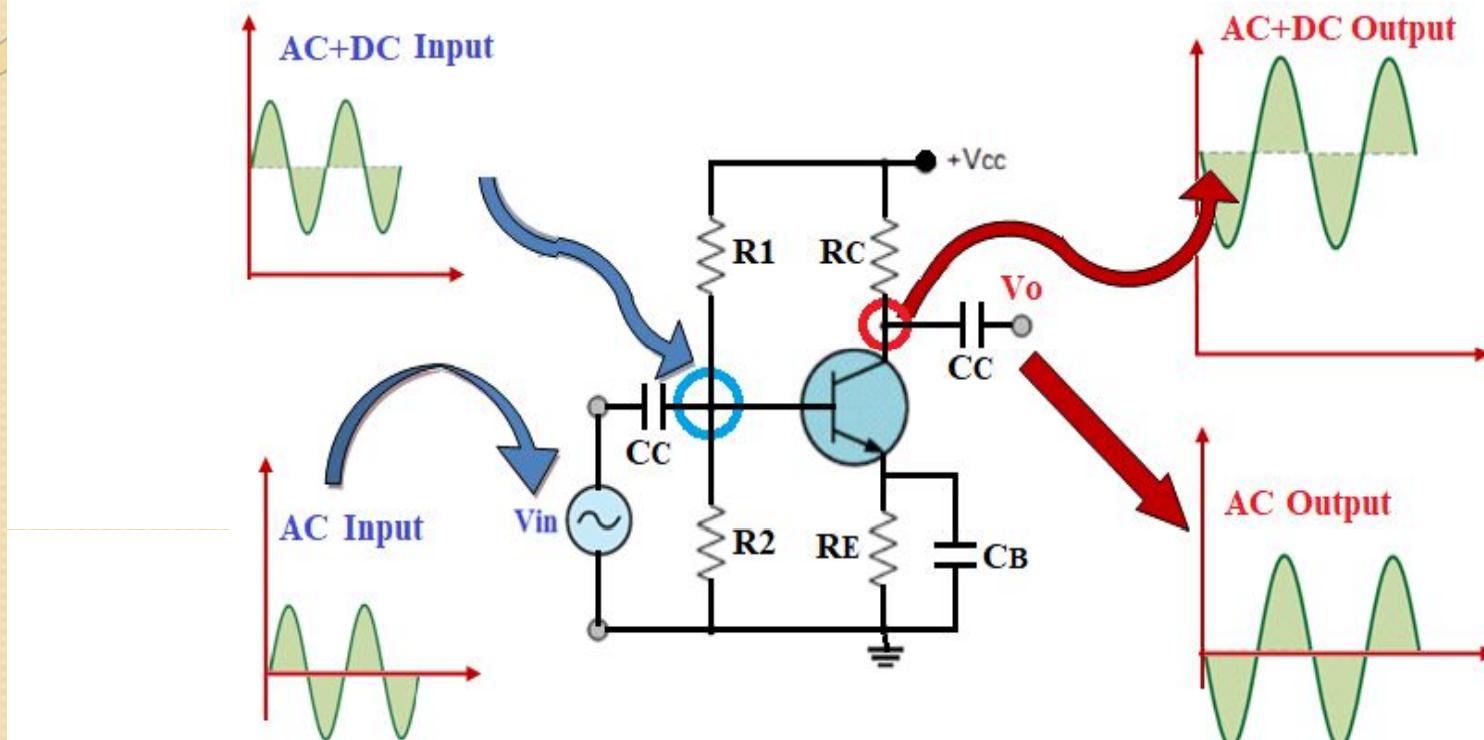


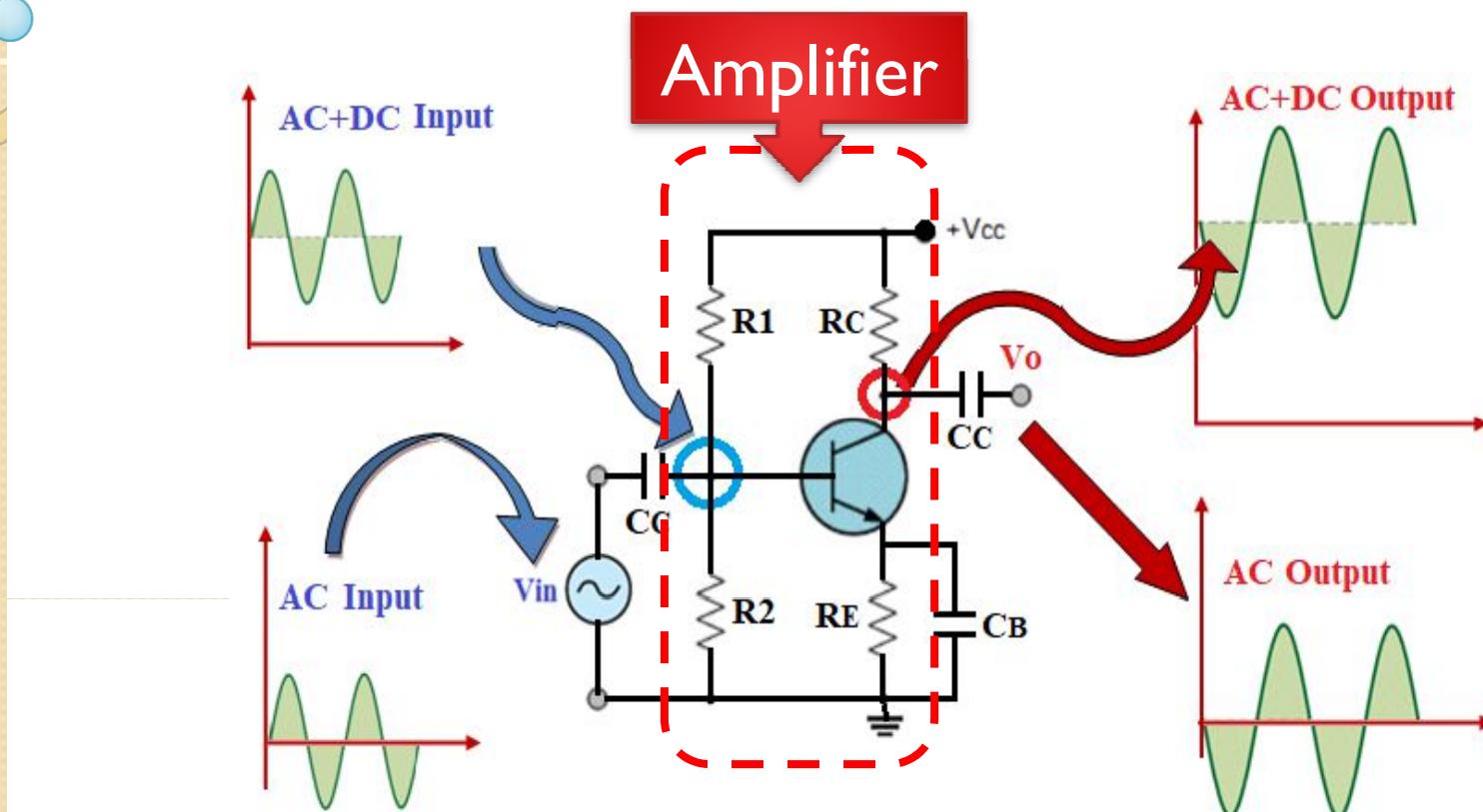
# BJT AMPLIFIERS Small signal analysis and design

1. Introduction
2. Two-port system
3. BJT configurations
4. BJT Small signal models
5. Hybrid  $\pi$  model
6. Circuit model of a voltage amplifier
7. App 1: C-E Fixed bias amplifier

# Introduction



# Introduction



## Introduction

Amplifier

**Large signal  
Analysis**

**Best Q, Maximum swing  
Avoid distortions**

**DC+AC  
Analysis**

**Small signal  
Analysis**

**Find: Parameters of the  
amplifier  
Gain in voltage, Gain in  
current, impedances**

**AC  
Analysis**



## Introduction

**Small signal  
Analysis**

1

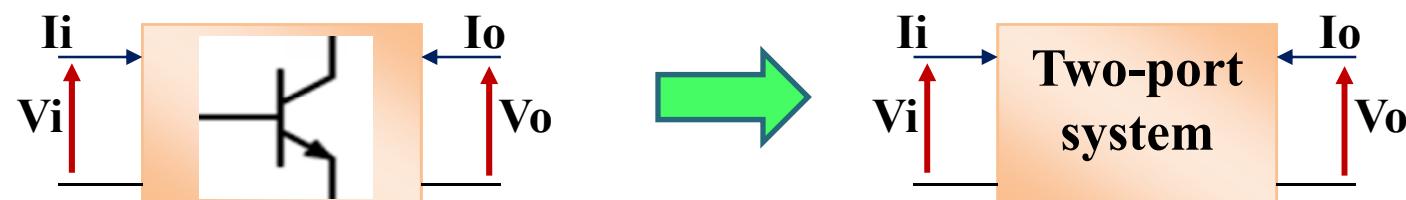
**Find Small signal  
models for the BJT**

2

**Find Small signal  
models for the  
Amplifier**

## Introduction

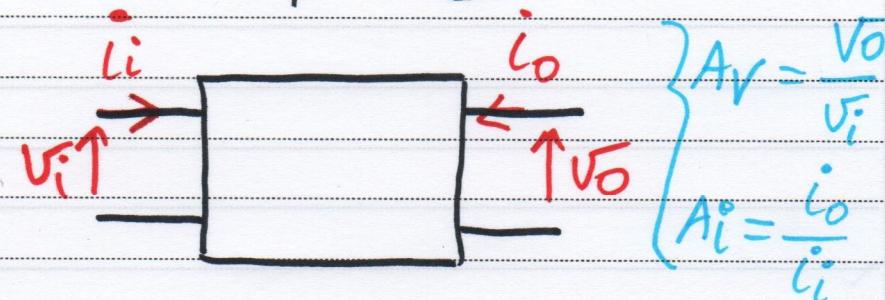
- ✓ Small signal models is an equivalent circuit (**two port system**) that represents the AC characteristics of the transistor (Amplifier).
- ✓ A model uses circuit elements that approximate the behavior of the transistor.



