

## Recursive **void** Methods

- A *recursive* method is a method that includes a call to itself
- Recursion is based on the general problem solving technique of breaking down a task into subtasks
  - In particular, recursion can be used whenever one subtask is a smaller version of the original task

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## Vertical Numbers

- The *static recursive method* `writeVertical` takes one (nonnegative) `int` argument, and writes that `int` with the digits going down the screen one per line
  - Note: Recursive methods need not be static
- This task may be broken down into the following two subtasks
  - Simple case: If  $n < 10$ , then write the number  $n$  to the screen
  - Recursive Case: If  $n \geq 10$ , then do two subtasks:
    - Output all the digits except the last digit
    - Output the last digit

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## Vertical Numbers

- Given the argument 1234, the output of the first subtask would be:

1  
2  
3  
4

- The output of the second part would be:

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## Vertical Numbers

- The decomposition of tasks into subtasks can be used to derive the method definition:
  - Subtask 1 is a smaller version of the original task, so it can be implemented with a recursive call
  - Subtask 2 is just the simple case

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## Algorithm for Vertical Numbers

- Given parameter **n**:
 

```
if (n<10)
    System.out.println(n);
else
{
    writeVertical
        (the number n with the last digit removed);
    System.out.println(the last digit of n);
}
```

  - Note:  $n/10$  is the number **n** with the last digit removed, and  $n\%10$  is the last digit of **n**

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## A Recursive **void** Method (Part 1 of 2)

Display 11.1 A Recursive void Method

```

1 public class RecursionDemo1
2 {
3     public static void main(String[] args)
4     {
5         System.out.println("writeVertical(3):");
6         writeVertical(3);
7
8         System.out.println("writeVertical(12):");
9         writeVertical(12);
10
11        System.out.println("writeVertical(123):");
12        writeVertical(123);
13    }
14
15    public static void writeVertical(int n)
16    {
17        if (n < 10)
18        {
19            System.out.println(n);
20        }
21        else
22        {
23            writeVertical(n/10);
24            System.out.println(n%10);
25        }
26    }
27 }
```

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## A Recursive **void** Method (Part 2 of 2)

Display 11.1 A Recursive void Method (continued)

```

16        System.out.println(n);
17    }
18    else //n is two or more digits long:
19    {
20        writeVertical(n/10);
21        System.out.println(n%10);
22    }
23 }
24 }
```

### SAMPLE DIALOGUE

```

writeVertical(3):
3
writeVertical(12):
1
2
writeVertical(123):
1
2
3
```

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## Tracing a Recursive Call

- Recursive methods are processed in the same way as any method call  
`writeVertical(123);`
  - When this call is executed, the argument `123` is substituted for the parameter `n`, and the body of the method is executed
  - Since `123` is not less than `10`, the `else` part is executed

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## Tracing a Recursive Call

- The else part begins with the method call:  
`writeVertical(n/10);`
- Substituting `n` equal to `123` produces:  
`writeVertical(123/10);`
- Which evaluates to  
`writeVertical(12);`
- At this point, the current method computation is placed on hold, and the recursive call `writeVertical` is executed with the parameter `12`
- When the recursive call is finished, the execution of the suspended computation will return and continue from the point above

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## Execution of `writeVertical(123)`

```

if (123 < 10)
{
    System.out.println(123);
}
else //n is two or more digits long:
{
    writeVertical(123/10);
    System.out.println(123%10);
}

```

Computation will stop here until the recursive call returns.

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## Tracing a Recursive Call

- `writeVertical(12);`
- When this call is executed, the argument `12` is substituted for the parameter `n`, and the body of the method is executed
  - Since `12` is not less than `10`, the `else` part is executed
  - The else part begins with the method call:  
`writeVertical(n/10);`
  - Substituting `n` equal to `12` produces:  
`writeVertical(12/10);`
  - Which evaluates to  
`writeVertical(1);`

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## Tracing a Recursive Call

- So this second computation of `writeVertical` is suspended, leaving two computations waiting to resume, as the computer begins to execute another recursive call
- When this recursive call is finished, the execution of the second suspended computation will return and continue from the point above

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## Execution of `writeVertical(12)`

```

if (12 < 10)
{
    System.out.println(12);
}
else // n is two or more digits long:
{
    writeVertical(12/10);
    System.out.println(12%10);
}
    
```

Computation will stop here until the recursive call returns.

