

$$\frac{10-A}{1} - \frac{A}{2} - \frac{A-B}{8} = 0$$

$$10-A - \frac{A}{2} - \frac{A}{8} + \frac{B}{8} = 0$$

$$80 - 8A - 4A - A + B = 0$$

$$13A - B = 80$$

$$\frac{10-C}{13} - \frac{C-B}{1} - \frac{C}{4} = 0$$

$$\frac{10-4C}{52} - \frac{52C - 52B}{52} - \frac{13C}{52} = 0$$

$$40 = 69C - 52B$$

$$\frac{10-B}{4} - \frac{B-A}{8} - \frac{B}{5} - \frac{B-C}{1} = 0$$

$$\frac{20-3B+A}{8} - \frac{B-5B+5C}{5} = 0$$

$$(100 - 15B + 5A) - 48B + 40C = 0$$

$$100 = 63B - 5A - 40C$$

In to Canonical form

$$R_2 R_7 (V - A) - R_1 R_2 (A - B) - R_1 R_7 A = 0$$

$$R_2 R_7 V - A R_2 R_7 - A R_1 R_2 + B R_1 R_2 - A R_1 R_7 = 0$$

$$V(R_2 R_7) = A(R_1 R_2 + R_1 R_7 + R_2 R_7) - B(R_1 R_2)$$

$$R_4 R_7 R_8 (V-B) - R_3 R_4 R_8 (B-A) - R_3 R_7 R_8 (B) - R_3 R_7 R_4 (B-C) = 0$$

$$R_4 R_7 R_8 (V) - B (R_4 R_7 R_8) - R_3 R_4 R_8 (B) + R_3 R_4 R_8 (A) - R_3 R_7 R_8 (B) \\ - R_3 R_7 R_4 B + R_3 R_7 R_4 (C) = 0.$$

$$R_4 R_7 R_8 (V) = B (R_4 R_7 R_8 + R_3 R_4 R_8 + R_3 R_7 R_8 + R_3 R_4 R_7) - R_3 R_4 R_8 (A) \\ - R_3 R_4 R_7 (C)$$

$$\frac{V-C}{R_5} - \frac{C-B}{R_8} - \frac{C}{R_6} = 0$$

$$R_6 R_8 (V-C) - R_5 R_6 (C-B) - R_5 R_8 C = 0$$

$$R_6 R_8 (V) = C (R_6 R_8 + R_5 R_6 + R_5 R_8) - R_5 R_6 (B)$$

Given a set of approximate  $x, y \rightarrow$  plane (Best fitting line in least square sense).

$ax+b=y$  (std. line)  $\rightarrow$  Compute  $a$  &  $b$ .

lin-reg  $\rightarrow x, y$  (now vectors)  $\rightarrow$  coordinate points.

$$ax+b=y$$

$$a \cdot \begin{pmatrix} \vdots \\ \vdots \end{pmatrix} + \begin{pmatrix} b \\ \vdots \end{pmatrix} = \begin{pmatrix} \vdots \\ \vdots \end{pmatrix}$$

$$\begin{bmatrix} x_1 & 1 \\ x_2 & 1 \\ x_3 & 1 \\ \vdots & 1 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \end{bmatrix} \rightarrow \text{sol}$$

$$a \cdot \underset{1 \times m}{(x_1 \ x_2 \ x_3 \ \dots)} + b \cdot \underset{1 \times m}{(1, 1, \dots)} = \underset{1 \times m}{(y_1, y_2, \dots)} \rightarrow \text{sol}$$

$$\begin{pmatrix} x_1 & x_2 & x_3 & \dots \\ 1 & 1 & 1 & \dots \end{pmatrix} \begin{pmatrix} a & b \end{pmatrix} = \underset{1 \times m}{(\dots)}$$

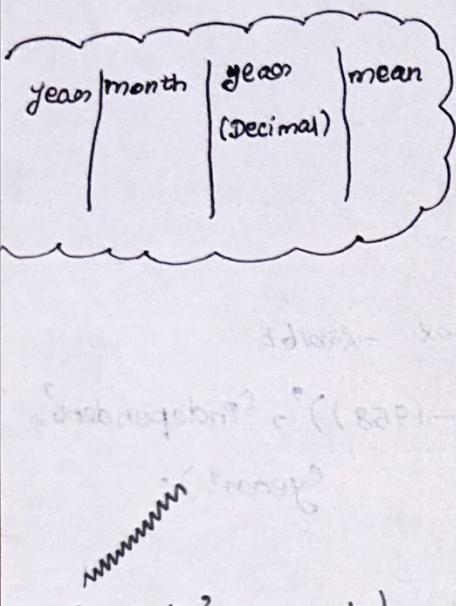
## Live Scripts

- \* works: only with scripts. → very useful in create small & impactful projects
- \* No workspace: Commandline level. (at seek Command line: workspace variables)
- \* can't have i/p & o/p arguments.