## BJT AMPLIFIERS Small signal analysis and design

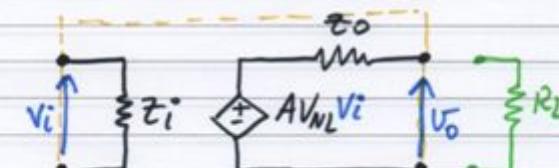
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two port system



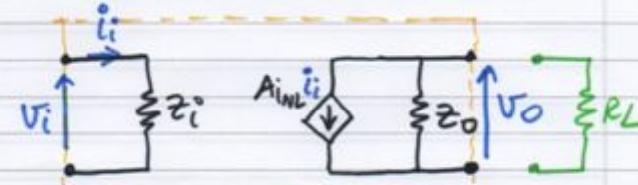
$$\left. \begin{array}{l} A_v = \frac{v_o}{v_i} \\ A_{i_o} = \frac{i_o}{i_i} \end{array} \right\}$$

BJT Amplifier using  
voltage dep. source



$A_{VNL}$ : is The No loaded gain  
in Voltage.

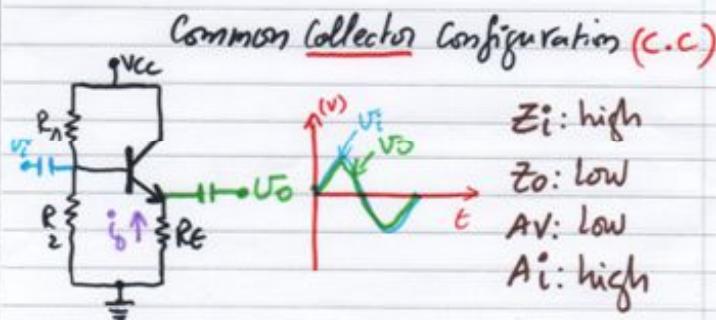
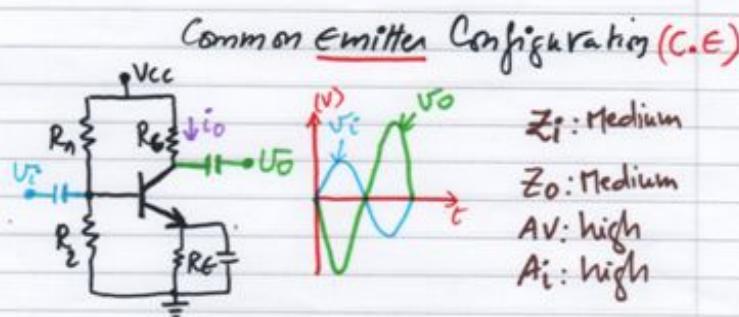
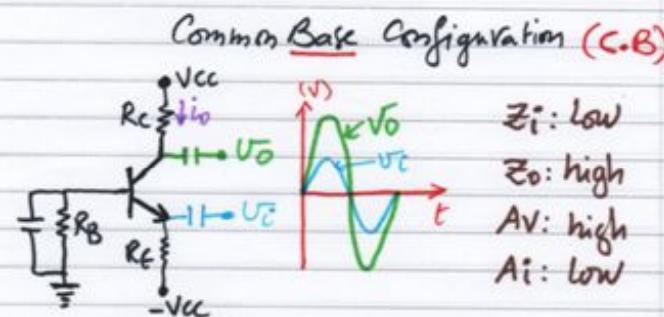
BJT Amplifier using  
current dep. source



$A_{iNL}$ : is The No loaded gain  
in current.

## BJT AMPLIFIERS Small signal analysis and design

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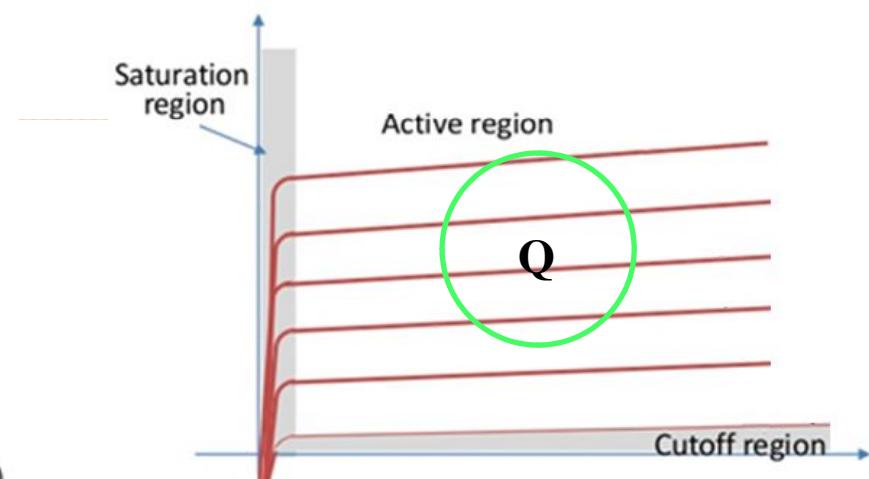
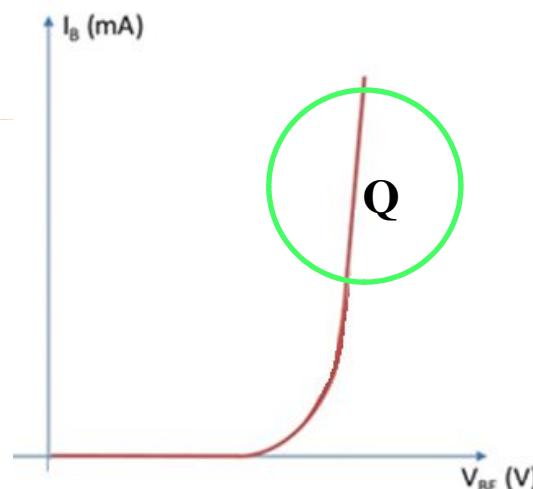


## BJT AMPLIFIERS Small signal analysis and design

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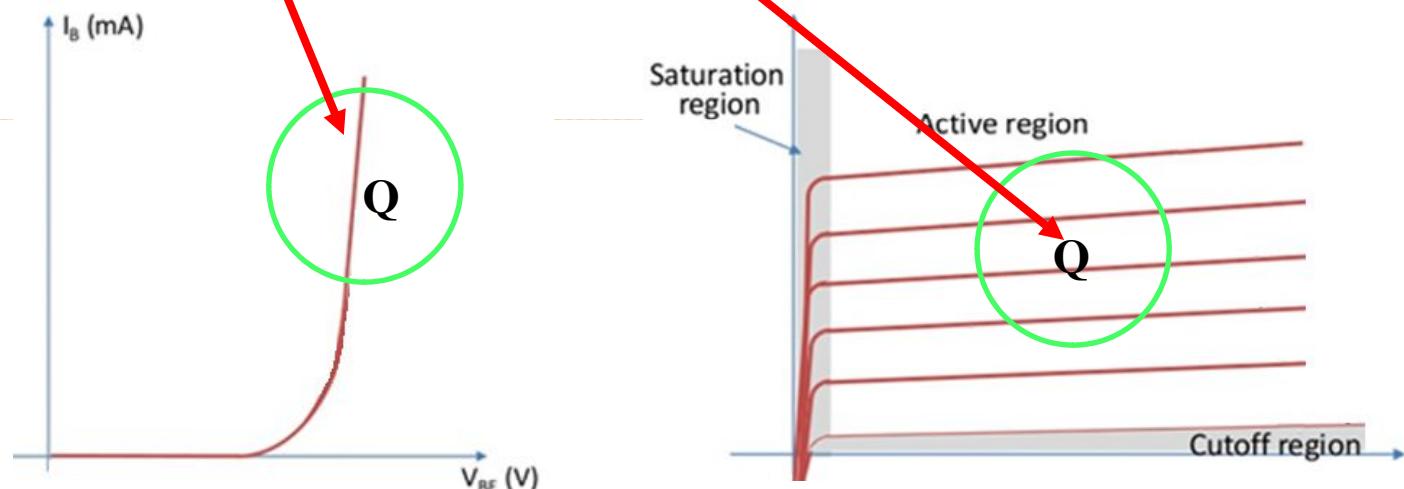
## Small signal models

**Small signal models for the BJT take advantage of the relative linearity of the base and collector curves in the area or locality of an operating point**



## Small signal models

Small signal models for the BJT take advantage of the relative linearity of the base and collector curves in the area or locality of an operating point



## Small signal models

There are two models commonly used in small signal AC analysis of a transistor:

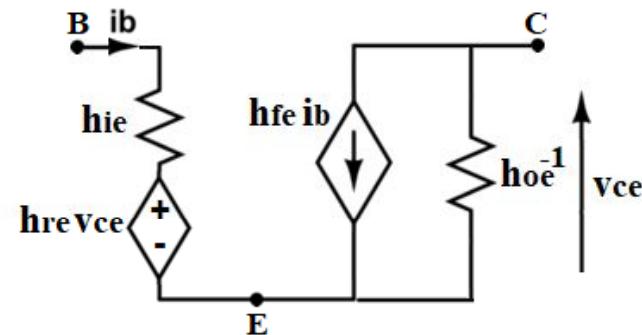
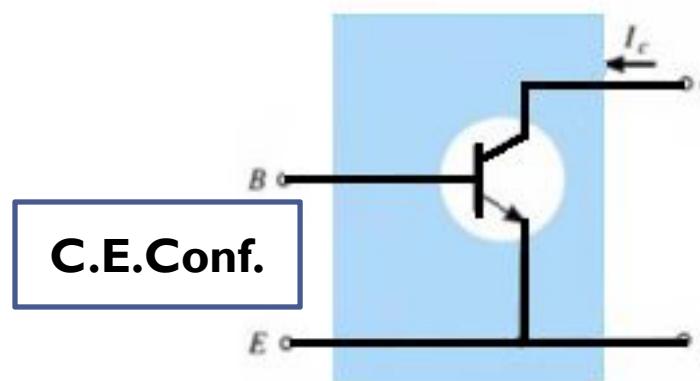
- Hybrid  $\pi$  equivalent model.
- $r_e$  model.

## BJT AMPLIFIERS Small signal analysis and design

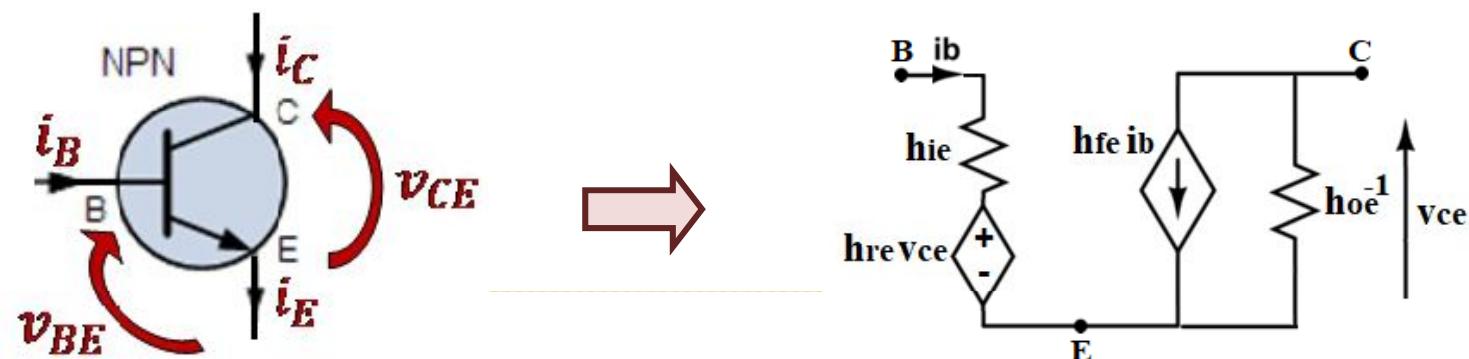
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➤ Hybrid  $\pi$  model.

The parameters can  
be found on the  
specification sheet  
of the transistor.



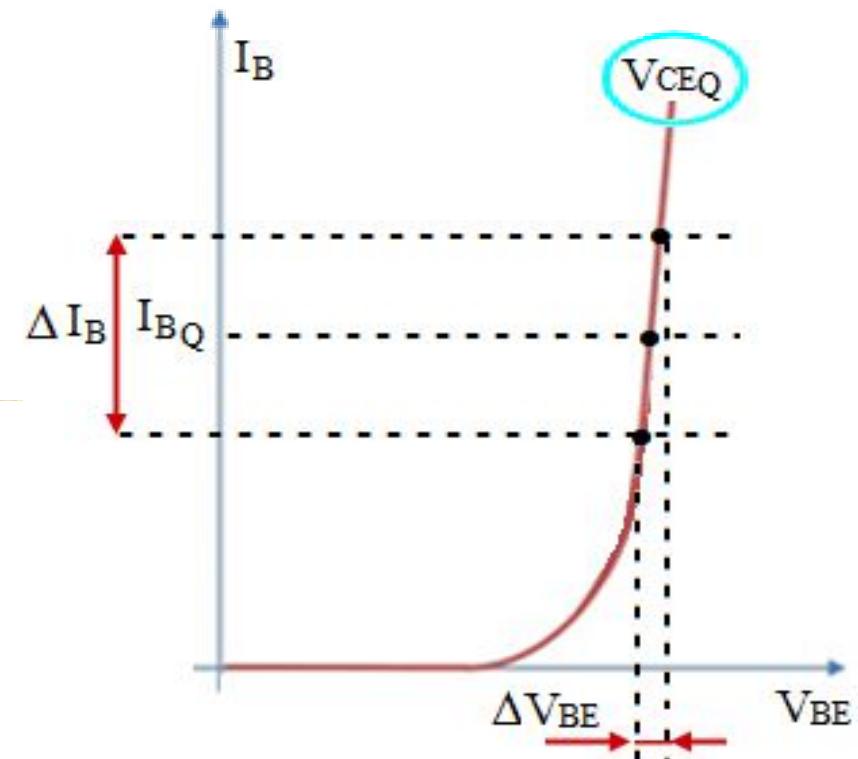
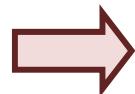
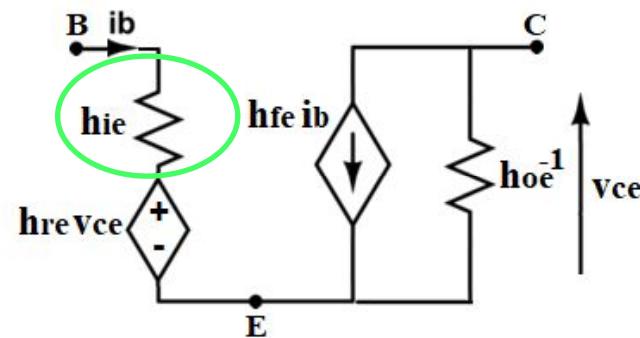
➤ Parameters of the **Hybrid** model.



➤ Parameters of the **Hybrid** model.

- Input impedance  $h_{ie}$

$$h_{ie} = \frac{\Delta v_{BE}}{\Delta i_B} \Big|_{V_{CEQ}}$$



➤ Parameters of the Hybrid model.

hie??

$$hie = \frac{\Delta V_{BE}}{\Delta I_B} |_{I_B}$$

$$I_B = I_s e^{\frac{V_{BE}}{V_T}}$$

$$\frac{\Delta I_B}{\Delta V_{BE}} = I_s e^{\frac{V_{BE}}{V_T}} |_{I_B}$$

↓

$$hie = \frac{\Delta V_{BE}}{\Delta I_B} = \frac{V_T}{I_B}$$

$$I_B = \beta$$

$$I_{CQ} = \frac{I_{CB}}{\beta} \approx \frac{I_{CQ}}{hie}$$

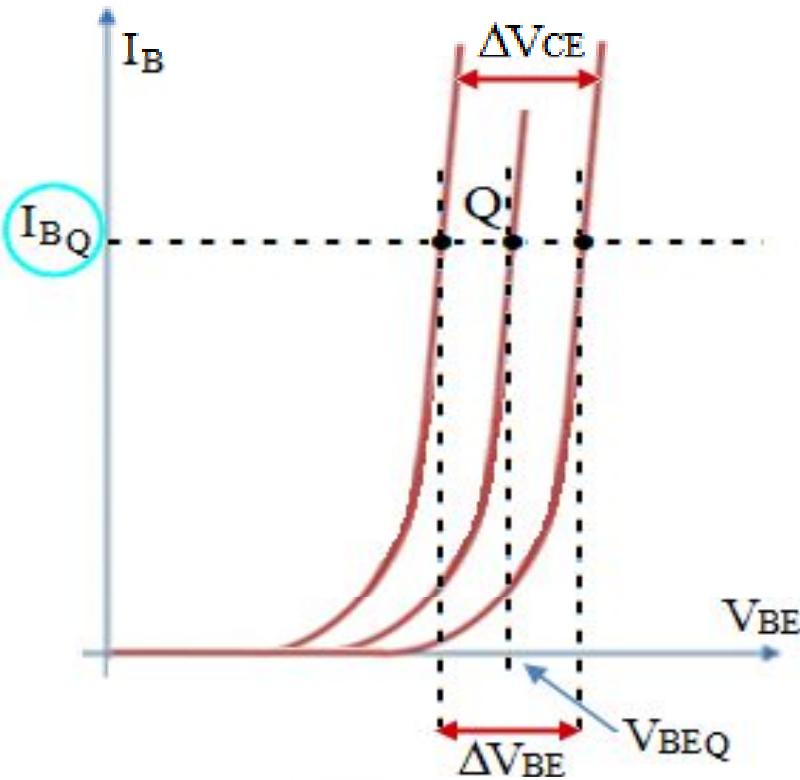
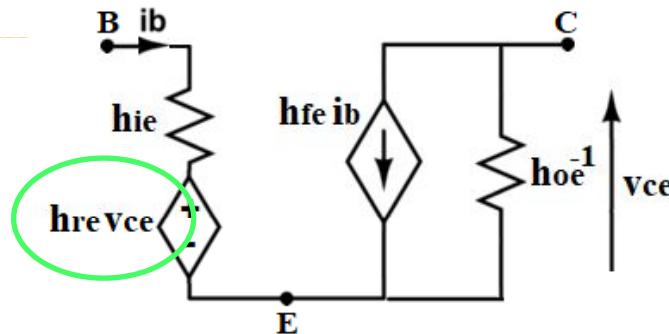
$$hie = h_f e \frac{V_T}{I_{CQ}}$$

V<sub>T</sub>: Thermal Voltage

➤ Parameters of the **Hybrid** model.

