE dimension or incorporate both.

Polarization estimates for each Congress appear in Figure 2. All measures generally capture the expected trend in the first NOMINATE dimension. However, performance diverges with the addition of the second dimension.<sup>5</sup> Difference-in-means detects the increase in polarization that

---

<sup>5</sup>I calculate difference-in-means using the Euclidean distance between group means, and I calculate variance using the trace of the covariance matrix.



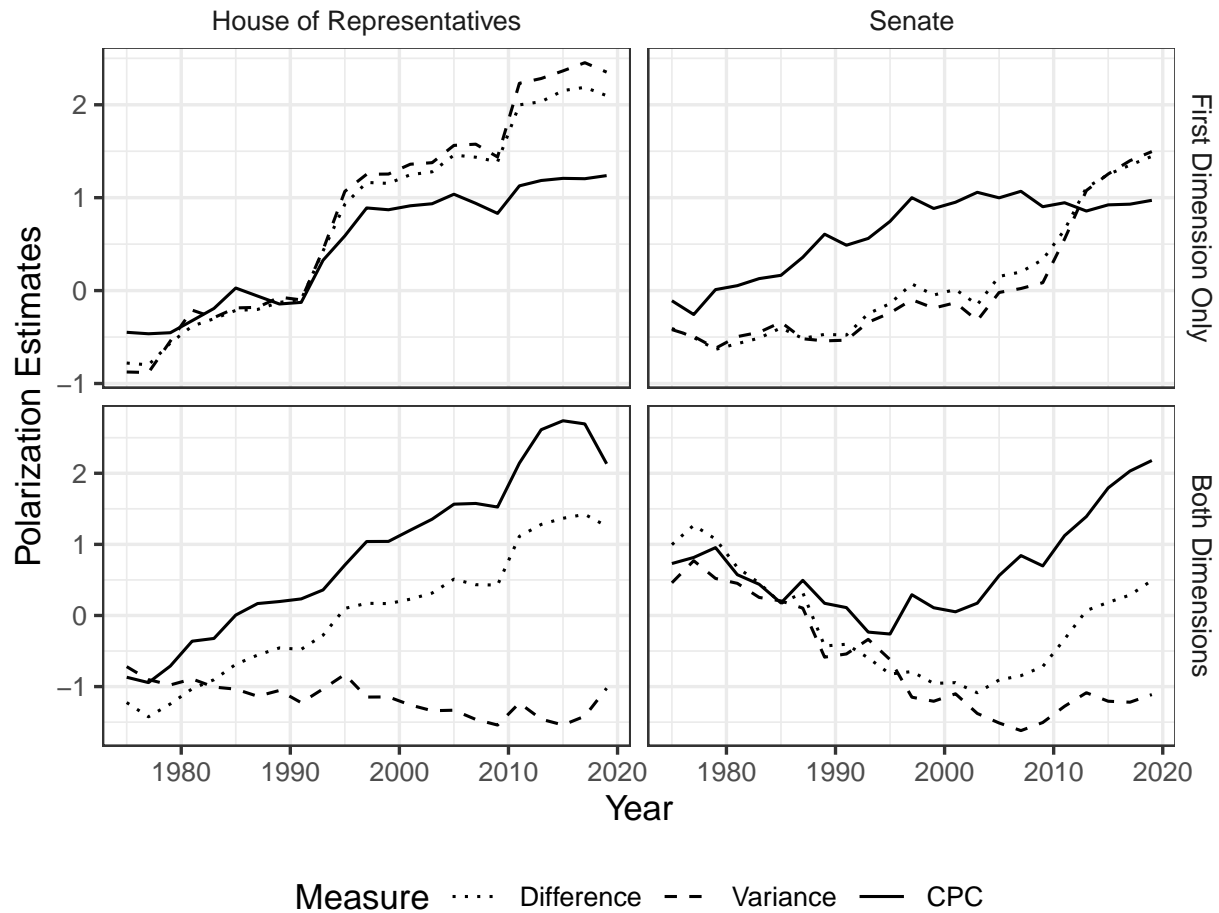


Figure 2: Congressional Polarization Estimates. Calculated using NOMINATE ideal point estimates; each measure unit-normalized to enable comparison.

