

# Assignment 1: Design an up-down decade counter using JK-Flip Flop

# For a Decade UP-Down counter it can count  $0 \rightarrow 9$  in both directions.

# In this counting there are 10 stages so,

$$16 > 10$$

$$2^4 > 10$$

$\therefore$  We need four JK-Flip Flops for this counter

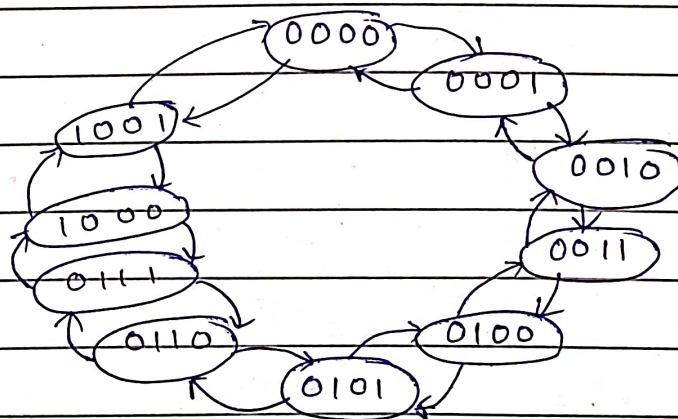
# We will implement both Up and Down counter in a single circuit using a ~~sta~~ select line.

If the select line is M let's say -

$M = 0 \rightarrow$  Up counting

$M = 1 \rightarrow$  Down counting

# The states  $\rightarrow$



# Now, we will draw the truth tables  $\rightarrow$

For  $M=0$ 

$Q_A$	$Q_B$	$Q_C$	$Q_D$	$Q_{A+1}$	$Q_{B+1}$	$Q_{C+1}$	$Q_{D+1}$
0	0	0	0	0	0	0	1
0	0	0	1	0	0	1	0
0	0	1	0	0	0	1	1
0	0	1	1	0	1	0	0
0	1	0	0	0	1	0	1
0	1	0	1	0	1	1	0
0	1	1	0	0	1	1	1
0	1	1	1	1	0	0	0
1	0	0	0	1	0	0	1
1	0	0	1	0	0	0	0

\* Other combinations are don't cares

Now excitation table of JK flip flop

$Q_n$	$Q_{n+1}$	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

for  $M=0$ 

$Q_A$	$Q_B$	$Q_C$	$Q_D$	$Q_{A+1}$	$Q_{B+1}$	$Q_{C+1}$	$Q_{D+1}$	$J_A$	$K_A$	$J_B$	$K_B$	$J_C$	$K_C$	$J_D$	$K_D$
0	0	0	0	0	0	0	1	0	x	0	x	0	x	1	x
0	0	0	1	0	0	1	0	0	x	0	x	1	x	x	1
0	0	1	0	0	0	1	1	0	x	0	x	x	0	1	x
0	0	1	1	0	1	0	0	0	x	1	x	x	1	x	1
0	1	0	0	0	1	0	1	0	x	x	0	0	x	1	x
0	1	0	1	0	1	1	0	0	x	x	0	1	x	x	1
0	1	1	0	0	1	1	1	0	x	x	0	x	0	1	x
0	1	1	1	1	0	0	0	1	x	x	1	x	1	x	1
1	0	0	0	1	0	0	1	x	0	0	x	0	x	1	x
1	0	0	1	0	0	0	0	x	1	0	x	0	x	x	1