### Mauna Loa Observatory - Hawaii

- \* CO<sub>2</sub> Concentration: collected over 50 years. (In atmosphere) - NOAA (org.)

<https://www.esrl.noaa.gov/gmd/ccgg/about/co2-measurements.html>.



open .xsl

CO<sub>2</sub> = xlsread ('CO<sub>2</sub> Mauna Loa.xlsx'); → load

years = CO<sub>2</sub> (:, 3); → 3 column alone

CO<sub>2</sub> = CO<sub>2</sub> (:, 4); → 4 column alone.

plot (years, CO<sub>2</sub>, 'g'); grid on; → Foss grid

title ('Monthly CO<sub>2</sub> Concentrations');

xlabel ('years'); ylabel ('CO<sub>2</sub> (PPM)');

'periodic' - upwards!

Zoom manually

click magnifier → update code → copy paste.

Add description: Text.

\* Live Scripts - not a new feature

\* we can run normal scripts & even functions → as sections.

(% %)

Live script: lot more formatting freedom - text, Images, hyperlinks.

'Format'

'Smooth & plot' → the data

smoothdata → function introduced in 2017

window = 12 → (12 points from the original

data would be combined to produce each new point in the smooth data)

\* smoothdata (Co2, 'movmean', window)

↳ moving mean (Roughly: moves centers of the  
(method) window from beginning to end).

$\text{window} = 12;$

```
Smoothed = smoothdata(Car, "movmean", window);
```

Plot (years, CO<sub>2</sub>, 'g', years, smoothed, 'K') ; grid on;

title ('sparks (monthly co2 Concentration and %d-month Smoothing,window)')

xlabel ("years"); ylabel ("CO<sub>2</sub> (ppm)");

legend ('monthly', 'smoothed', 'location', 'best'));

growth: very much like an exponential  $\rightarrow$  try exponential fit!

matlab's curve fitting toolbox → 2016b

model = fitType(<sup>1</sup>'a+b\*exp(n\*(years-1958))', 'Independent',  
                   /  
                   'years');

Formula  
 $a + b e^{n(years - 1958)}$  → growth (exponential)

years → independent variable.  $a, b$  &  $n$  → constants determined by MATLAB.

\* o/p → model to be ffk

`fitOptions ('method', 'NonLinearLeastSquares', 'StartPoint', [0,0,0]);`

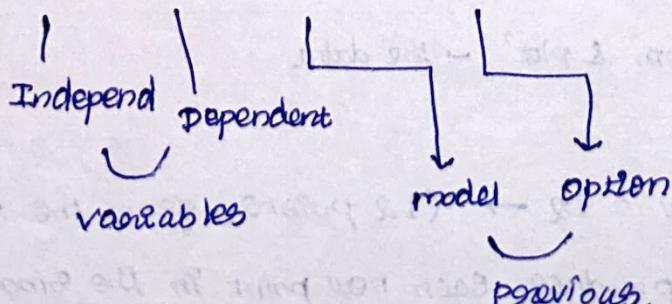
method of choosing best

values of  $a, b \in \mathbb{N}$

initial values or

In an internal  
prospective method  
to have sum of  
minimal squared  
differences.

`fPK(gear, CO2, model, options)`



```

model = fittype ('a+b*exp(n*(years-1958))', 'Independent', 'years');
options = fitoptions ('Method', 'NonLinearLeastSquares', 'StartPoint', [0,0,0]);
Co2_fit = fit (years, Co2, model, options);
Co2_model = Co2_fit.a + Co2_fit.b * exp(Co2_fit.n * (years - 1958));
plot (years, smoothed, 'k', years, Co2_model, 'r--'); grid on;
title ('Co2 Smoothed and Co2 model');
 xlabel ('years'); ylabel ('Co2 (PPM)');
 legend ('Smoothed', 'Model', 'Location', 'best');

```

model → used to fit

options → helps in designing model

fit → uses model, options to fit the curve

↓  
struct      'Co2\_model' → uses a, b, n → To calculate values of model for  
even years. (element of variable years)

'Now we have model → Co2\_model' → plot

\* Plotting → Smoothed & fitted plots.

'Perfect fit'

\* Root Square mean error ≈ 0.2 (Avg error: 2 parts per million) → Good fit!

In usual script: second graph - replace first!

But Livescript: No!

'Renesas curve fitting toolbox'!

extrapolate:

future = years(end) : 1/12 : 2050;

Co2\_future = Co2\_fit.a + Co2\_fit.b \* exp(Co2\_fit.n \*  
(future - 1958));

plot (years, Co2, 'g', future, Co2\_future, 'r--'); grid on;

title ('Co2 measured and projected to the future');

Calculator ( - - - )

Legend ( - - - )

### Convert non-Live to Live Script

\* Table of Contents: Insert  $\rightarrow$  Table of Contents (Automatically created) - Live Links.

TypeSet evaluation.