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## Tracing a Recursive Call

`writeVertical(1);`

- When this call is executed, the argument `1` is substituted for the parameter `n`, and the body of the method is executed
- Since `1` is less than `10`, the `if-else` statement Boolean expression is finally true
- The output statement writes the argument `1` to the screen, and the method ends without making another recursive call
- Note that this is the stopping case

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## Execution of `writeVertical(1)`

```

if (1 < 10)
{
    System.out.println(1);
}
else // n is two or more digits long:
{
    writeVertical(1/10);
    System.out.println(1%10);
}
    
```

No recursive call this time

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## Tracing a Recursive Call

- When the call `writeVertical(1)` ends, the suspended computation that was waiting for it to end (the one that was initiated by the call `writeVertical(12)`) resumes execution where it left off
- It outputs the value `12%10`, which is `2`
- This ends the method
- Now the first suspended computation can resume execution

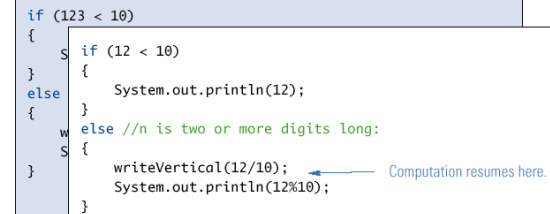
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## Completion of `writeVertical(12)`

```

if (123 < 10)
{
    S
}
else
{
    W
    S
}
    
```



```

    if (12 < 10)
    {
        System.out.println(12);
    }
    else // n is two or more digits long:
    {
        writeVertical(12/10);
        System.out.println(12%10);
    }
    
```

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## Tracing a Recursive Call

- The first suspended method was the one that was initiated by the call `writeVertical(123)`
- It resumes execution where it left off
- It outputs the value `123%10`, which is `3`
- The execution of the original method call ends
- As a result, the digits 1,2, and 3 have been written to the screen one per line, in that order

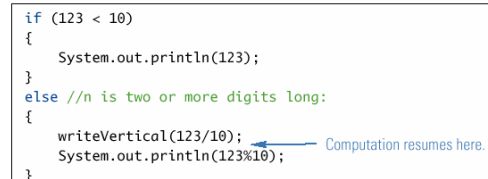
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## Completion of `writeVertical(123)`

```

if (123 < 10)
{
    System.out.println(123);
}
else // n is two or more digits long:
{
    writeVertical(123/10);
    System.out.println(123%10);
}
    
```



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## A Closer Look at Recursion

- The computer keeps track of recursive calls as follows:
  - When a method is called, the computer plugs in the arguments for the parameter(s), and starts executing the code
  - If it encounters a recursive call, it temporarily stops its computation
  - When the recursive call is completed, the computer returns to finish the outer computation

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## A Closer Look at Recursion

- When the computer encounters a recursive call, it must temporarily suspend its execution of a method
  - It does this because *it must know the result of the recursive call before it can proceed*
  - It saves all the information it needs to continue the computation later on, when it returns from the recursive call
- Ultimately, this entire process terminates when one of the recursive calls does not depend upon recursion to return

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## General Form of a Recursive Method Definition

- The general outline of a successful recursive method definition is as follows:
  - One or more cases that include one or more recursive calls to the method being defined
    - These recursive calls should solve "smaller" versions of the task performed by the method being defined
  - One or more cases that include no recursive calls: *base cases* or *stopping cases*

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## Pitfall: Infinite Recursion