$$J_A = \sum m(7) + d(8, 9, 10, 11, 12, 13, 14, 15)$$

$$K_A = \sum m(9) + d(0, 1, 2, 3, 4, 5, 6, 7, 10, 11, 12, 13, 14, 15)$$

$$J_B = \sum m(3) + d(4, 5, 6, 7, 10, 11, 12, 13, 14, 15)$$

$$K_B = \sum m(7) + d(0, 1, 2, 3, 8, 9, 10, 11, 12, 13, 14, 15)$$

$$J_C = \sum m(1, 5) + d(2, 3, 6, 7, 10, 11, 12, 13, 14, 15)$$

$$K_C = \sum m(3, 7) + d(0, 1, 4, 5, 8, 9, 10, 11, 12, 13, 14, 15)$$

$$J_D = \sum m(0, 2, 4, 6, 8) + d(1, 3, 5, 7, 9, 10, 11, 12, 13, 14, 15)$$

$$K_D = \sum m(1, 3, 5, 7, 9) + d(0, 2, 4, 6, 8, 10, 11, 12, 13, 14, 15)$$

For  $M=0$

for  $J_A$

$Q_A Q_B$		$Q_C Q_D$			
		00	01	11	10
00					
01				1	
11		X	X	X	X
10		X	X	X	X

$$J_A = Q_B Q_C Q_D$$

for  $K_A$

$Q_A Q_B$		$Q_C Q_D$			
		00	01	11	10
00		X	X	X	X
01		X	X	X	X
11		X	X	X	X
10			1	X	X

$$K_A = Q_D$$

for  $J_B$

$Q_A Q_B$		$Q_C Q_D$			
		00	01	11	10
00				1	
01		X	X	X	X
11		X	X	X	X
10				X	X

$$J_B = Q_C Q_D$$

Teacher's Signature .....



for  $K_B$ 

$Q_A Q_B \backslash Q_C Q_D$	00	01	11	10
00	X	X	X	X
01			1	
11	X	X	X	X
10	X	X	X	X

$$K_B = Q_C Q_D$$

for  $J_C$ 

$Q_A Q_B \backslash Q_C Q_D$	00	01	11	10
00		1	X	X
01		1	X	X
11	X	X	X	X
10			X	X

$$J_C = \bar{Q}_A Q_D$$

for  $K_C$ 

$Q_A Q_B \backslash Q_C Q_D$	00	01	11	10
00	X	X	1	
01	X	X	1	
11	X	X	X	X
10	X	X	X	X

$$K_C = Q_D$$

for  $J_D$ 

$Q_A Q_B \backslash Q_C Q_D$	00	01	11	10
00	1	X	X	1
01	1	X	X	1
11	X	X	X	X
10	1	X	X	X

$$J_D = 1$$

Similarly,

$$K_D = 1$$

for  $M=1$ 

$Q_A$	$Q_B$	$Q_C$	$Q_D$	$Q_{A+1}$	$Q_{B+1}$	$Q_{C+1}$	$Q_{D+1}$	$J_A$	$K_A$	$J_B$	$K_B$	$J_C$	$K_C$	$J_D$	$K_D$
0	0	0	0	1	0	0	1	1	x	0	x	0	x	1	x
0	0	0	1	0	0	0	0	0	x	0	x	0	x	x	1
0	0	1	0	0	0	0	1	0	x	0	x	x	1	1	x
0	0	1	1	0	0	1	0	0	x	0	x	x	0	x	1
0	1	0	0	0	0	1	1	0	x	x	1	1	x	1	x
0	1	0	1	0	1	0	0	0	x	x	0	0	x	x	1
0	1	1	0	0	1	0	1	0	x	x	0	x	1	1	x
0	1	1	1	0	1	1	0	0	x	x	0	x	0	x	1
1	0	0	0	0	1	1	1	x	1	1	x	1	x	1	x
1	0	0	1	1	0	0	0	x	0	0	x	0	x	x	1

for  $M=1$ for  $J_A$ 

$Q_A Q_B$	$Q_C Q_D$	00	01	11	10
00		1			
01					
11		x	x	x	x
10		x	x	x	x

$$J_A = \overline{Q_B} \overline{Q_C} \overline{Q_D}$$

for  $K_A$ 

$Q_A Q_B$	$Q_C Q_D$	00	01	11	10
00		x	x	x	x
01		x	x	x	x
11		x	x	x	x
10		1		x	x

$$K_A = \overline{Q_D}$$

for  $J_B$  :-

$Q_A Q_B$   $Q_C Q_D$

	00	01	11	10
00				
01	X	X	X	X
11	X	X	X	X
10	1		X	X

$$J_B = Q_A \bar{Q}_D$$

for  $K_B$  :-

$Q_A Q_B$   $Q_C Q_D$

	00	01	11	10
00	X	X	X	X
01	1			
11	X	X	X	X
10	X	X	X	X

$$K_B = \bar{Q}_C \bar{Q}_D$$

for  $J_C$  :-

$Q_A Q_B$   $Q_C Q_D$

	00	01	11	10
00			X	X
01	1		X	X
11	X	X	X	X
10	1		X	X

$$J_C = \bar{Q}_B \bar{Q}_C \bar{Q}_D$$

$$Q_B \bar{Q}_D + Q_A \bar{Q}_D$$

for  $K_c = -$ 

$Q_A Q_B \backslash Q_C Q_D$	00	01	11	10
00	X	X		1
01	X	X		1
11	X	X	X	X
10	X	X	X	X