Insert  $\rightarrow$  Evaluation

$$\text{CO}_2 = a + b e^{n(\text{year} - 1958)}$$

Highlight  $\rightarrow$   Bold

$\text{CO}_2 \rightarrow \text{Index} \rightarrow \text{CO}_2$

'Hide code'  $\rightarrow$  No code will be shown in document.

Live script from non-Livescript  
Publish  $\rightarrow$  html

Save as  $\rightarrow$  .m to .mlx (That's it)

Fog installed version: Save as  $\rightarrow$  .mlx (open new one)

\* 2016  $\rightarrow$  until Livescript not invented!

\* 2050  $\rightarrow$  600 ppm  $\uparrow$

\* Act!

## Error handling:

\* Behave in unexpected way! - handle them well

\* diff (end+1) → out of index.

Run → debug

'Not a good way! when others (know nothing) uses it!'

Not enough info: error message: (long time: forget what's inside the hood)

## Solution:

```

function h = my_harmonic(n)
    if ~isscalar(n) || n < 1 || n ~= floor(n)
        error('positive integer input expected ...');
    end
    h = 1;
    for ii = 2:n
        h = h + 1/ii;
    end
end

```

→ my\_harmonic (0)  
error!  
→ my\_harmonic (2.3)  
error!  
→ my\_harmonic ([2,3])  
error!

→ disrupts entire program!

end if chain: throws an error!

```

function h = harmonic_chain(n)
    h = sub_harmonic(n);
end
function h = sub_harmonic(n)
    h = my_harmonic(n);
end.

```

'useless'

tells position of stack - when error is realized.

Assumes 2 hours of calculation! → Boom! (waste of time!)

Avoid! → convert bad I/P to good I/P.

If ~isscalar(n)

n = n(1);

→ picks first element of array.

\*  $n = \max(1, \text{round}(\text{abs}(n)))$ ;  $\rightarrow$  round to integers

### Exception handling!

\* code: designated as being executed only when an exception occurs in that part of the program.

try

```
h = my_harmonic(n);
```

catch

```
h = [];
```

$\rightarrow$  If error do this (catch)

end

C++, Java also same keyword

warning('wrong input provided');  $\rightarrow$  provide info: location executes throwing

try

```
out = X(r, n) * Y(n, c)
```

Catch ME

```
If error (ME, identifier, 'Matlab:badsubscript')
```

```
[xsize] = size(X); [ysize] = size(Y);
```

$m_1 = \text{strcmp}(^{\text{Accessed}} X(^{\text{r}}, ^{\text{d}}, ^{\text{n}}, ^{\text{c}}) \text{ and } Y(^{\text{n}}, ^{\text{d}}, ^{\text{r}}, ^{\text{c}}))$ , but  $^{\text{r}}, ^{\text{n}}, ^{\text{d}}, ^{\text{c}}$ ;

$m_2 = \text{strcmp}(^{\text{Error}} X(^{\text{r}}, ^{\text{d}}, ^{\text{n}}, ^{\text{c}}) \text{ and } Y(^{\text{n}}, ^{\text{d}}, ^{\text{r}}, ^{\text{c}}), 'X S220,$

```
error([m1, m2])
```

end

end

'still cause error' - detailed error

(Catch)

ME?  $\rightarrow$  when an error is caught  $\rightarrow$  that variable after catch is assigned an object that has info about the error!  
(kind of error thrown),

\* message - that would have been printed - if no error

stored in property of the object.

\* ME → struct of fields

Identifier: name of one of those fields.

↳ Accessing property (field) by dot operator,

Identifier: 'MATLAB: badSubscript' → By running  
error  
(found)!

List of Identifiers: exist but not given by MATLAB:

make errors - find yourself.

>> MException.last

ans =

: Properties

MException.last → preference to a struct  
(Object property)

Identifier: ' ' → why? (Shows only info of most recently uncaught error).

But now: thrown inside error function → caught! Identifiers ' ' !

'Use meaningful identifiers'

Instead e.g.:

error([m<sub>1</sub>, m<sub>2</sub>]); →

error('JMF:element\_prod: badSubscript', [m<sub>1</sub>, m<sub>2</sub>]);

JMF → string (used) - nothing

message!

## Another way - Built-in function

```
m1 = ""
m2 = ""
myE = MException("JMF", "", [m1, m2]);
throw(myE);
```

\* Rethrow → error

rethrow(ME); → error not caught.

(go & get caught)

## Version 1

function out = element\_prod(x, y, r, n, c)

% Element\_Prod two-element product for matrix mult.

% element\_Prod (x, y, r, n, k) = x(r, n) \* y(n, c) {n-index}

% must be summed over to produce the element at row r &

column c of the product of matrices x & y.

### Version 1

out = x(r, n) \* y(n, c);

end

## matmul.m

function C = matmul(A, B)

[rowA, colA] = size(A);

[rowB, colB] = size(B);

if ~ismatrix(A) || ~ismatrix(B)

error('function matmul requires matrices...');

else

colA == rowB

error('Inner dimensions must agree!');

end

C = zeros(rowA, colB);

for ii = 1:rowA

for jj = 1:colB

for kk = 1:colA

$$c(p, q) = C(pp, qq) + \text{element\_prod}(A, B, pp, qq, RR);$$

```

    end
    end
    end
end

```

product: changing message (version): Annoying!

thrown message!