- Reverse voltage gain  $h_{re}$

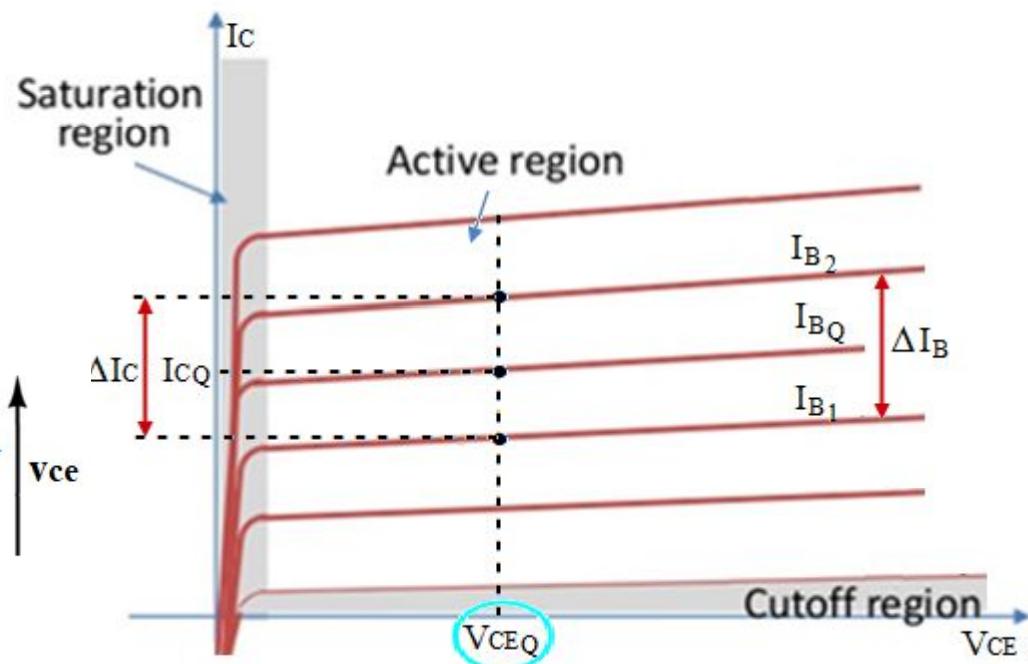
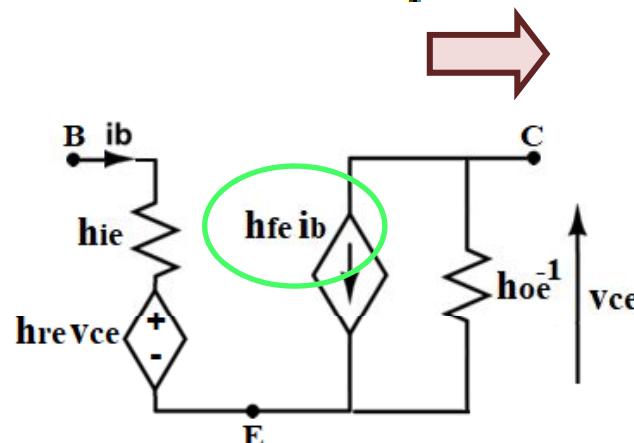
$$h_{re} = \frac{\Delta v_{BE}}{\Delta v_{CE}} \Big|_{I_{BQ}}$$



➤ Parameters of the Hybrid model.

- Forward current gain  $h_{fe}$

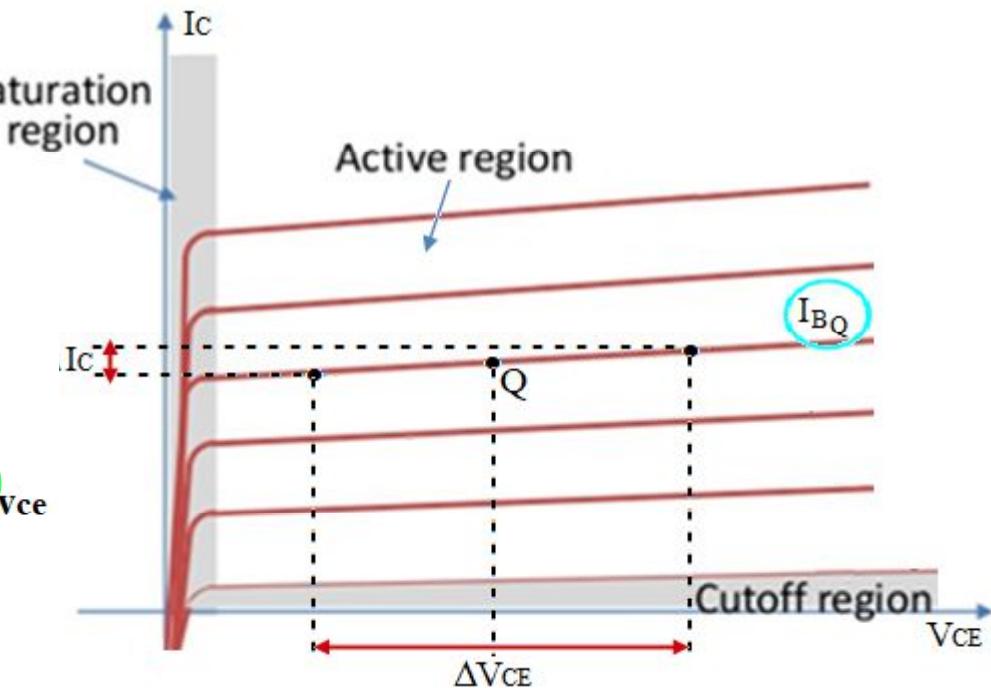
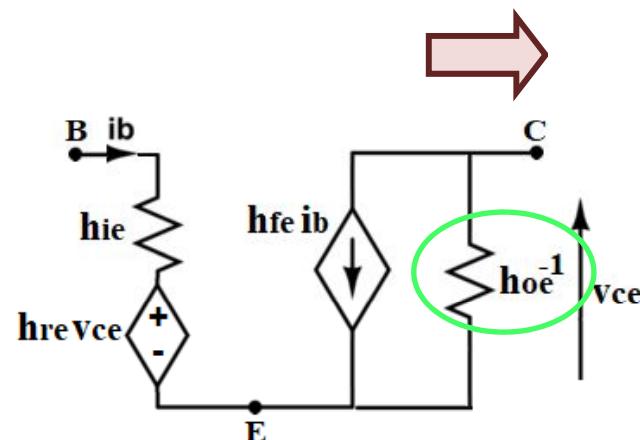
$$h_{fe} = \frac{\Delta i_C}{\Delta i_B} \Big|_{V_{CEQ}}$$



➤ Parameters of the **Hybrid** model.

- Output admittance  $h_{oe}$

$$h_{oe} = \frac{\Delta i_C}{\Delta v_{CE}} \Big|_{I_{BQ}}$$

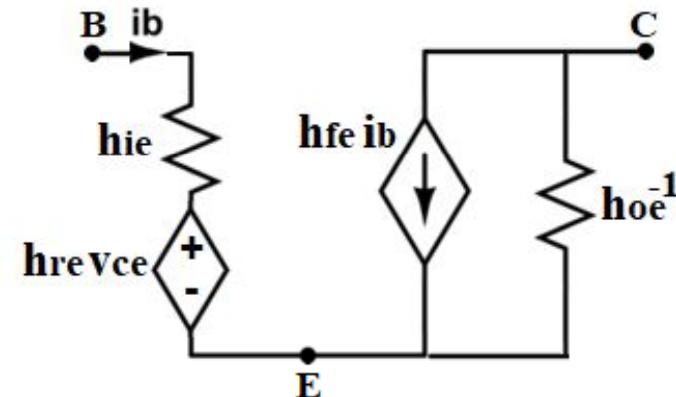


## Small signal models

### ➤ Example about Hybrid model

The hybrid parameters are drawn from the specification sheet for the 2N2222A BJT.

