

1. Stack frames

1> Data analysis

Part 2:

Since the result is so long, in order to make the result more clear, I re-formatted output as results shows below:

```
pc2-033-l:~/Documents/CS2002/W04Practical/Files hl74$ ./main-stack
Stack reserved for local variables are from 140721149507744 to 140721149507824
Value of arguments:
"val" : 1234 address : 140721149507816
"depth" : 1 address : 140721149507812
"*end" : 0x7ffc3220f958 address : 140721149507800
-----
Value for local variables are:
"quot" : 123 address : 140721149507792
"mod" : 4 address : 140721149507784
"*start" : 0x7ffc3220f8f0 address : 140721149507776
"len" : 0 address : 140721149507772
=====

Stack reserved for local variables are from 140721149507664 to 140721149507744
Value of arguments:
"val" : 123 address : 140721149507736
"depth" : 2 address : 140721149507732
"*end" : 0x7ffc3220f958 address : 140721149507720
-----
Value for local variables are:
"quot" : 12 address : 140721149507712
"mod" : 3 address : 140721149507704
"*start" : (nil) address : 140721149507696
"len" : 0 address : 140721149507692
=====

Stack reserved for local variables are from 140721149507584 to 140721149507664
Value of arguments:
"val" : 12 address : 140721149507656
"depth" : 3 address : 140721149507652
"*end" : 0x7ffc3220f958 address : 140721149507640
-----
Value for local variables are:
"quot" : 1 address : 140721149507632
"mod" : 2 address : 140721149507624
"*start" : (nil) address : 140721149507616
"len" : 0 address : 140721149507612
=====

Stack reserved for local variables are from 140721149507504 to 140721149507584
Value of arguments:
"val" : 1 address : 140721149507576
"depth" : 4 address : 140721149507572
"*end" : 0x7ffc3220f958 address : 140721149507560
-----
Value for local variables are:
"quot" : 0 address : 140721149507552
"mod" : 1 address : 140721149507544
"*start" : 0x7be260 address : 140721149507536
"len" : 6 address : 140721149507532
=====
```

Since this is a recursive function, so the reading order should be from down to up, or to say from inside to outside. So this report will analyse the data that being outputted from depth 4 to depth 1.

By calculating absolute addresses for each %rbp, such as for basic recursion, by subtracting addresses 140721149507744-140721149507824 we get 80, where this number is always 80 when subtracting 140721149507664-140721149507744, which is the second recursion. Where we can find that there are 16 bytes offset by subtracting 80 by 16.

In addition to check whether the result suits to comments in part 1, the easiest way of doing that is to check single value first.

Arguments:

“val” is in stack space %rbp – 8, Compare with what I have commented in “itos-commented.s”, operations on val is:

C	Assembler
val / 10	cqto idivq %rcx
val % 10	cqto idivq %rcx callq lab
compare val with 0	Cmpq \$0, %rcx cmpq \$0, -8(%rbp)

Then check the value above, we gets value 1, 12, 123, 1234 by several recursion, comparing with result “val” checked.

-12(%rbp) refers to the argument “depth”, calculate the depth of recursion. The operation on it is to add 1 in recursion function

start = itos_recur(quot, depth + 1, end);	movl -12(%rbp), %eax addl \$1 %eax callq itos_recur
---	---

Then check the value above, we will see depth goes from 4 to 1 which shows the depth of recursion from inside to outside. Then depth was checked.

-24(%rbp) refers to the pointer to pointer of end address, which points the address of address of start. Which can be checked with its address never being changed.

Local variables:

-32(%rbp) refers to “quot” : In C program quot refers to: quot = val / 10, which represented in assembly code is as:

movq %rax -32(%rbp)

Which copy the operated value of %rax (see “val”) to quot.

Another operation on quot in C program is compare quot with 0 and if not equal to 0, start recursion, which represented in assembly code is as

cmpq \$0 -32(%rbp)

```
je .LBB1_2
```

Where .LBB1_2 refers to “else:” part. Since quot will be used as recursive argument as val, the assembly code register quot to %rdi.

-40(%rbp) refers to “mod”, which will print the non-decimal part of the division. It represent in C program is same as the division of quot, but it calls function “labs”. Next operation on mod in assembly code is

```
Movq -40(%rbp), %rax  
addq $48 %rax
```

Which adds an char ‘0’ + mod to *(*end)++ %rax by reading from c program (Confusion 1) Values of quot and mod can be checked through output of program, which are obviously passed.

-48(%rbp) refers to pointer “start”. From assembly code in >.LBB1_5, related code on start is:

```
movq -24(%rbp), %rax # %rax = *end  
movq (%rax), %rdx # %rdx = %rax  
movq %rdx, %rsi # %rsi = %rdx  
addq $1, %rsi # %rsi += 1  
movq %rsi, (%rax) # %rax = %rsi  
movb %cl, (%rdx) # %rdx = %cl  
movq -48(%rbp), %rax # %rax = *start
```

From comments afterwards, *start = %rsi = %rdx += 1 = *end += 1. Since only when the program cannot be a recursion start can points to malloc(len)

-52(%rbp) refers to “len” only available in else bracket, which only appears in the deepest recursion, as the values in the image are always 0 because len has not accessed.