occurred in the House, but it implausibly suggests the Senate didn't begin polarizing until the mid-2000s and, even in 2019, remained almost a full standard deviation less polarized than it was in the late 1970s. Variance does even worse with the addition of the second dimension, suggesting flat or declining polarization levels leading up to the present-day. The CPC consistently recovers trends that more closely reflect expectations in both one and two dimensions.

Evaluating general trends is informative but, in some cases, it is difficult to tell how much estimates deviate from each other. To assess whether those deviations lead each measure to reflect polarization more or less closely, I evaluate how polarization estimates correlate with each chamber's party unity score—the percentage of legislators voting with their party on votes in which

	House of Representatives			Senate		
	Difference	Variance	CPC	Difference	Variance	CPC
First Dimension Only	0.958	0.95	<b>0.959</b>	0.783	0.682	<b>0.948</b>
Both Dimensions	0.953	-0.837	<b>0.956</b>	-0.799	-0.923	<b>0.065</b>

Table 1: Correlation Between Congressional Polarization Estimates and Party Unity Scores. Bolded values denote measure with highest correlation.

a majority of Democrats oppose a majority of Republicans (Brookings Institution 2022). Each measure should indicate a positive correlation between polarization and party unity.

Results are shown in Table 1. All three measures correlate highly with party unity when examining only the first dimension, though the CPC holds a narrow performance advantage in the House and a significant one in the Senate. When considering both dimensions, difference-in-means shows a strong correlation in the House, though it is again narrowly bested by the CPC. Variance struggles in both chambers, suggesting negative associations between polarization and party unity. Though correlations with all measures are lower in the Senate, the CPC is the only measure that still shows a positive association with party unity.

This underscores an important benefit of the CPC. Aldrich, Montgomery, and Sparks (2014) show that high-dimensional estimates are crucial for accurate ideal point estimation, especially in polarized contexts. Researchers using current measures may need to ignore higher-dimensional information as a pragmatic matter, but the CPC allows it to be preserved, resulting in more accurate polarization estimates.

## Comparative Elite Polarization: A Multi-Group Test

Measuring polarization in multi-party systems is a persistent challenge (Gidron, Adams, and Horne 2020; Wagner 2021). To demonstrate that the CPC can capture polarization across contexts with different numbers of groups, I use a set of elite ideological ideal points from six Western countries (Barberá 2015). As depicted in Figure 3A, these countries differ in the extent to which their latent elite groups are internally homogeneous and externally heterogeneous, and even in how

many groups exist within each country. The United Kingdom and Netherlands have high intergroup heterogeneity, the United States has high intragroup homogeneity, and Spain has a fair amount of both. Italy and Germany both have two identifiable modes, but their intragroup homogeneity is relatively low.