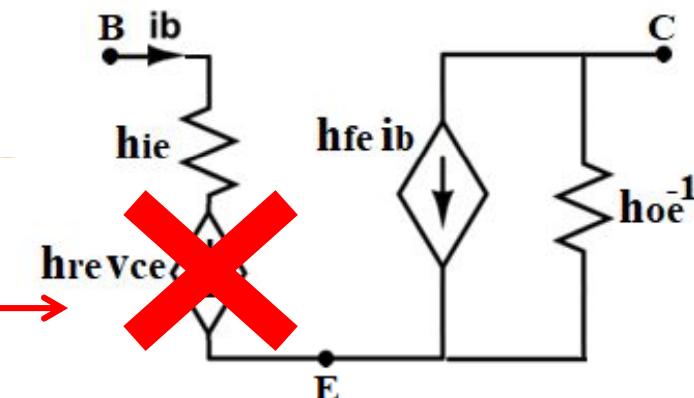
Parameter	Min	Max
$h_{ie}$ ( $K\Omega$ )	2	4
$h_{re} \times 10^{-4}$	-	8
$h_{fe}$	50	300
$h_{oe}$ ( $\mu S$ )	5	35



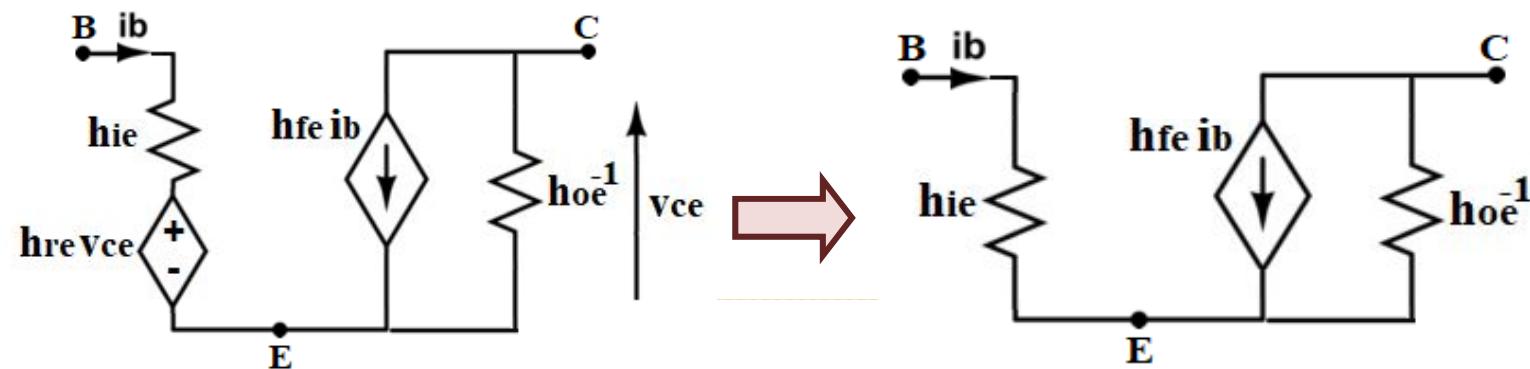
## ➤ Example about Hybrid model

The hybrid parameters are drawn from the specification sheet for the 2N2222A BJT.

Parameter	Min	Max
$h_{ie}$ ( $K\Omega$ )	2	4
$h_{re}$ ( $\times 10^{-4}$ )	—	8
$h_{fe}$	50	300
$h_{oe}$ ( $\mu S$ )	5	35



➤ Simplified hybrid model

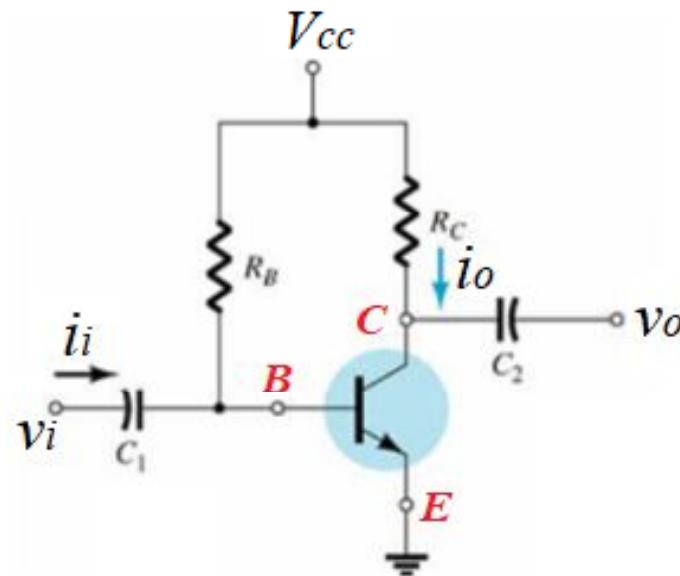


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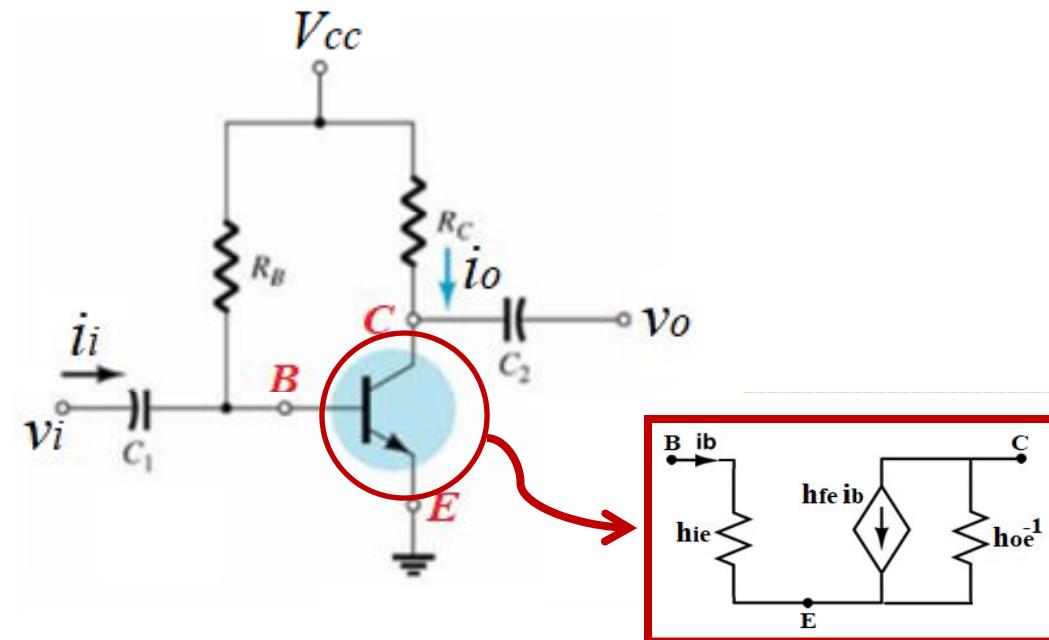
## Circuit model of a voltage amplifier

