

# Lecture 6 – Programming Paradigms

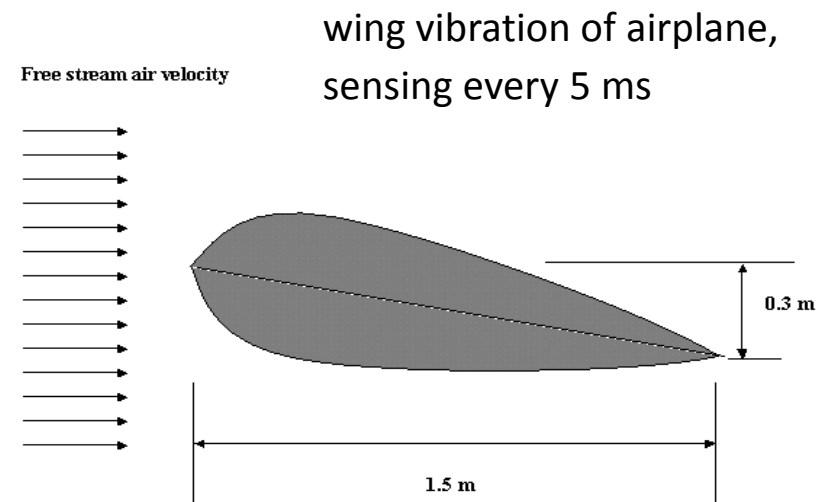
## CSE 456: Embedded Systems



# Timing Guarantees

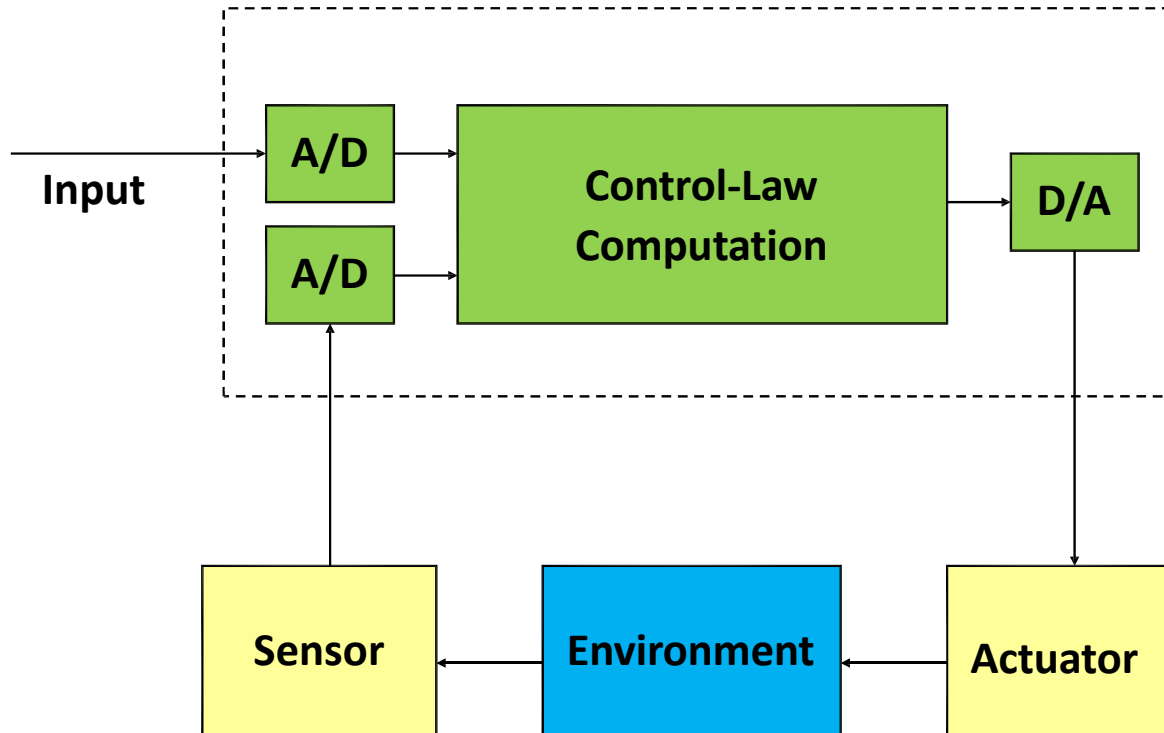
- *Hard real-time systems* can be often found in *safety-critical applications*. They need to provide the result of a computation within a fixed time bound.
- *Typical application domains*:
  - avionics, automotive, train systems, automatic control including robotics, manufacturing, media content production

sideairbag in car,  
reaction after event in <10  
mSec



# Simple Real-Time Control System

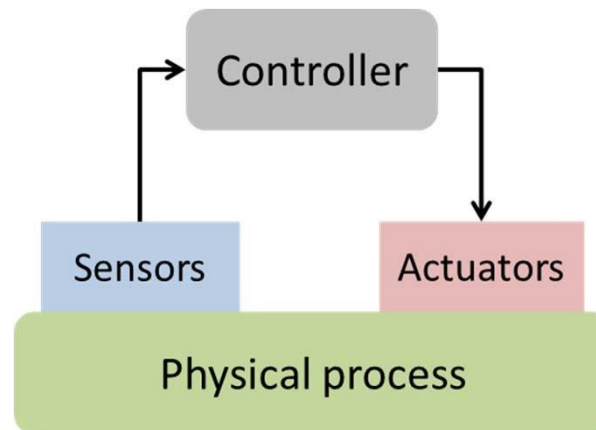
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# Real-Time Systems

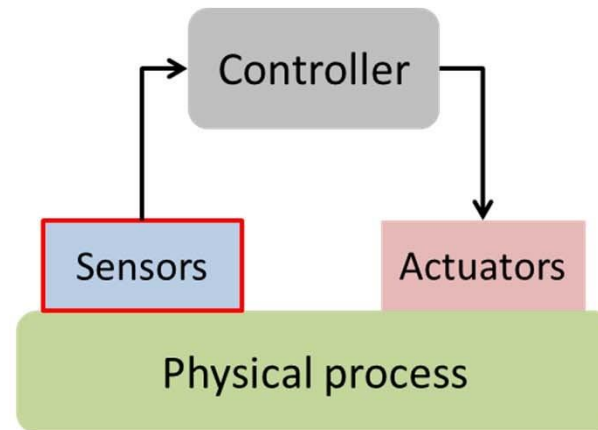
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In many *cyber-physical systems (CPSs)*, correct timing is a matter of *correctness*, not performance: *an answer arriving too late is consider to be an error.*



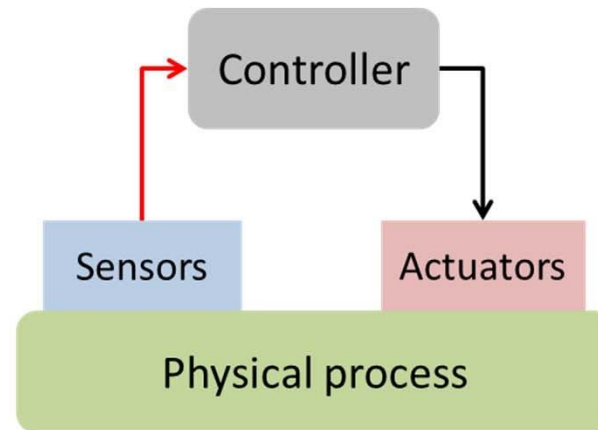
# Real-Time Systems

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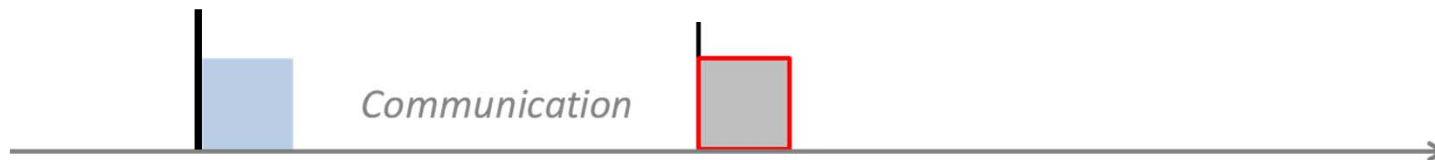
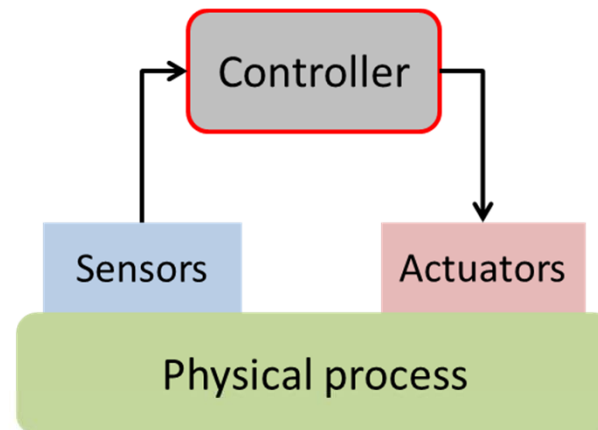
# Real-Time Systems