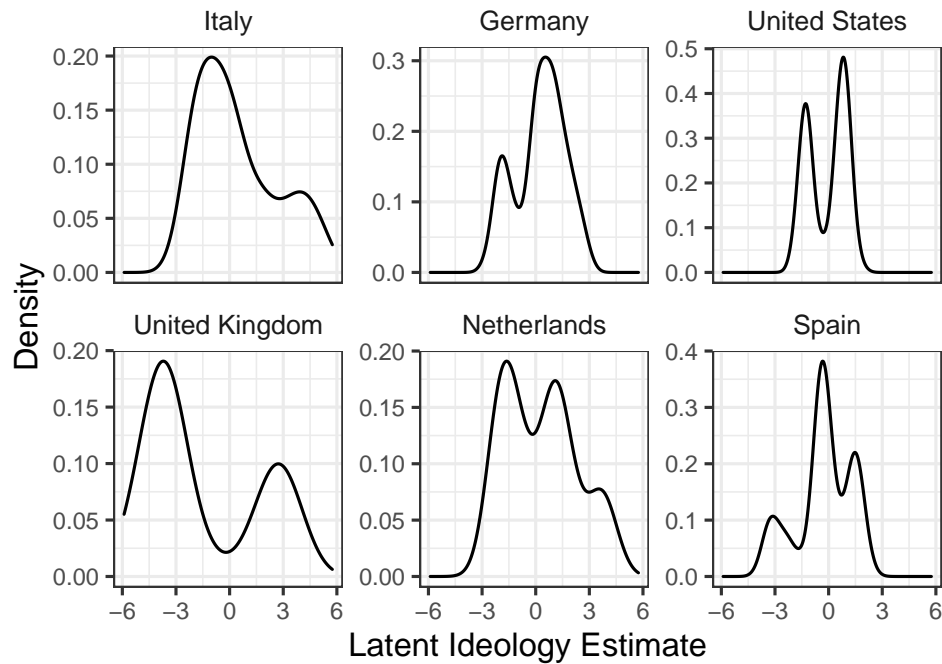
With all this variation, it is difficult to identify polarization levels simply by evaluating density plots. To generate expectations for how countries should compare in their levels of elite ideological polarization, I apply Dalton's (2008) measure of party system polarization to expert-coded data on left-right party positions (Düpont et al. 2022). These benchmarks appear in the upper-left facet of Figure 3B and reveal three groupings. Italy and Germany have similar, low levels of polarization. The United States, United Kingdom and Netherlands are similar to each other in their polarization levels, all higher than those in Italy and Germany. Finally, Spain has by far the highest level of polarization. A well-performing measure of polarization applied to the elite ideology data in Figure 3A should generally reflect these expert judgments.

The other three facets in Figure 3B display the degree to which difference-in-means, variance, and the CPC suggest the party systems are polarized. CPC estimates, shown in the upper-right facet, approximate the expert-coded data much better than difference-in-means or variance do.<sup>6</sup> The CPC indicates that Germany and Italy are the least polarized countries, with the United States, United Kingdom, and Netherlands significantly more so. Though the CPC does not capture the large difference between Spain and the Netherlands that appears in the expert-coded data, it does identify Spain as the most polarized country in the sample.

---

<sup>6</sup>Difference-in-means and the CPC require knowledge of the cluster to which each observation belongs, so I use three clustering methods to assign observations to clusters. Estimates are consistent across methods (SI section S5.2). The number of clusters in each country is implied by Figure 3A. For example, Germany has two clusters, Spain has three, and so on. Silhouette scores corroborate choices of cluster numbers (SI section S5.1). Users should note, however, that different methods sometimes suggest different numbers of clusters—particularly in multidimensional data—and these differences will affect CPC estimates.

