# Package 'cscore'

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Title Weighted Composite Scoring for Scales
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<b>Description</b> Weighted composite scoring for scales used in psychological and social behavioral research.
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average\_score

Calculate Unweighted Composite Scores

# Description

Create composite scores of scales by specifying the indicators that go into each respective composite variable.

# Usage

```
average_score(
  data = .,
  composite_list,
  digits = 3,
  return_metrics = FALSE,
  file = NULL,
  name = NULL
)
```

# **Arguments**

data	A dataframe object. This should be a structured dataset where each column represents a variable and each row represents an observation.
composite_list	A required composite_list object. Each name in the list represents a composite variable, and the corresponding vector contains the column names that are associated with the indicators comprising said composite variable.
digits	The decimal places for the metrics to be rounded to. Default is 3. This argument is only relevant if return_metrics = TRUE.
return_metrics	Logic to determine whether to return reliability and validity metrics. Set to TRUE for a list of dataframes with reliability and validity metrics.
file	An optional file path. If specified, the results will be written as a formatted excel workbook. This argument is only relevant if return_metrics = TRUE.
name	A required string denoting the name of the composite variable.

# **Details**

Unweighted composite scores are calculated as the simple arithmetic mean of the indicators, assigning equal weight to each.

Let  $I_{cj}$  denote the value of indicator j for case c, and let there be m total indicators. The unweighted composite score for case c is:

average\_score 3

$$\bar{C}_c = \frac{1}{m} \sum_{j=1}^m I_{cj}$$

where  $\bar{C}_c$  is the composite score and all indicators contribute equally regardless of their variance, scale, or distribution.

#### Value

If return\_metrics = FALSE, a dataframe identical to the input dataframe, with additional columns appended at the end, is returned. These new columns represent the calculated composite scores. If return\_metrics = TRUE, a list containing the following dataframes is returned:

- Data: A dataframe with the composite variables appended as new variables.
- Metrics: A matrix of indicator loadings and weights metrics.
- Validity: A matrix of composite reliability and validity metrics.

```
data(grit)
# Specify the named list with composite names and their respective indicators
composite_list <- composite_list(</pre>
  # Lower-order composites
  extraversion = sprintf("e%01d", seq(10)),
neuroticism = sprintf("n%01d", seq(10)),
agreeableness = sprintf("a%01d", seq(10)),
conscientiousness = sprintf("c%01d", seq(10)),
openness = sprintf("o%01d", seq(10)),
  consistency_interest = sprintf("gs%01d", c(2,3,5,7,8,11)),
  perseverance_effort = sprintf("gs\%01d", c(1,4,6,9,10,12)),
  # Higher-order composites
                             = c("consistency_interest", "perseverance_effort")
  grit
 )
# Calculate unweighted composite scores
average_score(data = grit,
                 composite_list = composite_list)
# Calculate unweighted composite scores, reliability, & validity
average_score(data = grit,
                 composite_list = composite_list,
                 digits = 3,
                 return_metrics = TRUE,
                 file = "composite.xlsx")
unlink("composite.xlsx")
```

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composite\_list

Composite List

# Description

A duplicate of base R's list function. Create a list of composite variable named vectors by specifying their corresponding indicator items. Composite variables with indicators comprising the names of other composite variables are automatically categorized as higher-order composites. These are separated into its own higher list of composite vectors. The remaining composite variables are allocated into the lower list of composite vectors.

# Usage

```
composite_list(...)
clist(...)
cl(...)
```

#### **Arguments**

. . . Required named objects. Each vector should include the columns representing the indicator variables.

# Value

Two lists of lower and higher-order named composite vectors.

```
data(grit)
# Specify the named list with composite names and their respective indicators
composite_list <- composite_list(</pre>
  # Lower-order composites
  extraversion
                        = sprintf("e%01d", seq(10)),
  neuroticism
                         = sprintf("n%01d", seq(10)),
  agreeableness
                         = sprintf("a%01d", seq(10)),
  conscientiousness = sprintf("c%01d", seq(10)),
openness = sprintf("o%01d", seq(10)),
  consistency_interest = sprintf("gs%01d", c(2,3,5,7,8,11)),
  perseverance_effort = sprintf("gs\%01d", c(1,4,6,9,10,12)),
  # Higher-order composites
  grit
                         = c("consistency_interest", "perseverance_effort")
 )
```

composite\_model 5

composite\_model

Build a Composite Structural Model from Link Paths

## **Description**

Combines one or more sets of 'link' paths into a unified structural model. Each input must be a data frame generated by the 'link()' function, specifying directed associations between variables. The function merges these links, identifies the outcome variable(s), and computes a valid topological ordering. The model is assumed to be a directed acyclic graph.

# Usage

```
composite_model(...)
```

## **Arguments**

One or more 'link' path objects created by the 'link()' function. Each must be a data frame with columns 'from' and 'to', representing directed edges in the model.

#### Value

A list with three components:

paths A data frame of all combined directed edges.

**outcomes** A character vector of terminal outcome node(s) (i.e., nodes with no outgoing edges). **order** A character vector of all nodes sorted in topological order, from predictors to outcomes.

```
# Define composite structure
composite_list <- composite_list(</pre>
  extraversion
                      = sprintf("e%01d", seq(10)),
  neuroticism
                      = sprintf("n%01d", seq(10)),
 agreeableness = sprintf("a%01d", seq(10)),
  conscientiousness = sprintf("c%01d", seq(10)),
                       = sprintf("o%01d", seq(10)),
  openness
  consistency\_interest = sprintf("gs\%01d", c(2,3,5,7,8,11)),
  perseverance_effort = sprintf("gs%01d", c(1,4,6,9,10,12)),
                        = c("consistency_interest", "perseverance_effort")
  grit
# Define model structure
composite_model <- composite_model(</pre>
  link(
    from = c("extraversion";
             "neuroticism",
             "agreeableness",
             "conscientiousness",
             "openness"),
    to = c("grit")
 )
```

composite\_score

Calculate Composite Scores

## **Description**

Create composite scores of scales by specifying the indicators that go into each respective composite variable. See help documents average\_score, correlation\_score, discriminant\_score, information\_score, median\_score, or sd\_score for information on how the composite scores for each weighting scheme are calculated.