Version 2

try

```
out = X(r, n) * X(n, C);
```

catch ME

```
if isequal(ME, identifier, 'MATLAB:badSubscript')
```

```
[Xsize] = size(X); [Ysize] = size(Y);
```

```
m1 = sprintf('Accessed ..')
```

```
m2 = sprintf('.. - - - )
```

```
error([m1, m2]);
```

end

end

Particular  
error-caused!

Version: 1

(By running!)

Version 3 : No identifiers

myE = - - - -

throw(MYE)

→ exception thrown (prev. case: not thrown  
as e,  
identifiers)

Rethrow

rethrow(ME); ①. error - not caught & error.

## Assertion

\* Assumptions: about variables in code - if that violated - MATLAB let you know.

function assert - example

```
% do some computation  
x=abs(randn)  
% do some more computation  
assert(x>=0)  
% keep working
```

end

→ helps to exterminate bugs while developing!

e.g. once done - remove / comment it?

Assumption: important to proper behaviour of the code!  
Introduce assertion!

we are using abs()

how x will be negative?

do some more → if makes x negative!

O/P

Assertion failed.

I'm sure the tiger cages locked or  
I'm sure this pool I'm about to dive in head first  
is deep enough!

save → time (normally don't throw error!  
if it does: no worries!

Assertion is there!)

## Error handling - Summary

- \* Exception: error thrown in designated portion of code
- \* Handler: runs when error is thrown: instead of errors & exit
  - try-catch block
- \* Identify errors with `Catch ME`, `Exception`, `last`
- \* Throw errors (detected): `throw` function
- \* Rethrow error with `rethrow` function (undetected)
- \* `assert` function to identify incorrect assumptions!

## Algorithmic Complexity

\*  $1 + 1 = 2$

$1 + 1 + 2 = 3$

$1 + 1 + 2 + 3 = 5$

Recursive call  $\rightarrow$  lot of recursive calls!

`fib0(50)`

Running forever!

Busy with recursive calls!



`fib0(50)  $\rightarrow$  fib0(49) + fib0(48)`

`fib0(49)  $\rightarrow$  48`

`fib0(48)  $\rightarrow$  47`

'Twice'  $\rightarrow$  called!

## use persistent:

```
function [f, cnt] = fib0cnt(n)
```

```
    persistent count;
```

```
    if isempty(count)
```

```
        Count = 1;
```

```
    else
```

```
        Count = Count + 1;
```

```
    end
```

```
    if n <= 2
```

```
        f = 1;
```

```
    else
```

```
        f = fib0cnt(n-2) + fib0cnt(n-1);
```

```
    end
```

```
    cnt = Count;
```

```
end.
```

→ count (retains even if it's local)

Note: A persistent variable can't be an o/p argument!

`fibocnt(3) → 3 calls!`

`(5) → 9 calls!`

`25 → 150049 calls!`

`35 → 18604978 calls!`

'Need to clean - persistent  
variable' → Since it  
returns!

↓  
"Not a elegant solution"

Algorithm: wrong approach!

① non recursive!

② memory!

function  $f = \text{fib0\_last}(n)$

if  $n \leq 2$

$f = \text{ones}(1, n);$

else

$f = \text{fib0\_last}(n-1);$

$f = [f \ f(\text{end}-1) + f(\text{end})];$

end

end

$[1 \ 1] \rightarrow [1 \ 1 \ 2] \rightarrow [1 \ 1 \ 2 \ 3] \rightarrow [1 \ 1 \ 2 \ 3 \ 5]$

go to deep - then climb

$2 \rightarrow [1 \ 1]$

$3 \rightarrow [[1 \ 1], 2] \rightarrow [1 \ 1 \ 2]$

$4 \rightarrow [1 \ 1 \ 2 \ 3]$

$30 \rightarrow 57$  nec calls!

Reverse

\*  $v = 1:10;$

\*  $v(\text{end}:-1:1);$

$\text{flip}(v)$

1	2	3	4	5	6	7	8
2	1	3	4	5	6	7	8
3	2	1	4	5	6	7	8
4	3	2	1	5	6	7	8
5	4	3	2	1	6	7	8
6	5	4	3	2	1	7	8
7	6	5	4	3	2	1	8
8	7	6	5	4	3	2	1

$i = 1$ , swap  $a[1], a[0] \rightarrow i++$ , shift  
 $a[1] \rightarrow a[0]$

2	1	3	4	5	6	7	8
3	1	3	4	5	6	7	8
3	1	1	4	5	6	7	8
3	2	1	4	5	6	7	8
7	6	5	4	3	2	1	8
8	6	5	4	3	2	1	8
8	6	6	5	4	3	2	1
8	7	6	5	4	3	2	1