## A: Kernel Density Plots of Ideal Points



## B: Ideological Polarization Estimates

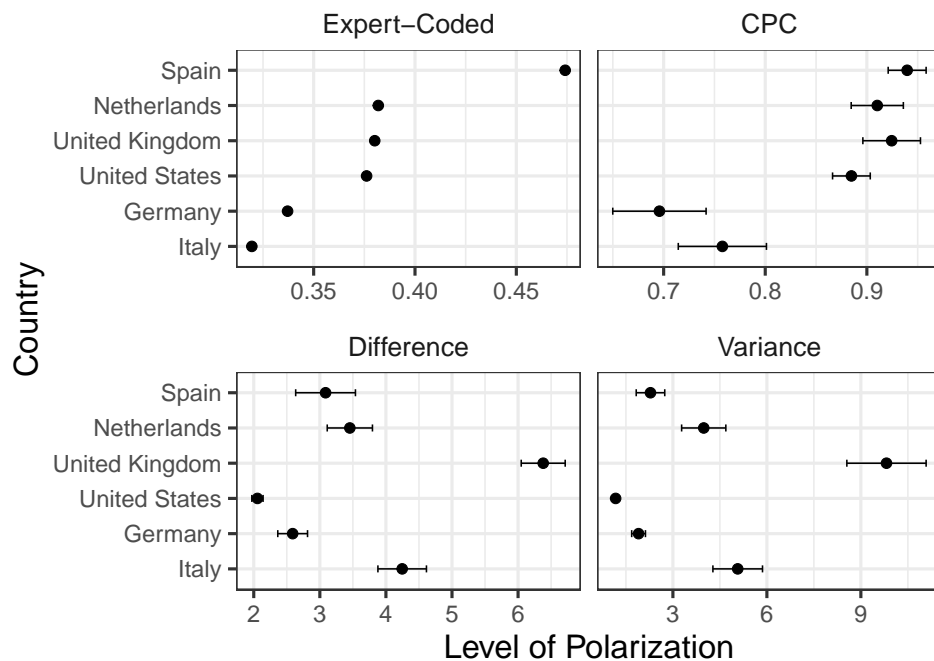


Figure 3: Estimates of Elite Polarization. Kernel density plots for each country (A) and polarization estimates with bootstrapped 95% confidence intervals (B). SI section S5.3 presents point estimates and standard errors.

In contrast, difference-in-means and variance often produce polarization estimates at odds with the expert-coded benchmarks, not to mention the visual representation of the data. Both measures suggest the United States is the least polarized of the six countries, with Italy the second-most polarized despite a near-unimodal distribution of ideal points. Worse still, both difference-in-means and variance suggest polarization in Spain is relatively low, while the expert-coded data show it as by far the highest. In short, they fail to produce polarization estimates that resemble country-expert judgments when there are varying numbers of groups in the data, even in the simplest unidimensional space. The CPC much more closely reflects how experts view ideological polarization in party systems.

## Affective Polarization: Multiple Dimensions and Groups

In the United States, affective polarization appears to run deeper than ideological or issue polarization (Mason 2018), and a robust research program examines this development in comparative perspective (Wagner 2021). In the previous two applications, I addressed problems associated with multidimensional and multi-group data *separately*. By employing party affect data, I can address them *simultaneously*. Party systems have different numbers of parties across cases, meaning the number of groups present in the data will vary. The number of parties also determines the number of dimensions; respondents' assessments across multiple party feeling thermometers represents the several dimensions of their party affect. A measure of polarization should be able to accommodate both sources of variation. To estimate affective polarization, I apply each measure to party feeling thermometers (see also Gidron, Adams, and Horne 2020; Ward and Tavits 2019) from module four of the Comparative Study of Electoral Systems (CSES).

One way to assess validity is to calculate correlations between polarization estimates produced by each measure and indicators that tap attitudes theoretically related to party affect.<sup>7</sup> The CSES contains several good candidates. First, the proportion of respondents indicating “it makes a big

---

<sup>7</sup>See SI section S6.1 for country-level affective polarization estimates.

difference who is in power.” Second, the proportion who believe “who people vote for can make a big difference.” These both capture the degree to which respondents believe their political system presents starkly differentiated options to voters, a belief that likely intensifies with stronger party affect (Ward and Tavits 2019). Third, the proportion of respondents expressing they “feel very close” to their political party. Respondents should hold their party identity more intensely when their party affect is strong (Mason 2018). Finally, the proportion of respondents indicating they occupy extreme positions of a left-right self-placement scale. Citizens tend to distrust parties more when those parties are ideologically distant, so the degree of ideological extremity should also be related to affective polarization (Wagner 2021).<sup>8</sup>

Figure 4 illustrates how affective polarization correlates with each of these items. Each variable should exhibit positive correlations with polarization estimates. That is true of CPC estimates in all four cases. Difference-in-means and variance also uncover a strong, positive relationship between affective polarization and ideological extremity, but their relationships with other variables are less consistent. Difference-in-means uncovers positive correlations between polarization and beliefs about whether it matters who is in power, but variance displays negative associations with that correlate as well as beliefs about whether one’s vote makes a difference. More concerning, difference-in-means and variance suggest that polarization is negatively related to respondents feeling “very close” to their party. This result would seem to be at odds with the very definition of affective polarization, part of which emphasizes in-group affection, a sentiment that should strengthen when group members are more similar to each other. This finding lends further credence to the notion that the measures most often used to measure polarization do not successfully capture intragroup homogeneity, rendering the accounts of polarization they provide incomplete.

