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# Problem 1

```
clc;clear;

%2D FFT
N=16;
L=2.*pi;
f=zeros(N,N);
x=zeros(1,N);
y=zeros(1,N);

%Exact Fuctional Values
for j = 1:N
    for p=1:N
        x(j)=(L/N).*(j-1);
        y(p)=(L/N).*(p-1);
        f(j,p)= cos(3.*x(j)).*sin(5.*y(p))+sin(6.*x(j)).*cos(4.*y(p));
    end
end

%Continuous Fourier Transform for exact coefficients
f_kc=zeros(N,N);
m=-(N/2):1:((N/2)-1);
for j = 1:N
    for p=1:N
        f_kc(j,p)= (1/(2.*pi.*2.*pi)).*(integral2(@(x,y)
((cos(3.*x).*sin(5.*y)+sin(6.*x).*cos(4.*y))).*exp(-1i.*2.*pi.*((m(j).*x/
L)+(m(p).*y/L)))),0,L,0,L));
    end
end

%2D FFT
for p=1:N
    f_x=myFFT_tocall(f);
end
f_x=f_x.';

for m=1:N
    f_y=myFFT_tocall(f_x);
end
f_xy=f_y.'; %2D FFT transform coefficients

%2D inverse FFT
for i =1:N
    f_y(1:N,i)=fftshift(f_y(1:N,i));
end

%inverse in x dir:
for p=1:N
    ffuncy(p,1:N)=ifft(f_y(1:N,p).*N);
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end

for i= 1:N
    funcy(1:N,i)=fftshift(funcy(1:N,i));
end

%in y-direction
for m=1:N
    funcx=ifft(funcy.*N);           %2D FFT functional values
end
```

## My FFT Routine: Problem 1

```
function output=myFFT_tocall(f)

N=16;
M = log2(N);

% bitreversing

f1 = bitrevorder(f(1:N,1));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
        out1 = f1/N;
        out1=fftshift(out1);

        % bitreversing

f1 = bitrevorder(f(1:N,2));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    end
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    out2 = f1/N;
    out2=fftshift(out2);

    f1 = bitrevorder(f(1:N,3));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out3 = f1/N;
    out3=fftshift(out3);

    f1 = bitrevorder(f(1:N,4));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out4 = f1/N;
    out4=fftshift(out4);

    f1 = bitrevorder(f(1:N,5));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out5 = f1/N;
    out5=fftshift(out5);

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f1 = bitrevorder(f(1:N,6));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out6 = f1/N;
    out6=fftshift(out6);

f1 = bitrevorder(f(1:N,7));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp= 0;
        end
    out7 = f1/N;
    out7=fftshift(out7);

f1 = bitrevorder(f(1:N,8));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out8 = f1/N;
    out8=fftshift(out8);

f1 = bitrevorder(f(1:N,9));

%fft algorithm

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%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out9 = f1/N;
    out9=fftshift(out9);

    f1 = bitrevorder(f(1:N,10));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out10 = f1/N;
    out10=fftshift(out10);

    f1 = bitrevorder(f(1:N,11));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out11 = f1/N;
    out11=fftshift(out11);

    f1 = bitrevorder(f(1:N,12));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;

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        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out12 = f1/N;
    out12=fftshift(out12);

f1 = bitrevorder(f(1:N,13));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out13 = f1/N;
    out13=fftshift(out13);

f1 = bitrevorder(f(1:N,14));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out14 = f1/N;
    out14=fftshift(out14);

f1 = bitrevorder(f(1:N,15));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;

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        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out15 = f1/N;
    out15=fftshift(out15);

f1 = bitrevorder(f(1:N,16));

%fft algorithm
%for x=1:N
    for l =1:M
        k = 2^l;
        w = exp((-1i.*2.*pi.*(0:k-1))./(k));
        for t=0:k:N-1
            temp(t+1:t+k) = [f1(t+1:t+k/2)+f1(t+k/2+1:t+k).*w(1:k/2), f1(t
+1:t+k/2)+f1(t+k/2+1:t+k).*w(k/2+1:k)] ;
            end
            f1=temp;
            temp = 0;
        end
    out16 = f1/N;
    out16=fftshift(out16);

    output=[out1.' out2.' out3.' out4.' out5.' out6.' out7.' out8.' out9.'
    out10.' out11.' out12.' out13.' out14.' out15.' out16.'];
end

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