Operations on len is add depth with 3 or 2 and malloc it, in assembler code it represents as:

```
movl $3, %edx # %edx = 3  
movl $2, %esi # %esi = 2  
cmovll %edx, %esi # if compare gets 0 then %esi = %edx  
addl %esi, %eax # %eax += %esi  
movl %eax, -52(%rbp) # local variable len = %eax  
movslq -52(%rbp), %rdi # %rdi = len  
callq malloc # call function "malloc"
```

2> confusion:

Several confusion available during reading and commenting through the assembly code and c file:

In itos0, line 108, addq added 48 to %rax

In itos0, line 109, where values of %al come from and what are stack frame that %al and %cl located?

In itos_stack.c, line 22, what is mean by *(*end)++ = ‘-’, especially what is mean by “-”

In itos_stack.c, line 26, why the end pointer to pointer = ‘0’ + mod

In itos_stack.c, line 41, what is mean by ‘\0’

In stack.c, line 8, what this condition holds?

2. Division by invariant integers using multiplication

Part 3:

<1>

Since $\text{ceil}(2^{65}/10) * n/2^{65} - \text{floor}(n/10) = (\text{ceil}(2^{65}/10) - 2^{65}/10) * n/2^{65} + (n/10 - \text{floor}(n/10))$

$2^{65} \equiv 2^1 \equiv 2 \pmod{10}$, hence $\text{ceil}(2^{65} / 10) - 2^{65}/10 = 8/10$.

$n/10 - \text{floor}(n/10)$ can be up to $9/10$ for $n \equiv 9 \pmod{10}$, for $n = 2^{63} - 1$ this gives an upper bound on the error, which is:

$$8/10 * (2^{63}-1)/2^{65} + 9/10 = 2^3/10 * (2^{63}-1)/2^{65} + 9/10 = 2^3/10 * 2^{63}/2^{65} - 2^3/10 * 1/2^{65} + 9/10 \\ = 11/10 - 1/(10 * 2^{62}) \approx 1.1 \rightarrow \text{since the latter number was so small}$$

<2>

$2^{66} \equiv 4 \pmod{10}$ hence $\text{ceil}(2^{66} / 10) - 2^{66}/10 = 6/10$.

$n/10 - \text{floor}(n/10)$ can be up to $9/10$ for $n \equiv 9 \pmod{10}$, for $n = 2^{63} - 1$,

$$6/10 * (2^{63}-1)/2^{66} + 9/10 = 3/40 + 9/10 - 6/(10 * 2^{66}) \approx 0.975 < 1$$

So formula 3 does give us $\text{floor}(n/10)$ as desired.

<3> instructions:

data transfer:

```
movq %rdx %r14 : copy values from %rdx to %r14
movabsq $7378697629483820647, %rcx : copy absolute value (num.) to %rcx
```

Arithmetic:

```
imulq %rcx : signed multiply
shrq $63, %rax : right shifts (unsigned divides) Count specified by the constant $63, the 16 bit
contents of effective address (%rax)
sarlq $2, %rdx : Right shift, count specified by the contents (2), the 8-bit %rdx contents of effective
address.
```

control flow:

```
retq : return start
callq itos_recurse : start an recursion with arguments in %esi, %rdi, %rdx
```

Represent negative number:

`negq %rbx` (Line 59 in `itos_1`) to handle negative data by make the negative data be positive using `negq`

Extension:

1. Analysis on `itos1.s`

In `itos1.s`, arguments are stored in `%r15`, `%r14`, `%rbx`, which are pushed into the stack so that according to the memory hierarchy, register is very fast so that this instructions can be faster than using `(%rbp - 8)` as arguments.

```
.cfi_startproc
pushq   %r15
.cfi_def_cfa_offset 16
pushq   %r14
.cfi_def_cfa_offset 24
pushq   %rbx
.cfi_def_cfa_offset 32
.cfi_offset %rbx, -32
.cfi_offset %r14, -24
.cfi_offset %r15, -16
```

Local arguments are operated directly without copy data of them into another register.

Negative numbers are handled with negq.

Confusion: what roles are “leaq” playing in this file?

2. (Original makefile is stored in BackUp folder)

For making MIPS architecture, an warning happens that what I have done is same as what I have learnt in Lecture 8. I cannot find the reason why it goes wrong.

```
pc2-033-l:~/Documents/CS2002/W04Practical/Files hl74$ make
clang -c -S -Wall -Wextra -target MIPS -O0 itos.c -o itos4.s
error: unknown target triple 'MIPS', please use -triple or -arch
make: *** [Makefile:39: itos4.s] Error 1
pc2-033-l:~/Documents/CS2002/W04Practical/Files hl74$ make
clang -c -S -Wall -Wextra -arch MIPS -O0 itos.c -o itos4.s
clang-7: warning: argument unused during compilation: '-arch MIPS' [-Wunused-command-line-argument]
pc2-033-l:~/Documents/CS2002/W04Practical/Files hl74$ ls
itos0-commented.s  itos1.s  itos3.s  itos.h  itos-stack.c  itos-stack.s  main.c  main-stack*  stack.c  s
itos0.s           itos2.s  itos.c   itos.o  itos-stack.o  main*         main.o  Makefile     stack.h
pc2-033-l:~/Documents/CS2002/W04Practical/Files hl74$ ^C
pc2-033-l:~/Documents/CS2002/W04Practical/Files hl74$ ^C
pc2-033-l:~/Documents/CS2002/W04Practical/Files hl74$ make
clang -c -S -Wall -Wextra -target mips -O0 itos.c -o itos4.s
error: unable to create target: 'No available targets are compatible with this triple.'
1 error generated.
make: *** [Makefile:39: itos4.s] Error 1
```

Next I tried to make file as in <https://github.com/MIPT-ILab/mips-traces/blob/master/Makefile> but it still doesn't work.