$$K_c = \bar{Q}_D$$

for  $J_D$  and  $K_D \rightarrow$ 

$$J_D = 1, K_D = 1$$

So, finally

$$J_A = \bar{M} Q_B Q_C Q_D + M \bar{Q}_B \bar{Q}_C \bar{Q}_D$$

$$\cancel{J_A} \quad K_A = \bar{M} Q_D + M \bar{Q}_D = M \oplus Q_D$$

$$J_B = \bar{M} Q_C Q_D + M Q_A \bar{Q}_D$$

$$K_B = \bar{M} Q_C Q_D + M \bar{Q}_C \bar{Q}_D$$

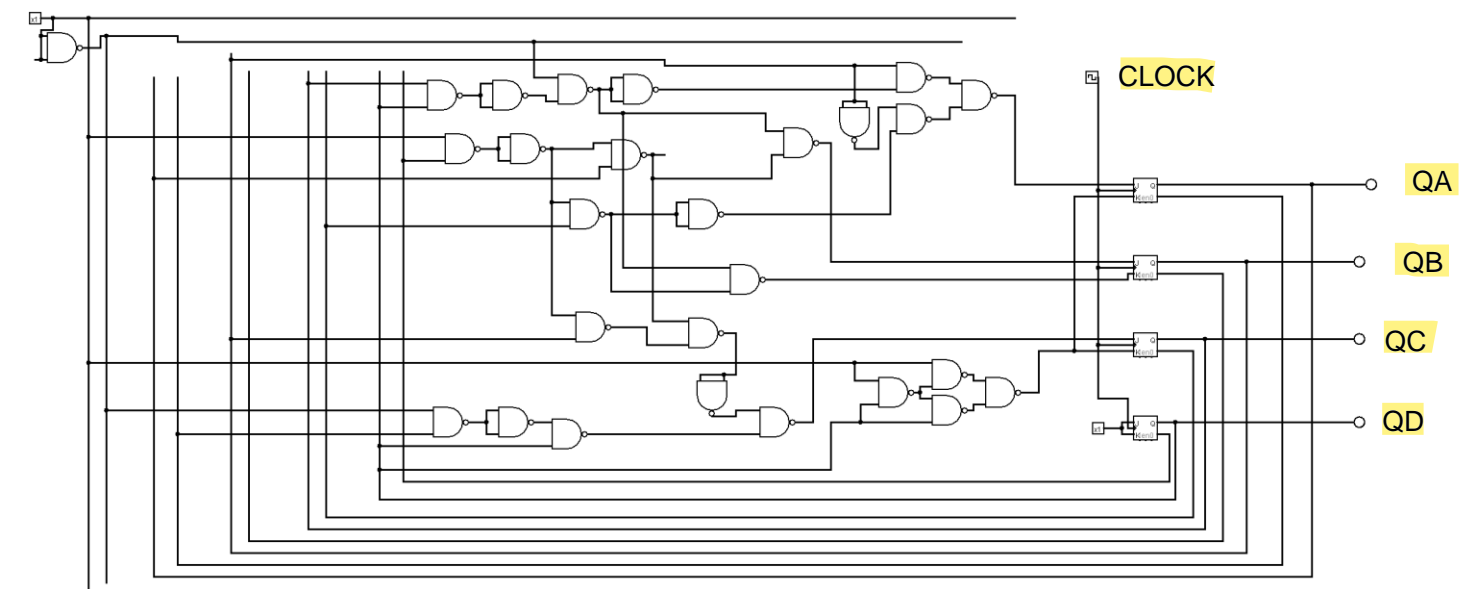
$$J_C = \bar{M} \bar{Q}_A Q_D + M \bar{Q}_D (Q_B + Q_A)$$

$$K_C = \bar{M} Q_D + M \bar{Q}_D = M \oplus Q_D$$

$$J_D = M + \bar{M} = K_D = 1$$



M and M'



# CIRCUIT DESIGN