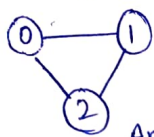


Graph Questions

(1) Find if Path exists in graph.



Given, $n=3$

edges = $[[0,1],[1,2],[0,1]]$

Answer: True

src = 0

dest = 2.

Approach:

Case I: There will be a path b/w src and dest only and only if they are in the same component.

Case II: There will be no path if src and dest are not in same component.

So, we can use any traversal (BFS or DFS) and ~~if~~ if nodes in between comes out to be destination. It shows they are in the same component. Hence there is a path b/w src and dest. Return True. otherwise False, if dest nodes is not found while traversing.

Code:

```
bool isValidPath(int n, vector<vector<int>>> edges, int srcsrc, int dest) {
```

```
    vector<int> vis(n, 0);
```

```
    if (src == dest)
```

```
        return true;
```

→ Corner case

```
    unordered_map<int, vector<int>> adj;
```

```
    for (auto &it : edges) {
```

```
        adj[it[0]].push-back(it[1]);
```

```
        adj[it[1]].push-back(it[0]);
```

```
    }
```

```
    queue<int> q;
```

```
    q.push(src);
```

```
    vis[src] = 1;
```

```
    while (!q.empty()) {
```

```
        int node = q.front();
```

```
        q.pop();
```

```
        for (auto &it : adj[node]) {
```

```
            if (it == dest)
```

```
                return true;
```

```
            if (vis[it] == 0) {
```

```
                vis[it] = 1;
```

```
                q.push(it);
```

```
            }
```

```
        } } return false; }
```

→ Convert adjacency matrix to adjacency list by using unordered map.

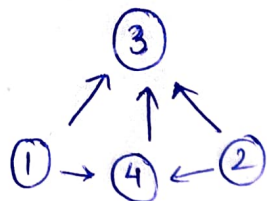
→ simple BFS traversal with simple condition

→ It returns if there is a path or not

(2) find the Town Judge

Given, $n=4$

trust = $[[1, 3], [4, 3], [2, 3], [1, 4], [2, 4]]$



Output = 3

Approach: To be a Town Judge, There are 2 conditions:

- (i) Town Judge doesn't trust any body/node.
- (ii) All other nodes trust Town Judge.

Intuition is that $1 \rightarrow 3$ which denotes 1 trusts 3 and 1 goes to 3, where ~~in~~_{out} degree of 1 increases by 1 and indegree of 3 increase by 1.

To be a Town Judge,

Indegree = $n-1$ and

outdegree = 0.

We can achieve by just traversing the adjacency matrix and maintain 2 vectors indeg and outdeg increase indegree and outdegree as the edges comes out.

Code:

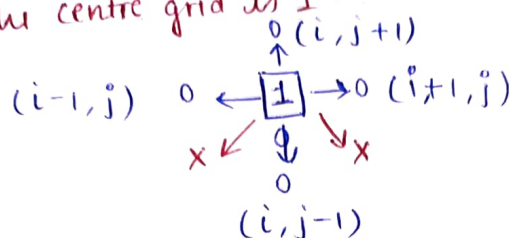
```
int findJudge (int n, vector<vector<int>> & trust) {  
    vector<int> in(n+1, 0), out(n+1, 0);  
    for (auto &it : trust) {  
        inout [it[0]]++;  
        in[it[1]]++;  
    }  
    for (i = 1; i <= n; i++) {  
        if (in[i] == n-1 && out[i] == 0)  
            return i;  
    }  
    return -1;  
}
```

(3) Number of Islands

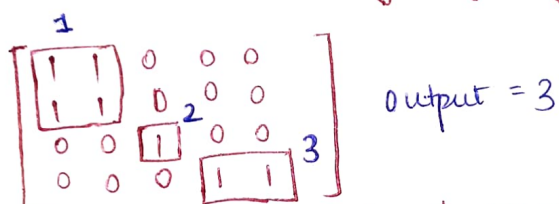
Given, grid = $\begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 \end{bmatrix}$

output = 3

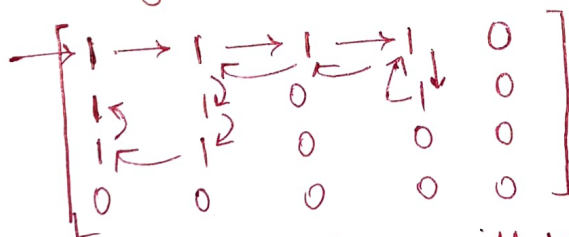
Explanation: Area is said to be island only and only if left, right, up and downward grid is 0, and the centre grid is 1.



{ we are not considering diagonally }

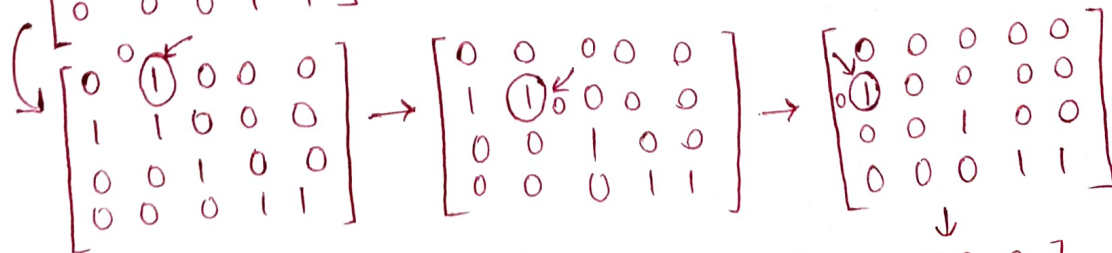


Approach: We have to make the land as water (1 → 0) after traversing it and after adding it to our island.

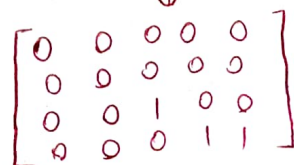


Starting from $[0,0]$, we will traverse it by DFS and all the connected 1's will be called and the output is 1 here.

DFS (1) →



Now, count of island will increase by 1, ans = 1



Now
DFS(2) →

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 \end{bmatrix} \rightarrow \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 \end{bmatrix}$$

This won't be consider as this diagonal grid
{ ans ++ }
{ ans = 2 }

DFS(3) →

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ - & - & - & - & - \\ - & - & - & - & - \\ - & - & - & - & - \\ 0 & 0 & 0 & 1 & 1 \end{bmatrix} \rightarrow \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ - & - & - & - & - \\ - & - & - & - & - \\ - & - & - & - & - \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix} \rightarrow \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ - & - & - & - & - \\ - & - & - & - & - \\ - & - & - & - & - \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

ans ++
{ ans = 3 }

```
bool isValid(int i, j, n, m, grid) {
    if (i >= 0 && i < n && j >= 0 && j < m, grid[i][j] == '1')
        return true;
    return false;
}
```

```
void dfs(i, j, n, m, grid) {
    grid[i][j] = '0';
    if (isValid(i, j+1, n, m, grid))
        dfs(i, j+1, n, m, grid);
    if (isValid(i+1, j, n, m, grid))
        dfs(i+1, j, n, m, grid);
    if (isValid(i, j-1, n, m, grid))
        dfs(i, j-1, n, m, grid);
    if (isValid(i-1, j, n, m, grid))
        dfs(i-1, j, n, m, grid);
}
```

```
int numberOfIslands(grid) {
    int n, m;
    int ans;
    for (i = 0; i < n; i++)
        for (j = 0; j < m; j++)
            if (grid[i][j] == '1') {
                ans++;
                dfs(i, j, n, m, grid);
            }
    return ans;
}
```