Swap  $\rightarrow a[2] \& a[0]$

\* time\_9k only evaluates - functions with no arguments

» time9k(@() my\_flip(1:1e4))

↓  
function handle to anonymous function!

ans =

0.1402 (Accurate)

\* KTC Doc  $\rightarrow$  Runs multiple times  $\rightarrow$  returns average!

our algorithm:

$$\begin{array}{l} 1000 \rightarrow 0.1412 \\ 100000 \rightarrow 14.19 \end{array} \quad \left. \begin{array}{l} \text{factors: 100 (size)} \\ \text{time: koh!} \end{array} \right.$$

$$\begin{array}{l} 20000 \rightarrow 0.56 \\ 40000 \rightarrow 0.07 \end{array} \quad \left. \begin{array}{l} \text{Time } \uparrow \text{ by 4} \end{array} \right.$$

'quadratic Relationship'

2 nested loops:  $(n-1)(1 \text{ to } n-1)$

$$(n-1)\left(\frac{1}{2}n\right) - \approx \frac{1}{2}n - \frac{1}{2}n^2$$

↳ Average!

'quadratic'

million  $\rightarrow$  20 minutes

10 million  $\rightarrow$  half a day +.

Better Solution - Swap!

1	2	3	4	5	6	7	8	Tada!
8	2	3	4	5	6	7	1	
8	7	3	4	5	6	2	1	
8	7	6	4	5	3	2	1	
8	7	6	5	4	3	2	1	

$$\boxed{\frac{1}{2}n} \quad ; \text{ swapping!}$$

1 Addition  $\rightarrow 0.0040$

10 Addition  $\rightarrow 0.0485$ ) great (1 hah: 14 seconds  $\rightarrow$  previous algo!)

flip()  $\rightarrow$  matlab builtin

>> L = mpeik(@() flip(1:107))

→ Better than ours!

ans =

0.0285

why? → Low level features [not even implemented in MATLAB] like many built-in functions

Improvement - Constant time!

$$t(N) \approx C \log(N) \rightarrow O(\log N)$$

$$t(N) \approx CN^2 \rightarrow O(N^2)$$

$$t(N) \approx CN \rightarrow O(N) \rightarrow \text{Linear}$$

$$t(N) \approx C \rightarrow O(C)$$

Complexity theory/Analysis of Algorithm - Field of Algo..

Any problems: do better than N:

Sum of  $N$  positive integers

$$\text{Sum}(1:100) = 1+2+3+\dots+100 = 5050$$

Carl Friedrich Gauss:

$$1+100 = 101$$

$$2+99 = 101$$

$$50+51 = 101$$

$$50 \times 101 = 5050$$

50 such sums

$$\boxed{\frac{n(n+1)}{2}}$$

'Constant time' - Independent of size!

\* n th fibonacci formula: Using golden ratio!

\* Searching: `find(v, 1)` → returns index

'Binary Search' → much faster!

$$\log_2(\text{size})$$

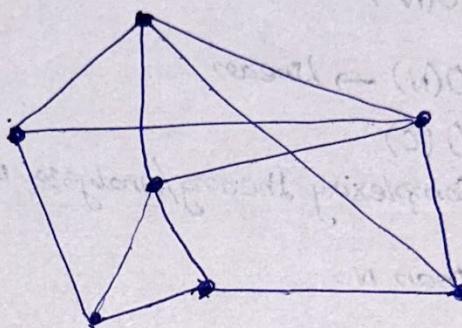
1024 → 10 steps

$$t(N) \approx cN \log(N) \rightarrow O(N \log N)$$

Traveling salesperson problem!

many cities - many paths - shortest path - visit each city & return home!

Simplest worst case: when shortest road connecting each pair of cities doesn't pass through any other cities.



\*<sup>1</sup> factorial steps!

(See all solutions)

↳ 'simple solution - catching eye': (worst than  $n^2$ )

Impractical for even 20 digits!

'Best (still known)':  $\alpha^n$

$$t(N) \approx C\alpha^N \Rightarrow O(\alpha^N)$$

$$N^2 = 100 \text{ steps}, \alpha^{10} = 1000 \text{ steps}$$

$$\alpha^{20} = \text{million}$$

$$\alpha^{30} = \text{billion}$$

'many real world problems': follows this: have no solution!

better than  $O(\alpha^N)$

If one can solve this: (Sales man problem)!

Able to solve other problems too - efficiently!

'Fed Ex, DHL, UPS - postal service' — minimize fuel, work etc..

'changing base is just equal as changing constant  $C'$

$$k(N) \approx \underline{C} \log(N) \rightarrow \therefore \text{No bases included.}$$

'No effect on complexity'

Matrix multiplication —  $\Theta(n^3)$

$$\begin{array}{l} M \times M^2 \\ (\text{add}) \quad (m \times m - \text{o/p size}) \end{array} = M^3$$

$$\therefore \text{I/p} \rightarrow N = 2M^2 \quad (\text{I/p} = M^2, M \times M = (2M^2) \text{ size})$$

o/p  $\rightarrow M^2 \text{ size.}$

$$M^3 = C N^{3/2}$$

$$k(N) \approx C N^{3/2} \Rightarrow \Theta(N^{3/2})$$

1969: Strassen  $\rightarrow n^{2.8}$  (Power)  $\rightarrow$  Complicated steps.