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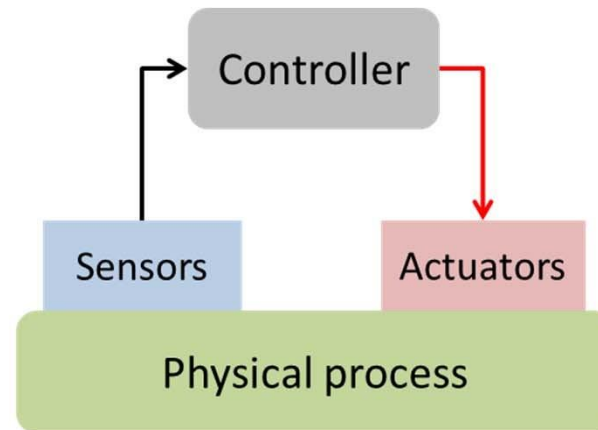
# Real-Time Systems

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# Real-Time Systems

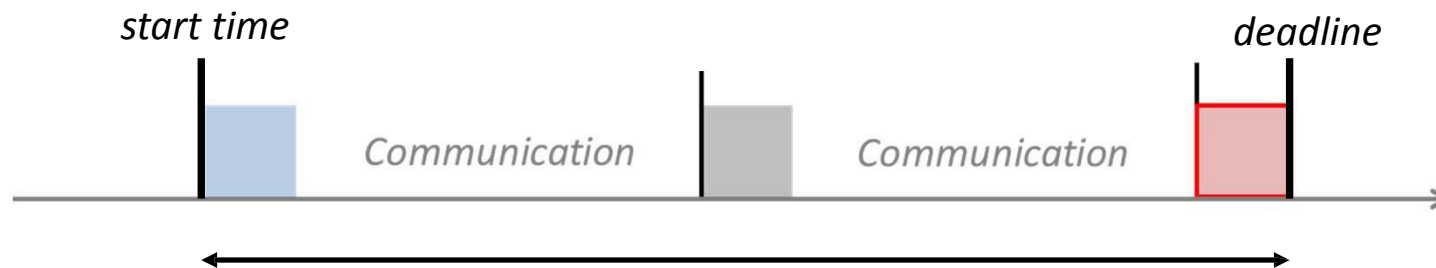
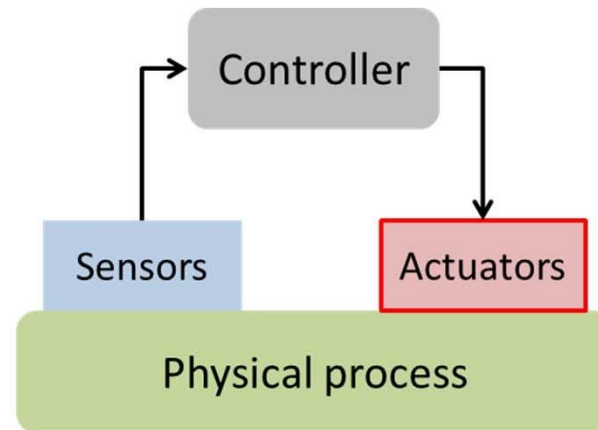
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# Real-Time Systems

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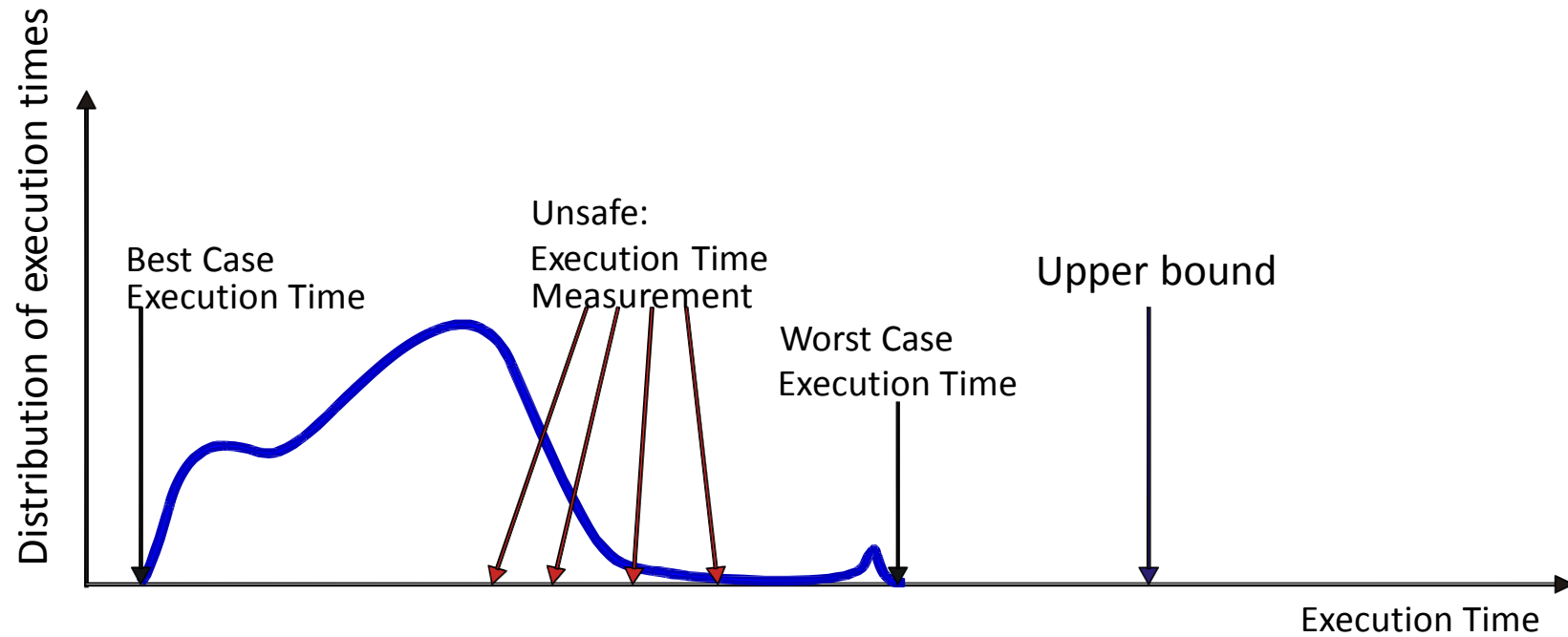
# Real-Time Systems

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- *Embedded controllers* are often expected to *finish the processing* of data and events reliably *within defined time bounds*. Such a processing may involve sequences of computations and communications.
- Essential for the analysis and design of a real-time system: *Upper bounds on the execution times* of all tasks are statically known. This also includes the communication of information via a wired or wireless connection.
  - This value is commonly called the *Worst-Case Execution Time* (WCET).
  - Analogously, one can define the lower bound on the execution time, the *Best-Case Execution Time* (BCET).

# Distribution of Execution Times

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# Modern Hardware Features

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- Modern processors *increase the average performance* (execution of tasks) by using *caches, pipelines, branch prediction*, and *speculation* techniques, for example.
- *These features make the computation of the WCET very difficult*: The execution times of single instructions vary widely.
- The microarchitecture has a large *time-varying internal state* that is changed by the execution of instructions and that influences the execution times of instructions.
  - *Best case* - everything goes smoothly: no cache miss, operands ready, needed resources free, branch correctly predicted.
  - *Worst case* - everything goes wrong: all loads miss the cache, resources needed are occupied, operands are not ready.
  - *The span between the best case and worst case may be several hundred cycles.*

# (Most of) Industry's Best Practice

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- **Measurements:** determine execution times directly by observing the execution or a simulation on a set of inputs.
  - *Does not guarantee an upper bound* to all executions unless the reaction to all initial system states and all possible inputs is measured.
  - *Exhaustive execution* in general not possible: Too large space of (input domain)  $\times$  (set of initial execution states).
- **Simulation** suffers from the same restrictions.
- **Compute upper bounds** along the structure of the program:
  - Programs are *hierarchically* structured: Instructions are “nested” inside statements.
  - Therefore, one may compute the upper execution time bound for a statement from the upper bounds of its constituents, for example of single instructions.
  - *But:* The execution times of individual instructions varies largely!

