

## Laboratory practice No. 4: Hash tables and Binary Tree

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### 3) Practice for final project defense presentation

**3.1** To calculate collisions between bees we chose a tree data structure, called Octree. Octree is an efficient option to calculate collision in a three-dimensional space by recursively subdividing it into eight octants. In this case we used the octants as the quadrants where each bee will be, so the octree will be responsible for locating each bee in a specific quadrant and for analyzing if there is more than one bee in the quadrant and if that happens, this quadrant will be divided into another octants and so on.

As it was said before, this data structure is really efficient mainly due to it has a really good complexity in time, because insertion and search (the functions that we used) are  $O(n \log n)$  for the worst case, where  $n$  will be the number of nodes.

**3.2** We think that it is really difficult to do the family tree with a different implementation because one of the unique ways that the search and insert functions will be long  $n$  is making a self-balancing binary search tree. It doesn't work really well in this problem because there are some cases in which the names of either the paternal family or maternal family members are unknown so the tree will be unbalanced and it is not possible to balance it because that could make that the order of the family members change so that tree would not have the order of the tree that the problem mentioned and neither of the classic family tree.

### 3.3 Description of exercise 2.1 Pos-order in a binary tree

To solve the problem, first we implement some of the Binary class functions that we already had from the workshop, like insert. Then, we made three new functions. The first one to build a tree from an array, the second one to post-order the elements of the tree and the third one and the most important, the function that makes all in one and solves the problem, the function sort. There we receive an array (that is the pre-order traversal), with this array we build the new tree and print it in post-order. Print it in a post-order traversal means that : first we traverse (pass over) the left subtree, then the right subtree and finally the root node. Basically, it just needs the array with the pre-order of the tree and then it works perfectly.

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## Description of exercise 2.2 Tree Summing

In this exercise, we create a recursive function to determine if the given elements of a tree add up to a specific number. Besides that, we read the input that will be located in a txt file and using the class Counter (of the collections module of python) we saved the elements with the number of times it is repeated. Then we split the input to have each part of it individually. Therewith, we identify and store the integer that determines the objective of the sum (value) and on the other hand the numbers that are the elements of the tree (exp). Finally with the above action, we call the recursive function sending in the value and exp to determine if it accomplishes the sum of the objective or not and depending on that we return yes or not.

### 3.4 Complexity

#### 3.4.1 Complexity of Pos-Order in a binary tree

*Time complexity for the worst case*

$O(n * m) + O(m) + O(m) + O(n * m) \Rightarrow \text{Sum law}$   
 $O(n * m)$  where  $n$  is the array's length and  $m$  is the number of nodes  
 Due to  $n = m$ , the time complexity for the worst case will be  $O(n^2)$

Why this complexity? Because the function building tree will have to go through the array that was given and keep inserting each element in the binary tree, and as we know the insertion in the binary tree is  $O(n)$ .

#### 3.4.2 Complexity of Tree summing

*Time complexity for the worst case*

$O(n) + O(m) + O(1) \Rightarrow \text{Sum law}$   
 $O(n + m)$  where  $n$  is the number of nodes in the binary tree and  $m$  is the number of rows in the

Why this complexity? Because the algorithm will have to split the rows in the txt file and then it goes through each row in a recursive way, to find if the sum of a certain combination of the numbers is equal to the target given.

## 4) Practice for midterms

**4.1 4.1.1 b :** the strings that begin with the same letter collide

**4.1.2 d:**  $O(1)$

**4.2 1.** It returns the lowest common ancestor to the node 1 and node 2

**2.** The complexity for the worst case is  $T(n) = T(n/2) + T(n/2) + C$ , what means  $O(n)$

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## ESTRUCTURA DE DATOS 1

### Código ST0245

3. We can improve the algorithm mystery using the condition that if  $n$  is less than the data it will be assigned to the left node; else, to the right node, so we will avoid going through the two sides. This could improve the complexity to  $O(\log_2 n)$ .

**4.3** 1. Last line : return True

2. The complexity of areEqual in the worst case is  $O(n)$  since  $n=m$  so  $O(n+m) = O(n)$

**4.4** 4.4.1 **c** :  $T(n)=2T(n/2)+C$ , que es  $O(n)$

4.4.2 **a** :  $O(n)$

4.4.3 **d** : Wilkenson, Joaquina, Eustaquia, Florinda, Eustaquio, Jovín, Sufranio, Piolina, Wilberta, Piolín, Usnavy

4.4.4 **a**: Change the order of the lines 03, 04 and 05 to 05, 04, 03.

**4.5** Line 4 : toInsert == p.data

Line 6 : toInsert > p.data

**4.6** 4.6.1 **d** : 4

4.6.2 Return 0

4.6.3 if(raiz.hijos.size()== 0) ???

