

## Assignment 06 Solution

Q1. A permutation perm of  $n + 1$  integers of all the integers in the range  $[0, n]$  can be represented as a string  $s$  of length  $n$  where:

- $s[i] == 'I'$  if  $\text{perm}[i] < \text{perm}[i + 1]$ , and
- $s[i] == 'D'$  if  $\text{perm}[i] > \text{perm}[i + 1]$ .

Given a string  $s$ , reconstruct the permutation perm and return it. If there are multiple valid permutations perm, return **any of them**.

**Example 1:**

**Input:**  $s = "IDID"$

**Output:**

$[0, 4, 1, 3, 2]$

```
In [151... def findPermutation(s):
    n = len(s)
    perm = []
    low, high = 0, n

    for c in s:
        if c == 'I':
            perm.append(low)
            low += 1
        else:
            perm.append(high)
            high -= 1

    perm.append(low)

    return perm
```

```
In [152... s = "IDID"
perm = findPermutation(s)
print(perm)

[0, 4, 1, 3, 2]
```

Q2. You are given an  $m \times n$  integer matrix matrix with the following two properties:

- Each row is sorted in non-decreasing order.
- The first integer of each row is greater than the last integer of the previous row.

Given an integer target, return true if target is in matrix or false otherwise.

You must write a solution in  $O(\log(m * n))$  time complexity. You are given an  $m \times n$  integer matrix matrix with the following two properties:

- Each row is sorted in non-decreasing order.
- The first integer of each row is greater than the last integer of the previous row.

Given an integer target, return true if target is in matrix or false otherwise.

You must write a solution in  $O(\log(m * n))$  time complexity.

**Input:** matrix =  $[[1, 3, 5, 7], [10, 11, 16, 20], [23, 30, 34, 60]]$ , target = 3

**Output:** true

**Example 1:**

```
In [167...
```

Out[167]:

1	3	5	7
10	11	16	20
23	30	34	60

```
In [153... def searchMatrix(matrix, target):
    m = len(matrix)
    n = len(matrix[0])
    low = 0
    high = m * n - 1

    while low <= high:
        mid = (low + high) // 2
        row = mid // n
        col = mid % n

        if matrix[row][col] == target:
            return True
        elif matrix[row][col] < target:
            low = mid + 1
        else:
            high = mid - 1

    return False

def searchMatrix(matrix, target):
    m = len(matrix)
    n = len(matrix[0])
    low = 0
    high = m * n - 1

    while low <= high:
        mid = (low + high) // 2
        row = mid // n
        col = mid % n

        if matrix[row][col] == target:
            return True
        elif matrix[row][col] < target:
            low = mid + 1
        else:
            high = mid - 1

    return False
```

```
In [154... matrix = [[1, 3, 5, 7], [10, 11, 16, 20], [23, 30, 34, 60]]
target = 3
print(searchMatrix(matrix, target))
```

True

### Question 3

Given an array of integers `arr`, return *true* if and only if it is a valid mountain array.

Recall that `arr` is a mountain array if and only if:

- `arr.length >= 3`
- There exists some `i` with  $0 < i < arr.length - 1$  such that:
  - `arr[0] < arr[1] < ... < arr[i - 1] < arr[i]`
  - `arr[i] > arr[i + 1] > ... > arr[arr.length - 1]`