# Determine the WCET

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## *Complexity of determining the WCET of tasks:*

- In the general case, it is even *undecidable* whether a finite bound exists.
- For *restricted classes of programs* it is possible, in principle. Computing accurate bounds is *simple for "old" architectures*, but very *complex for new architectures* with pipelines, caches, interrupts, and virtual memory, for example.

## *Analytic (formal) approaches* exist for hardware and software.

- In case of software, it requires the *analysis of the program flow* and the *analysis of the hardware* (microarchitecture). Both are combined in a complex analysis flow.
- *For the rest of the lecture, we assume that reliable bounds on the WCET are available*, for example by means of exhaustive measurements or simulations, or by analytic formal analysis.

# Different Programming Paradigms

# Why Multiple Tasks on one Embedded Device?

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- The concept of *concurrent tasks* reflects our intuition about the *functionality of embedded systems*.
- Tasks help us *manage the complexity of concurrent activities* as happening in the system environment:
  - *Input data* arrive from various *sensors* and input devices.
    - These input streams may have different data rates like in multimedia processing, systems with multiple sensors, automatic control of robots
  - The system may also receive *asynchronous (sporadic) input events*.
    - These input event may arrive from user interfaces, from sensors, or from communication interfaces, for example.

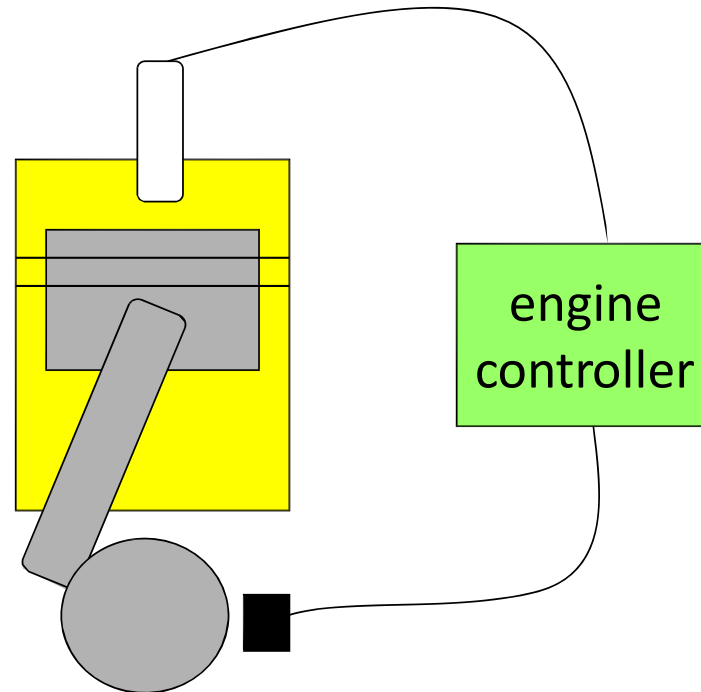


# Example: Engine Control

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## *Typical Tasks:*

- ☐ spark control
- ☐ crankshaft sensing
- ☐ fuel/air mixture
- ☐ oxygen sensor
- ☐ Kalman filter – control algorithm



# Overview

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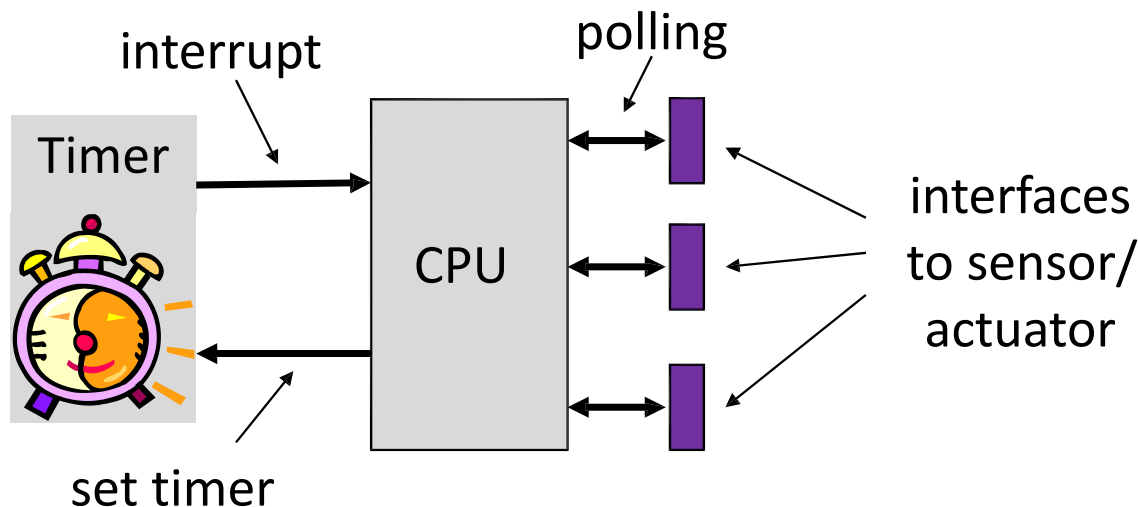
- ☐ There are many *structured ways of programming an embedded system*.
- ☐ In this lecture, only the main principles will be covered:
  - ☐ *time triggered approaches*
    - ☐ periodic
    - ☐ cyclic executive
    - ☐ generic time-triggered scheduler
  - ☐ *event triggered approaches*
    - ☐ non-preemptive
    - ☐ preemptive – stack policy
    - ☐ preemptive – cooperative scheduling
    - ☐ preemptive - multitasking

# Time-Triggered Systems

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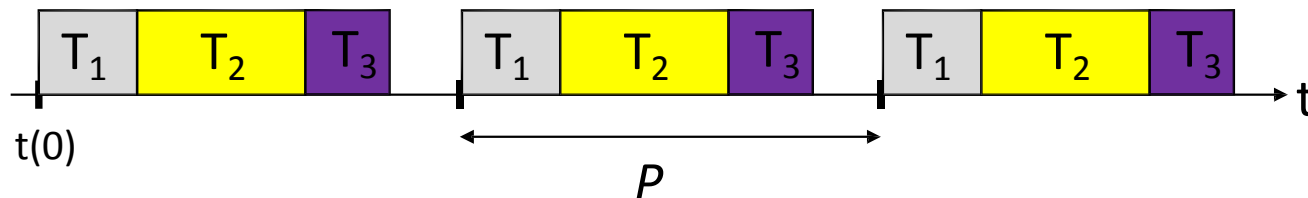
## *Pure time-triggered model:*

- ❑ *no interrupts* are allowed, except by timers
- ❑ the *schedule* of tasks is *computed off-line* and therefore, complex sophisticated algorithms can be used
- ❑ the scheduling at run-time is fixed and therefore, it is *deterministic*
- ❑ the interaction with environment happens through *polling*



# Simple Periodic TT Scheduler

- A *timer interrupts regularly* with period  $P$ .
- All tasks have *same period  $P$* .



- *Properties:*
  - later tasks, for example  $T_2$  and  $T_3$ , have unpredictable starting times
  - the communication between tasks or the use of common resources is safe, as there is a static ordering of tasks, for example  $T_2$  starts after finishing  $T_1$
  - as a necessary precondition, the sum of WCETs of all tasks within a period is bounded by the period  $P$ :

$$\sum_{(k)} WCET(T_k) < P$$

# Simple Periodic Time-Triggered Scheduler

main:

```
determine table of tasks (k, T(k)), for k=0,1,...,m-1;  
i=0; set the timer to expire at initial phase t(0);  
while (true) sleep();
```

usually done offline

set CPU to low power mode;  
processing starts again after interrupt

Timer Interrupt:

```
i=i+1;  
set the timer to expire at i*P + t(0);  
for (k=0,...,m-1){ execute task T(k); }  
return;
```

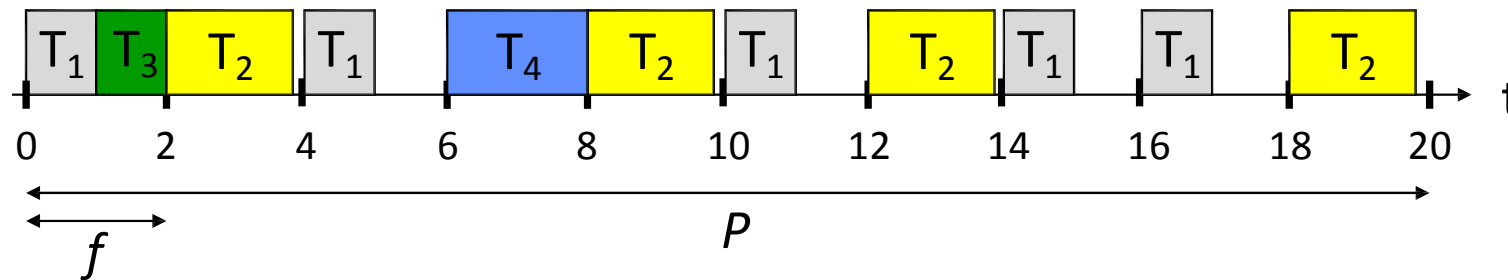
for example using a function pointer in C;  
task(= function) returns after finishing.

k	T (k)
0	T <sub>1</sub>
1	T <sub>2</sub>
2	T <sub>3</sub>
3	T <sub>4</sub>
4	T <sub>5</sub>

m=5

# Time-Triggered Cyclic Executive Scheduler

- Suppose now, that *tasks may have different periods*.
- To accommodate this situation, the *period  $P$  is partitioned into frames of length  $f$* .



