

Implement Synchronous Mod-7 Up/Down Counter. (Assignment-8)

This counter will be able to count both up and down direction with a mode select input to control the count direction.

Range for Up counting - 0 to $N-1 \Rightarrow 0$ to 6

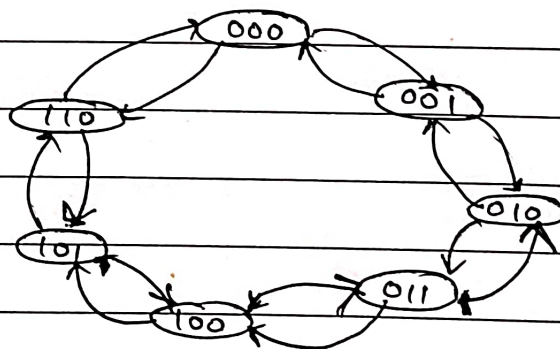
Range for down counting $\Rightarrow 6$ to 0

Number of States = 7

Number of Flip-flops = 3 (A, B, C)

$$\{ 7 \leq 8 \Rightarrow 7 \leq 2^3 \}$$

Counting diagram



Now, we will draw or write State Table

mode $M=0 \Rightarrow$ Up count

$M=1 \Rightarrow$ down count

STATE TABLE

i/p's of T-flip-flops

M	Q _A	Q _B	Q _C	Q _{A+1}	Q _{B+1}	Q _{C+1}	T _A	T _B	T _C
0	0	0	0	0	0	1	0	0	1
0	0	0	1	0	1	0	0	1	1
0	0	1	0	0	1	1	0	0	1
0	0	1	1	1	0	0	1	1	1
0	1	0	0	1	0	1	0	0	1
0	1	0	1	1	1	0	0	1	1
0	1	1	0	0	0	0	1	1	0

Up counting

Excitation Table for T → using here ↑

Q _n	Q _{n+1}	T
0	0	0
0	1	1
1	0	1
1	1	0

M.	Q _A	Q _B	Q _C	Q _{A+1}	Q _{B+1}	Q _{C+1}	T _A	T _B	T _C
1.	1	1	0	1	0	1	0	1	1
1.	1	0	1	1	0	0	0	0	1
1.	1	0	0	0	1	1	1	1	1
1.	0	1	1	0	1	0	0	0	1
1.	0	1	0	0	0	1	0	1	1
1.	0	0	1	0	0	0	0	0	1
1.	0	0	0	1	1	0	1	1	0

Down counting

$$T_A = \sum m(3, 6, 8, 12) + d(7, 15)$$

$$T_B = \sum m(1, 3, 5, 6, 8, 10, 12, 14) + d(7, 15)$$

$$T_C = \sum m(0, 1, 2, 3, 4, 5, 9, 10, 11, 12, 13, 14) + d(7, 15)$$

K-Maps

< for T_A >

$MQ_A \backslash QBQC$	00	01	11	10
00			1	
01			X	1
11	1		X	
10	1			

< for T_B >

$MQ_A \backslash QBQC$	00	01	11	10
00		1	1	
01		1	X	1
11	1		X	1
10	1			1

< For T_c >

$MQA \backslash Q_B Q_C$	00	01	11	10
00	1	1	1	1
01	1	1	X	
11	1	1	X	1
10		1	1	1

$$T_A = M \bar{Q}_B \bar{Q}_C + \bar{M} Q_B Q_C + \bar{M} Q_A Q_B$$

$$T_B = \bar{M} Q_C + M \bar{Q}_C + Q_A Q_B$$

$$T_C = \bar{M} \bar{Q}_B + Q_C + M Q_A + \bar{Q}_A Q_B$$

$$T_A = M \bar{Q}_B \bar{Q}_C + \bar{M} Q_B \cdot (\bar{Q}_A \text{ NAND } \bar{Q}_C)$$

$$T_B = (M \oplus Q_C) \text{ NAND } (Q_A \text{ NAND } Q_B)$$

$$T_C = \bar{M} \bar{Q}_B + Q_C + M Q_A + \bar{Q}_A Q_B$$

$$= (\bar{M} \text{ NAND } \bar{Q}_B) \text{ NAND } \bar{Q}_C + (M \text{ NAND } Q_A) \text{ NAND } (\bar{Q}_A \text{ NAND } Q_B)$$

