### **Tutorial Emu86**

#### 1) Numbering systems tutorial

#### What is it?

There are many ways to represent the same numeric value. Long ago, humans used sticks to count, and later learned how to draw pictures of sticks in the ground and eventually on paper. So, the number 5 was first represented as: | | | | (for five sticks).

Later on, the Romans began using different symbols for multiple numbers of sticks: | | still meant three sticks, but a **V** now meant five sticks, and an **X** was used to represent ten of them!

Using sticks to count was a great idea for its time. And using symbols instead of real sticks was much better.

#### **Decimal System**

Most people today use decimal representation to count. In the decimal system there are 10 digits:

These digits can represent any value, for example: **754**.

The value is formed by the sum of each digit, multiplied by the **base** (in this case it is **10** because there are 10 digits in decimal system) in power of digit position (counting from zero):

Position of each digit is very important! for example if you place "7" to the end:

547

it will be another value:

**Important note:** any number in power of zero is 1, even zero in power of zero is 1:

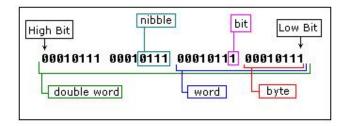
#### **Binary System**

Computers are not as smart as humans are (or not yet), it's easy to make an electronic machine with two states: **on** and **off**, or **1** and **0**. Computers use binary system, binary system uses 2 digits:

#### 0, 1

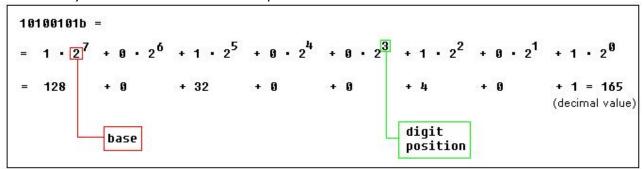
And thus the base is 2.

Each digit in a binary number is called a **BIT**, 4 bits form a **NIBBLE**, 8 bits form a **BYTE**, two bytes form a **WORD**, two words form a **DOUBLE WORD** (rarely used):



There is a convention to add "b" in the end of a binary number, this way we can determine that 101b is a binary number with decimal value of 5.

The binary number 10100101b equals to decimal value of 165:



## **Hexadecimal System**

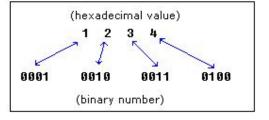
Hexadecimal System uses 16 digits:

0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F

And thus the base is 16.

Hexadecimal numbers are compact and easy to read. It is very easy to convert numbers from binary system to hexadecimal system and vice-versa, every nibble (4 bits) can be converted to a hexadecimal digit using this table:

| Decimal<br>(base 10) | Binary<br>(base 2) | Hexadecimal (base 16) |
|----------------------|--------------------|-----------------------|
| 0                    | 0000               | 0                     |
| 1                    | 0001               | 1                     |
| 2                    | 0010               | 2                     |
| 3                    | 0011               | 3                     |
| 4                    | 0100               | 4                     |
| 5                    | 0101               | 5                     |
| 6                    | 0110               | 6                     |
| 7                    | 0111               | 7                     |
| 8                    | 1000               | 8                     |
| 9                    | 1001               | 9                     |
| 10                   | 1010               | А                     |
| 11                   | 1011               | В                     |
| 12                   | 1100               | С                     |
| 13                   | 1101               | D                     |
| 14                   | 1110               | E                     |
| 15                   | 1111               | F                     |



There is a convention to add "h" in the end of a hexadecimal number, this way we can determine that 5Fh is a hexadecimal number with decimal value of 95.

We also add "O" (zero) in the beginning of hexadecimal numbers that begin with a letter (A..F), for example **OE120h**.

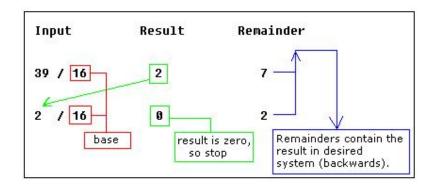
The hexadecimal number **1234h** is equal to decimal value of 4660:

# **Converting from Decimal System to Any Other**

In order to convert from decimal system, to any other system, it is required to divide the decimal value by the **base** of the desired system, each time you should remember the **result** and keep the **remainder**, the divide process continues until the **result** is zero.

The **remainders** are then used to represent a value in that system.

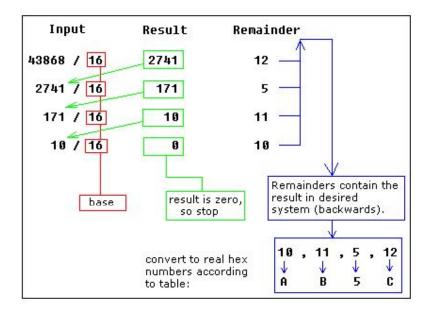
Let's convert the value of **39** (base <u>10</u>) to *Hexadecimal System* (base 16):



As you see we got this hexadecimal number: **27h**. All remainders were below **10** in the above example, so we do not use any letters.