---

<sup>8</sup>These expectations are derived in the context of democratic regimes, so I limit my analysis to countries with a Polity score above 8.

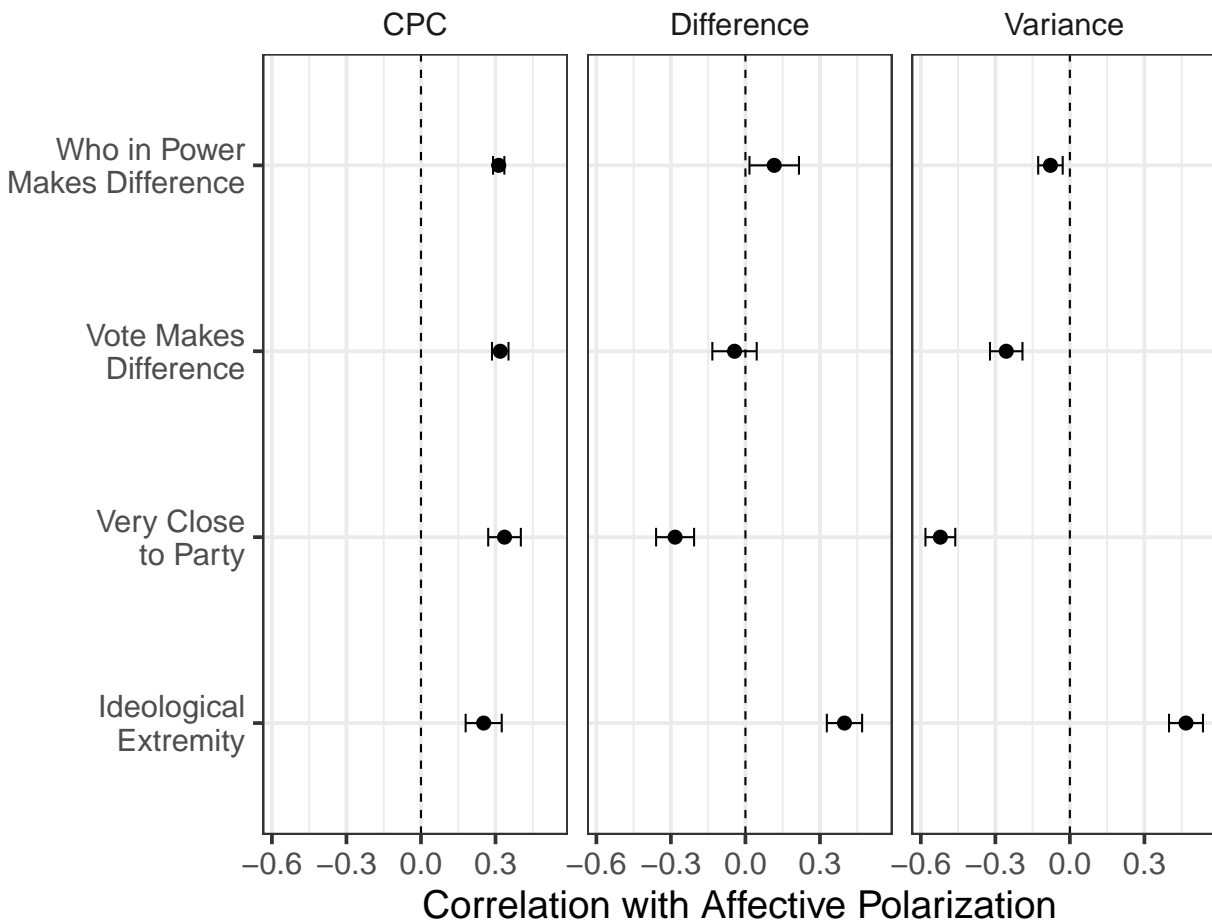


Figure 4: Correlates of Affective Polarization. Error bars give bootstrapped 95% confidence intervals. Full results in SI section S6.2.