- We have a *problem* to determine a feasible schedule, if there are *tasks with a long execution time*.
  - long tasks could be partitioned into a sequence of short sub-tasks
  - but this is tedious and error-prone process, as the local state of the task must be extracted and stored globally

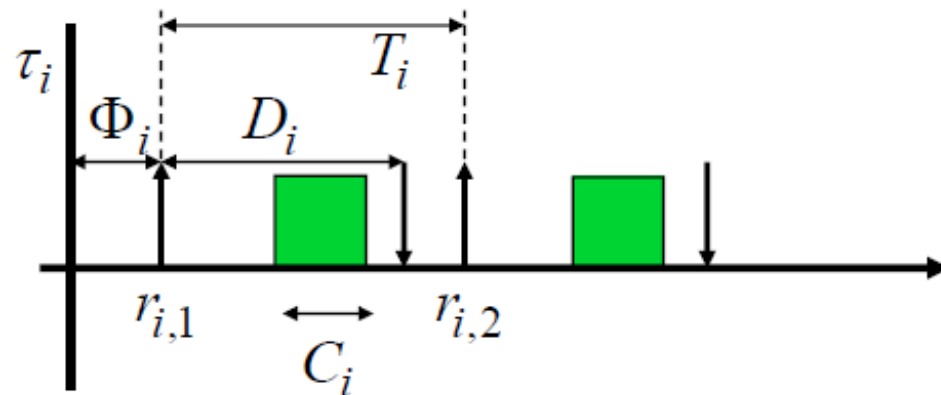
# Time-Triggered Cyclic Executive Scheduling

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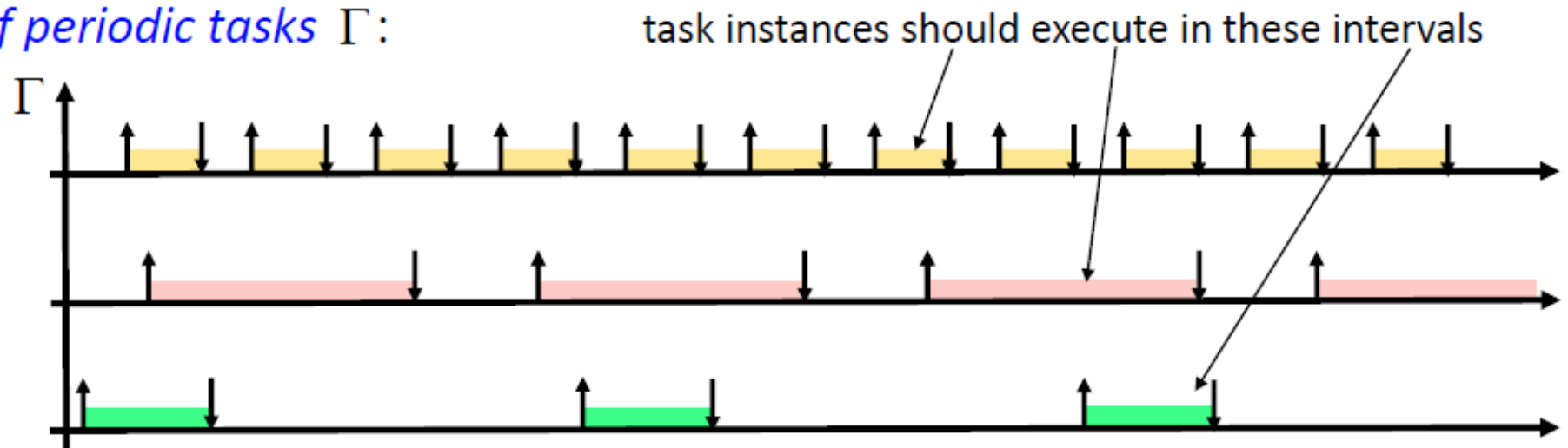
- *Examples for periodic tasks:* sensory data acquisition, control loops, action planning and system monitoring.
- When a control application consists of several concurrent periodic tasks with individual timing constraints, *the schedule has to guarantee* that each periodic instance is *regularly activated* at its proper rate and is *completed within its deadline*.
- *Definitions:*
  - $\Gamma$  : denotes the set of all periodic tasks
  - $\tau_i$  : denotes a periodic task
  - $\tau_{i,j}$  : denotes the  $j$ th instance of task  $i$
  - $r_{i,j}, d_{i,j}$  : denote the release time and absolute deadline of the  $j$ th instance of task  $i$
  - $\Phi_i$  : phase of task  $i$  (release time of its first instance)
  - $D_i$  : relative deadline of task  $i$

# Time-Triggered Cyclic Executive Scheduling

- *Example* of a single periodic task  $\tau_i$ :



- *A set of periodic tasks*  $\Gamma$ :





# Time-Triggered Cyclic Executive Scheduling

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- The following *hypotheses* are assumed on the tasks:
  - *The instances of a periodic task are regularly activated at a constant rate.* The interval  $T_i$  between two consecutive activations is called period. The release times satisfy

$$r_{i,j} = \Phi_i + (j-1)T_i$$

- *All instances have the same worst case execution time  $C_i$ .* The worst case execution time is also denoted as  $WCET(i)$ .
  - *All instances of a periodic task have the same relative deadline  $D_i$ .* Therefore, the absolute deadlines satisfy

$$d_{i,j} = \Phi_i + (j-1)T_i + D_i$$

# Time-Triggered Cyclic Executive Scheduling

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*Some conditions for period  $P$  and frame length  $f$ :*

- A task executes at most once within a frame:

$$f \leq T_i \quad \forall \text{ tasks } \tau_i$$

period of task

- $P$  is a multiple of  $f$ .

- Period  $P$  is least common multiple of all periods  $T_k$

- Tasks start and complete within a single frame:

$$f \geq C_i \quad \forall \text{ tasks } \tau_i$$

worst case execution time  
of task

- Between release time and deadline of every task there is at least one full frame:

$$2f - \gcd(T_i, f) \leq D_i \quad \forall \text{ tasks } \tau_i$$

relative deadline of task

# Time-Triggered Cyclic Executive Scheduling

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Example

$\Gamma$	$T_i$	$\Phi_i$	$D_i$	$C_i$	frame
$\tau_1$	12	2	8	2.8	2
$\tau_2$	12	3	9	3	3
$\tau_3$	4	0	4	1	1, 2, 3