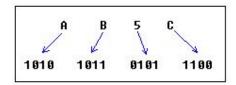
Arquitectura de Computadoras 2011 – UTN FRMza – Ingeniería en Sistemas

Here is another more complex example: let's convert decimal number **43868** to hexadecimal form:



The result is **OAB5Ch**, we are using **the above table** to convert remainders over **9** to corresponding letters.

Using the same principle we can convert to binary form (using **2** as the divider), or convert to hexadecimal number, and then convert it to binary number using **the above table**:



As you see we got this binary number: 1010101101011100b

#### **Signed Numbers**

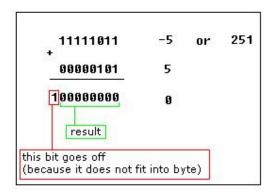
There is no way to say for sure whether the hexadecimal byte **OFFh** is positive or negative, it can represent both decimal value "**255**" and "- **1**".

8 bits can be used to create **256** combinations (including zero), so we simply presume that first **128** combinations (**0..127**) will represent positive numbers and next **128** combinations (**128..256**) will represent negative numbers.

Arquitectura de Computadoras 2011 – UTN FRMza – Ingeniería en Sistemas

In order to get "- 5", we should subtract 5 from the number of combinations (256), so it we'll get: 256 - 5 = 251.

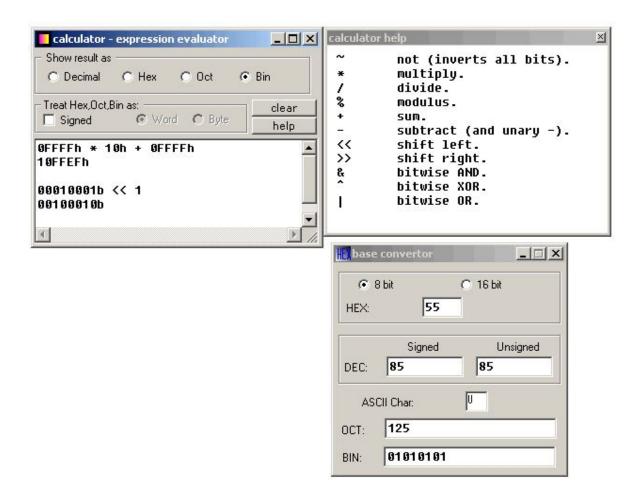
Using this complex way to represent negative numbers has some meaning, in math when you add "- 5" to "5" you should get zero. This is what happens when processor adds two bytes 5 and 251, the result gets over 255, because of the overflow processor gets zero!



When combinations **128..256** are used the high bit is always **1**, so this maybe used to determine the sign of a number.

The same principle is used for **words** (16 bit values), 16 bits create **65536** combinations, first 32768 combinations (**0..32767**) are used to represent positive numbers, and next 32768 combinations (**32767..65535**) represent negative numbers.

There are some handy tools in emu8086 to convert numbers, and make calculations of any numerical expressions, all you need is a click on **Math** menu:



**Base converter** allows you to convert numbers from any system and to any system. Just type a value in any text-box, and the value will be automatically converted to all other systems. You can work both with **8 bit** and **16 bit** values.

**Multi base calculator** can be used to make calculations between numbers in different systems and convert numbers from one system to another. Type an expression and press enter, result will appear in chosen numbering system. You can work with values up to **32 bits**. When **Signed** is checked evaluator assumes that all values (except decimal and double words) should be treated as **signed**. Double words are always treated as signed values, so **OFFFFFFFFh** is converted to **-1**.

For example you want to calculate: 0FFFFh \* 10h + 0FFFFh (maximum memory location that can be accessed by 8086 CPU). If you check **Signed** and **Word** you will get -17 (because it is evaluated as (-1) \* 16 + (-1). To make calculation with unsigned values uncheck **Signed** so that the evaluation will be 65535 \* 16 + 65535 and you should get 1114095.

You can also use the **base converter** to convert non-decimal digits

to signed decimal values, and do the calculation with decimal values (if it's easier for you).

These operation are supported:

```
not (inverts all bits).
multiply.
divide.
modulus.
sum.
subtract (and unary -).
shift left.
shift right.
bitwise AND.
bitwise XOR.
bitwise OR.
```

Binary numbers must have "**b**" suffix, example: 00011011b

Hexadecimal numbers must have " $\mathbf{h}$ " suffix, and start with a zero when first digit is a letter (A..F), example: 0ABCDh

Octal (base 8) numbers must have "o" suffix, example: 770