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## 大纲



- · 广义线性模型(GLM
- 基本统计方法
- 高级统计方法

# 推荐阅读



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# Statistical Parametric Mapping

The Analysis of Functional Brain Images



Karl J. Friston . John T. Ashburner . Stefan J. Niebel

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## 充 计 学

dical Statistics

孙振球 徐勇勇

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第5版

## 医学统计学

Medical Statistics

孙振球 徐勇勇

副主编 刘红波 马 骏

## Warm-up



### ▶ 目的:

统计描述(descriptive statistics) 统计推断(inferential statistics)

### ▶ 资料类型:

- (1)数值变量(numerical variable) [定量或准确则量的变量,表现为数值大小的不同]
- (2)分类变量(categorical variable) [只有不相容的类别或属性]
  - ① 无序分类变量(计数资料): [无大小之分的属性或类别]

性别:两类无序交量 血型,四类、序变量

② 有序分类变量(等级资料): [各属性或类别有程度之分]

## Warm-up



> 医学统计方法:

①差异性比较

②相关性分析

3影响性分析

两组十十十年

SA-ANDVA

定量资料

定性资料

结局为定量资料—线性回归

结局为定性资料—Logistic回归

结局为生存资料—Cox回归

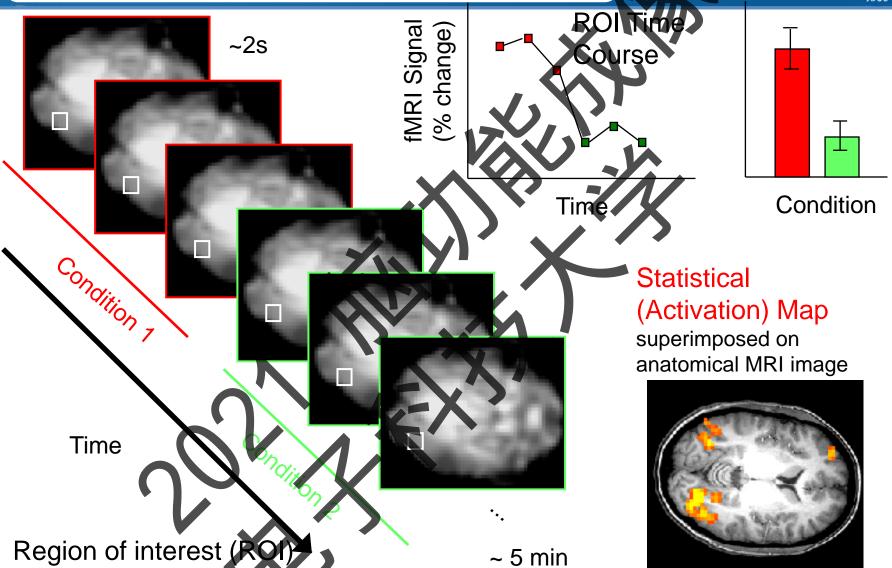




- ➤ Background (GLM)
- > t-test
- One-way /
- > Two-wax ANOVA

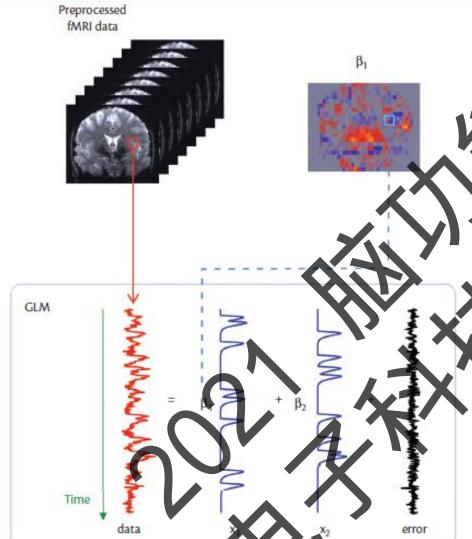
## Statistical Parametric Mapping





### General Linear Model (GLM)





model (X) containing a set of regressors (X) and X2). One beta value (representing an amplitude) is calculated for each of the regressors included in the model (i.e., B 1 for X1 and B2 for X2), and what is left over is the error (i.e., the residuals).

This is typically done for all voxels separately, known as a voxelwise analysis, and the results (beta values, or probabilities based on them) are stored, displayed, and possibly analyzed further in the form of voxelwise maps (images, as shown for B1 in the top right.).