- In the `writeVertical` example, the series of recursive calls eventually reached a call of the method that did not involve recursion (a stopping case)
- If, instead, every recursive call had produced another recursive call, then a call to that method would, in theory, run forever
  - This is called *infinite recursion*
  - In practice, such a method runs until the computer runs out of resources, and the program terminates abnormally

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## Pitfall: Infinite Recursion

- An alternative version of `writeVertical`
  - Note: No stopping case!

```
public static void
    newWriteVertical(int n)
{
    newWriteVertical(n/10);
    System.out.println(n%10);
}
```

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11-25

## Pitfall: Infinite Recursion

- A program with this method will compile and run
- Calling `newWriteVertical(12)` causes that execution to stop to execute the recursive call `newWriteVertical(12/10)`
  - Which is equivalent to `newWriteVertical(1)`
- Calling `newWriteVertical(1)` causes that execution to stop to execute the recursive call `newWriteVertical(1/10)`
  - Which is equivalent to `newWriteVertical(0)`

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## Pitfall: Infinite Recursion

- Calling `newWriteVertical(0)` causes that execution to stop to execute the recursive call `newWriteVertical(0/10)`
  - Which is equivalent to `newWriteVertical(0)`
  - ... And so on, forever!
- Since the definition of `newWriteVertical` has no stopping case, the process will proceed *forever* (or until the computer runs out of resources)

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## Stacks for Recursion

- To keep track of recursion (and other things), most computer systems use a *stack*
  - A stack is a very specialized kind of memory structure analogous to a stack of paper
  - As an analogy, there is also an inexhaustible supply of extra blank sheets of paper
  - Information is placed on the stack by writing on one of these sheets, and placing it on top of the stack (becoming the new top of the stack)
  - More information is placed on the stack by writing on another one of these sheets, placing it on top of the stack, and so on

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## Stacks for Recursion

- To get information out of the stack, the top paper can be read, *but only the top paper*
- To get more information, the top paper can be thrown away, and then the new top paper can be read, and so on
- Since the last sheet put on the stack is the first sheet taken off the stack, a stack is called a *last-in/first-out* memory structure (*LIFO*)

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## Stacks for Recursion

- To keep track of recursion, whenever a method is called, a new "sheet of paper" is taken
  - The method definition is copied onto this sheet, and the arguments are plugged in for the method parameters
  - The computer starts to execute the method body
  - When it encounters a recursive call, it stops the computation in order to make the recursive call
  - It writes information about the current method on the *sheet of paper*, and places it on the stack

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## Stacks for Recursion

- A new *sheet of paper* is used for the recursive call
  - The computer writes a second copy of the method, plugs in the arguments, and starts to execute its body
  - When this copy gets to a recursive call, its information is saved on the stack also, and a new *sheet of paper* is used for the new recursive call

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## Stacks for Recursion

- This process continues until some recursive call to the method completes its computation without producing any more recursive calls
  - Its *sheet of paper* is then discarded
- Then the computer goes to the top *sheet of paper* on the stack
  - This sheet contains the partially completed computation that is waiting for the recursive computation that just ended
  - Now it is possible to proceed with that suspended computation

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## Stacks for Recursion

- After the suspended computation ends, the computer discards its corresponding sheet of paper (the one on top)
- The suspended computation that is below it on the stack now becomes the computation on top of the stack
- This process continues until the computation on the bottom sheet is completed

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## Stacks for Recursion

- Depending on how many recursive calls are made, and how the method definition is written, the stack may grow and shrink in any fashion
- The stack of paper analogy has its counterpart in the computer
  - The contents of one of the *sheets of paper* is called a *stack frame* or *activation record*
  - The stack frames don't actually contain a complete copy of the method definition, but reference a single copy instead

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## Pitfall: Stack Overflow

- There is always some limit to the size of the stack
  - If there is a long chain in which a method makes a call to itself, and that call makes another recursive call, . . . , and so forth, there will be many suspended computations placed on the stack
  - If there are too many, then the stack will attempt to grow beyond its limit, resulting in an error condition known as a *stack overflow*
- A common cause of stack overflow is infinite recursion