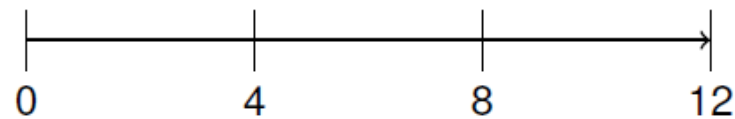
$$P = 12, f = 4$$

# Time-Triggered Cyclic Executive Scheduling

Example

$\Gamma$	$T_i$	$\Phi_i$	$D_i$	$C_i$	frame
$\tau_1$	12	2	8	2.8	2
$\tau_2$	12	3	9	3	3
$\tau_3$	4	0	4	1	1, 2, 3

$$P = 12, f = 4$$

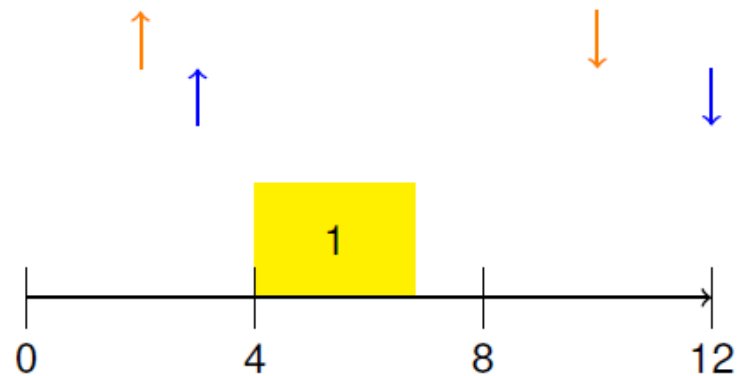


# Time-Triggered Cyclic Executive Scheduling

Example

$\Gamma$	$T_i$	$\Phi_i$	$D_i$	$C_i$	frame
$\tau_1$	12	2	8	2.8	2
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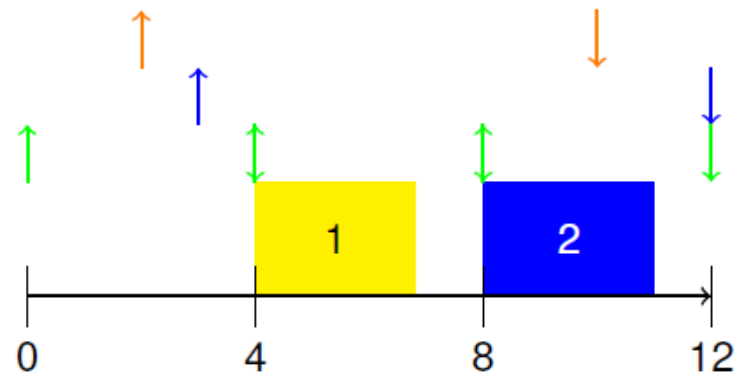


# Time-Triggered Cyclic Executive Scheduling

Example

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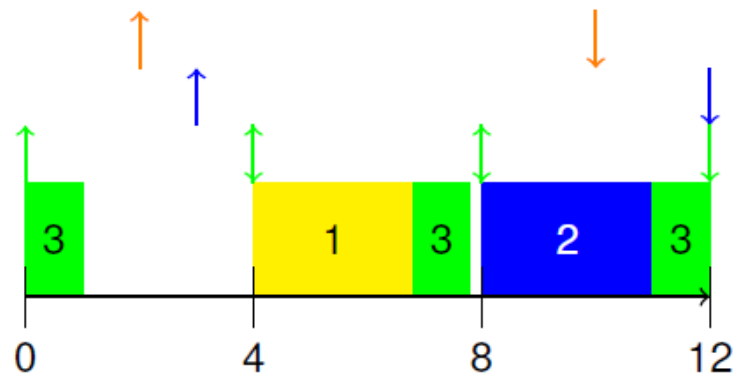


# Time-Triggered Cyclic Executive Scheduling

## Example

$\Gamma$	$T_i$	$\Phi_i$	$D_i$	$C_i$	frame
$\tau_1$	12	2	8	2.8	2
$\tau_2$	12	3	9	3	3
$\tau_3$	4	0	4	1	1, 2, 3

$$P = 12, f = 4$$



# Time-Triggered Cyclic Executive Scheduling

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*Example with 4 tasks:*

□  $\tau_1 : T_1 = 6, D_1 = 6, C_1 = 2$

$\tau_2 : T_2 = 9, D_2 = 9, C_2 = 2$

$\tau_3 : T_3 = 12, D_3 = 8, C_3 = 2$

$\tau_4 : T_4 = 18, D_4 = 10, C_4 = 4$

□  $P = 36, f = 4$



# Time-Triggered Cyclic Executive Scheduling

*Example with 4 tasks:*

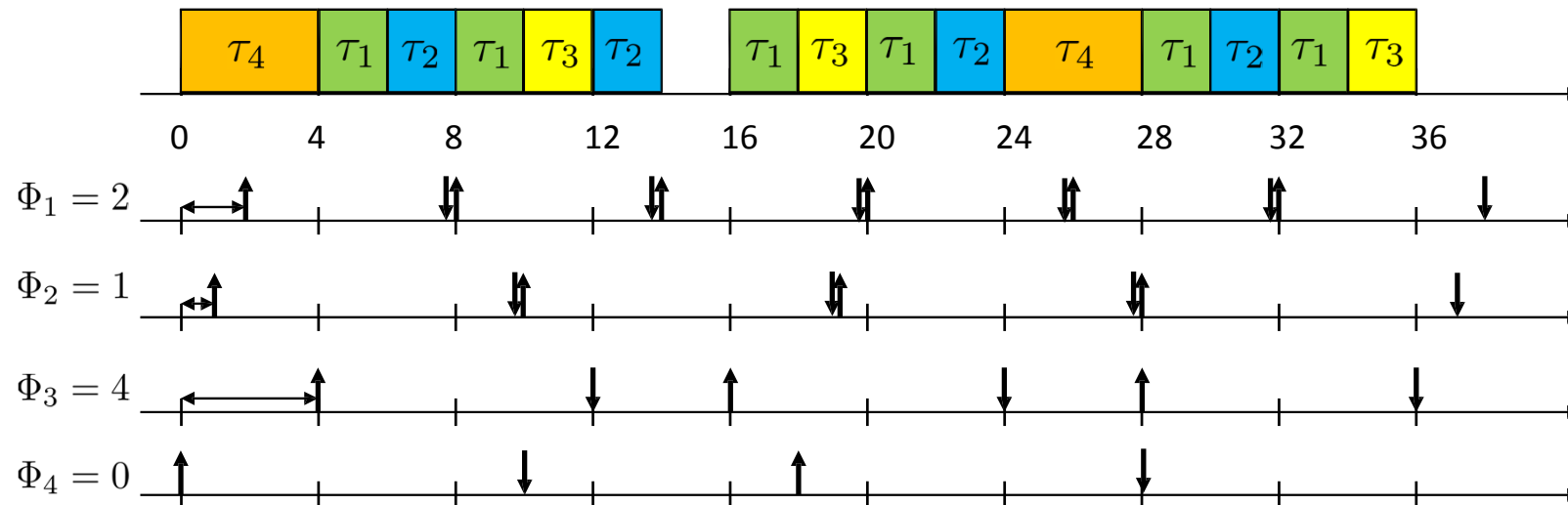
$$\tau_1 : T_1 = 6, D_1 = 6, C_1 = 2$$

$$\tau_2 : T_2 = 9, D_2 = 9, C_2 = 2$$

$$\tau_3 : T_3 = 12, D_3 = 8, C_3 = 2$$

$$\tau_4 : T_4 = 18, D_4 = 10, C_1 = 4$$

$$\square P = 36, f = 4$$



# Time-Triggered Cyclic Executive Scheduling

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## *Checking for correctness of schedule:*

- ☐  $f_{ij}$  denotes the number of the frame in which that instance  $j$  of task  $\tau_i$  executes.
- ☐ Is  $P$  a common multiple of all periods  $T_i$ ?
- ☐ Is  $P$  a multiple of  $f$ ?
- ☐ Is the frame sufficiently long?

$$\sum_{\{i \mid f_{ij}=k\}} C_i \leq f \quad \forall 1 \leq k \leq \frac{P}{f}$$

- ☐ Determine offsets such that instances of tasks start after their release time:

$$\Phi_i = \min_{1 \leq j \leq P/T_i} \{(f_{ij} - 1)f - (j - 1)T_i\} \quad \forall \text{ tasks } \tau_i$$

- ☐ Are deadlines respected?

$$(j - 1)T_i + \Phi_i + D_i \geq f_{ij}f \quad \forall \text{ tasks } \tau_i, 1 \leq j \leq P/T_i$$

## Example: Cyclic Executive Scheduling

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$\Gamma$	$T_i$	$D_i$	$C_i$
$\tau_1$	4	4	1.0
$\tau_2$	5	5	1.8
$\tau_3$	20	20	1.0
$\tau_4$	20	20	2.0

# Example: Cyclic Executive Scheduling

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## Conditions:

$$f \leq \min\{4, 5, 20\} = 4$$

$$f \geq \max\{1.0, 1.0, 1.8, 2.0\} = 2.0$$

$$2f - \gcd(T_i, f) \leq D_i \quad \forall \text{ tasks } \tau_i$$

possible solution:  $f = 2$

$\Gamma$	$T_i$	$D_i$	$C_i$
$\tau_1$	4	4	1.0
$\tau_2$	5	5	1.8
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# Example: Cyclic Executive Scheduling