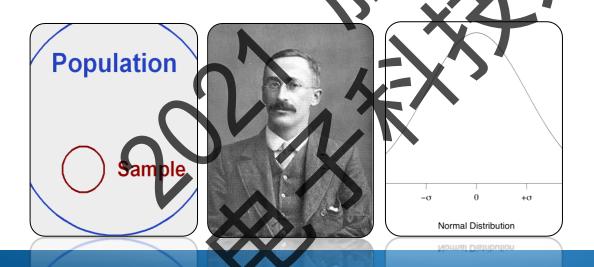
- ➤ Background (GLM)
- > t-test
- One-way A
- > Two-way ANOVA



## *t*-test—Background



- Samples vs Populations
- Descriptive vs Inferential
- William Sealy Gosset ('Student')
- Distributions, probabilities and Pvalues
- Assumptions of t-tests



### *t*-test—one sample/group *t*-test



### Group 1



**S2** 

**S1** 



**S3** 



**S4** 







Sn

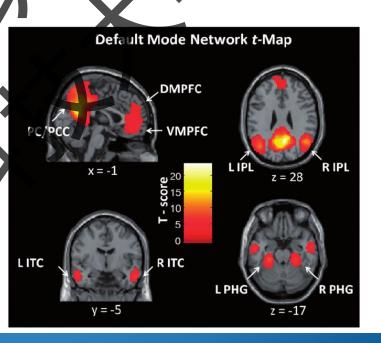


for one group

H0: 
$$\mu = \mu 0 = 0$$
, no corr.

H1: 
$$\mu \neq \mu 0 = 0$$
, a significant corr.

$$t = \frac{\overline{x} - \mu_0}{s / \sqrt{n}},$$



## t-test—two-sample/group t-test



### **Group 1**



P1



**P2** 



**P3** 



**P4** 



**P5** 



### Group 2





**S3** 















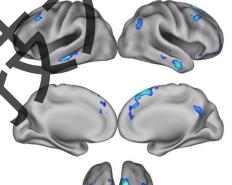


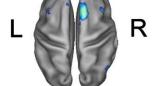
### Is there different connectivity

of PATKINGS and CONTROLs.
Between-subjects

difference

µ1≠µ2, significant diff.





<sup>-1.0</sup> t value -4.0

$$t=\frac{\overline{x}_1-\overline{x}_2}{2}$$

$$S_{\overline{x}_1-\overline{x}_2}$$

$$s_{\bar{x}_1 - \bar{x}_2} = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

### t-test—Paired/matched t-test(I)





Cond 1



Cond 2

**S1 S1** 

**S2 S2** 

**S3 S3** 

**S4 S4** 

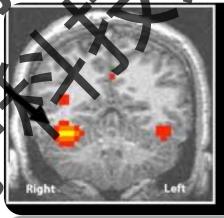
**S5** 

Sn

■ Is there different activation of the FFG Within-subjects for faces vs obje design

H0:  $\mu 1 = \mu 2$ , There is no difference in activation of the FFG during face vs object stimuli

1≠µ2, There is a significant difference in activation of the FFG during face vs object





### t-test—Paired/matched t-test(II)



| Pre- | treatmer | nt |
|------|----------|----|
| (B   | aseline) |    |

Post-treatment (T1)



Group 1

Is there different connectivity of Time O and Time 1.



Group 2

Within-subjects



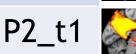
P1\_t0







P2\_t0









H0. µ1=µ2, no difference

design



P3\_t0





H1:  $\mu$ 1+ $\mu$ 2, significant diff.

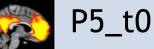


P4\_t0



















Pn\_t0

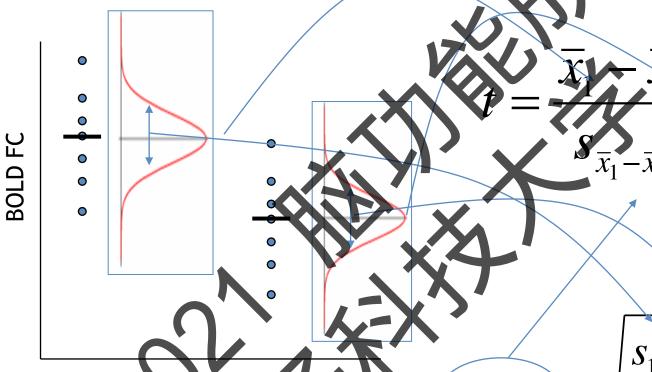




### t-test—Calculating t



\* Independent Samples t-test t = differences between sample means / standard error of sample means



Condition 1 Condition 2 (Patients) (Controls)

$$S_{\overline{x}_1 - \overline{x}_2} = \sqrt{\frac{S_1}{n_1} + \frac{S_2}{n_2}}$$