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## Recursion Versus Iteration

- Recursion is not absolutely necessary
  - Any task that can be done using recursion can also be done in a nonrecursive manner
  - A nonrecursive version of a method is called an *iterative version*
- An iteratively written method will typically use loops of some sort in place of recursion
- A recursively written method can be simpler, but will usually run slower and use more storage than an equivalent iterative version

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## Iterative version of `writeVertical`

Display 11.2 Iterative Version of the Method in Display 11.1

```

1 public static void writeVertical(int n)
2 {
3     int nsTens = 1;
4     int leftEndPiece = n;
5     while (leftEndPiece > 9)
6     {
7         leftEndPiece = leftEndPiece/10;
8         nsTens = nsTens*10;
9     }
10    //nsTens is a power of ten that has the same number
11    //of digits as n. For example, if n is 2345, then
12    //nsTens is 1000.
13
14    for (int powerOf10 = nsTens;
15         powerOf10 > 0; powerOf10 = powerOf10/10)
16    {
17        System.out.println(n/powerOf10);
18        n = n%powerOf10;
19    }

```

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## Recursive Methods that Return a Value

- Recursion is not limited to `void` methods
- A recursive method can return a value of any type
- An outline for a successful recursive method that returns a value is as follows:
  - One or more cases in which the value returned is computed in terms of calls to the same method
  - the arguments for the recursive calls should be intuitively "smaller"
  - One or more cases in which the value returned is computed without the use of any recursive calls (the base or stopping cases)

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## Another Powers Method

- The method `pow` from the `Math` class computes powers
  - It takes two arguments of type `double` and returns a value of type `double`
- The recursive method `power` takes two arguments of type `int` and returns a value of type `int`
  - The definition of `power` is based on the following formula:  
 $x^n$  is equal to  $x^{n-1} * x$

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## Another Powers Method

- In terms of Java, the value returned by `power(x, n)` for  $n > 0$  should be the same as  
 $\text{power}(x, n-1) * x$
- When  $n=0$ , then `power(x, n)` should return `1`
  - This is the stopping case

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## The Recursive Method **power** (Part 1 of 2)

Display 11.3 The Recursive Method **power**

```

1 public class RecursionDemo2
2 {
3     public static void main(String[] args)
4     {
5         for (int n = 0; n < 4; n++)
6             System.out.println("3 to the power " + n
7                               + " is " + power(3, n));
8     }
9
10    public static int power(int x, int n)
11    {
12        if (n < 0)
13        {
14            System.out.println("Illegal argument to power.");
15            System.exit(0);
16        }
17    }

```

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## The Recursive Method **power** (Part 1 of 2)

Display 11.3 The Recursive Method **power** (continued)

```

16     if (n > 0)
17         return ( power(x, n - 1)*x );
18     else // n == 0
19         return (1);
20 }
21 }

```

### SAMPLE DIALOGUE

```

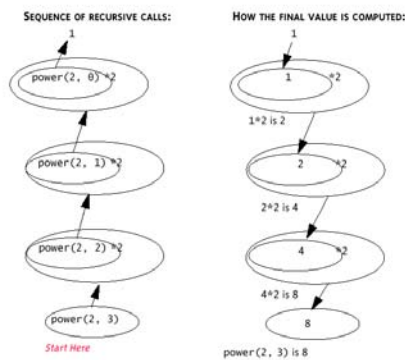
3 to the power 0 is 1
3 to the power 1 is 3
3 to the power 2 is 9
3 to the power 3 is 27

```

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## Evaluating the Recursive Method Call **power(2, 3)**

Display 11.4 Evaluating the Recursive Method Call **power(2, 3)**

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## Thinking Recursively

- If a problem lends itself to recursion, it is more important to think of it in recursive terms, rather than concentrating on the stack and the suspended computations
- power(x, n)** returns **power(x, n-1) \* x**
- In the case of methods that return a value, there are three properties that must be satisfied, as follows:

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## Thinking Recursively

1. There is no infinite recursion
  - Every chain of recursive calls must reach a stopping case
2. Each stopping case returns the correct value for that case
3. For the cases that involve recursion: *if* all recursive calls return the correct value, *then* the final value returned by the method is the correct value
- These properties follow a technique also known as *mathematical induction*

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## Tail Recursion

- When the recursive method does nothing after the recursive call except return the value then the method is called **tail recursive**
- Tail recursive methods can easily be converted into an equivalent iterative algorithm
  - Your compiler may do this automatically for greater efficiency
  - A similar effect can be achieved if the compiler re-uses the stack frame for successive recursive calls

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## Recursive Design Techniques

- The same rules can be applied to a recursive **void** method:
  1. There is no infinite recursion
  2. Each stopping case performs the correct action for that case
  3. For each of the cases that involve recursion: if all recursive calls perform their actions correctly, then the entire case performs correctly

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## Binary Search

- Binary search uses a recursive method to search an array to find a specified value
- The array must be a sorted array:
 

```
a[0] ≤ a[1] ≤ a[2] ≤ . . . ≤ a[finalIndex]
```
- If the value is found, its index is returned
- If the value is not found, -1 is returned
- Note: Each execution of the recursive method reduces the search space by about a half

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## Binary Search

- An algorithm to solve this task looks at the middle of the array or array segment first
- If the value looked for is smaller than the value in the middle of the array
  - Then the second half of the array or array segment can be ignored
  - This strategy is then applied to the first half of the array or array segment

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## Binary Search

- If the value looked for is larger than the value in the middle of the array or array segment
  - Then the first half of the array or array segment can be ignored
  - This strategy is then applied to the second half of the array or array segment
- If the value looked for is at the middle of the array or array segment, then it has been found
- If the entire array (or array segment) has been searched in this way without finding the value, then it is not in the array

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## Pseudocode for Binary Search

Display 11.5 Pseudocode for Binary Search ♦

### ALGORITHM TO SEARCH $a[first]$ THROUGH $a[last]$

```

/**
Precondition:
 $a[first] \leq a[first + 1] \leq a[first + 2] \leq \dots \leq a[last]$ 
*/

```

### TO LOCATE THE VALUE KEY:

```

if (first > last) //A stopping case
    return -1;
else
{
    mid = approximate midpoint between first and last;
    if (key == a[mid]) //A stopping case
        return mid;
    else if key < a[mid] //A case with recursion
        return the result of searching a[first] through a[mid - 1];
    else if key > a[mid] //A case with recursion
        return the result of searching a[mid + 1] through a[last];
}

```

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## Recursive Method for Binary

Display 11.6 Recursive Method for Binary Search ♦

```

1 public class BinarySearch
2 {
3     /**
4     Searches the array a for a key. If key is not in the array segment, then -1 is
5     returned. Otherwise returns an index in the segment such that key == a[index].
6     Precondition: a[first] <= a[first + 1] <= ... <= a[last]
7     */
8     public static int search(int[] a, int first, int last, int key)
9     {
10         int result = 0; //to keep the compiler happy.
11
12         if (first > last)
13             result = -1;
14         else
15         {
16             int mid = (first + last)/2;
17
18             if (key == a[mid])
19                 result = mid;
20             else if (key < a[mid])
21                 result = search(a, first, mid - 1, key);
22             else if (key > a[mid])
23                 result = search(a, mid + 1, last, key);
24         }
25         return result;
26     }
27 }

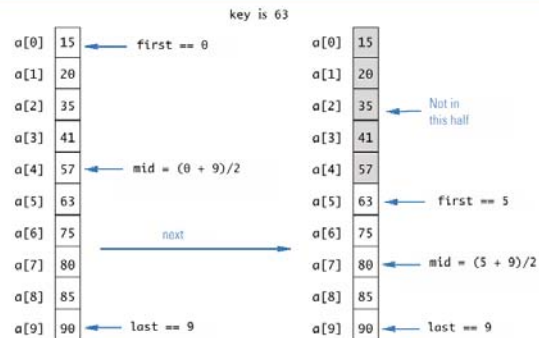
```