# Usage

```
composite_score(
  data = .,
  composite_list,
  composite_model = NULL,
 weight = c("correlation", "regression", "average", "sd_upweight", "sd_downweight",
   "median", "median_decay", "median_gauss", "mutual_info", "irt", "glm", "pca"),
  decay_rate = 0.5,
  sigma = 0.5,
  entropy = c("emp", "mm", "shrink", "sg"),
  nmi_method = c("geometric", "average"),
  threshold = 10,
  pred_type = c("glm", "rf"),
  item_type = NULL,
  pmm_k = 5,
  maxiter = 10,
  verbose = 0,
  alpha = 0.5,
  nfolds = 10,
  ntrees = 100,
  importance = c("permutation", "impurity"),
  family = c("gaussian", "binomial", "multinomial", "poisson"),
  return_metrics = FALSE,
  digits = 3,
  file = NULL,
  name = NULL,
  seed = NULL
)
cscore(
  data = .,
  composite_list,
  composite_model = NULL,
 weight = c("correlation", "regression", "average", "sd_upweight", "sd_downweight",
   "median", "median_decay", "median_gauss", "mutual_info", "irt", "glm", "pca"),
  decay_rate = 0.5,
  sigma = 0.5,
  entropy = c("emp", "mm", "shrink", "sg"),
  nmi_method = c("geometric", "average"),
  threshold = 10,
```

```
pred_type = c("glm", "rf"),
  item_type = NULL,
  pmm_k = 5,
  maxiter = 10,
  verbose = 0,
  alpha = 0.5,
  nfolds = 10,
  ntrees = 100,
  importance = c("permutation", "impurity"),
  family = c("gaussian", "binomial", "multinomial", "poisson"),
  return_metrics = FALSE,
  digits = 3,
  file = NULL,
  name = NULL,
  seed = NULL
)
cs(
  data = .,
  composite_list,
  composite_model = NULL,
 weight = c("correlation", "regression", "average", "sd_upweight", "sd_downweight",
  "median", "median_decay", "median_gauss", "mutual_info", "irt", "glm", "pca"),
  decay_rate = 0.5,
  sigma = 0.5,
  entropy = c("emp", "mm", "shrink", "sg"),
  nmi_method = c("geometric", "average"),
  threshold = 10,
  pred_type = c("glm", "rf"),
  item_type = NULL,
  pmm_k = 5,
  maxiter = 10,
  verbose = 0,
  alpha = 0.5,
  nfolds = 10,
  ntrees = 100,
  importance = c("permutation", "impurity"),
  family = c("gaussian", "binomial", "multinomial", "poisson"),
  return_metrics = FALSE,
  digits = 3,
  file = NULL,
  name = NULL,
  seed = NULL
)
```

#### **Arguments**

data

A dataframe object. This should be a structured dataset where each column represents a variable and each row represents an observation.

composite\_list A required composite\_list object. Each name in the list represents a composite variable, and the corresponding vector contains the column names that are associated with the indicators comprising said composite variable.

composite\_model

An optional composite\_model object. Combines one or more sets of 'link' paths specifying directed associations between variables. The model is assumed to be a directed acyclic graph.

weight

The weighting schema used to calculate composite scores. Choose from the following families:

## **Covariance Family:**

- "average": Unweighted average (straight mean).
- "correlation": Correlation-weighted composite scores.
- "regression": Regression-weighted composite scores.

## **Standard Deviation (SD) Family:**

- "sd\_upweight": Upweights indicators with higher standard deviation.
- "sd\_downweight": Downweights indicators with higher standard deviation.

## **Median Family:**

- "median": Uses the median of the indicators as the composite score.
- "median\_decay": Applies a decay-weighted distance from the median.
- "median\_gauss": Applies a Gaussian-weighted distance from the median.

## **Information Family:**

• "mutual\_info": Shared mutual information-weighted composite scores.

#### **Discriminant Family:**

- "irt": Item response theory discriminant parameter-weighted composite scores.
- c("pca", "glm"): Principal component analysis and generalized linear model weighted composite scores.

decay\_rate

Numeric. Reflects the decay rate (i.e., sensitivity) of the distance-to-median weighting schema. The default value is set to 0.5.

sigma

Numeric. Reflects the sigma value for the Gaussian function in the distance-to-median weighting schema. The default value is set to 0.5.

entropy

String. Reflects the mutual information entropy estimator from the infotheo package. Four estimators are available: emp to compute the entropy of the empirical probability distribution. Empirical entropy is suitable for simple calculations without corrections. mm applies an asymptotic bias-corrected estimator making it suitable for small sample sizes. shrink applies a shrinkage estimate of the Dirichlet probability distribution to provide a stable estimate useful for small sample sizes or sparse data. sg applies a Schurmann-Grassberger estimate of the Dirichlet probability distribution to serve as an alternative to the Shrinkage approach.

nmi\_method

String. Reflects the method used for calculating Normalized Mutual Information (NMI) values. "average" will normalize MI values using the average entropies of variables A and B. "geometric" will normalize MI values using the geometric mean of entropies of variables A and B.

threshold

Integer. Specifies the maximum number of unique values to consider the input as discrete. Defaults to 10.

pred\_type

Prediction method schema for predictive weighting. Schemas include c("glm", "rf"). "glm" runs glmnet::cv.glmnet() for regularization linear regression. "rf" runs ranger::ranger() for Random Forest modeling. Default is "glm".

item\_type String. Specifies the item response model(s) to be used, passed to the itemtype

argument in mirt::mirt(). See ?mirt::mirt for the full list of supported item

types and their definitions. Defaults to NULL.

pmm\_k Integer. Number of donor candidates used for predictive mean matching (PMM)

during imputation. If set to 0, PMM is disabled and raw predictions are used.

maxiter Integer. Maximum number of iterations for chained equations in missRanger::missRanger().