**4.7** 4.7.1 **a** : 0, 2, 1, 7, 5, 10, 13, 11, 9, 4

4.7.2 **b** : 2

**4.8** **b** : 2

**4.9** **a** : 5, 3, 6, 1, 7, 4, 8, 0, 2

**4.10** 4.10.1 **b** : 2, 3, 4, 0, 5, 7, 6

4.10.2 **a** : 5

4.10.3 **b** : No

**4.11** 4.11.1 Line 10 : raiz.id

4.11.2 The complexity in the worst case is **a** :  $T(n-1) + c$  that means  $O(n)$

**4.12** 4.12.1 **i** : A = 1, B = 2, C = 3, D = 4, E = 5, F = 6, G = 7, H = 8, I = 9, J = 10.

4.12.2 **i** : G,D,B,A,C,E,F,I,H,J

4.12.3 **a** :  $O(n)$

### 5) Recommended reading (optional)

Mapa conceptual

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## 6) Teamwork and gradual progress (optional)

### 6.1 Meeting minutes

IH	Isabella Montoya Henao	Entrante	48 min 50 s	10:29 a.m.	...
IH	Isabella Montoya Henao	Entrante	15 min 29 s	23/04 3:56 p.m.	...
IH	Isabella Montoya Henao	Saliente		23/04 3:18 p.m.	...
IH	Isabella Montoya Henao	Entrante	47 min 58 s	23/04 11:36 a.m.	...
IH	Isabella Montoya Henao	Saliente	1 min 21 s	22/04 4:00 p.m.	...
IH	Isabella Montoya Henao	Saliente	34 min 35 s	22/04 3:25 p.m.	...
IH	Isabella Montoya Henao	Entrante		22/04 3:24 p.m.	...
IH	Isabella Montoya Henao	Entrante	1 h 16 min	22/04 10:09 a.m.	...
IH	Isabella Montoya Henao	Entrante	53 min 28 s	21/04 6:22 p.m.	...
IH	Isabella Montoya Henao	Entrante	1 h 14 min	20/04 10:48 a.m.	...
IH	Isabella Montoya Henao	Llamada perdida		19/04 9:09 a.m.	...
IH	Isabella Montoya Henao	Saliente	23 min 12 s	17/04 4:20 p.m.	...

IH	Isabella Montoya Henao	Entrante	1 h 52 min	17/04 2:27 p.m.	...
IH	Isabella Montoya Henao	Entrante	1 h 28 min	16/04 2:42 p.m.	...
IH	Isabella Montoya Henao	Entrante	1 h 38 min	11/04 5:14 p.m.	...
IH	Isabella Montoya Henao	Entrante	18 min 18 s	06/04 5:43 p.m.	...
IH	Isabella Montoya Henao	Saliente	17 s	06/04 2:09 p.m.	...
IH	Isabella Montoya Henao	Saliente		06/04 2:08 p.m.	...
IH	Isabella Montoya Henao	Saliente	1 min 29 s	06/04 2:04 p.m.	...
IH	Isabella Montoya Henao	Entrante	1 min 3 s	06/04 2:03 p.m.	...
IH	Isabella Montoya Henao	Entrante	48 min 39 s	05/04 3:21 p.m.	...
IH	Isabella Montoya Henao	Entrante	56 min 47 s	02/04 5:10 p.m.	...

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### Código ST0245

### 6.2 History of changes of the code

Commits on Apr 27, 2021			
Update ejercicio21.py	imontoyah committed 3 days ago	Verified	540685e
Update TreeSumming-2.2.py	miarango committed 3 days ago	Verified	6a7018b
Add files via upload	miarango committed 3 days ago	Verified	3acb9a1
Add files via upload	imontoyah committed 3 days ago	Verified	5e674a8
Commits on Apr 30, 2021			
Rename Octree1.py to Octree.py	miarango committed 1 minute ago	Verified	19816dd
Add files via upload	miarango committed 2 minutes ago	Verified	f8884f0
Update readerAbejas.py	imontoyah committed 1 hour ago	Verified	1104ec1
Add files via upload	imontoyah committed 1 hour ago	Verified	9e0fcab
Update ejercicio21.py	imontoyah committed 1 hour ago	Verified	45cb323
Delete nada	imontoyah committed 2 hours ago	Verified	79beb7f
Add files via upload	imontoyah committed 2 hours ago	Verified	f98d8c5
Create nada	imontoyah committed 2 hours ago	Verified	e403d50
Add files via upload	imontoyah committed 2 hours ago	Verified	3b1a4fc

### 6.3 History of changes of the report

<p>▶ April 27, 11:49 AM Current version Isabella Montoya Henao Maria Arango</p>	<p>▶ April 25, 2:55 PM Maria Arango</p>	<p>▶ April 19, 7:34 AM Isabella Montoya Henao Maria Arango</p>
<p>▶ April 27, 6:25 AM Isabella Montoya Henao</p>	<p>▶ April 25, 11:20 AM Maria Arango</p>	<p>THIS MONTH</p>
<p>YESTERDAY</p>	<p>THURSDAY</p>	<p>▶ April 18, 9:13 PM Maria Arango</p>
<p>▶ April 26, 6:45 PM Maria Arango</p>	<p>April 22, 2:34 PM Isabella Montoya Henao</p>	<p>▶ April 17, 7:12 PM Isabella Montoya Henao Maria Arango</p>
<p>▶ April 26, 4:16 PM Maria Arango</p>	<p>WEDNESDAY</p>	<p>▶ April 17, 6:45 PM Isabella Montoya Henao</p>
<p>▶ April 26, 2:24 PM Isabella Montoya Henao</p>	<p>April 21, 6:52 AM Isabella Montoya Henao</p>	<p>▶ April 16, 6:13 AM Isabella Montoya Henao</p>
	<p>LAST WEEK</p>	
	<p>▶ April 20, 2:14 PM Isabella Montoya Henao</p>	
	<p>▶ April 18, 2:49 PM Maria Arango</p>	
	<p>▶ April 18, 1:22 PM Maria Arango</p>	
	<p>▶ April 17, 8:37 PM Maria Arango</p>	

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