## Conditions:

$$f \leq \min\{4, 5, 20\} = 4$$

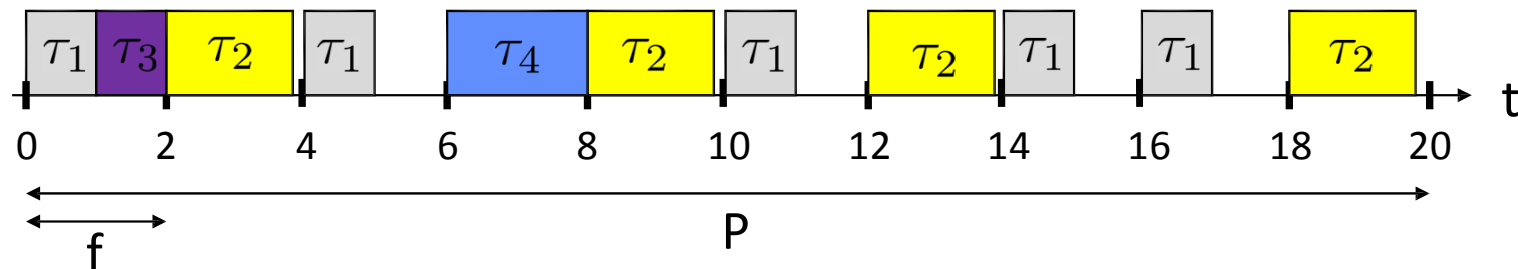
$$f \geq \max\{1.0, 1.0, 1.8, 2.0\} = 2.0$$

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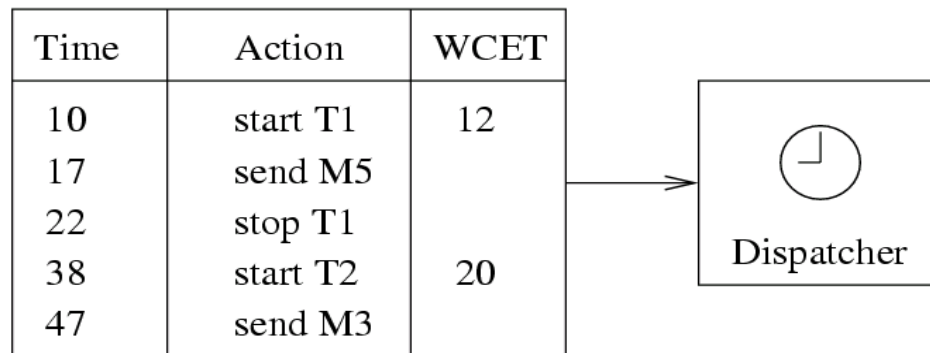
$\Gamma$	$T_i$	$D_i$	$C_i$
$\tau_1$	4	4	1.0
$\tau_2$	5	5	1.8
$\tau_3$	20	20	1.0
$\tau_4$	20	20	2.0

## Feasible solution ( $f=2$ ):



# Generic Time-Triggered Scheduler

- In an *entirely time-triggered system*, the temporal control structure of all tasks is established a priori by off-line support-tools.
- This *temporal control structure is encoded in a Task-Descriptor List (TDL)* that contains the cyclic schedule for all activities of the node.
- This *schedule* considers the required precedence and mutual exclusion relationships among the tasks such that an explicit coordination of the tasks by the operating system at run time is not necessary.
- *The dispatcher is activated by a synchronized clock tick.* It looks at the TDL, and then performs the action that has been planned for this instant [Kopetz].



# Simplified Time-Triggered Scheduler

main:

determine static schedule  $(t(k), T(k))$ , for  $k=0,1,\dots,n-1$ ;  
determine  $l$ ; period of the schedule  $P$ ;

set  $i=k=0$  initially; set the timer to expire at  $t(0)$ ;

while (true)

sleep();

Timer

Interrupt:

~~$k_{old} = i$~~   $k := i \bmod n$ ;

set the timer to expire at  $\lfloor i/n \rfloor * P +$

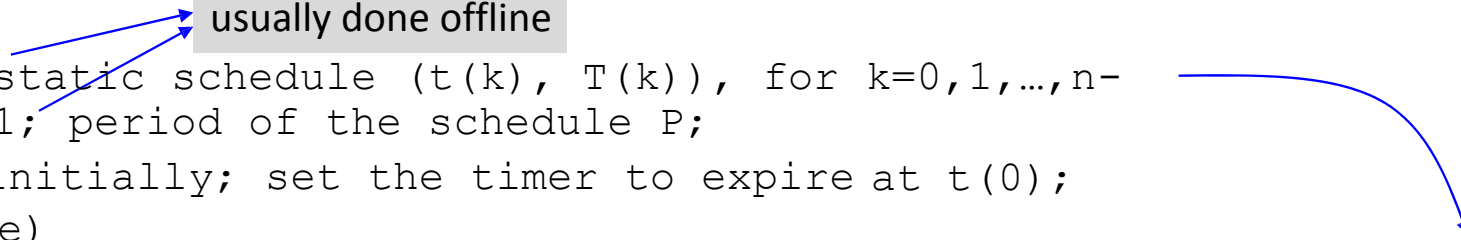
$t(k)$ ;

~~execute~~ task  $T(k_{old})$ ;

usually done offline

set CPU to low power mode;  
processing continues after interrupt

for example using a function pointer in C;  
task returns after finishing.



k	$t(k)$	$T(k)$
0	0	$T_1$
1	3	$T_2$
2	7	$T_1$
3	8	$T_3$
4	12	$T_2$

$n=5, P = 16$

# Summary Time-Triggered Scheduler

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## *Properties:*

- ☐ *deterministic schedule*; conceptually simple (static table); relatively easy to validate, test and certify
- ☐ *no problems* in using *shared resources*
- ☐ external communication only via *polling*
- ☐ *inflexible* as no adaptation to the environment
- ☐ serious *problems* if there are *long tasks*

## *Extensions:*

- ☐ *allow interrupts* → be careful with shared resources and the WCET of tasks!!
- ☐ *allow preemptable* background tasks
- ☐ *check for task overruns* (execution time longer than WCET) using a watchdog timer

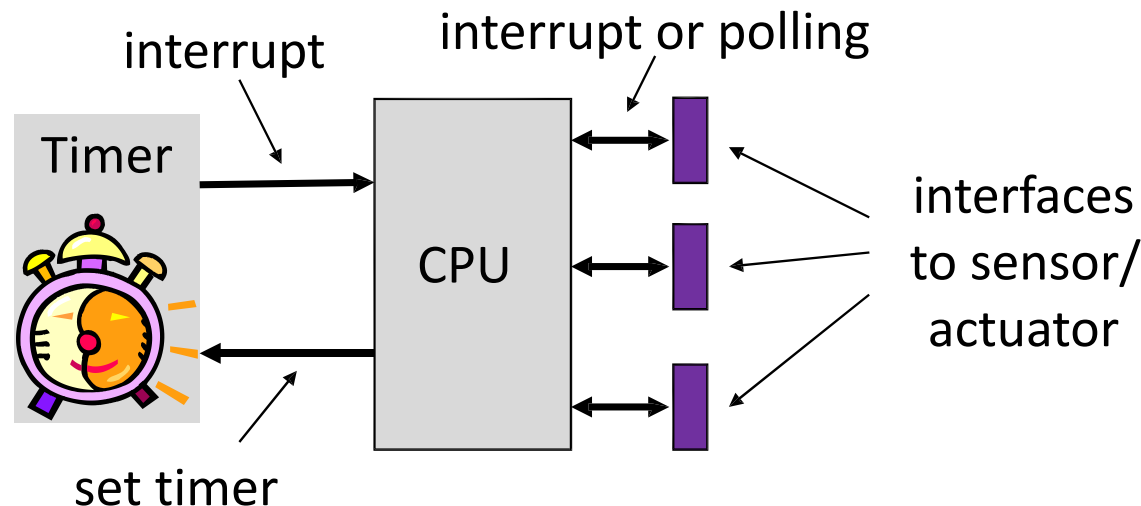


# Event Triggered Systems

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*The schedule of tasks is determined by the occurrence of external or internal events:*

- *dynamic and adaptive*: there are possible problems with respect to timing, the use of shared resources and buffer over- or underflow
- *guarantees* can be given either off-line (if bounds on the behavior of the environment are known) or during run-time



# Non-Preemptive Event-Triggered Scheduling

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## *Principle:*

- ☐ To each event, there is associated a corresponding task that will be executed.
- ☐ Events are emitted by (a) external interrupts or (b) by tasks themselves.
- ☐ All events are collected in a single queue; depending on the queuing discipline, an event is chosen for execution, i.e., the corresponding task is executed.
- ☐ Tasks can not be preempted.