Iteration continues until convergence or the specified limit is reached.

verbose Logical. If 1, print progress messages and intermediate output. Defaults to 0.

> Numeric. Elastic net mixing parameter, with  $0 \le alpha \le 1$ . Controls the relative weighting of L1 (lasso) and L2 (ridge) penalties in the model. The penalty

term is defined as (1 - alpha)/2 \* sum(beta^2) + alpha \* sum(abs(beta)), where beta is the vector of coefficients. When alpha = 1, the penalty is pure

lasso; when alpha = 0, it is ridge regression.

nfolds Integer. The number of folds used for random forest k-fold cross-validation.

Controls how the data are partitioned during resampling. Must be at least 2.

Default is 10.

Integer. Number of trees to grow in the random forest model. Default in ranger

is 500.

Character string. Specifies the type of variable importance measure to compute. Must be one of "permutation" or "impurity".

> • "permutation": Computes mean decrease in predictive accuracy by permuting each variable and measuring the resulting drop in model performance (typically using out-of-bag data). This method is more computationally expensive but generally provides more reliable and differentiated estimates of variable importance. It is robust to scale and less biased in the presence of correlated or irrelevant predictors.

> "impurity": Computes mean decrease in node impurity (e.g., Gini for classification, variance for regression) aggregated over all trees. This method is fast and computed during model training, but can be biased toward variables with many categories or continuous values, and tends to distribute importance more evenly across predictors—even when some are irrelevant or redundant.

Recommend using "impurity" for speed and "permutation" for interpretability, reliability, or feature selection. Default is "permutation".

Character string. Specifies the model family. Must be one of "gaussian", "binomial", "multinomial", or "poisson". This argument determines the loss function used in penalized model fitting via cv.glmnet. The supported options are:

- "gaussian": for linear regression with continuous outcomes.
- "binomial": for binary classification using logistic regression. The response should be a factor with two levels or a numeric vector containing 0 and 1.
- "multinomial": for multi-class classification with three or more unordered outcome categories. The response should be a factor.
- "poisson": for modeling count data under a Poisson distribution with a log link. The response should be a non-negative count-valued numeric vector.

Default is "gaussian".

return\_metrics Logic. Determines whether to return reliability and validity metrics. Set to TRUE for a list of dataframes with reliability and validity metrics.

alpha

ntrees

importance

family

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digits	Integer. The decimal places for the metrics to be rounded to. Default is 3. This argument is only relevant if return_metrics = TRUE.
file	An optional file path. If specified, the results will be written as a formatted excel workbook. This argument is only relevant if return_metrics = TRUE.
name	An optional string denoting the name of the study/analysis.
seed	Integer. Seed for reproducibility. Defaults to NULL, where no seed is set.

#### Value

If return\_metrics = FALSE, a dataframe identical to the input dataframe, with additional columns appended at the end, is returned. These new columns represent the calculated composite scores. If return\_metrics = TRUE, a list containing the following dataframes is returned:

- Data: A dataframe with the composite variables appended as new variables.
- Metrics: A matrix of indicator loadings and weights metrics.
- Validity: A matrix of composite reliability and validity metrics.

## **Examples**

correlation\_score

Calculate Correlation-Weighted Composite Scores

## **Description**

Create composite scores of scales by specifying the indicators that go into each respective composite variable.

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#### **Usage**

```
correlation_score(
  data = .,
  composite_list,
 weight = c("correlation", "regression"),
 digits = 3,
  return_metrics = FALSE,
  file = NULL,
 name = NULL
)
```

#### **Arguments**

data

represents a variable and each row represents an observation. composite\_list A required composite\_list object. Each name in the list represents a composite variable, and the corresponding vector contains the column names that are associated with the indicators comprising said composite variable. Required weighting schema. Schemas include c("correlation", "regression"). weight Default is "correlation". digits The decimal places for the metrics to be rounded to. Default is 3. This argument

A dataframe object. This should be a structured dataset where each column

is only relevant if return\_metrics = TRUE.

return\_metrics Logic to determine whether to return reliability and validity metrics. Set to TRUE for a list of dataframes with reliability and validity metrics.

file An optional file path. If specified, the results will be written as a formatted excel workbook. This argument is only relevant if return\_metrics = TRUE.

A required string denoting the name of the composite variable. name

## **Details**

Composite scores are calculated as either correlation-weighted or regression-weighted means of the indicators.

Correlation-weighted scores. For a given composite, a correlation matrix is computed using all its indicators. Let  $w_i$  denote the weight for indicator j, computed as the average correlation with all other indicators:

$$w_j = \frac{1}{n} \sum_{i=1}^n r_{ij}, \quad i \neq j$$

where  $r_{ij}$  is the Pearson correlation between indicators i and j, and n is the number of indicators. Self-correlations  $(r_{jj})$  are excluded. The weights are then normalized:

$$w_j^* = \frac{w_j}{\frac{1}{m} \sum_{k=1}^{m} w_k}$$

where m is the number of indicators in the composite. The correlation-weighted composite score  $\bar{C}_c$  for case c is then:

$$\bar{C}_c = \frac{1}{m} \sum_{j=1}^m I_{cj} \cdot w_j^*$$

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where  $I_{cj}$  is the value of indicator j for case c.