The exact equation varies depending on which type of t-test used

### *t*-test—Alternatives



- lacksquare 1 Sample t-test (sample vs. hypothesized mean)  $t=rac{\overline{x}-\mu_0}{s/\sqrt{n}},$
- 2 Sample t-test (group1/condition 1 vs group2/condition 2)

|             | Independent  | Related  |
|-------------|--|--|
|             | Samples  | Samples  |
|             |  | also called dependent means test                     |
| Interval    | Independent  | Paired samples                                       |
| measures/   | samples t-test   | t-test   |
| parametric  | $=\frac{\bar{x}_1-\bar{x}_2}{s_{\bar{x}_1-\bar{x}_2}}$ | $t = \frac{\overline{X}_D - \mu_0}{s_D / \sqrt{n}}.$ |
| Ordinal non | Mann-Whitney   | Wilcoxon test  |
| parametric  | U-Test   | )  |
|             |  |  |
| Y A         |  |  |

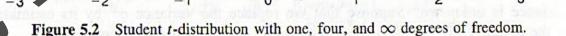
## t-test—Degrees of Freedom (df)



- The number of 'entities' that are free to vary when estimating t
- n 1 (for paired sample t; one-sample)
- n1+n2-2 (for two-sample)
- Larger sample or no. of observations = more df

Putting it all together...

t (df) = t: t-value
p:p-value







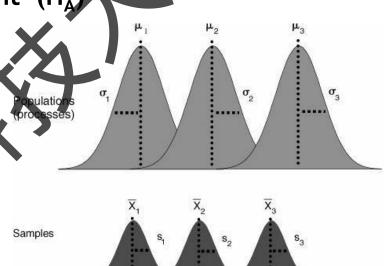
- ➤ Background (GLM)
- > t-test
- One-way A
- > Two-wax ANOVA



## ANOVA- Analysis of Variance



- More than 2 groups and/or conditions
  - e.g. objects, faces and bodies
- Do this without inflating the Type I error rate
- Still compares the differences in means between groups/conditions but it uses the variance of data to calculate if means are significantly different  $(H_A)$
- Tests the null hypothesis that the means are the same via the F- test
- Extra assumptions



### How? The F-statistic

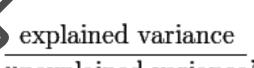


 $\div df$  R

F-ratio =  $MS_M / MS_R$ 

*÷ df* м

- By comparing the variance (SST = SSM + SSR)
  SST (variability between scores)
  SSM (variability explained by model)
  SSR (variability due to individual difference
- F- ratio
  - Magnitude of the difference between the different conditions
  - p-value associated with F is probability that differences between groups could occur by chance if null-hypothesis is correct
  - need for post-hoc testing / planned contrasts (ANOVA can tell you if there is an effect but not where)



unexplained variance'



## One-way ANOVA—Between Groups



One Factor, 3+ levels Is the different connectivity

| Offic   | i accoi,  | J . (C ) ( | is the dumerent connect                    |
|---------|-----------|------------|--|
| Level 1 | Level 2   | Level 3    | among MDD, SZ and HC.                      |
| M1      | <b>S1</b> | HC1        | Between-groups                             |
| M2      | <b>S2</b> | HC2        | design                                     |
| M3      | <b>S3</b> | HC3        | H0: $\mu1=\mu2=\mu3$ , no difference       |
| M4      | <b>S4</b> | HC4        | H1: Means are not all equal.               |
| M5      | <b>S5</b> | HC5        |  |
| •••     |           |            | $df_m=?$ $df_m=g-1$<br>$df_R=?$ $df_R=N-g$ |
| Mn      | Sn        | HCn        | $df_R = ? df_R = N-g$                      |
|         | Sm        | HÖm        |  |
|         |           |            |  |

## One-way ANOVA—Repeated



### One Factor, 3+ levels

Is there diverent connectivity

among Time 0, 1 and 2.

|               | Post-treatmer  | nt            |  |
|---------------|----------------|---------------|--|
| Pre-treatment | (2 weeks)      | Post-treatmen | t within-groups design                                   |
| (Baseline)    |                | (4 weeks)     | H0: $\mu 1 = \mu 2 = \mu 3$ , no difference              |
| Level 1       | Level 2        | Level 3       | H1. Means are not all equal.                             |
| M1_T0         | M1_T1          | M1_ <b>T2</b> | $E = MS_{between} \qquad \qquad E(2.42) =$               |
| M2_T0         | M2_T1          | M2_T2         | $F = \frac{1}{MS_{error}} \qquad F(2,12) =$              |
| M3_T0         | M3_T1          | M3_T2         | $df_{Between} = a - 1 = 3 - 1 = 2$                       |
| M4_T0         | M4_ <b>7</b> 1 | M4_T2         | $df_{Within} = N - a = 21 - 3 = 18$                      |
| M5_T0         | M5_T1          | M54T2         | $af_{Subjects} = s - 1 = 7 - 1 = 6$                      |
| •••           | J<br>シ         |               | $df_{Error} = df_{Within} - df_{Subjects} = 18 - 6 = 12$ |
| M7 TO         | M7 T1          | M7 T2         | $df_{Total} = N - 1 = 21 - 1 = 20$                       |