## *Extensions:*

- ☐ A *background task* can run if the event queue is empty. It will be preempted by any event processing.
- ☐ *Timed events* are ready for execution only after a time interval elapsed. This enables periodic instantiations, for example.

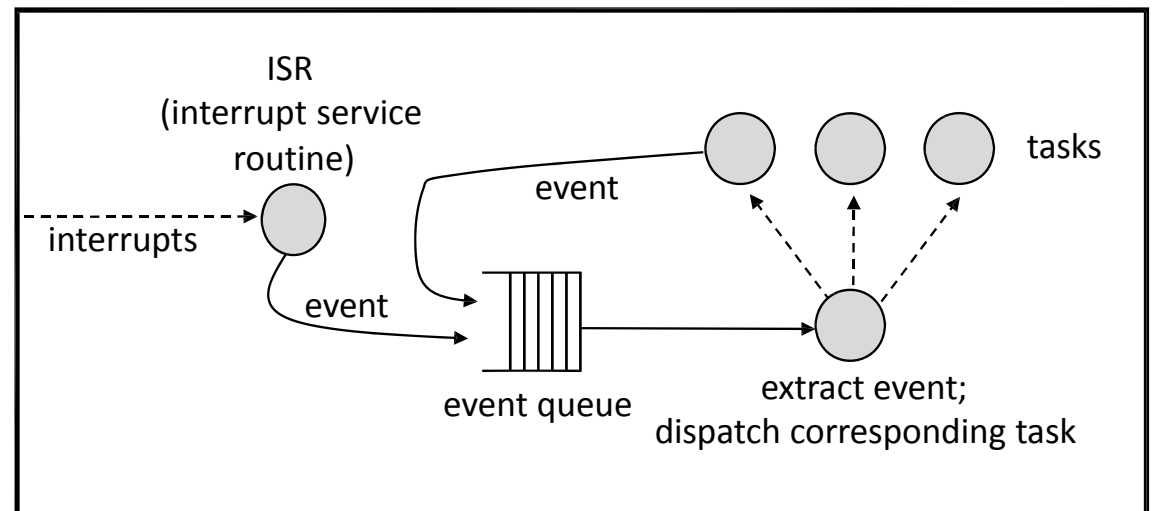
# Non-Preemptive Event-Triggered Scheduling

```
main:
  while (true) {
    if (event queue is empty) {
      sleep();
    } else {
      extract event from event queue;
      execute task corresponding to event;
    }
  }
}
```

set the CPU to low power mode;  
continue processing after interrupt

for example using a function pointer in C;  
task returns after finishing.

```
Interrupt:
  put event into event queue;
  return;
```

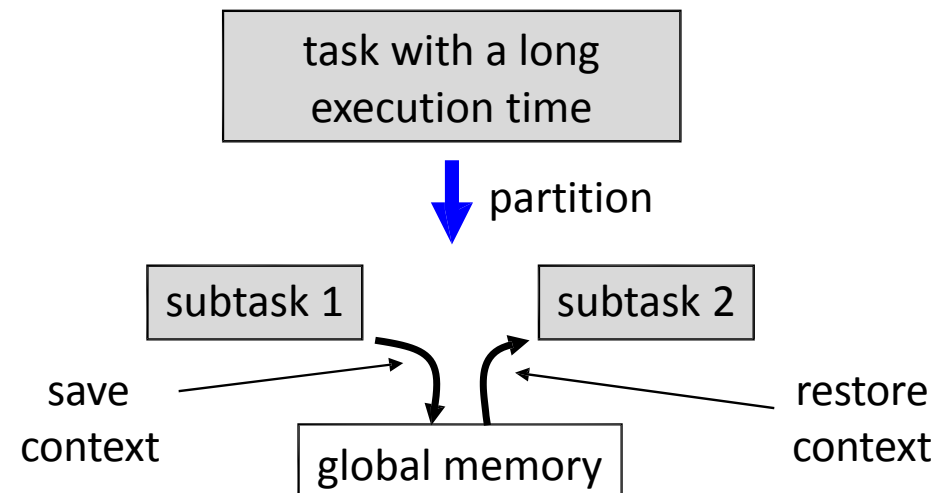


# Non-Preemptive Event-Triggered Scheduling

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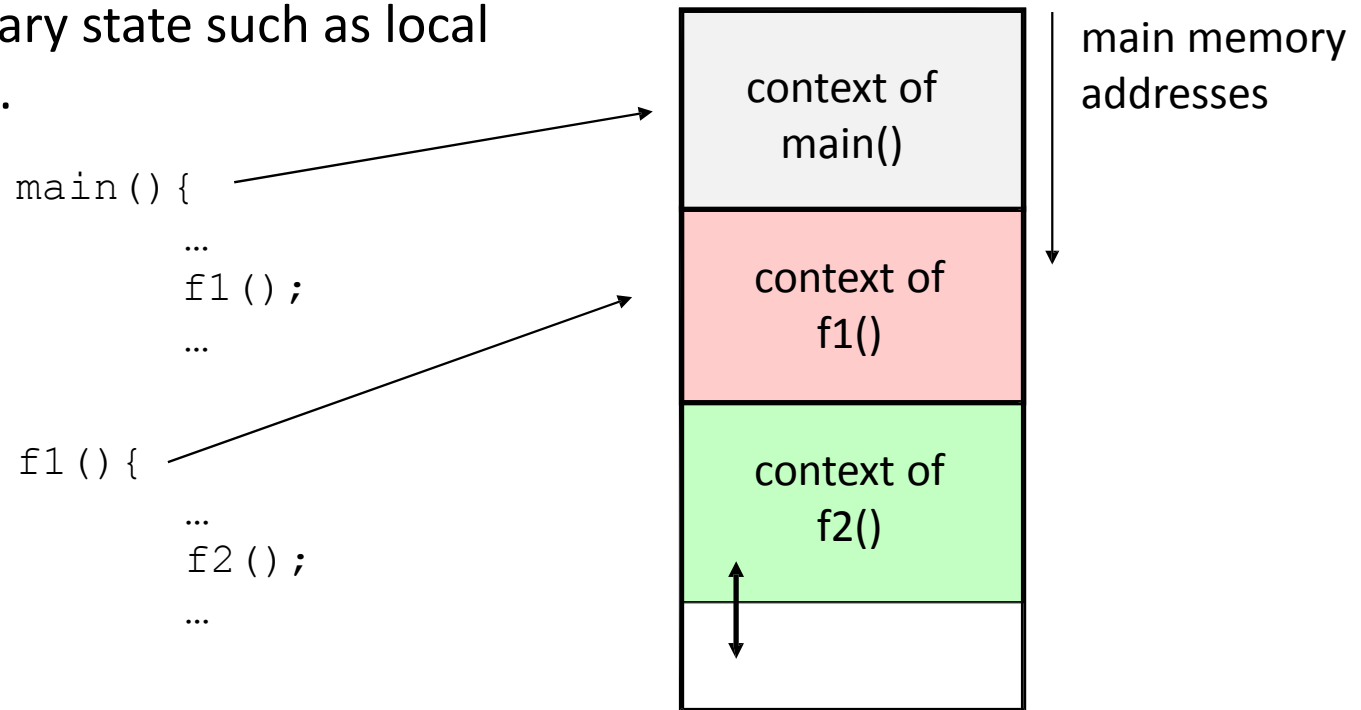
## Properties:

- *communication between tasks* does not lead to a simultaneous access to shared resources, but interrupts may cause problems as they preempt running tasks
- *buffer overflow* may happen if too many events are generated by the environment or by tasks
- *tasks with a long running time* prevent other tasks from running and may cause buffer overflow as no events are being processed during this time
  - partition tasks into smaller ones
  - but the local context must be stored

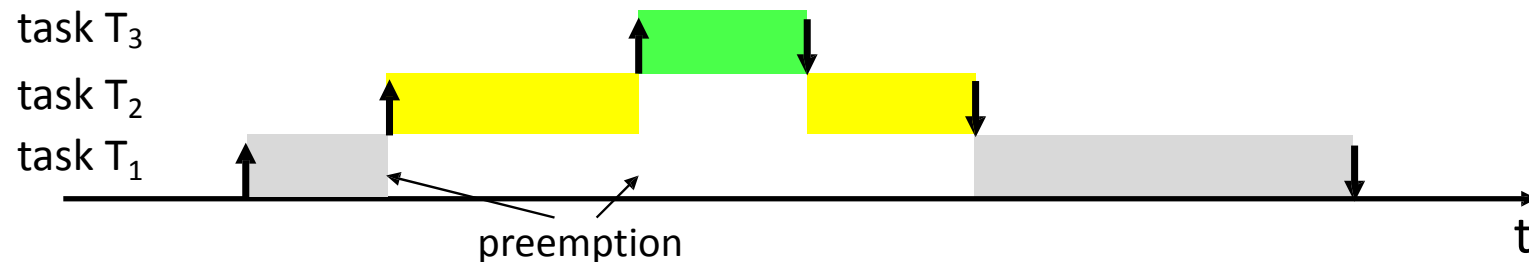


# Preemptive Event-Triggered Scheduling – Stack Policy

- This case is similar to non-preemptive case, but *tasks can be preempted by others*; this resolves partly the problem of tasks with a long execution time.
- If *the order of preemption is restricted*, we can use the usual stack-based context mechanism of function calls. The context of a function contains the necessary state such as local variables and saved registers.