*Regression-weighted scores.* A linear model is fit with the correlation-weighted composite scores as the outcome and the indicators as predictors:

$$\bar{C}_c = \beta_0 + \sum_{j=1}^m \beta_j I_{cj} + \varepsilon_c$$

The regression weights are the standardized coefficients  $\beta_i$ , normalized as:

$$w_j = \frac{\beta_j}{\frac{1}{m} \sum_{k=1}^m \beta_k}$$

The regression-weighted composite score is then:

$$\bar{C}_c = \frac{1}{m} \sum_{j=1}^m I_{cj} \cdot w_j$$

# Value

If return\_metrics = FALSE, a dataframe identical to the input dataframe, with additional columns appended at the end, is returned. These new columns represent the calculated composite scores. If return\_metrics = TRUE, a list containing the following dataframes is returned:

- Data: A dataframe with the composite variables appended as new variables.
- Metrics: A matrix of indicator loadings and weights metrics.
- Validity: A matrix of composite reliability and validity metrics.

```
data(grit)
# Specify the named list with composite names and their respective indicators
composite_list <- composite_list(</pre>
  # Lower-order composites
  extraversion = sprintf("e%01d", seq(10)),
  neuroticism = sprintf("n%01d", seq(10)),
agreeableness = sprintf("a%01d", seq(10)),
conscientiousness = sprintf("c%01d", seq(10)),
openness = sprintf("o%01d", seq(10)),
  consistency\_interest = sprintf("gs\%01d", c(2,3,5,7,8,11)),\\
  perseverance_effort = sprintf("gs%01d", c(1,4,6,9,10,12)),
  # Higher-order composites
                            = c("consistency_interest", "perseverance_effort")
  grit
 )
# Calculate correlation-weighted composite scores
correlation_score(data = grit,
                     composite_list = composite_list)
# Calculate correlation-weighted composite scores, reliability, & validity
```

```
correlation_score(data = grit,
                  composite_list = composite_list,
                  digits = 3,
                  return_metrics = TRUE,
                  file = "composite.xlsx")
unlink("composite.xlsx")
```

discriminant\_score

Calculate Discriminant-Weighted Composite Scores

#### **Description**

Create composite scores of scales by specifying the indicators that go into each respective composite variable.

# Usage

```
discriminant_score(
  data = .,
  composite_list,
  composite_model = NULL,
  weight = c("irt", "pca", "glm"),
  pred_type = c("glm", "rf"),
  item_type = NULL,
  pmm_k = 5,
  maxiter = 10,
  verbose = 0,
  digits = 3,
  alpha = 0.5,
  nfolds = 10,
  ntrees = 100,
  importance = c("permutation", "impurity"),
  family = c("gaussian", "binomial", "multinomial", "poisson"),
  return_metrics = FALSE,
  seed = NULL,
  file = NULL.
  name = NULL
)
```

# **Arguments**

data

A dataframe object. This should be a structured dataset where each column represents a variable and each row represents an observation.

composite\_list A required composite\_list object. Each name in the list represents a composite variable, and the corresponding vector contains the column names that are associated with the indicators comprising said composite variable.

composite\_model

An optional composite\_model object. Combines one or more sets of 'link' paths specifying directed associations between variables. The model is assumed to be a directed acyclic graph.

Required weighting schema. Schemas include c("irt", "pca", "glm"). c("pca", weight "glm") run the same weighting schema. Default is "irt".

Prediction method schema for predictive weighting. Schemas include c("glm", pred\_type

"rf"). "glm" runs glmnet::cv.glmnet() for regularization linear regression. "rf" runs ranger::ranger() for Random Forest modeling. Default is "glm".

item\_type Character string or vector specifying the item response model(s) to be used, passed to the itemtype argument in mirt::mirt(). See ?mirt::mirt for the

full list of supported item types and their definitions. Defaults to NULL.

Integer. Number of donor candidates used for predictive mean matching (PMM) pmm\_k during imputation. If set to 0, PMM is disabled and raw predictions are used.

Integer. Maximum number of iterations for chained equations in missRanger::missRanger(). maxiter

Iteration continues until convergence or the specified limit is reached.

Logical; if 1, print progress messages and intermediate output. Defaults to 0. The decimal places for the metrics to be rounded to. Default is 3. This argument

is only relevant if return\_metrics = TRUE.

Elastic net mixing parameter, with  $\emptyset \le \text{alpha} \le 1$ . Controls the relative weighting of L1 (lasso) and L2 (ridge) penalties in the model. The penalty term is defined as  $(1 - alpha)/2 * sum(beta^2) + alpha * sum(abs(beta))$ , where beta is the vector of coefficients. When alpha = 1, the penalty is pure lasso;

when alpha = 0, it is ridge regression.

Integer. The number of folds used for random forest k-fold cross-validation. Controls how the data are partitioned during resampling. Must be at least 2.

Default is 10.

Integer. Number of trees to grow in the random forest model. Default in ranger

is 500.

Character string specifying the type of variable importance measure to compute. Must be one of "permutation" or "impurity".

- "permutation": Computes mean decrease in predictive accuracy by permuting each variable and measuring the resulting drop in model performance (typically using out-of-bag data). This method is more computationally expensive but generally provides more reliable and differentiated estimates of variable importance. It is robust to scale and less biased in the presence of correlated or irrelevant predictors.
- "impurity": Computes mean decrease in node impurity (e.g., Gini for classification, variance for regression) aggregated over all trees. This method is fast and computed during model training, but can be biased toward variables with many categories or continuous values, and tends to distribute importance more evenly across predictors—even when some are irrelevant or redundant.

Recommend using "impurity" for speed and "permutation" for interpretability, reliability, or feature selection. Default is "permutation".

Character string specifying the model family. Must be one of "gaussian", "binomial", "multinomial", or "poisson". This argument determines the loss function used in penalized model fitting via cv.glmnet. The supported options are:

- "gaussian": for linear regression with continuous outcomes.
- "binomial": for binary classification using logistic regression. The response should be a factor with two levels or a numeric vector containing 0 and 1.

verbose

digits

alpha

nfolds

ntrees

importance

family

• "multinomial": for multi-class classification with three or more unordered outcome categories. The response should be a factor.

• "poisson": for modeling count data under a Poisson distribution with a log link. The response should be a non-negative count-valued numeric vector.