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## Execution of the Method **search** (Part 1 of 2)

Display 11.7 Execution of the Method **search**

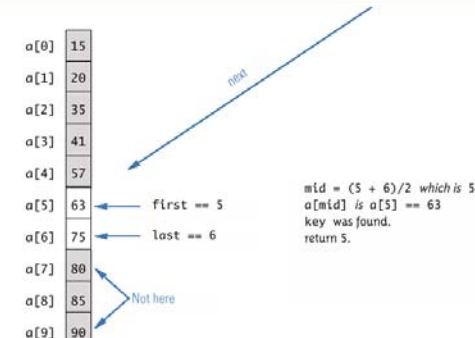


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## Execution of the Method **search** (Part 1 of 2)

Display 11.7 Execution of the Method **search** (continued)



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## Checking the **search** Method

### 1. There is no infinite recursion

- On each recursive call, the value of **first** is increased, or the value of **last** is decreased
- If the chain of recursive calls does not end in some other way, then eventually the method will be called with **first** larger than **last**

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## Checking the **search** Method

### 2. Each stopping case performs the correct action for that case

- If **first** > **last**, there are no array elements between **a[first]** and **a[last]**, so **key** is not in this segment of the array, and **result** is correctly set to **-1**
- If **key** == **a[mid]**, **result** is correctly set to **mid**

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## Checking the **search** Method

3. For each of the cases that involve recursion, *if* all recursive calls perform their actions correctly, *then* the entire case performs correctly
  - If **key** < **a[mid]**, then **key** must be one of the elements **a[first]** through **a[mid-1]**, or it is not in the array
  - The method should then search only those elements, which it does
  - The recursive call is correct, therefore the entire action is correct

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## Checking the **search** Method

- If **key** > **a[mid]**, then **key** must be one of the elements **a[mid+1]** through **a[last]**, or it is not in the array
- The method should then search only those elements, which it does
- The recursive call is correct, therefore the entire action is correct

The method **search** passes all three tests:

Therefore, it is a good recursive method definition

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## Efficiency of Binary Search

- The binary search algorithm is extremely fast compared to an algorithm that tries all array elements in order
  - About half the array is eliminated from consideration right at the start
  - Then a quarter of the array, then an eighth of the array, and so forth

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## Efficiency of Binary Search

- Given an array with 1,000 elements, the binary search will only need to compare about 10 array elements to the key value, as compared to an average of 500 for a serial search algorithm
- The binary search algorithm has a worst-case running time that is logarithmic:  $O(\log_2 n)$ 
  - A serial search algorithm is linear:  $O(n)$
- If desired, the recursive version of the method **search** can be converted to an iterative version that will run more efficiently

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## Iterative Version of Binary Search (Part 1 of 2)

Display 11.9 Iterative Version of Binary Search

```

1  /**
2   Searches the array a for key. If key is not in the array segment, then -1 is
3   returned. Otherwise returns an index in the segment such that key == a[index].
4   Precondition: a[lowEnd] <= a[lowEnd + 1] <= ... <= a[highEnd]
5   */
6  public static int search(int[] a, int lowEnd, int highEnd, int key)
7  {
8      int first = lowEnd;
9      int last = highEnd;
10     int mid;

11     boolean found = false; //so far
12     int result = 0; //to keep compiler happy

13     while ( (first <= last) && !(found) )
14     {
15         mid = (first + last)/2;

```

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## Iterative Version of Binary Search (Part 2 of 2)

Display 11.9 Iterative Version of Binary Search (continued)

```

16     if (key == a[mid])
17     {
18         found = true;
19         result = mid;
20     }
21     else if (key < a[mid])
22     {
23         last = mid - 1;
24     }
25     else if (key > a[mid])
26     {
27         first = mid + 1;
28     }
29 }

30 if (first > last)
31     result = -1;

32 return result;
33 }

```

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