## Conclusion

Polarization is a critical concept that bears on a wide variety of social scientific phenomena, yet efforts to quantify it often fail to capture its two conceptual elements: intergroup heterogeneity and intragroup homogeneity. The cluster-polarization coefficient accounts for both features, aligning concept with measure and producing sensible estimates of polarization across contexts. The CPC's greater accuracy is largely driven by its ability to capture intragroup homogeneity, but it should be noted that including this feature may not always be theoretically appropriate or empirically practical. For example, research on party system polarization primarily focuses on ideological

distance between parties, party families, or coalitions at the aggregate level (e.g. Dalton 2008). As such, there are also fewer data points available in each case. In these situations, researchers may still prefer alternate operationalizations of polarization.

Though difference-in-means and variance are the most commonly used measures in political science, the measure perhaps most similar to the CPC is that of Esteban and Ray (1994), which is used most frequently in economics and ethnic studies. However, Clark (2009) shows this measure is not much different from variance, with correlations as high as 0.933. Maoz and Somer-Topcu (2010) further argue it is based on arbitrary assumptions, such as a small number of groups, and is very highly correlated with the number and size of groups. The CPC is conceptually simpler than Esteban and Ray's measure, and the adjusted CPC is explicitly developed to correct for the types of problems scholars have identified with it.

I focused here on party-based polarization, but similar dynamics arise across an array of contexts. Existing work that could benefit from employing the CPC includes studies of polarization in mass policy preferences (DiMaggio, Evans, and Bryson 1996), racial polarization (Jardina and Ollerenshaw 2022), economic polarization (Dwyer 2013), and religious polarization (Montalvo and Reynal-Querol 2003). By introducing the CPC and providing open-source software to simplify its implementation, I aim to advance the critical study of polarization's causes and consequences.

## References

- Abramowitz, Alan I., and Kyle L. Saunders. 2008. "Is Polarization a Myth?" *The Journal of Politics* 70, no. 2 (April): 542–555.
- Ahler, Douglas J., and David E. Broockman. 2018. "The Delegate Paradox: Why Polarized Politicians Can Represent Citizens Best." *The Journal of Politics* 80, no. 4 (October): 1117–1133.
- Ahler, Douglas J., and Gaurav Sood. 2018. "The Parties in Our Heads: Misperceptions about Party Composition and Their Consequences." *The Journal of Politics* 80, no. 3 (July): 964–981.
- Aldrich, John H. 2011. *Why Parties? A Second Look*. Chicago: The University of Chicago Press.