Matlab `convolution`  $\rightarrow (700 \times 700)$  by  $(700 \times 700)$

1.4968 seconds

Matlab `nnbuilt`  $\rightarrow 0.0044$

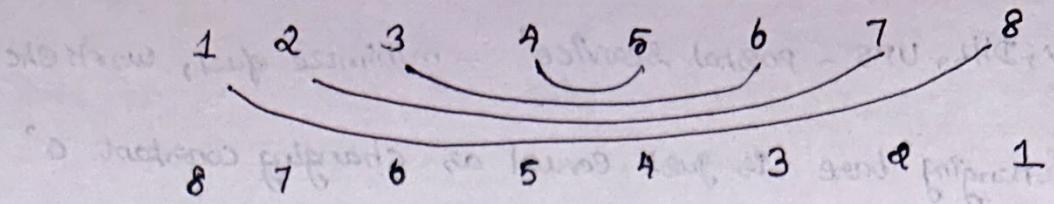
why? 340 x faster!

Now best:  $M^{2.373}$

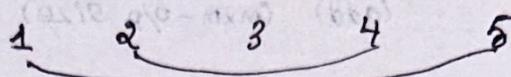
— Slower than current  $M^3$  implementations  
(Complicated steps)

MATLAB Algo  $\rightarrow$  not written in MATLAB

(uses microcontrollers — multi programming)



$start = 1$      $start = 2$      $start = 3$      $start = 4$      $start = 5$   
 $end = 8$      $end = 7$      $end = 6$      $end = 5$      $end = 6$   
 ↓              ↓              ↓              ↓              ↓  
 Swap.          Swap          Swap          Swap          If ( $start > end$ )  
 return.



$start = 1$      $start = 2$      $start = 3$   
 $end = 5$      $end = 4$      $end = 3$ .

Perce solutions  $\rightarrow$  have whole  $v \rightarrow$  %p array  
in heap.

Say: 10000 elements  $\rightarrow$  5000  $\times$  10000 elements  $\rightarrow$  in heap (depth)  
 :- 5000 recursion calls!

Solution:

1 2 3 4 5 6

fun [2 3 4 5 6] (1)

fun [(3 4 5 6) 2 1]

only - few elements goes inside recursion.

function out reverse (in)

if ( $length(v) \leq 1$ )

  out = in;

else

  out = [reverse (in(2:end)) reverse (1)];

end

10	9	8	7	6	5	4	3	2	1
5	4	3	2	1	10	9	8	7	6
2	1	3	5	4	*	6	(8)	10	9
1	2	3	4	5	6	7	8	9	10

len odd  $\rightarrow$

$$\frac{\text{len}}{2} = 2$$

$$a = \text{IP}(1 : \text{len}/2);$$

$$b = \text{IP}(\text{len}/2 + 1);$$

$$c = \text{IP}(\text{len}/2 + 1 : \text{end});$$

$$v = [c \ b \ a]$$

reversal

until length  $\geq 1$ .

end

len even  $\rightarrow$

$$a = \text{IP}(1 : \text{len}/2)$$

$$b = \text{IP}(\text{len}/2 + 1 : \text{end});$$

$$v = [b \ a]$$

reverse

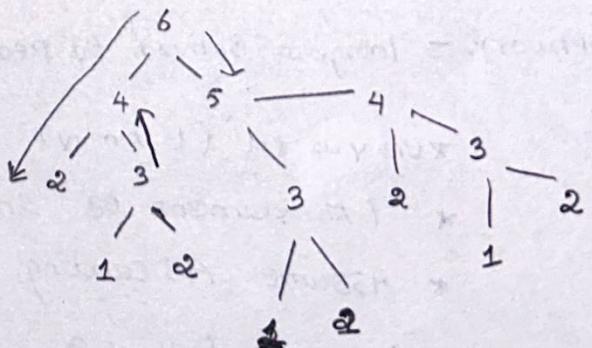
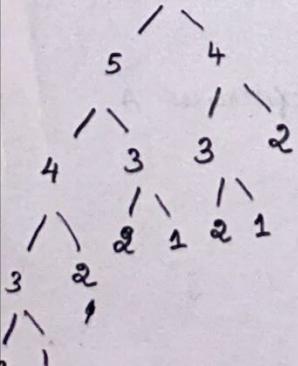
### Fibonacci profiles

- \* we used  $\rightarrow$  penultimate variable to profile (how many calls)
- \* Another way - use trace  $\rightarrow$  vector  $\rightarrow$  having elements each time - recursive call.