**Example 1:**

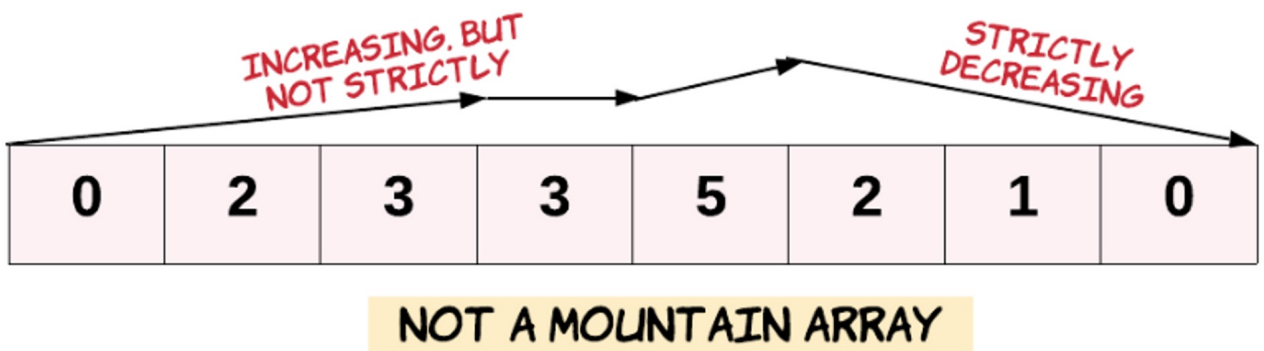
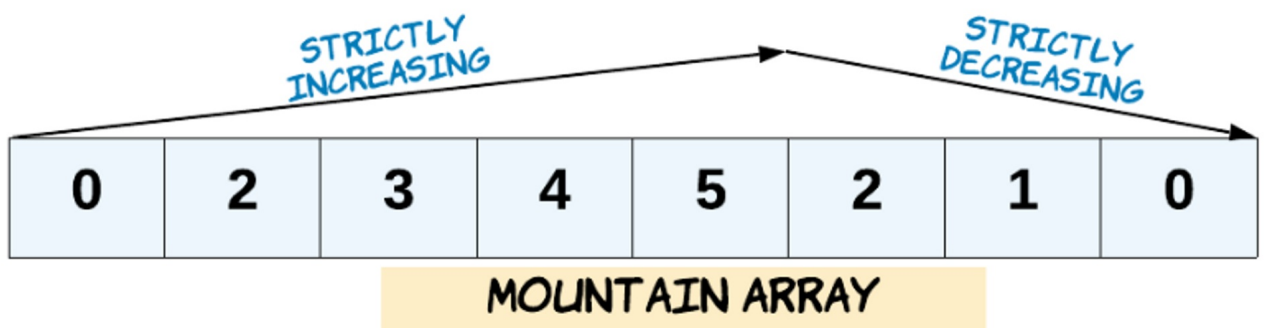
**Input:** `arr = [2,1]`

**Output:**

false

In [168,...

Out[168]:



```
In [155... def validMountainArray(arr):
    n = len(arr)
    i = 0

    while i + 1 < n and arr[i] < arr[i + 1]:
        i += 1

    if i == 0 or i == n - 1:
        return False

    while i + 1 < n and arr[i] > arr[i + 1]:
        i += 1

    return i == n - 1
```

```
In [156... arr = [2, 1]
print(validMountainArray(arr))
```

False

### Question 4

Given a binary array nums, return *the maximum length of a contiguous subarray with an equal number of 0 and 1*.

#### Example 1:

**Input:** nums = [0,1]

**Output:** 2

**Explanation:**

[0, 1] is the longest contiguous subarray with an equal number of 0 and 1.

```
In [157...] def findMaxLength(nums):
    count_map = {0: -1}
    count = 0
    max_length = 0

    for i, num in enumerate(nums):
        if num == 1:
            count += 1
        else:
            count -= 1

        if count in count_map:
            max_length = max(max_length, i - count_map[count])
        else:
            count_map[count] = i

    return max_length
```

```
In [158...] nums = [0, 1]
print(findMaxLength(nums))

2
```

#### Question 5

The **product sum** of two equal-length arrays a and b is equal to the sum of  $a[i] * b[i]$  for all  $0 \leq i < a.length$  (**0-indexed**).

- For example, if  $a = [1,2,3,4]$  and  $b = [5,2,3,1]$ , the **product sum** would be  $15 + 22 + 33 + 41 = 22$ .

Given two arrays nums1 and nums2 of length n, return *the minimum product sum\** if you are allowed to **rearrange** the **order** of the elements in\* nums1.

