



Capital University of Science and Technology

Department of Computer Science

CS3613 – Theory of Automata and Formal Languages

ASSIGNMENT NO. 3

Semester: Fall 2022

Max Marks: 10

Instructor: Hashim Ayub

Assigned Date: 20 Dec 2022

Due Date: 26 Dec 2022

Name:

Reg. No.

PROBLEMS

1. Consider the Context Free Grammar: $S \rightarrow aSa \mid bb \mid b$

Prove that this generates the language defined by the regular expression

$$a^* bbb$$

2. Consider the following CFG:

$$S \rightarrow XWG$$

$$X \rightarrow aX \mid bX \mid G$$

$$W \rightarrow bb \mid aa \mid bW \mid aW$$

$$G \rightarrow aG \mid bG$$

Prove that this generates the language of all strings with a triple b in them which is the language defined by $(a + b)^* bbb (a + b)^*$

3. Consider the following CFG:

$$S \rightarrow aX$$

$$X \rightarrow aX \mid bX \mid A$$

What is the language of this CFG that will be generated?

4. What is the language this CFG will be generating while considering the

following CFG:

$$S \rightarrow XaXaX$$

$$X \rightarrow aX \mid bX \mid A$$

5. Consider the CFG:

$$S \rightarrow SS \mid XaXaX \mid A$$

$$X \rightarrow bX \mid A$$

Prove that X can generate any b^* .

6. Show that the set $L = \{a^n b^n \mid n \geq 1\}$ is not a regular.

7. Consider a grammar G is given as follows

$$S \rightarrow AB \mid aaB$$

$$A \rightarrow a \mid Aa$$

$$B \rightarrow b$$

Determine whether the grammar G is ambiguous or not. If G is ambiguous, construct an unambiguous grammar equivalent to G.

8. Simplify the following grammar

$$S \rightarrow aAa \mid bBb \mid BB$$

$$A \rightarrow C$$

$$B \rightarrow S \mid A$$

$$C \rightarrow S \mid \varepsilon$$

9. Discuss in detail about ambiguous grammar and removing ambiguity from grammar.

10. Construct a derivation tree for the string 0011000 using the grammar

$$S \rightarrow A0S \mid 0 \mid SS$$

$$A \rightarrow S1A \mid 10$$