6, [ ]

①

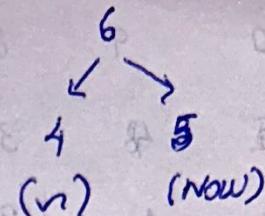
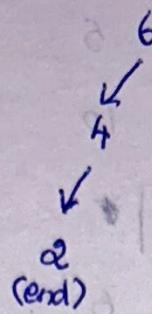
$$f\text{ib}(n-2) + f\text{ib}(n-1)$$



{ 6, 4, 2, 3, 1, 2,

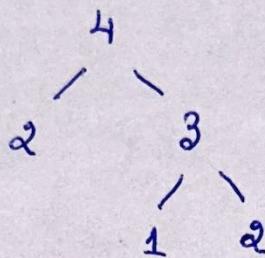
5, 3, 1, 2, 4, 2, 3, 1, 2 }

why  $\rightarrow$  since



Continues!

1 1 2 3



$fbo(4, [] )$

$$fbo(2, [4]) + fbo(3, [4, 2]) \longrightarrow$$
$$\begin{matrix} \downarrow & \nearrow \\ [4 & 2] & [4 & 2 & 3] \\ [4 & 2 & 3 & 1] \end{matrix}$$

$fbo(\dots)$

$fbo(\dots) \rightarrow$  This needs previous ones o/p

Social network - largest subgraph of people - each follow each other

\* unique id (1 to N)

\* i-th element of  $s_n \rightarrow$  vector (1st is id - i follows)

\* Assume: Ascending order.

\* A may follow B - B may/may not follow A.

\* Profiling - how much time - spent by various parts

\* Built in - profiler (function)

\* Shows time (most times), how many times each func. called?  
\* Matlab online - don't have this feature.

Improve algorithm:

\* Any unnecessary work.

function A = rooting\_V1(V, W)

(Same Length)

A = zeros(length(V), length(W));

for ii = 1: length(V)

    for jj = 1: length(W)

        A(ii, jj) = nthroot(V(ii), jj) \* nthroot(W(jj), jj);

    end

end

end

$$A(ii, jj) = V(ii)^{1/jj} \times W(jj)^{1/jj}$$

$$A(2, 3) = V(2)^{1/2} \times W(3)^{1/3}$$

\* nthroot → Inbuilt function

\* n<sup>th</sup> → Algorithm

t8c; rooting\_V1(rands(1e6, 1, 1e3); rands(1e6, 1, 1e3)); loc,

7.9233 seconds! (1000 elements)

$$10000 \rightarrow 100 \times 7.9233 = 80 \text{ seconds}$$

Unnecessary works.

each time calculating  $A(ii)^{1/jj} \rightarrow \therefore jj \text{ times}$

Unnecessary!

modifyfor  $pp = 1 : \text{length}(v)$  $x = \text{nroot}(v(pp), pp); \rightarrow 1 \text{ calculation!}$  instead of  
 $\text{length}(w) \times \text{times!}$ for  $qq = 1 : \text{length}(w)$  $A(pp, qq) = x * \text{nroot}(w(qq), qq);$ 

end end

Now: 4.008896 seconds.

\* is equal  $(A_1, A_2) = 1 (\text{reg})!$   $\rightarrow$  Answer of part, new version same!modify $rw = zeros(1, \text{length}(w));$ for  $qq = 1 : \text{length}(w)$  $rw(qq) = \text{nroot}(w(qq), qq); \rightarrow \text{Not runned 1000 times!}$ for  $pp = 1 : \text{length}(v)$  $x = \text{nroot}(v(pp), pp);$ for  $qq = 1 : \text{length}(w)$  $A(pp, qq) = x * rw(qq);$ 

end

end

Now: 0.031786 (100 times faster)

\* general  $(A_1, A_3)!$ Now: 2000 times instead of million times  
by already doing nroot for ii, jj.modify - 1 million multiplications! $kpc; A3 = \text{rooting\_V3}(v, m); \text{toc}$ SHELL -  $n^2$  algorithm?

1.500814 seconds (instead of

12 minutes).

→ save time!

Precalculating! → General practice

\* Trade off b/w memory & time (But small memory)

one vector of length  $n \rightarrow$  2 orders of magnitude time save

'cool'!

\*  $A = \text{zeros}(\text{length}(v), \text{length}(w)); \rightarrow$  pre allocation!

'Saves time'! / some case: Default! (no value: 0 or -1)

without preallocation:

%  $A = \text{zeros}(\text{length}(v), \text{length}(w));$

↓

410.850459 seconds (7 minutes)

↓

Saved by pre allocation

Profile

>> profile on

>>  $f2 = \text{rooting\_v2}(v, w);$

>> profile viewer → window opens. ( $n$ th root  $\rightarrow$  1000 times)  
5.808 Seconds  
with live link.

rooting\_v2 → line by line (time), info!

$x = \text{nthroot}(v(99), 99); \rightarrow 0.2\% \text{ (1000 times)}$

↓

Line-time-bar chart

early in installed version?

unnecessary work!

\* speed up - without extra memory! (avoid unnecessary work)!