Default is "gaussian".

return\_metrics Logic to determine whether to return reliability and validity metrics. Set to TRUE for a list of dataframes with reliability and validity metrics.

seed An integer seed for reproducibility. Defaults to NULL, where no seed is set.

file An optional file path. If specified, the results will be written as a formatted excel

workbook. This argument is only relevant if return\_metrics = TRUE.

name A required string denoting the name of the composite variable.

#### **Details**

Discriminant composite scores combine psychometric discrimination and predictive utility into a single weighting schema. Two primary discriminant sources are supported: **latent composite loadings** and **predictive weights**. The composite score for case c is computed as:

$$\bar{C}_c = \frac{1}{m} \sum_{j=1}^m I_{cj} \cdot w_j^*$$

where  $I_{cj}$  is the value of indicator j for case c, and  $w_j^*$  is the final normalized weight. The weighting proceeds in two stages:

## 1. Discriminant weighting from latent structure.

If weight = "irt", a unidimensional Item Response Theory (IRT) model is estimated:

$$P(Y_{cj} = 1) = \text{logit}^{-1}(a_j \cdot \theta_c + b_j)$$

where  $a_j$  is the discrimination parameter for indicator j, and  $\theta_c$  is the latent trait estimate for case c. The discrimination parameters  $a_j$  are extracted and normalized:

$$w_j = \frac{a_j}{\sum_{k=1}^m a_k}$$

If weight = "glm" or "pca", a single-factor principal component analysis (PCA) is conducted. The first factor score is extracted as a latent proxy  $Z_c$ . A penalized linear model is then fit:

$$Z_c = \sum_{j=1}^{m} \beta_j \cdot I_{cj} + \varepsilon_c$$

where  $\beta_j$  are estimated using elastic net regularization (via **glmnet**). These are normalized analogously to IRT:

$$w_j = \frac{\beta_j}{\sum_{k=1}^m \beta_k}$$

#### 2. Predictive weighting from external outcomes (optional).

If one or more outcome variables are provided via outcomes, an additional predictive weighting stage is applied. Two methods are available:

(a) Generalized Linear Model (GLM). Each outcome Y is regressed on the indicators  $I_{cj}$  using elastic net regularization. For each fitted model, the normalized coefficients  $\gamma_j^{(r)}$  are extracted. The final predictive weights are averaged over all outcomes:

$$p_j = \frac{1}{R} \sum_{r=1}^R \gamma_j^{(r)}$$

where R is the number of outcomes. The predictive weights are then normalized:

$$p_j^* = \frac{p_j}{\sum_{k=1}^m p_k}$$

(b) Random Forest (RF). Each outcome Y is predicted via a random forest, and variable importance scores (e.g., permutation or impurity) are extracted for each indicator. These are averaged across outcomes and normalized in the same manner as the GLM approach.

#### 3. Final weight aggregation.

If predictive weights  $p_j^*$  are available, they are combined with the latent discrimination weights  $w_j$  to form final composite weights:

$$w_j^* = \frac{w_j + p_j^*}{\frac{1}{m} \sum_{k=1}^m (w_k + p_k^*)}$$

If no predictive targets are provided,  $w_i^*$  defaults to normalized discrimination weights.

#### Value

If return\_metrics = FALSE, a dataframe identical to the input dataframe, with additional columns appended at the end, is returned. These new columns represent the calculated composite scores. If return\_metrics = TRUE, a list containing the following dataframes is returned:

- **Data**: A dataframe with the composite variables appended as new variables.
- Metrics: A matrix of indicator loadings and weights metrics.
- Validity: A matrix of composite reliability and validity metrics.

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export\_metrics

Export Metrics (Reliability & Validity)

#### **Description**

A function to export a metrics object as a formatted excel workbook to the specified file path. The format is consistent with what is typically reported in APA 7th edition, and can be copy and pasted directly into a Word document or similar document software.

# Usage

```
export_metrics(metrics, digits, name = NULL, file)
```

# **Arguments**

metrics	A required list object. The list should contain an array for composite scores under data, a data frame of indicator loadings and weights under metrics, and composite validity value under validity.
digits	The decimal places for the metrics to be rounded to. Default is 3.
name	An optional string denoting the study/analysis name.
file	A required file path. If specified, the results will be written as a formatted excel workbook.

# Details

Indicator loadings  $(\lambda_i)$  are computed as the bivariate correlation between each indicator  $I_i$  and the correlation-weighted composite score  $\bar{C}_c$ :

$$\lambda_i = \operatorname{cor}(I_i, \bar{C}_c)$$

Two reliability metrics are reported: Cronbach's alpha ( $\alpha$ ) and composite reliability ( $\rho_c$ , also referred to as McDonald's omega,  $\omega$ ).

Cronbach's alpha is defined as:

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$$\alpha = \frac{k\bar{c}}{\bar{v} + (k-1)\bar{c}}$$

where k is the number of indicators,  $\bar{c}$  is the average inter-item covariance, and  $\bar{v}$  is the average indicator variance. Alpha assumes tau-equivalence (equal loadings across indicators) and is sensitive to the number of indicators. While widely used, it is not recommended due to these limitations; it is reported here for completeness only.

Composite reliability ( $\rho_c$ ) is a weighted reliability estimate based on user-defined indicator weights. It uses the same formula as McDonald's omega but allows loadings to be weighted according to the composite score structure:

$$\rho_c = \frac{\left(\sum \lambda_i w_i\right)^2}{\left(\sum \lambda_i w_i\right)^2 + \sum e_{w_i}}$$

where  $w_i$  is the weight for indicator i, and  $e_{w_i}$  is the weighted measurement error:

$$e_{w_i} = (1 - \lambda_i^2) \cdot w_i$$

Although this metric is labeled  $\rho_c$  to align with PLS-SEM nomenclature, it is mathematically equivalent to omega and may be reported as either.