### ➤ Amplifier circuit



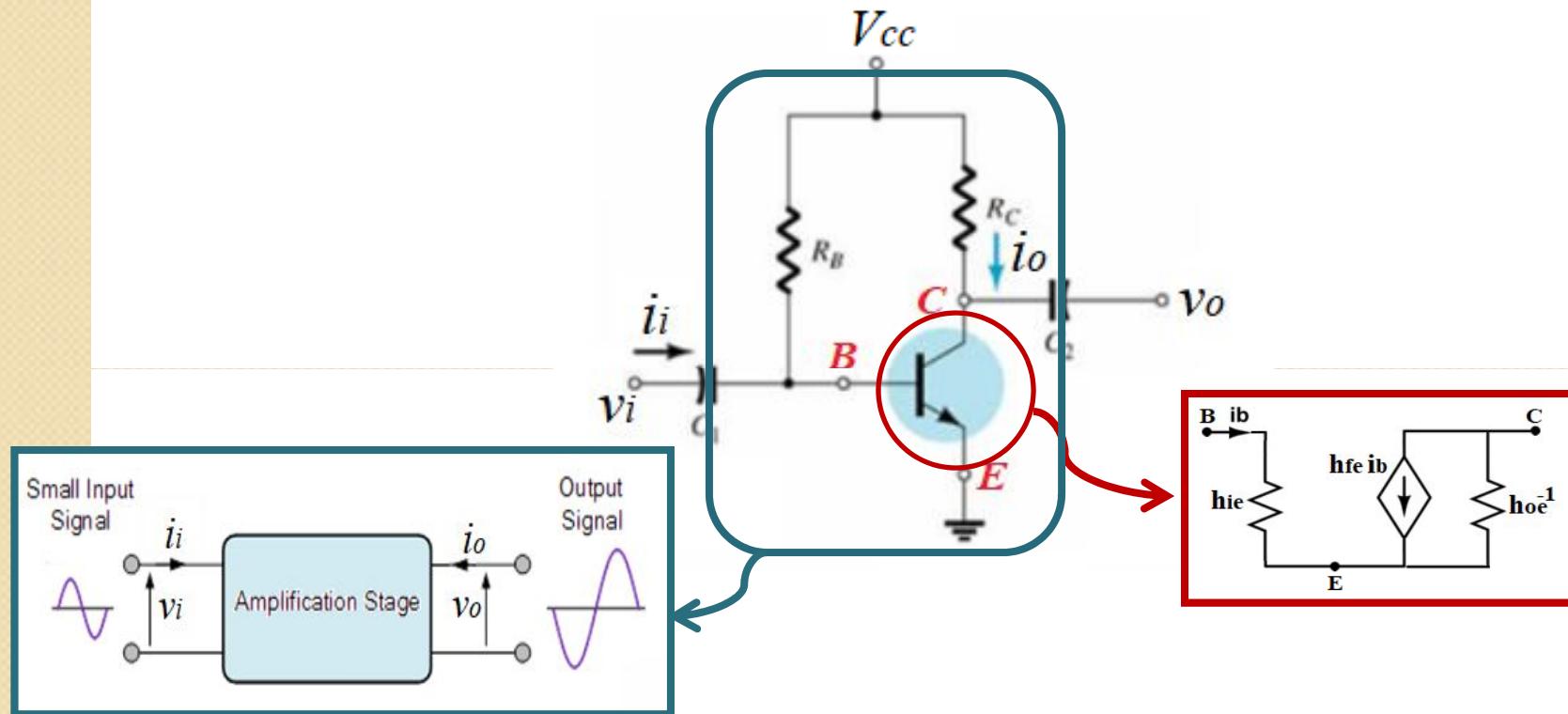
## Circuit model of a voltage amplifier

### ➤ Amplifier circuit



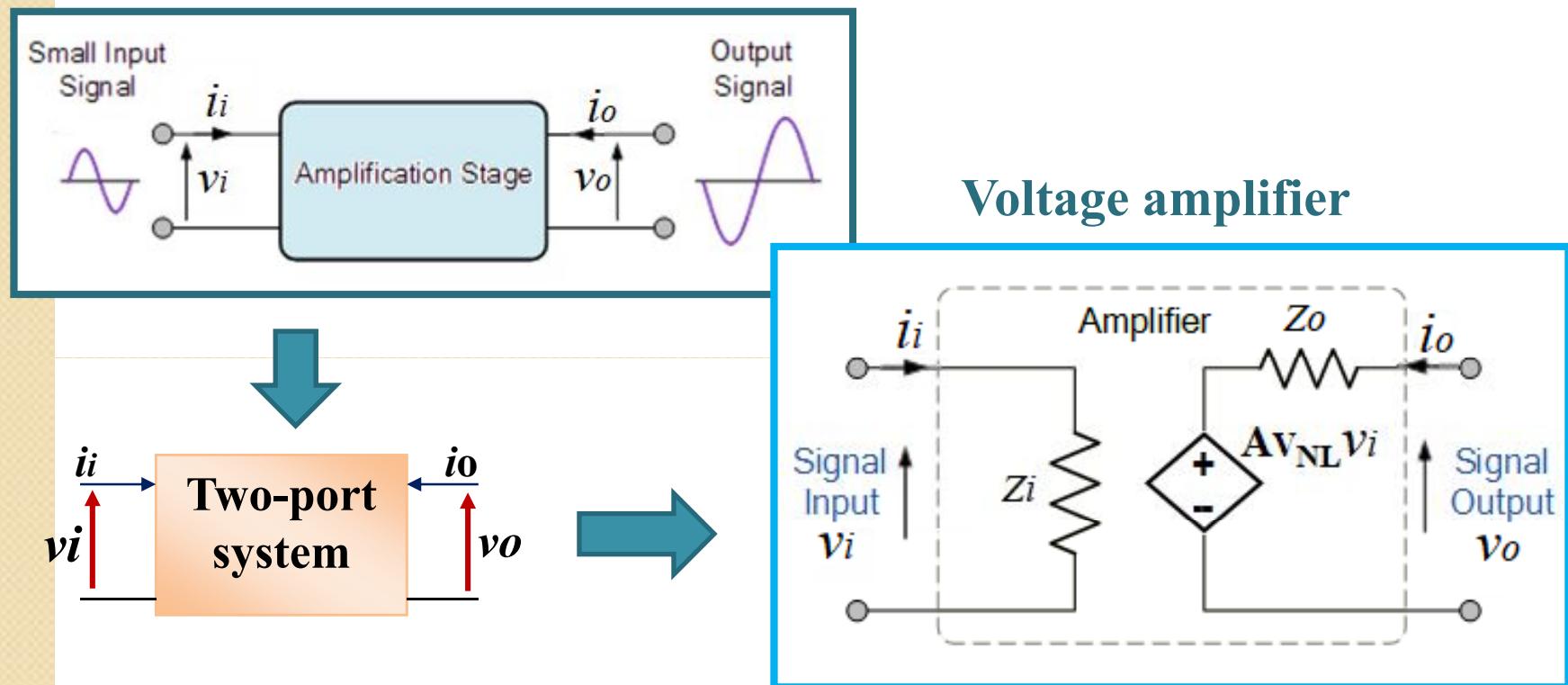
# Circuit model of a voltage amplifier

## ➤ Amplifier circuit



## Circuit model of a voltage amplifier

### ➤ Amplifier circuit

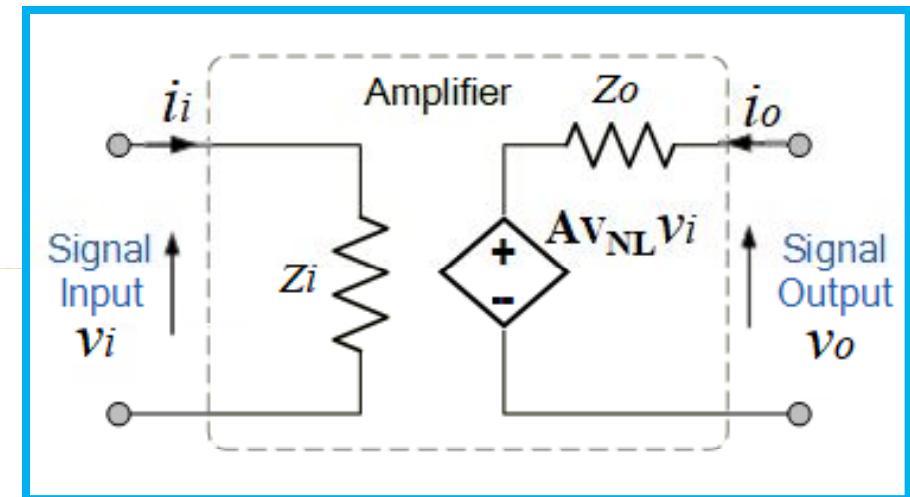


## Circuit model of a voltage amplifier

### ➤ Parametres of a voltage amplifier

***Input impedance:***  
 $Z_i = v_i / i_i$

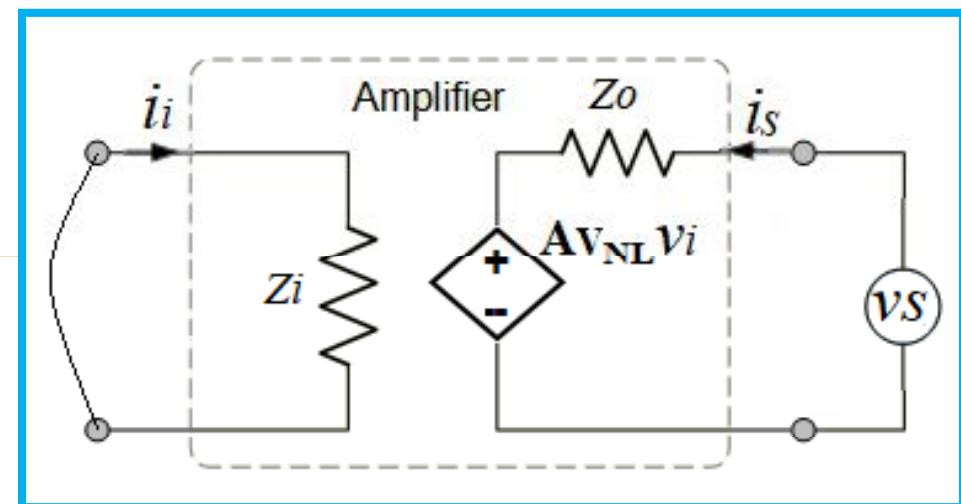
Voltage amplifier



## Circuit model of a voltage amplifier

### ➤ Parametres of a voltage amplifier

*Output impedance:*  
 $Z_o = v_s/i_s$  ( $v_i=0$ )



