

Macro-Backbone

**Monetary Policy and Exchange Rate
Volatility in a Small Open Economy**

Paper Results Summary

Benchmark Results : optimal monetary policy in close economy

- Optimal Monetary Policy : the one that replicates the flexible price equilibrium allocation Rotemberg and Woodford (1999)
 - Intuition : 在完全彈性價格（無黏著）下，企業每期都選擇效率加成、市場出清、沒有價格分散。
 - 補貼 τ 消除了長期的壟斷加成扭曲；當央行讓 $\tilde{m}c_t = 0$ (產出缺口與實質邊際成本，以對數偏離計)黏著的限制變成「不痛不癢」：沒有人有改價誘因，結果與「大家每期都能改價」的有效率配置等價。

Paper Results Summary

Benchmark Results : Similar results with other open economy Literature

- Optimal Monetary Policy : 偏離 $\tilde{m}c_t = 0$ ，因為多了改善貿易條件（terms of trade）的誘因
 - 貿易條件(**TOT**)：常指出口價格／進口價格。對本國而言，**ToT** 變好代表用同樣的出口能換到更多進口，等同於進口相對變便宜，對本國消費者是好事。
 - 有價格黏著（Calvo/黏性價格）時，名目匯率與總需求的變動會短期改動進口與出口的相對價格（視定價貨幣與定價假設而定），因此央行能藉由利率/匯率反應，影響 ToT。
 - 貨幣當局可以用通膨與匯率在短期內模仿關稅/補貼的效果，把部分福利由外國「搬」到本國（典型的**beggar-thy-neighbor**誘因）

Paper Results Summary

Results of this paper

- Optimal Monetary Policy : Special Case
 - **Parameter settings** : $\sigma = \eta = \gamma = 1$
 - Optimal Allocation by Social planner :

- Maximize : $U_N(C_t, N_t)$

- Subject to $Y_t = A_t N_t$ $C_t = \vartheta_i C_t^i Q_{i,t}^{\frac{1}{\sigma}}$

$$Y_t = \left(\frac{P_{H,t}}{P_t}\right)^{-\eta} C_t \left[(1 - \alpha) + \alpha \int_0^1 (S_t^i S_{i,t})^{\gamma - \eta} Q_{i,t}^{\eta - \frac{1}{\sigma}} di \right]$$

Paper Results Summary

Results of this paper

- Optimal Monetary Policy : Special Case
 - **Optimal Allocation must satisfies :**
 - $$-\frac{U_N(C_t, N_t)}{U_C(C_t, N_t)} = (1 - \alpha) \frac{C_t}{N_t}$$
 - $$1 - \frac{1}{\epsilon} = (1 - \tau) \bar{N}_t^{1+\varphi}$$
 - **In the closed economy case, the optimal monetary policy requires stabilizing the output gap**
 - **Setting τ such that $(1 - \tau)(1 - \alpha) = 1 - \frac{1}{\epsilon}$**

Paper Results Summary

Results of this paper

- Optimal Monetary Policy : General Case (Under Domestic Inflation Targeting D.I.T)
 - $x_t = \pi_{H,t} = 0$ (by D.I.T) $\implies y_t = \bar{y}_t$ and $r_t = \bar{r}$
 - Central Bank should not follow $r_t = \bar{r}$ blindly (Multi-equilibria and fluctuations)
 - Suppose Central bank follows :
 - $r_t = \bar{r} + \phi_\pi \pi_{H,t} + \phi_x x_t$ and $\kappa_\alpha(\phi_\pi - 1) + (1 - \beta)\phi_x > 0 \iff \exists!$ optimal equilibrium allocation

Basic Model

Agents Problem : Households

Basic Model

Agents Problem : Households

Basic Model

Agents Problem : Firms

Basic Model

Agents Problem : Firms

Equilibrium

Agents Problem : Firms

Equilibrium

Agents Problem : Firms