Average Variance Extracted (AVE) measures the proportion of variance captured by the construct relative to measurement error. It is defined as:

$$AVE = \frac{\sum \lambda_{w_i}^2}{\sum \lambda_{w_i}^2 + \sum e_{w_i}}$$

where the weighted squared loading is:

$$\lambda_{w_i}^2 = \lambda_i^2 \cdot w_i$$

AVE is commonly used in the Fornell-Larcker criterion for discriminant validity:

$$\sqrt{\text{AVE}_i} > \max_j(r_{ij})$$

That is, the square root of AVE for a construct should exceed its highest correlation with any other construct.

# Value

A formatted excel workbook saved to specified file path.

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grit Grit Data

#### **Description**

This example data contains 500 responses from people completing the Big 5 personality inventory (John & Srivastava, 1999) and the Grit Scale (Duckworth et al., 2007) from OpenPsychoMetrics.

# Usage

data(grit)

#### **Format**

A data frame with 500 rows and 63 variables. All items are scored on a 1–5 Likert scale. Items marked with an asterisk (\*) are reverse-coded and have been recoded for convenience:

id Respondent ID

## **Extraversion:**

- e1 I am the life of the party.
- e2 I don't talk a lot. (\*))
- e3 I feel comfortable around people.
- e4 I keep in the background. (\*)
- e5 I start conversations.
- e6 I have little to say. (\*)
- e7 I talk to a lot of different people at parties.
- e8 I don't like to draw attention to myself. (\*)
- e9 I don't mind being the center of attention.
- e10 I am quiet around strangers. (\*)

# **Neuroticism:**

- n1 I get stressed out easily.
- n2 I am relaxed most of the time. (\*)
- n3 I worry about things.
- n4 I seldom feel blue. (\*)
- n5 I am easily disturbed.
- n6 I get upset easily.
- n7 I change my mood a lot.
- n8 I have frequent mood swings.
- n9 I get irritated easily.
- n10 I often feel blue.

# Agreeableness:

- a1 I feel little concern for others. (\*)
- a2 I am interested in people.
- a3 I insult people. (\*)

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- a4 I sympathize with others' feelings.
- a5 I am not interested in other people's problems. (\*)
- a6 I have a soft heart.
- a7 I am not really interested in others. (\*)
- a8 I take time out for others.
- a9 I feel others' emotions.
- a10 I make people feel at ease.

## **Conscientiousness:**

- c1 I am always prepared.
- c2 I leave my belongings around. (\*)
- c3 I pay attention to details.
- c4 I make a mess of things. (\*)
- c5 I get chores done right away.
- c6 I often forget to put things back in their proper place. (\*)
- c7 I like order.
- c8 I shirk my duties. (\*)
- c9 I follow a schedule.
- c10 I am exacting in my work.

#### **Openness:**

- o1 I have a rich vocabulary.
- o2 I have difficulty understanding abstract ideas. (\*)
- o3 I have a vivid imagination.
- o4 I am not interested in abstract ideas. (\*)
- o5 I have excellent ideas.
- o6 I do not have a good imagination. (\*)
- o7 I am quick to understand things.
- o8 I use difficult words.
- o9 I spend time reflecting on things.
- o10 I am full of ideas.

## **Grit:**

- gs1 I have overcome setbacks to conquer an important challenge.
- gs2 New ideas and projects sometimes distract me from previous ones. (\*)
- gs3 My interests change from year to year. (\*)
- gs4 Setbacks don't discourage me.
- gs5 I have been obsessed with a certain idea or project for a short time but later lost interest. (\*)
- gs6 I am a hard worker.
- gs7 I often set a goal but later choose to pursue a different one. (\*)
- gs8 I have difficulty maintaining my focus on projects that take more than a few months to complete. (\*)
- gs9 I finish whatever I begin.
- gs10 I have achieved a goal that took years of work.
- gs11 I become interested in new pursuits every few months. (\*)
- gs12 I am diligent.

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#### Source

OpenPsychoMetrics.

#### References

Duckworth, A.L., Peterson, C., Matthews, M.D., & Kelly, D.R. (2007). Grit: Perseverance and passion for long-term goals. Journal of Personality and Social Psychology, 9, 1087-1101.

John, O. P., & Srivastava, S. (1999). The Big-Five trait taxonomy: History, measurement, and theoretical perspectives. In L. A. Pervin & O. P. John (Eds.), Handbook of personality: Theory and research (2nd ed., pp. 102-138). Guilford Press.

information\_score

Calculate Information-Weighted Composite Scores

# **Description**

Create composite scores of scales by specifying the indicators that go into each respective composite variable.

# Usage

```
information_score(
 data = .,
  composite_list,
  entropy = c("emp", "mm", "shrink", "sg"),
  nmi_method = c("geometric", "average"),
  threshold = 10,
 digits = 3,
  return_metrics = FALSE,
  file = NULL,
 name = NULL
)
```

## **Arguments**

data

A dataframe object. This should be a structured dataset where each column represents a variable and each row represents an observation.

composite\_list A required composite\_list object. Each name in the list represents a composite variable, and the corresponding vector contains the column names that are associated with the indicators comprising said composite variable.

entropy

A string value reflecting the mutual information entropy estimator from the infotheo package. Four estimators are available: emp to compute the entropy of the empirical probability distribution. Empirical entropy is suitable for simple calculations without corrections. mm applies an asymptotic bias-corrected estimator making it suitable for small sample sizes. shrink applies a shrinkage estimate of the Dirichlet probability distribution to provide a stable estimate useful for small sample sizes or sparse data. sg applies a Schurmann-Grassberger estimate of the Dirichlet probability distribution to serve as an alternative to the Shrinkage approach.

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nmi method A string value reflecting the method used for calculating Normalized Mutual Information (NMI) values. "average" will normalize MI values using the average entropies of variables A and B. "geometric" will normalize MI values using the geometric mean of entropies of variables A and B. threshold An integer specifying the maximum number of unique values to consider the input as discrete. Defaults to 10. digits The decimal places for the metrics to be rounded to. Default is 3. This argument is only relevant if return\_metrics = TRUE. return\_metrics Logic to determine whether to return reliability and validity metrics. Set to TRUE for a list of dataframes with reliability and validity metrics. An optional file path. If specified, the results will be written as a formatted excel file workbook. This argument is only relevant if return\_metrics = TRUE. A required string denoting the name of the composite variable. name

#### **Details**

Composite scores are computed as the **information-weighted** mean of the indicators.