# Preemptive Event-Triggered Scheduling – Stack Policy



- *Tasks must finish in LIFO (last in first out) order* of their instantiation.
  - this restricts flexibility of the approach
  - it is not useful, if tasks wait some unknown time for external events, i.e., they are blocked
- *Shared resources* (communication between tasks!) *must be protected*, for example by disabling interrupts or by the use of semaphores.

# Preemptive Event-Triggered Scheduling – Stack Policy

main:

```
while (true) {  
    if (event queue is empty) {  
        sleep();  
    } else {  
        select event from event queue;  
        execute selected task;  
        remove selected event from queue;  
    }  
}
```

set CPU to low power mode;  
processing continues after interrupt

for example using a function  
pointer in C; task returns after  
finishing.

InsertEvent:

```
put new event into event queue;  
select event from event queue;  
if (selected task  $\neq$  running task) {  
    execute selected task;  
    remove selected event from queue;  
}  
return;
```

Interrupt:

```
InsertEvent (...);  
return;
```

may be called by interrupt  
service routines (ISR) or tasks

# Thread

---

- *A thread is a unique execution of a program.*
  - Several copies of such a “program” may run simultaneously or at different times.
  - Threads share the same processor and its peripherals.
- *A thread has its own local state.* This state consists mainly of:
  - register values;
  - memory stack (local variables);
  - program counter;
- *Several threads may have a shared state* consisting of global variables.



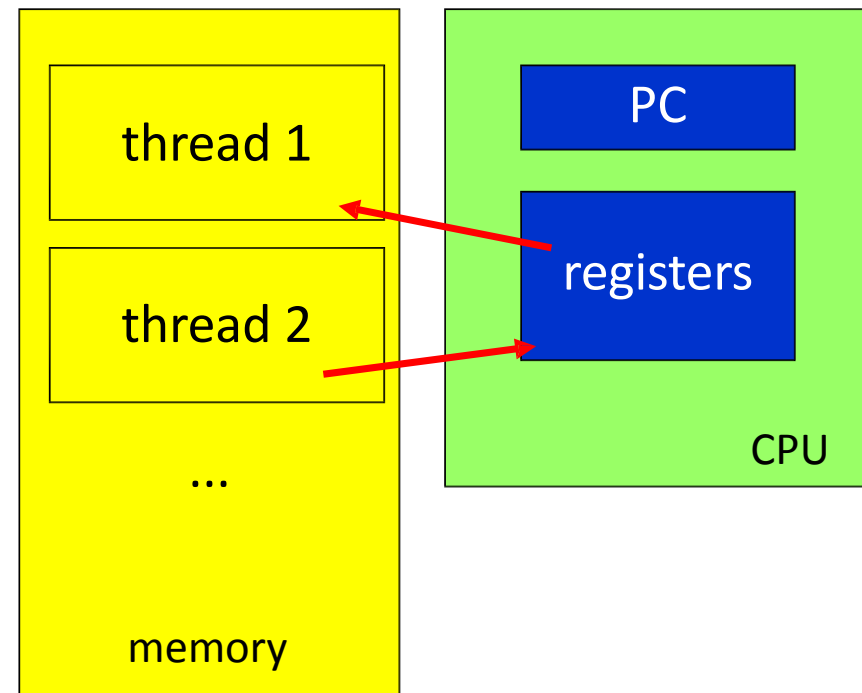
# Threads and Memory Organization

---

- *Activation record* (also denoted as the thread context) contains the thread local state which includes registers and local data structures.

- *Context switch:*

- current CPU context goes out
- new CPU context goes in



# Co-operative Multitasking

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- *Each thread allows a context switch to another thread* at a call to the `cswitch()` function.
  - This function is part of the underlying runtime system (operating system).
  - A *scheduler* within this runtime system chooses which thread will run next.
- **Advantages:**
  - predictable, where context switches can occur
  - less errors with use of shared resources if the switch locations are chosen carefully
- **Problems:**
  - programming errors can keep other threads out as a thread may never give up CPU
  - real-time behavior may be at risk if a thread runs too long before the next context switch is allowed

# Example: Co-operative Multitasking

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## Thread 1

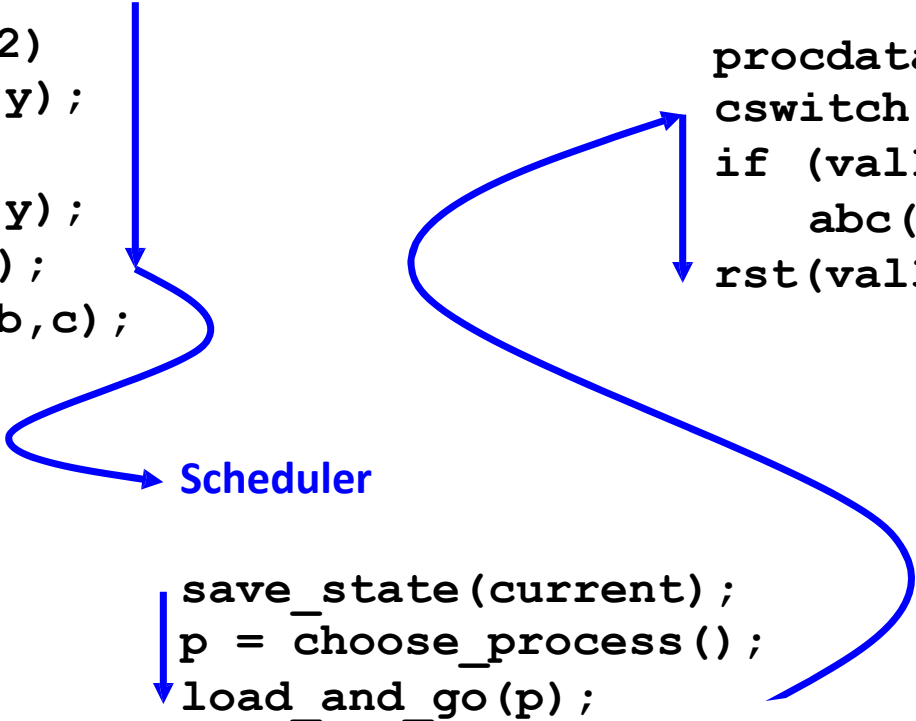
```
if (x > 2)
    sub1(y);
else
    sub2(y);
cswitch();
proca(a,b,c);
```

## Thread 2

```
procd(r,s,t);
cswitch();
if (val1 == 3)
    abc(val2);
rst(val3);
```

Scheduler

```
save_state(current);
p = choose_process();
load_and_go(p);
```



The diagram illustrates the flow of control in co-operative multitasking. Thread 1's code ends with a `cswitch()` call. A blue arrow points from this call to the Scheduler. The Scheduler's code block contains `save_state(current);`, `p = choose_process();`, and `load_and_go(p);`. A blue arrow points from the Scheduler to Thread 2's code, which begins with `procd(r,s,t);`. Another blue arrow points from the `cswitch()` call in Thread 2's code back to the Scheduler, completing the cycle.

# Preemptive Multitasking

## □ *Most general form of multitasking:*

- The scheduler in the runtime system (operating system) controls when contexts switches take place.
- The scheduler also determines what thread runs next.

## □ *State diagram corresponding to each single thread:*

- *Run:* A thread enters this state as it starts executing on the processor
- *Ready:* State of threads that are ready to execute but cannot be executed because the processor is assigned to another thread.
- *Blocked:* A task enters this state when it waits for an event.