- ➤ Background (GLM)
- > t-test
- One-way A
- > Two-way ANOVA



## Two-way ANOVA



- 2 way (\_ x \_) ANOVA and even 3 way ANOVA
- Two or more factors and many levels:

| Туре         | 2-way A    | ANOVA for i<br>groups   | ndependent<br>s        | rêpe       | eated measu           | res ANOVA           | mixed Al   | NOVA                    |                        |
|--------------|------------|-------------------------|------------------------|------------|-----------------------|---------------------|------------|-------------------------|------------------------|
| Participants |            |                         | 5                      |            | <b>yı</b>             |                     |            |                         |                        |
|              |            | Condition<br>I          | Condition II           |            | Condition I           | Condition II        |            | Condition<br>I          | Condition II           |
|              | Task I     | Participan<br>t group A | Participant<br>group B | Task       | Partici an            | Participant group A | Task I     | Participan<br>t group A | Participant<br>group B |
|              | Task<br>II | Participan<br>t group   | group N                | Task<br>II | Pakticisan<br>group A | Participant group A | Task<br>II | Participan<br>t group A | Participant<br>group B |
|              |            | Ö                       | V1                     | 术          |                       |                     |            |                         |                        |

## Two-way ANOVA—Between Groups



| A<br>B  | Level 1               | Level 2         |
|---------|-----------------------|-----------------|
|         | S <sub>1</sub>        | S <sub>16</sub> |
| Level 1 | s <sub>2</sub>        | S <sub>17</sub> |
|         | <b>S</b> <sub>3</sub> | S <sub>18</sub> |
|         | <b>S</b> <sub>4</sub> | s <sub>19</sub> |
|         | S <sub>5</sub>        | S <sub>20</sub> |
| Level 2 | S <sub>6</sub>        | 52              |
|         | S <sub>7</sub>        | S <sub>22</sub> |
|         | S <sub>8</sub>        | S <sub>23</sub> |
|         | S                     | S <sub>24</sub> |
|         | S <sub>10</sub>       | \$25            |

健康不吸烟 健康吸烟 精分吸烟 imple effect (4) effect (2) nteraction (1)

# Two-way ANOVA—Repeated



| A<br>B  | Level 1                          | Level 2                          |
|---------|----------------------------------|----------------------------------|
|         | S <sub>1</sub>                   | <b>S</b> <sub>1</sub>            |
| Level 1 | s <sub>2</sub>                   | s <sub>2</sub>                   |
|         | <b>S</b> <sub>3</sub>            | <b>S</b> <sub>3</sub>            |
|         | S <sub>4</sub><br>S <sub>5</sub> | S <sub>4</sub><br>S <sub>5</sub> |
|         | S <sub>5</sub>                   | S <sub>5</sub>                   |
| Level 2 | S <sub>1</sub>                   | 51                               |
|         | S <sub>2</sub>                   | S <sub>2</sub>                   |
|         | S                                | S <sub>3</sub>                   |
|         | \$ <sub>4</sub>                  | S <sub>4</sub>                   |
|         | <b>S</b> <sub>5</sub>            | \S_5                             |

# Two-way ANOVA—Mixed



| A<br>B  | Level 1  | Level 2                          |         |
|---------|--|----------------------------------|---------|
| Level 1 | S <sub>1</sub>   | s <sub>6</sub><br>s <sub>7</sub> |         |
|         | S <sub>3</sub>   | S <sub>8</sub> S <sub>9</sub>    |         |
|         | S <sub>4</sub><br>S <sub>5</sub>                                     | S <sub>10</sub>                  | 1) XX-1 |
| Level 2 | S <sub>1</sub><br>S <sub>2</sub><br>S <sub>4</sub><br>S <sub>4</sub> | \$6<br>\$7<br>\$8<br>\$9         |         |





- ➤ Background (GLM)
- > t-test
- One-way A
- > Two-way ANOVA



### Issues



- > Model selection (be carefull)
- > Post-hoc analysis
- > Multiple comparisons

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