- Aldrich, John H., Jacob M. Montgomery, and David B. Sparks. 2014. "Polarization and Ideology: Partisan Sources of Low Dimensionality in Scaled Roll Call Analyses." *Political Analysis* 22, no. 4 (October): 435–456.
- Barberá, Pablo. 2015. "Birds of the Same Feather Tweet Together: Bayesian Ideal Point Estimation Using Twitter Data." *Political Analysis* 23 (1): 76–91.
- Binder, Sarah A. 1999. "The Dynamics of Legislative Gridlock, 1947-96." *American Political Science Review* 93, no. 3 (September): 519–533.
- Brookings Institution. 2022. *Vital Statistics on Congress*. <https://www.brookings.edu/multi-chapter-report/vital-statistics-on-congress/>.
- Clark, Tom S. 2009. "Measuring Ideological Polarization on the United States Supreme Court." *Political Research Quarterly* 62, no. 1 (March): 146–157.
- Converse, Philip E. 1964. "The Nature of Belief Systems in Mass Publics." In *Ideology and Discontent*, edited by David E. Apter, 206–261. New York: The Free Press of Glencoe.
- Dalton, Russell J. 2008. "The Quantity and the Quality of Party Systems: Party System Polarization, Its Measurement, and Its Consequences." *Comparative Political Studies* 41, no. 7 (July): 899–920.
- DiMaggio, Paul, John Evans, and Bethany Bryson. 1996. "Have American's Social Attitudes Become More Polarized?" *American Journal of Sociology* 102, no. 3 (November): 690–755.
- Düpont, Nils, Yaman Berker Kavasoglu, Anna Lührmann, and Ora John Reuter. 2022. "A Global Perspective on Party Organizations: Validating the Varieties of Party Identity and Organization Dataset (V-Party)." *Electoral Studies* 75 (February).
- Dwyer, Rachel E. 2013. "The Care Economy? Gender, Economic Restructuring, and Job Polarization in the U.S. Labor Market." *American Sociological Review* 78, no. 3 (June): 390–416.
- Esteban, Joan-María, and Debraj Ray. 1994. "On the Measurement of Polarization." *Econometrica* 62, no. 4 (July): 819–851.
- Fiorina, Morris P. 2005. *Culture War? The Myth of a Polarized America*. New York: Pearson Longman.

- Gidron, Noam, James Adams, and Will Horne. 2020. *American Affective Polarization in Comparative Perspective*. New York: Cambridge University Press.
- Jardina, Ashley, and Trent Ollerenshaw. 2022. "The Polarization of White Racial Attitudes and Support for Racial Equality in the US." *Public Opinion Quarterly* 86, no. S1 (August): 576–587.
- Layman, Geoffrey C., and Thomas M. Carsey. 2002. "Party Polarization and "Conflict Extension" in the American Electorate." *American Journal of Political Science* 46, no. 4 (October): 786–802.
- Levendusky, Matthew S., and Jeremy C. Pope. 2011. "Red States vs. Blue States: Going Beyond the Mean." *Public Opinion Quarterly* 75 (2): 227–248.
- Lewis, Jeffrey B., Keith Poole, Howard Rosenthal, Adam Boche, Aaron Rudkin, and Luke Sonnet. 2021. *Voteview: Congressional Roll-Call Votes*. <https://voteview.com/>.
- Maoz, Zeev, and Zeynep Somer-Topcu. 2010. "Political Polarization and Cabinet Stability in Multiparty Systems: A Social Networks Analysis of European Parliaments, 1945–98." *British Journal of Political Science* 40, no. 4 (October): 805–833.
- Mason, Lilliana. 2018. *Uncivil Agreement: How Politics Became Our Identity*. Chicago: The University of Chicago Press.
- Montalvo, Jose G., and Marta Reynal-Querol. 2003. "Religious Polarization and Economic Development." *Economics Letters* 80:201–210.
- Park, Bernadette, and Charles M. Judd. 1990. "Measures and Models of Perceived Group Variability." *Journal of Personality and Social Psychology* 59, no. 2 (August): 173–191.
- Parsons, Bryan M. 2015. "The Social Identity Politics of Peer Networks." *American Politics Research* 43, no. 4 (July): 680–707.
- Rehm, Philipp, and Timothy Reilly. 2010. "United We Stand: Constituency Homogeneity and Comparative Party Polarization." *Electoral Studies* 29, no. 1 (March): 40–53.
- Wagner, Markus. 2021. "Affective Polarization in Multiparty Systems." *Electoral Studies* 69 (February).

- Ward, Dalston G., and Margit Tavits. 2019. "How Partisan Affect Shapes Citizens' Perception of the Political World." *Electoral Studies* 60 (August): 1–9.
- Wilder, David A. 1978. "Reduction of Intergroup Discrimination Through Individuation of the Out-Group." *Journal of Personality and Social Psychology* 36, no. 12 (December): 1361–1374.