Recurrent neural network regularization

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Abstract

We present a simple regularization technique for Recurrent Neural Networks (RNNs) with Long Short-Term Memory (LSTM) units. The technique is based on dropout and gives a large reduction in overfitting. We show that it is useful in a variety of sequence modeling problems that include language modeling, speech recognition, and machine translation.

1. Introduction

RNNs are a neural sequence model that achieves state of the art performance on important tasks that include language modeling (Mikolov, 2012), speech recognition (Graves et al., 2013), and machine translation (Cho et al., 2014). It is known that successful applications of neural networks require good regularization. Unfortunately, dropout (Srivastava, 2013), the most powerful regularization method for feedforward neural networks, does not work well for RNNs. As a result, practical applications often use RNNs that are too small, as large RNNs tend to overfit. To date, existing regularization methods give relatively small improvements for RNNs (Graves, 2013). In this work, we show how to correctly apply dropout to LSTMs, and demonstrate that it successfully reduces overfitting on three different problems.

2. Related work

Dropout (Srivastava, 2013) is a recently introduced regularization method that has enjoyed a lot of success with feed-forward neural networks. While there has been a lot of work extending dropout (Wang & Manning, 2013; Wan et al., 2013), there has been relatively little research in applying dropout to RNNs. The only paper on the topic is Bayer et al. (2013) which focuses on "marginalized dropout" (from Wang & Manning (2013)) which is a noiseless deterministic approximation to conventional dropout. Bayer et al. (2013) claims that conventional dropout cannot be used with RNNs because the recurrence causes large variance which hurts learning. In this work, we show how to overcome the above problem, by applying dropout to a specific subset of the RNNs connections. As a result, we are able to greatly reduce overfitting.

There has been extensive work on RNNs for language modeling (Mikolov, 2012; Sutskever, 2013). Moreover, there have been a number of architectural variations on the RNN that are work better learning with long term dependencies (Hochreiter & Schmidhuber, 1997; Graves et al., 2009; Cho et al., 2014; Jaeger et al., 2007; Koutník et al., 2014). In this work, we show how to correctly apply dropout to the LSTM, which is the most commonly-used RNN variant, although it is likely that this application of dropout extends to other RNNs.

In this paper, we consider the following RNN tasks: language modeling, speech recognition, and machine translation. Language modeling is the first task where RNNs achieved substantial success (Mikolov et al., 2010; 2011; Pascanu et al., 2013). RNNs have also been successfully used for speech recognition (Robinson et al., 1996; Graves et al., 2013) and have recently been applied to machine translation, where they are typically used for language modeling, re-ranking, or phrase modeling (Cho et al., 2014; Chow et al., 1987; Mikolov et al., 2013).

3. Regularizing RNN with LSTM cells

In this section we describe the deep LSTM 3.1. Next, we show how to regularize them 3.2, and we provide an intuition for why our regularization scheme works.

We use subscript to denote a timestep and superscript to denote a layer number. All our states are n-dimensional.

Let $h_k^l \in \mathbb{R}^n$ be a hidden state in layer l in step k. Moreover, let $T_{n,m} : \mathbb{R}^n \to \mathbb{R}^m$ be a linear transform and with a bias ($Wx + b$ for some W and b). Let $\odot$ be a element-wise multiplication and let h_k^0 be an input word vector. We use the activations h_k^L to predict y_k, since L is the number of layers in our deep LSTM.