#### Example 1:

**Input:** nums1 = [5,3,4,2], nums2 = [4,2,2,5]

**Output:** 40

**Explanation:**

We can rearrange nums1 to become [3,5,4,2]. The product sum of [3,5,4,2] and [4,2,2,5] is  $34 + 52 + 42 + 25 = 40$ .

```
In [159...] def minProductSum(nums1, nums2):
    nums1.sort()
    nums2.sort(reverse=True)
    min_product_sum = 0

    for i in range(len(nums1)):
        min_product_sum += nums1[i] * nums2[i]

    return min_product_sum
```

```
In [160...] nums1 = [5, 3, 4, 2]
nums2 = [4, 2, 2, 5]
print(minProductSum(nums1, nums2))

40
```

#### Question 6

An integer array original is transformed into a **doubled** array changed by appending **twice the value** of every element in original, and then randomly **shuffling** the resulting array.

Given an array changed, return original *if changed is a doubled\** array. If\* changed is *not a doubled\** array, return an empty array. The elements in\* original *may be returned in any\** order\*.

**Example 1:**

**Input:** changed = [1,3,4,2,6,8]

**Output:** [1,3,4]

**Explanation:** One possible original array could be [1,3,4]:

- Twice the value of 1 is  $1 * 2 = 2$ .
- Twice the value of 3 is  $3 * 2 = 6$ .
- Twice the value of 4 is  $4 * 2 = 8$ .

Other original arrays could be [4,3,1] or [3,1,4].

```
In [161.. from collections import Counter

def findOriginalArray(changed):
    original_count = Counter()
    changed_count = Counter(changed)

    for num in changed:
        if num == 0:
            if changed_count[num] % 2 == 1:
                return []
            continue

        if changed_count[num] > 0 and changed_count[num * 2] > 0:
            original_count[num * 2] += 1
            changed_count[num] -= 1
            changed_count[num * 2] -= 1
        else:
            return []

    original = []
    for num, count in original_count.items():
        original.extend([num] * count)

    return original
```

```
In [162.. changed = [1, 3, 4, 2, 6, 8]
result = findOriginalArray(changed)
print(result)

[]
```

**Question 7**

Given a positive integer n, generate an n x n matrix filled with elements from 1 to n<sup>2</sup> in spiral order.

