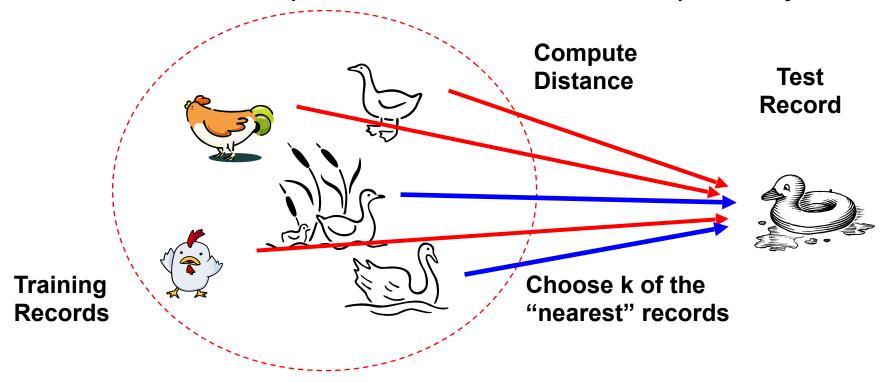
Classifiers: kNN

Dr. Srijith P K

Slide Credits: Dr. Vineeth N Balasubramanian

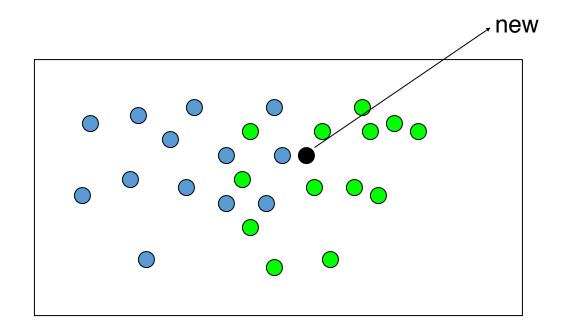


- Basic idea:
 - If it walks like a duck, quacks like a duck, then it's probably a duck





Majority vote within the k nearest neighbors



K= 1: blue K= 3: green



- An arbitrary instance is represented by (a₁(x), a₂(x), a₃(x),..., a_n(x))
 - a_i(x) denotes features
- Euclidean distance between two instances
 - $d(x_i, x_i)$ =sqrt (sum for r=1 to n $(a_r(x_i) a_r(x_i))^2$)
- L_p distance
 - p=2: Euclidean distance
 - p=1: Manhattan distance
 - p = ∞ : Max distance
 - p= 0: Count non-zero distance
- In case of continuous-valued target function
 - Mean value of k nearest training examples



Other Distance Metrics

• Cosine Distance Metric $\ \rho(\vec{x}_1,\vec{x}_2) = \cos(\angle(\vec{x}_1,\vec{x}_2)) = \frac{\vec{x}_1 \cdot \vec{x}_2}{\|\vec{x}_1\|_2 \ \|\vec{x}_2\|_2}$

• Edit Distance
$$x_1 = AAATCCCGTAA$$

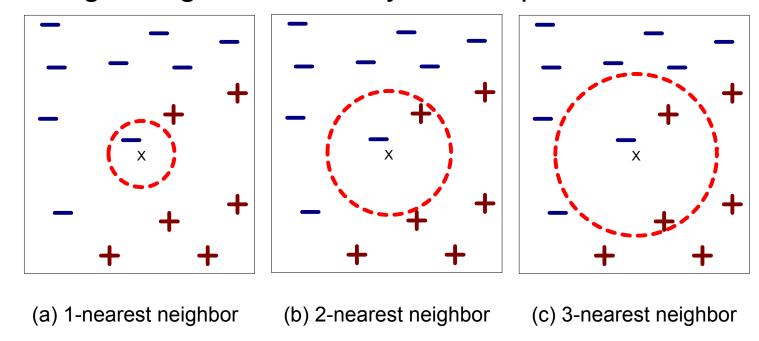
$$x_2 = AATCGCGTAA$$

Minimum number of insertions, deletions and mutations needed

$$\rho(x_1, x_2) = 2$$



- Choosing k is important
 - If k is too small, sensitive to noise points
 - If k is too large, neighborhood may include points from other classes