3.1. Long-short term memory units

The RNNs dynamics can be described in terms of deterministic transitions from previous hidden states to the hidden states in the next step. In all following equations, lower index t denotes time indexing, while upper index l represents stacked layers indexing. The transition is a function

$$\text{RNN} : h_t^{l-1}, h_{t-1}^l \to h_t^l$$

For classical RNNs, this function is given by

$$h_t^l = f(T_{n,n} h_t^{l-1} + T_{n,n} h_{t-1}^l), \text{ where } f \in \{\text{sigm}, \tanh\}$$

The LSTM has relatively complicated dynamics that make it easy to "memorize" information for extended number of time steps. The "long term" memory is stored in a vector of *memory cells* $c_k^l \in \mathbb{R}^n$. Although there are many LSTM architectures that differ in their connectivity sturcutre and activation functions, all LSTM architectures have explicit memory cells that make it easy to store information for extended periods of time. The LSTM can decide to overwrite this information, retrieve it, or keep it for the next time step. The LSTM architecture used in our experiments is given by the following equations (Graves et al., 2013):

$$\text{LSTM} : h_t^{l-1}, h_{t-1}^l, c_{t-1}^l \to h_t^l, c_t^l$$

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \text{sigm} \\ \text{sigm} \\ \text{sigm} \\ \tanh \end{pmatrix} T_{2n,4n} \begin{pmatrix} h_t^{l-1} \\ h_{t-1}^l \end{pmatrix}$$

$$c_t^l = f \odot c_{t-1}^l + i \odot g$$

$$h_t^l = o \odot \tanh(c_t^l)$$

In these equations, sigm and tanh are applied element-wise. Diagram 1 illustrates the LSTM equations.

3.2. Regularization with Dropout

The main contribution of this paper is a demonstration that correctly-used can dropout greatly reduce overfitting in LSTMs. To be effective, dropout must be placed on the non-recurrent connections 2. The following equation describes it more precisely, where $\mathbf{D}$ is the dropout operator that sets a random subset of its argument to zero:

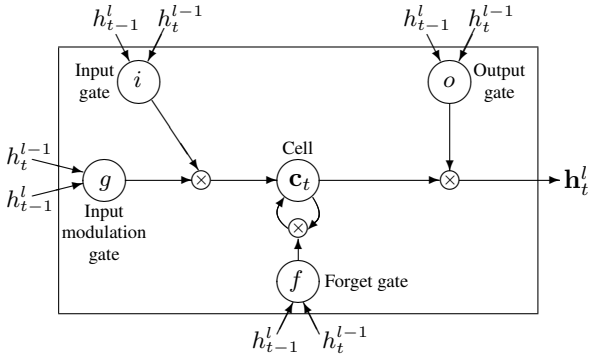

Figure 1. Graphical representation of LSTM memory cells used in this paper (there are minor differences in compare to (Graves, 2013)).

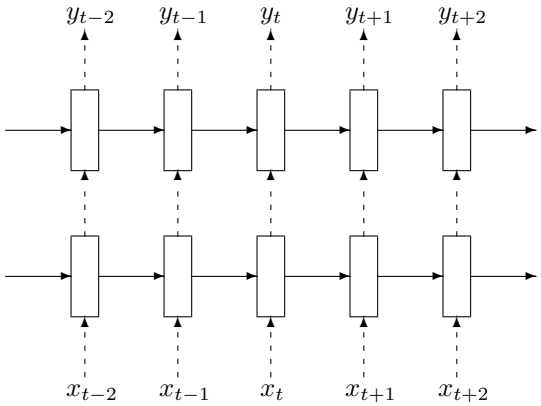

Figure 2. Regularized multilayer RNN. Dashed arrows indicate connections with applied dropout, while solid lines indicate connections where dropout is not applied.

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \text{sigm} \\ \text{sigm} \\ \text{sigm} \\ \tanh \end{pmatrix} T_{2n,4n} \begin{pmatrix} \mathbf{D}(h_t^{l-1}) \\ h_{t-1}^l \end{pmatrix}$$

$$c_t^l = f \odot c_{t-1}^l + i \odot g$$

$$h_t^l = o \odot \tanh(c_t^l)$$

We implement dropout for LSTMs as follows. The dropout operator corrupts the information carried by the units, which forces them to perform their intermediate computations more robustly. At the same time, we do not want to erase all the information. We would especially like the