ID: 1 to N

1	2	...	300
56	8		
877	45		
1357	77		

which two sets of people - have lots of people in common!

'cell array'

\* 2 & 2998 → Have 11 common people

\* load follows

who's

follows 1x3000 399256 by 263 cell.

\* 4 1/2 million pairs to look up

\* intersect ( )  
↳ finds common! (In two vectors)!

worst case: everybody follows everybody!

4 million pairs

Time save: If we found (say): 1 & 2 : Have 5 persons

Leave any two having less than 5 → SKIP  
(Save time)

118 seconds → 1.7 seconds

Caution: If every person has at least 6 → No need for own ~~if~~ case!

'skip' - 'continue' the loop' - avoid unnecessary work!

Focus on computationally intensive codes!

vectorization & other speed ups

\* 'Implementation' - makes difference

MATLAB & implicit looping:

- \* MATLAB - invented to work with matrices & arrays!
- \* Incorporate operators, notions - directly in MATLAB.

Implicit looping - everywhere!

\* add, sub, mul, div → doesn't require any loop (inbuilt)

MATLAB & implicit looping

\* Implicit → By lowlevel methods (Inside there: really fast)  
loops

Any function operates on entire vector → entire array

'Vectorize command' → using implicit looping

Avoid explicit loops by vectorization.



Translation of code from version uses

explicit looping to one that uses a vectorize command.

other languages - lack built-in support for

vectorization - even if has power of  
implicit looping!



Dramatic Speedups - less prone to errors  
& easy to debug!

Rooting - more modified!

function A = rooting\_v4(v, w)

A = zeros (length (v), length (w));

rv = nthroot (v, 1: length (v));

rw = nthroot (w, 1: length (w));

for i PP = 1: length (v)

for j JJ = 1: length (w)

A (PP, JJ) = rv (PP) \* rw (JJ)

end

end

→ 1.8 seconds!

end

timeit (@() rooting\_v3(v, w))

↳ ∵ timeit doesn't take %p functions!

Anonymous function!

what we are doing:  $A(99, 99) = \text{rv}(99) * \text{rw}(99) \rightarrow \text{matrix} \times \text{matrix}$

function A = rooting\_v5(v, m)

rv = nthroot (v, 1: length (v));

rw = nthroot (m, 1: length (m));

A = rv' \* rw';

end

$n \times n$  output

$(1 \times n) \times (n \times n)$

$(n \times 1) \times (1 \times n) =$   
 $(n \times n)$

0.2050 seconds!

↓  
easy to understand & implement!

Time Comparison & profile → using logical indexing.

\* Nested loop

\* Indexing using logic.

```

function A = small & zero - v1(A, limit)
    for pp = 1 : size(A, 1) → Rows
        for jj = 1 : size(A, 2) → columns
            if A(pp, jj) < limit
                A(pp, jj) = 0; → 1.3503 seconds
            end
        end
    end
end

```

```

>> A = rand(1e6, 1e4);
>> timeit(@() small & zero - v1(A, 50))
ans =
1.3503

```

### modify

```

function A = small & zero - v2(A, limit)
    A(A < limit) = 0; → 0.6662 !
    end

```

Same basic timeit → only expressions are allowed!

```

tic; A(A < 50) = 0; toc;

```

### Profile

```

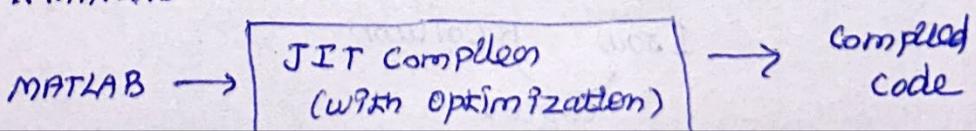
>> profile off
>> profile on
>> small & zero - v1(A, 50) → if → 7.65 seconds
>> profile viewer → end → 3.701
→ end → 3.563

```

why slow - when profiled?

- \* MATLAB optimizes the code

- \* MATLAB converts to translated (compiled)



## Just in Time results (Compilation)



\* Optimization results - guarantees no to change results.

\* Improved every year - MATLAB engineers improving it!

\* Optimization - orders of some operations, looping may be changed almost as implicit looping in the vectorized code! (But never be as good as vectorized) but trying to be!

\* Optimization methods: secret (changeable: programmers shouldn't take advantage).

\* Compiler saves translated in local file. (internal)

\* So often (restart MATLAB) - until edit) → no need to compile again!

Say: persistent (clear when restarted!)

\* Point: can't use profiler to compare the vectorized code with optimized code times!

Profiler: still useful for non vectorized ones?

\* Say every element of the array to zero - second element in its own row.

↳ seems like nested loops only solution (No!)

## Built-in function:

repmat → replicating matrices (makes copies of matrices and arrays)

>> A = randi(99, 4, 5);

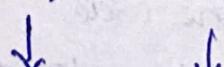
2 column : 71

55

99

11

repmat(A(:, 2), 1, size(A, 2))



1 row      5 column  
copies