Information-weighted scores. For a given composite, pairwise mutual information (MI) is computed between all indicators to form an information matrix  $I_{ij}$ . Self-information values on the diagonal are excluded. Each mutual information value is then normalized to obtain the Normalized Mutual Information (NMI).

The NMI between variables i and j can be computed using either arithmetic mean:

$$\mathrm{NMI}(i,j) = \frac{2 \cdot I(i,j)}{H(i) + H(j)}$$

or geometric mean:

$$NMI(i, j) = \frac{I(i, j)}{\sqrt{H(i) \cdot H(j)}}$$

where I(i,j) is the mutual information and H(i) and H(j) are the entropies of variables i and j, respectively. The method is selected via nmi\_method. The information weight for indicator j is the average of its NMI values:

$$w_j = \frac{1}{n} \sum_{i \neq j} \text{NMI}(i, j)$$

where n is the number of indicators and the sum excludes self-pairs. The weights are then normalized:

$$w_j^* = \frac{w_j}{\frac{1}{m} \sum_{k=1}^{m} w_k}$$

where m is the number of indicators in the composite. The information-weighted composite score  $\bar{C}_c^{\rm MI}$  for case c is calculated as:

$$\bar{C}_c^{\text{MI}} = \frac{1}{m} \sum_{i=1}^m I_{cj} \cdot w_j^*$$

where  $I_{cj}$  is the value of indicator j for case c.

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#### Value

If return\_metrics = FALSE, a dataframe identical to the input dataframe, with additional columns appended at the end, is returned. These new columns represent the calculated composite scores. If return\_metrics = TRUE, a list containing the following dataframes is returned:

- Data: A dataframe with the composite variables appended as new variables.
- Metrics: A matrix of indicator loadings and weights metrics.
- Validity: A matrix of composite reliability and validity metrics.

# **Examples**

```
data(grit)
# Specify the named list with composite names and their respective indicators
composite_list <- composite_list(</pre>
  # Lower-order composites
  extraversion = sprintf("e%01d", seq(10)),
  neuroticism
                          = sprintf("n%01d", seq(10)),
  neuroticism = sprintf("n%01d", seq(10)),
agreeableness = sprintf("a%01d", seq(10)),
conscientiousness = sprintf("c%01d", seq(10)),
openness = sprintf("o%01d", seq(10))
                          = sprintf("o%01d", seq(10)),
  openness
  consistency_interest = sprintf("gs\%01d", c(2,3,5,7,8,11)),
  perseverance_effort = sprintf("gs%01d", c(1,4,6,9,10,12)),
  # Higher-order composites
                           = c("consistency_interest", "perseverance_effort")
  grit
 )
# Calculate correlation-weighted composite scores
information_score(data = grit,
                    composite_list = composite_list)
# Calculate correlation-weighted composite scores, reliability, & validity
information_score(data = grit,
                    composite_list = composite_list,
                    digits = 3.
                    return_metrics = TRUE,
                    file = "composite.xlsx")
unlink("composite.xlsx")
```

link

Create Link Paths Between Node Sets

# Description

Generates a set of directed paths representing all combinations of links from nodes in 'from' to nodes in 'to'. The result is a data frame that can be used as input to 'composite\_model()' and related functions.

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#### **Usage**

```
link(from, to)
```

#### **Arguments**

from A character vector of source node names.
to A character vector of target node names.

#### Value

A data frame with two columns, 'from' and 'to', containing all directed edges from each element in 'from' to each element in 'to'.

# **Examples**

```
link(from = c("x1", "x2"), to = c("y"))
```

median\_score

Calculate Median Composite Scores & Metrics

#### **Description**

Create composite scores of scales by specifying the indicators that go into each respective composite variable.

# Usage

```
median_score(
  data = .,
  composite_list,
  weight = c("median", "median_decay", "median_gauss"),
  decay_rate = 0.5,
  sigma = 0.5,
  digits = 3,
  return_metrics = FALSE,
  file = NULL,
  name = NULL
)
```

# **Arguments**

data A dataframe object. This should be a structured dataset where each column

represents a variable and each row represents an observation.

composite\_list A required composite\_list object. Each name in the list represents a compos-

ite variable, and the corresponding vector contains the column names that are

associated with the indicators comprising said composite variable.

weight Required weighting schema. Schemas include c("median", "median\_decay",

"median\_gauss"). Default is "median".

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decay_rate	A numeric value reflecting the decay rate (i.e., sensitivity) of the distance-to-median weighting schema. The default value is set to 0.5.
sigma	A numeric value reflecting the sigma value for the Gaussian function in the distance-to-median weighting schema. The default value is set to $0.5$ .
digits	The decimal places for the metrics to be rounded to. Default is 3. This argument is only relevant if $return\_metrics = TRUE$ .
return_metrics	Logic to determine whether to return reliability and validity metrics. Set to TRUE for a list of dataframes with reliability and validity metrics.
file	An optional file path. If specified, the results will be written as a formatted excel workbook. This argument is only relevant if return_metrics = TRUE.
name	A required string denoting the name of the composite variable.

#### **Details**

Composite scores can be calculated using three median-based weighting schemes: **unweighted median**, **decay-weighted**, and **Gaussian-weighted**.

Unweighted median. The median composite score  $ar{C}_c^{\mathrm{med}}$  for case c is:

$$\bar{C}_c^{\mathrm{med}} = \mathrm{median}(I_{c1}, I_{c2}, \dots, I_{cm})$$

where  $I_{cj}$  is the value of indicator j for case c, and m is the number of indicators.