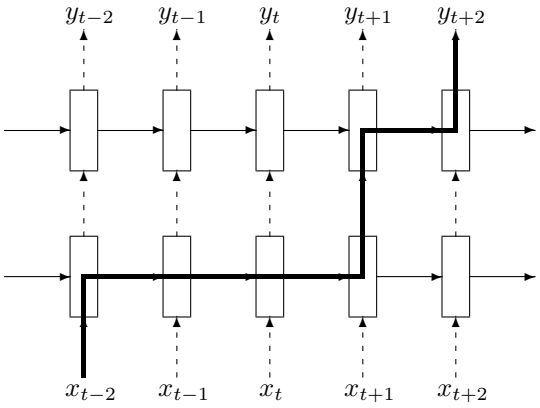

Figure 3. Thick lines show a how information flows in the LSTM. The information is affected by dropout $L + 1$ times, where L is depth of network.

Model	Validation set	Test set
A single model		
Pascanu et al. (2013)		107.5
Cheng et al.		100.0
non-regularized LSTM	120.7	114.5
Medium regularized LSTM	86.2	82.7
Large regularized LSTM	82.2	**78.4**
Model averaging		
Mikolov (2012)	83.5	89.4
Cheng et al.		80.6
2 non-regularized LSTMs	100.4	96.1
5 non-regularized LSTMs	87.9	84.1
10 non-regularized LSTMs	83.5	80.0
2 medium regularized LSTMs	80.6	77.0
5 medium regularized LSTMs	76.7	73.3
10 medium regularized LSTMs	75.2	72.0
2 large regularized LSTMs	76.9	73.6
10 large regularized LSTMs	72.8	69.5
38 large regularized LSTMs	71.9	**68.7**
Model averaging with dynamic RNNs		
Mikolov & Zweig (2012)		72.9

Table 1. Word-level perplexity on Penn-tree-bank dataset.

units to remember events that occurred many timeseps in the past. Figure 3 shows how information could flow from an event that occurred at x_{t-2} to the prediction in timestep $t+2$ in our implementation of dropout. We can see that the information is corrupted by the dropout operator exactly $L+1$ times, and this number is independent of the number of timesteps traversed by the information. A naive application of dropout would perturb the recurrent connections or the recurrent hidden state, which would make it difficult LSTM's to store information for many timesteps. By not using dropout on the recurrent connections, the LSTM is able to get most of the benefit of dropout without sacrifising its valuable ability to learn and store information for long periods of time.

4. Experiments

We present here results in there domains: language modeling 4.1, speech recognition 4.2, and machine translation 4.3.

4.1. Language modeling

We have conducted word-level prediction experiments on Penn tree bank (PTB) dataset (Marcus et al., 1993). This dataset consists of 929k training words, 73k validation words, and 82k test words. It has 10k words in vocabulary. We have trained regularized LSTMs of two sizes; we denote them the medium LSTM and the large LSTM. Both LSTMs have two layers, and are unrolled for 35 steps. We initilize hidden states to zeros. We pass final hidden states after unrollment as a initilia hidden state of the next unrollment. We set mini-batch to 20.

The medium-sized LSTM has 650 units per layer and its parameters are initialized uniformly in $[-0.05, 0.05]$. As described earlier, we apply 50% dropout on the non-recurrent connections. We train the LSTM for 39 epochs with learning rate of 1, and after 6 epochs we decrease it by a factor of 1.2 in each epoch. We clip the norm of the gradients (normalized by minibatch size) at 5. Training of such network on NVIDIA K20 takes about a half a day.

The large LSTM has 1500 units per layer and its parameters are initialized uniformly in $[-0.04, 0.04]$. We apply 65% dropout on the non-recurrent connections. We train

the meaning of life is that only if an end would be of the whole supplier. widespread rules are regarded as the companies of refuses to deliver. in balance of the nation 's information and loan growth associated with the carrier thrifts are in the process of slowing the seed and commercial paper.

the meaning of life is nearly in the first several months before the government was addressing such a move as president and chief executive of the nation past from a national commitment to curb grounds. meanwhile the government invests overcapacity that criticism and in the outer reversal of small-town america.