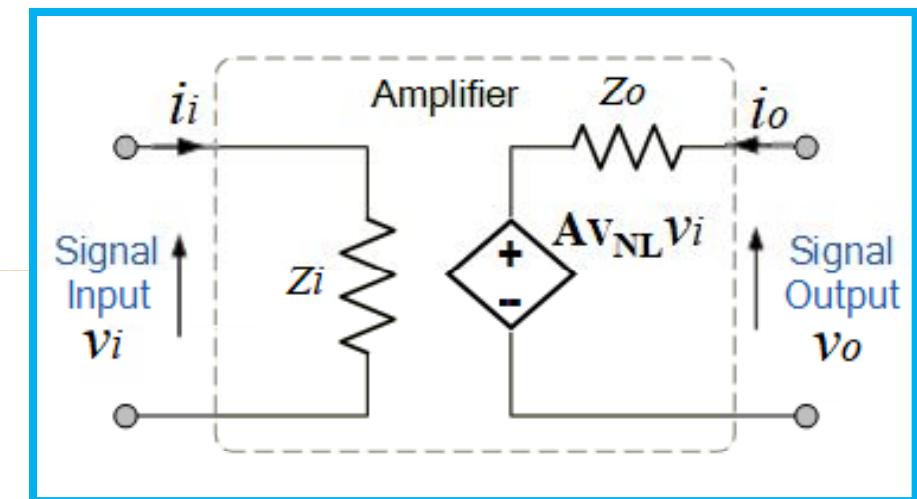
## Circuit model of a voltage amplifier

### ➤ Parametres of a voltage amplifier

*No loaded voltage*

*Gain: ( $R_L = \infty$ )*

$A_{VNL} = v_o/v_i$



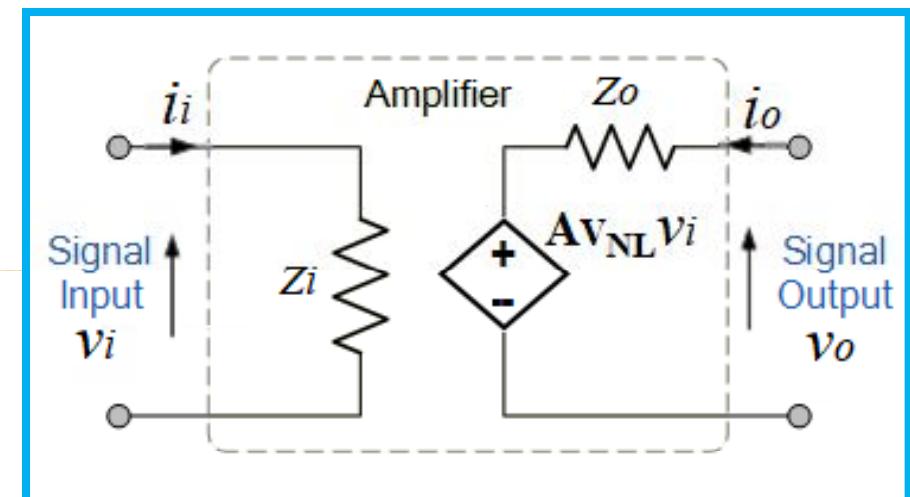
## Circuit model of a voltage amplifier

### ➤ Parametres of a voltage amplifier

*No loaded Current*

*Gain: ( $R_L=\infty$ )*

$$A_{iNL} = i_o / i_i$$



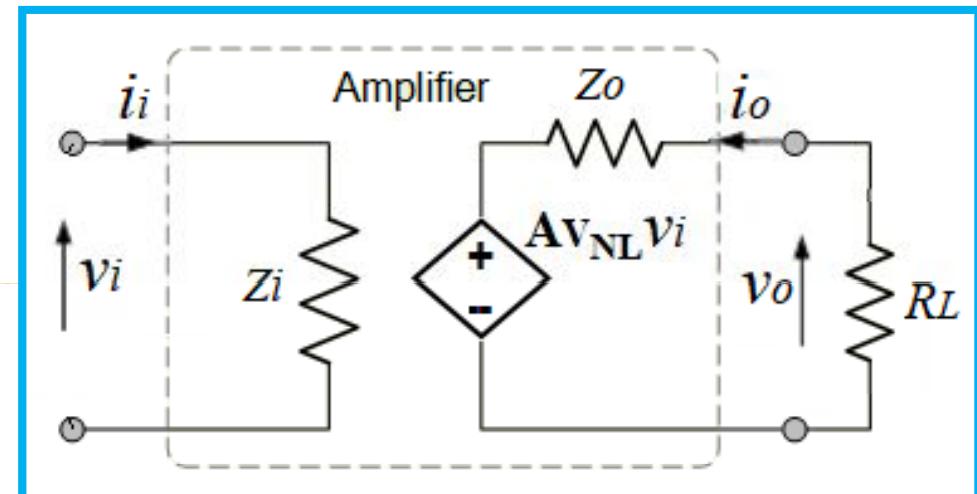
## Circuit model of a voltage amplifier

### ➤ Parametres of a voltage amplifier

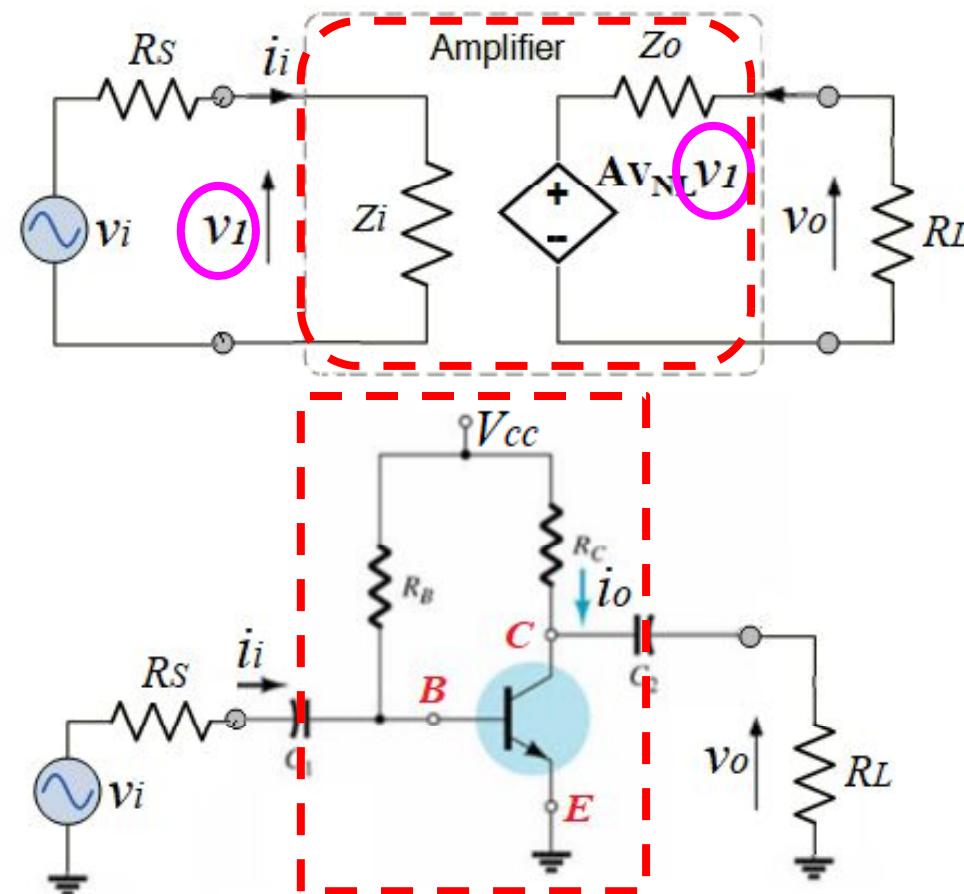