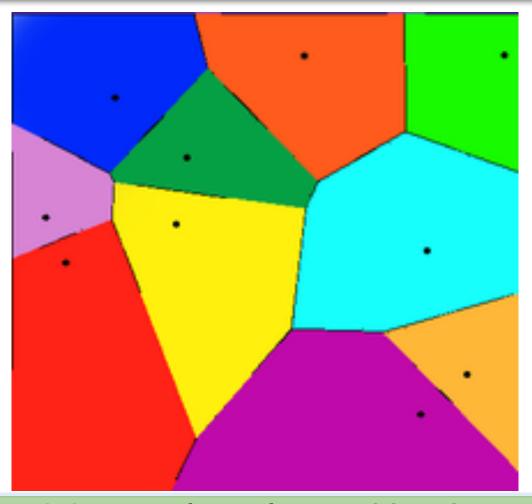


How to determine k

- Determined experimentally (think cross-validation!)
 - Start with k=1 and use a test set to validate the error rate of the classifier
 - Repeat with k=k+2
 - Choose the value of k for which the error rate is minimum
 - Note: k typically an odd number to avoid ties in binary classification



Voronoi Diagram





Pros and Cons

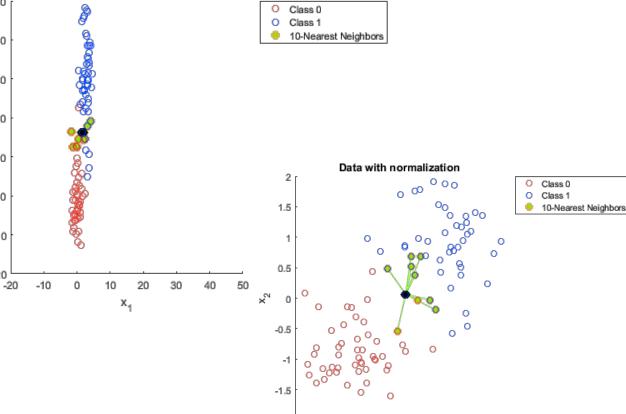
- Pros
 - Highly effective and simple method
 - Trains very fast ("Lazy" learner)
- Cons
 - Curse of dimensionality
 - In higher dimensions, all data points lie on the surface of the unit hypersphere!
 - Closeness in raw measurement space may not be good for the task
 - Storage: all training examples are saved in memory
 - A decision tree or linear classifier is much smaller
 - Slow at query time
 - Can be overcome and presorting and indexing training samples



Improvements

Data without normalization

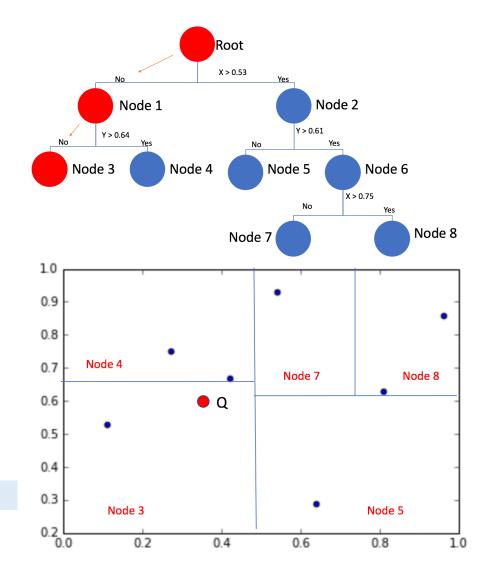
- Distance-Weighted Nearest Neighbors
 - •Assign weights to the neighbors based on their 'distance' from the query point (E.g., weight 'may' be inverse square of the distances)
 - Can also learn this -> "Metric Learning"
- •Scaling (normalization) attributes for 20/20 fair computation of distances





Improvements

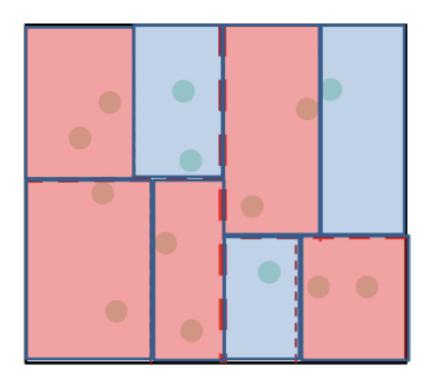
- Finding "close" examples in a large training set quickly
 - E.g. Efficient memory indexing using kd-trees
 - In 1-dimension, can reduce complexity from O(n) to O(log n) – assuming data is sorted
 - Other methods
 - Locality-Sensitive Hashing, Clustering-based methods





Improvements

- Not storing all examples
 - We can label each cell instead and discard the training data





Readings

- Chapters 8, 9, EA Introduction to ML 2nd Edn
- Chapter 14 (Sec 14. 4) + Chapter 2 (Sec 2. 5), Bishop, PRML