Figure 4. Some interesting samples drawn from large regularized model conditioned on "The meaning of life is". We have removed "unk", "N", "$" from possible outcomes.

the model for 55 epochs with learning rate of 1; we start decreasing the learning rate by a factor of 1.15 in each epoch after 14 epochs. We clip the norm of the gradients (normalized by minibatch size) at 10. Training of such network on NVIDIA K20 takes a day.

Moreover, for a comparison we have trained a non-regularized network. We optimized parameters to get the best validation performance. Lack of regularization puts constrains on size of the network, and we had to considered quite small network as a big one overfits. Our best performing non-regularized model has 200 units per layer, and two layers. Weights are initialized uniformaly in $[-0.1, 0.1]$. We train it for 4 epochs with learning rate 1, and then we descrese learning rate by 2 in each epoch until 13 epoch. Size of minibatch for this network is 20, and we unroll it for 20 steps. Training of such network on NVIDIA K20 takes 2-3 hours.

Table 1 compares previous results with our LSTMs, and figure 4 shows samples draw from a single large size regularized model.

4.2. Speech recognition

Deep Neural Networks have been used for acoustic modeling for more than half a century (the reader is encouraged to read Bourlard & Morgan (1993) for a good review). Acoustic modeling is a key component in mapping acoustic signals to sequences of words, as it models $p(s_t|X)$ where s_t is the phonetic state at time t, and X the acoustic observation. Recent work has shown that LSTMs are very capable of excellent acoustic modeling (Sak et al., 2014), and that relatively small LSTMs (in terms of their number of parameters) can overfit easily. A useful metric for measuring acoustic models is frame accuracy, which is measured on each s_t prediction for all timesteps t. Generally, this metric correlates with the actual metric of interest, the Word Error Rate (WER). However, since computing WER involves using a language model and tuning the decoding parameters for every change in the acoustic model, we decided to report frame accuracy in these experiments. Table 2 clearly shows that dropout improves the frame accuracy of the LSTM. Not surprisingly, the training frame accuracy drops due to the noise added during training, but as is often the case with dropout, this yields models that generalize better to unseen data. Note that the testing set is easier than the training set, given its higher accuracy. We report the performance of an LSTM on an internal Google Icelandic Speech dataset, which is relatively small (93k utterances), so overfitting is a greater concern.

4.3. Machine translation

We report the performance of the LSTM on a machine translation task. We formulate the translation task as a language modelling task, where the LSTM is trained to assign high probability to the correct translation given a source sentence. Thus, the LSTM is trained on sequences of the form `(source sentence, target sentence)` (**?**Cho et al., 2014). We compute the translations using a simple beam search with a beam of size 12 that finds the most likely sequence of words given the input sequence of words. We ran this experiment on the WMT'14 English to French dataset, on the "selected" subset from Schwenk (2014) which has 340M French words and 304M English words. Our LSTM has 4 hidden layers, where both the layers and the word embeddings are 1000-dimensional, and where the English vocabulary has 160,000 words and the French vocabulary has 80,000 words. We found the optimal dropout probability to be 0.2. Table 3 shows the comparative performance of both LSTMs. While this particular LSTM does not beat a standard SMT system (Schwenk et al., 2011), the result clearly shows that dropout improves the translation performance of the LSTM.

Model	Training set	Validation set
Non-regularized LSTM	71.6	68.9
Regularized LSTM	69.4	**70.5**

Table 2. Frame-level accuracy on Icelandic Speech Dataset. Training data contains 93k utterances.

Model	Test perplexity	Test BELU score
Non-regularized LSTM	5.8	25.9
Regularized LSTM	5.0	29.03
LIUM system		33.30

Table 3. Results on the English to French translation task.

5. Discussion

We presented a simple application of dropout to LSTMs that resulted in large performance boosts on many separate domains. Our results make dropout useful for RNNs, and our results suggest that this type of dropout could improve performance on a wide variety of applications.

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