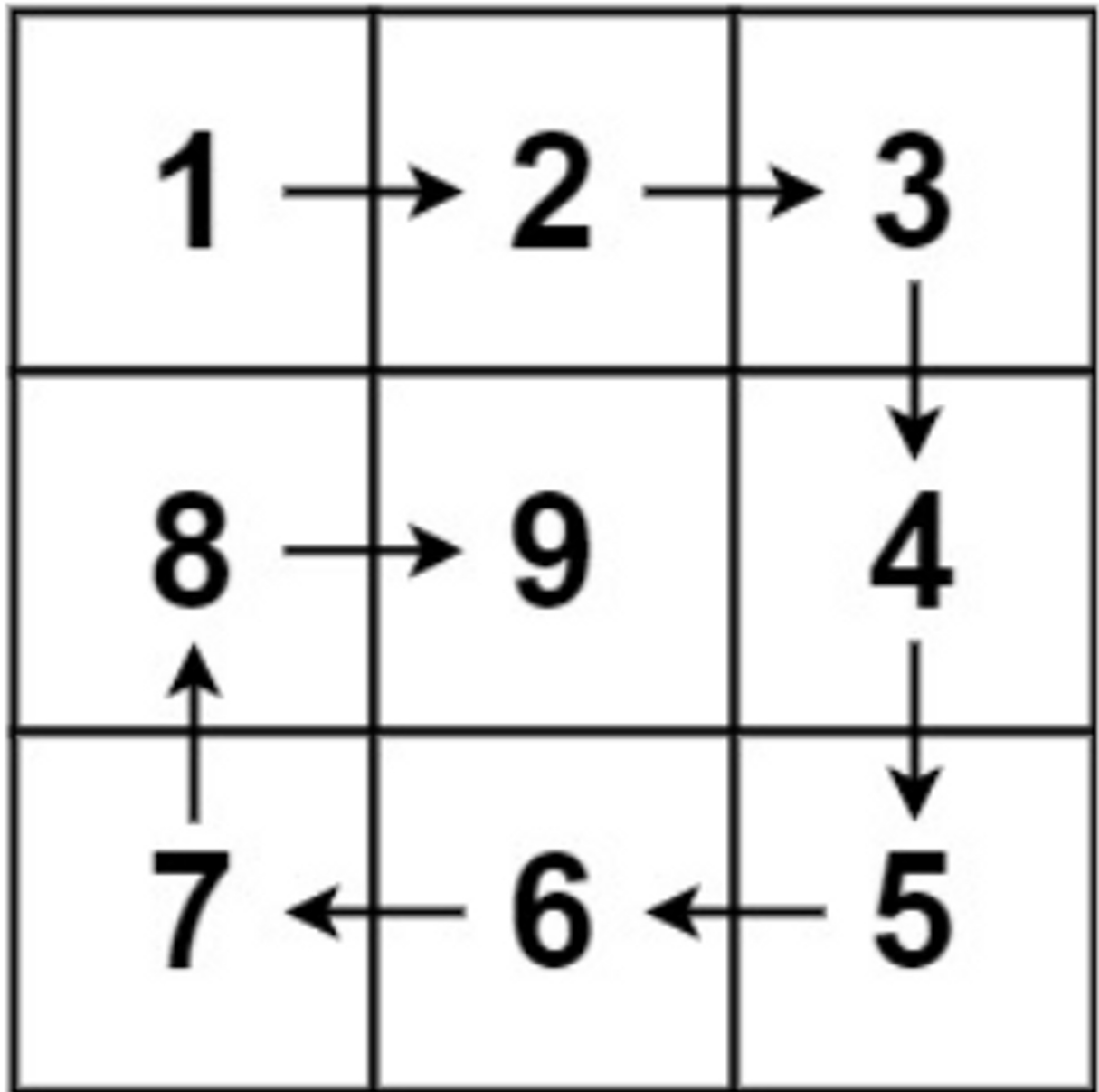
**Input:** n = 3

**Output:** [[1,2,3],[8,9,4],[7,6,5]]

**Example 1:**

```
In [169..
```

Out[169]:



```
In [163]: def generateMatrix(n):  
    matrix = [[0] * n for _ in range(n)]  
    row_start, row_end = 0, n - 1  
    col_start, col_end = 0, n - 1  
    num = 1  
  
    while num <= n * n:  
        # Fill top row  
        for j in range(col_start, col_end + 1):  
            matrix[row_start][j] = num  
            num += 1  
        row_start += 1  
  
        # Fill right column  
        for i in range(row_start, row_end + 1):  
            matrix[i][col_end] = num  
            num += 1  
        col_end -= 1  
  
        # Fill bottom row  
        for j in range(col_end, col_start - 1, -1):  
            matrix[row_end][j] = num  
            num += 1  
        row_end -= 1  
  
        # Fill left column  
        for i in range(row_end, row_start - 1, -1):  
            matrix[i][col_start] = num  
            num += 1  
        col_start += 1  
  
    return matrix
```

```
In [164... n = 3
result = generateMatrix(n)
print(result)

[[1, 2, 3], [8, 9, 4], [7, 6, 5]]
```

### Question 8

Given two [sparse matrices](#) mat1 of size m x k and mat2 of size k x n, return the result of mat1 x mat2. You may assume that multiplication is always possible.

**Input:** mat1 = [[1,0,0],[-1,0,3]], mat2 = [[7,0,0],[0,0,0],[0,0,1]]

**Output:**

[[7,0,0],[-7,0,3]]

**Example 1:**

```
In [170...
```

```
Out[170]:
```

$$\begin{bmatrix} 1 & 0 & 0 \\ -1 & 0 & 3 \end{bmatrix} \times \begin{bmatrix} 7 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 7 & 0 & 0 \\ -7 & 0 & 3 \end{bmatrix}$$

```
In [165... def multiply(mat1, mat2):
    m = len(mat1)
    n = len(mat2[0])
    k = len(mat2)
    result = [[0] * n for _ in range(m)]

    for i in range(m):
        for j in range(n):
            sum = 0
            for x in range(k):
                sum += mat1[i][x] * mat2[x][j]
            result[i][j] = sum

    return result
```

```
In [166... mat1 = [[1, 0, 0], [-1, 0, 3]]
mat2 = [[7, 0, 0], [0, 0, 0], [0, 0, 1]]
result = multiply(mat1, mat2)
print(result)

[[7, 0, 0], [-7, 0, 3]]
```

```
In [ ]:
```