Decay-weighted median. For each respondent, let  $M_c$  denote the within-row median:

$$M_c = \text{median}(I_{c1}, I_{c2}, \dots, I_{cm})$$

The absolute distance to the median is:

$$D_{cj} = |I_{cj} - M_c|$$

The decay weight for indicator j is then:

$$w_{cj} = \exp(-\gamma \cdot D_{cj})$$

where  $\gamma$  is the user-specified decay\_rate. Weights are row-normalized:

$$w_{cj}^* = \frac{w_{cj}}{\frac{1}{m} \sum_{k=1}^{m} w_{ck}}$$

The decay-weighted median composite score is:

$$\bar{C}_c^{\text{decay}} = \frac{1}{m} \sum_{j=1}^m I_{cj} \cdot w_{cj}^*$$

Gaussian-weighted median. Using the same distance  $D_{cj}$ , the Gaussian weight is:

$$w_{cj} = \exp\left(-\frac{D_{cj}^2}{2\sigma^2}\right)$$

where  $\sigma$  is the user-specified sigma parameter controlling the spread. Weights are row-normalized as before, and the final score is:

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$$\bar{C}_c^{\text{gauss}} = \frac{1}{m} \sum_{j=1}^m I_{cj} \cdot w_{cj}^*$$

All median-based methods treat each case independently. Weighting is performed per respondent, allowing differential emphasis on indicators based on their proximity to the respondent-specific median.

#### Value

If return\_metrics = FALSE, a dataframe identical to the input dataframe, with additional columns appended at the end, is returned. These new columns represent the calculated composite scores. If return\_metrics = TRUE, a list containing the following dataframes is returned:

- Data: A dataframe with the composite variables appended as new variables.
- Metrics: A matrix of indicator loadings and weights metrics.
- Validity: A matrix of composite reliability and validity metrics.

```
data(grit)
# Specify the named list with composite names and their respective indicators
composite_list <- composite_list(</pre>
  # Lower-order composites
  extraversion = sprintf("e%01d", seq(10)),
neuroticism = sprintf("n%01d", seq(10)),
  neuroticism - sprint("a%01d", seq(10)),
conscientiousness = sprintf("c%01d", seq(10)),
- sprintf("o%01d", seq(10)),
                         = sprintf("o%01d", seq(10)),
  consistency_interest = sprintf("gs%01d", c(2,3,5,7,8,11)),
  perseverance_effort = sprintf("gs%01d", c(1,4,6,9,10,12)),
  # Higher-order composites
                           = c("consistency_interest", "perseverance_effort")
  grit
 )
# Calculate median composite scores
median_score(data = grit,
              composite_list = composite_list)
# Calculate median composite scores, reliability, & validity
median_score(data = grit,
              composite_list = composite_list,
              digits = 3,
              return_metrics = TRUE,
               file = "composite.xlsx")
unlink("composite.xlsx")
```

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sd\_score

Calculate Standard Deviation Composite Scores

# Description

Create composite scores of scales by specifying the indicators that go into each respective composite variable.

# Usage

```
sd_score(
  data = .,
  composite_list,
  weight = c("sd_upweight", "sd_downweight"),
  digits = 3,
  return_metrics = FALSE,
  file = NULL,
  name = NULL
)
```

# Arguments

data	A dataframe object. This should be a structured dataset where each column represents a variable and each row represents an observation.
composite_list	A required composite_list object. Each name in the list represents a composite variable, and the corresponding vector contains the column names that are associated with the indicators comprising said composite variable.
weight	Required weighting schema. Schemas include $c("sd\_upweight", "sd\_downweight")$ . Default is "sd\_upweight".
digits	The decimal places for the metrics to be rounded to. Default is 3. This argument is only relevant if return_metrics = TRUE.
return_metrics	Logic to determine whether to return reliability and validity metrics. Set to TRUE for a list of dataframes with reliability and validity metrics.
file	An optional file path. If specified, the results will be written as a formatted excel workbook. This argument is only relevant if return_metrics = TRUE.
name	A required string denoting the name of the composite variable.

# **Details**

Standard deviation (SD)—weighted composite scores assign indicator weights based on their empirical variability. Two variants are supported: **upweighting** and **downweighting** by standard deviation.

Let  $I_{cj}$  denote the value of indicator j for case c. For each indicator j, its sample standard deviation  $\sigma_j$  is computed as:

$$\sigma_j = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (I_{ij} - \bar{I}_{ij})^2}$$

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where  $\bar{I}_{\cdot j}$  is the sample mean of indicator j across all n observations.

## 1. SD-Upweighted Composite.

Indicators with greater dispersion are weighted more heavily. The weights are normalized:

$$w_j = \frac{\sigma_j}{\frac{1}{m} \sum_{k=1}^m \sigma_k}$$

The final composite score for case c is:

$$\bar{C}_c^{(u)} = \frac{1}{m} \sum_{i=1}^m I_{cj} \cdot w_j$$

where m is the total number of indicators.

#### 2. SD-Downweighted Composite.

Indicators with greater dispersion are weighted less heavily by using the inverse of the standard deviation:

$$w_{j} = \frac{\sigma_{j}^{-1}}{\frac{1}{m} \sum_{k=1}^{m} \sigma_{k}^{-1}}$$

The resulting downweighted composite score is:

$$\bar{C}_c^{(d)} = \frac{1}{m} \sum_{j=1}^m I_{cj} \cdot w_j$$

Both upweighted and downweighted schemes produce unit-normalized weights ( $\bar{w}=1$ ). These can be used to emphasize or attenuate variability in the indicators depending on the analytic goal.

If return\_metrics = TRUE, the function returns reliability and validity metrics in addition to the composite score. See calc\_metrics for details.

## Value

If return\_metrics = FALSE, a dataframe identical to the input dataframe, with additional columns appended at the end, is returned. These new columns represent the calculated composite scores. If return\_metrics = TRUE, a list containing the following dataframes is returned:

- Data: A dataframe with the composite variables appended as new variables.
- Metrics: A matrix of indicator loadings and weights metrics.
- Validity: A matrix of composite reliability and validity metrics.

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