*Loaded voltage*

*Gain: ( $R_L \neq \infty$ )*

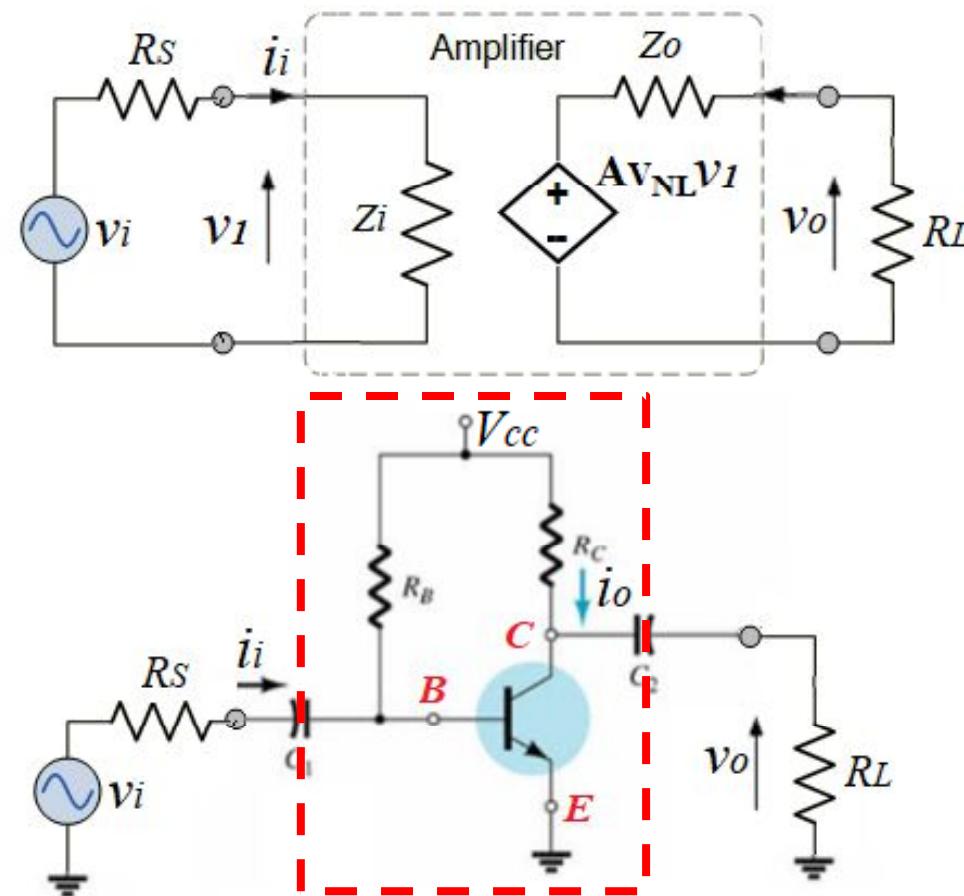
$A_v = v_o/v_i$



## Circuit model of a voltage amplifier



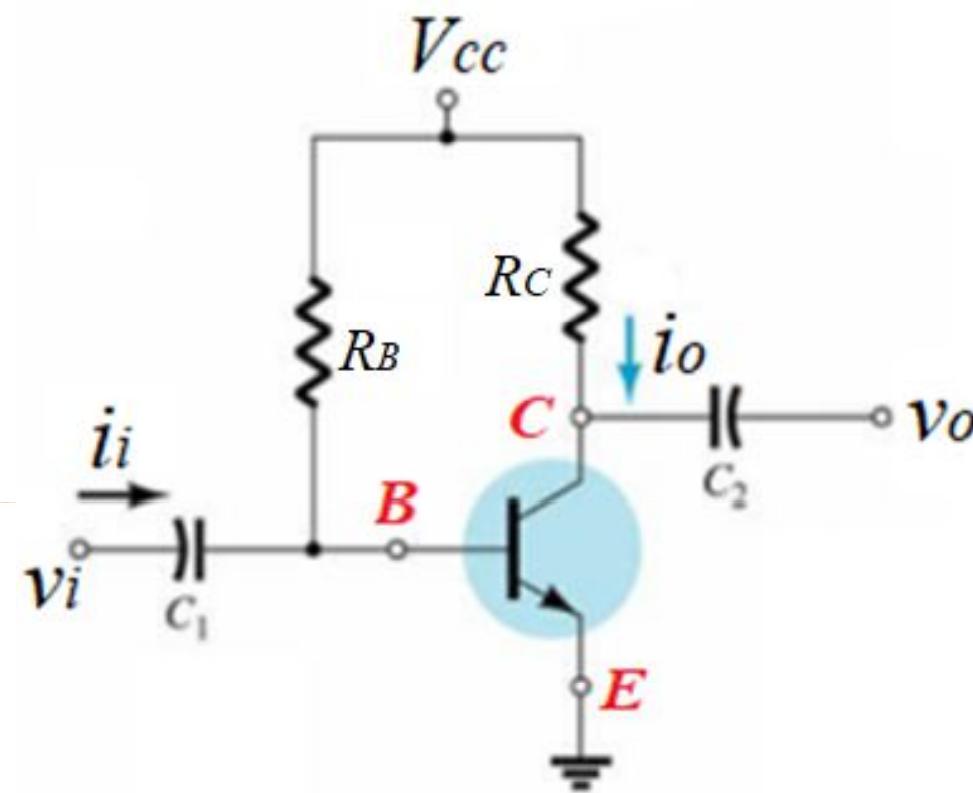
## Circuit model of a voltage amplifier



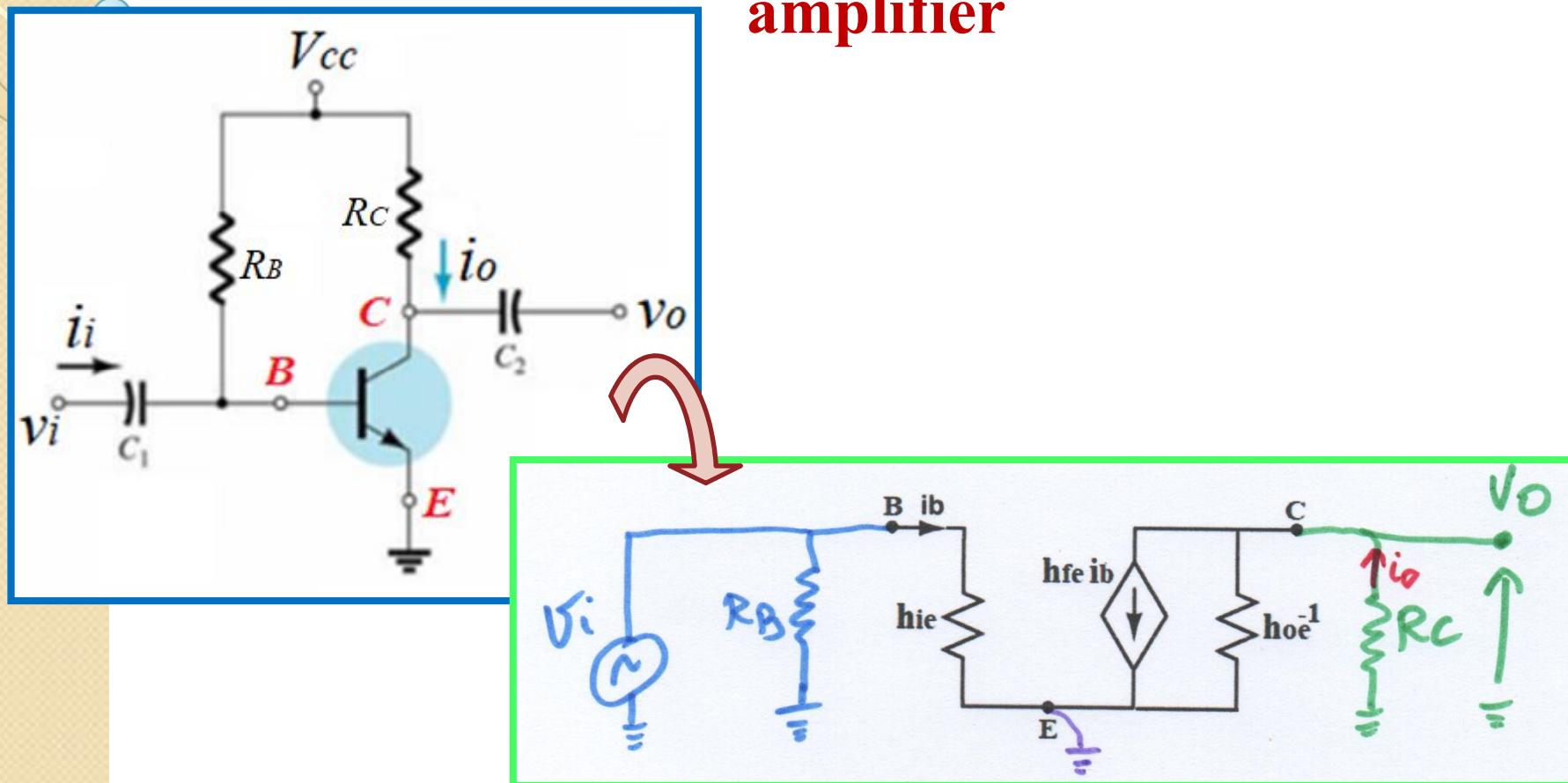
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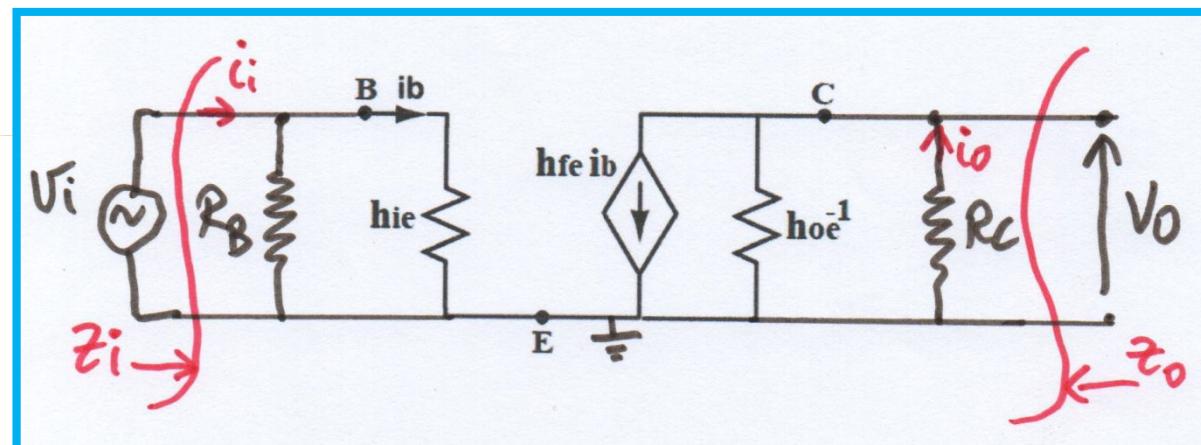
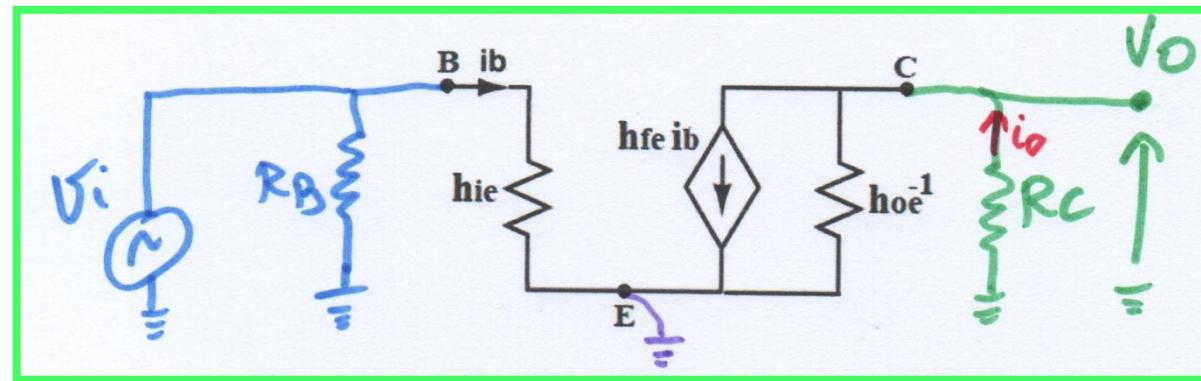
## App 1: Common Emitter Fixed bias amplifier



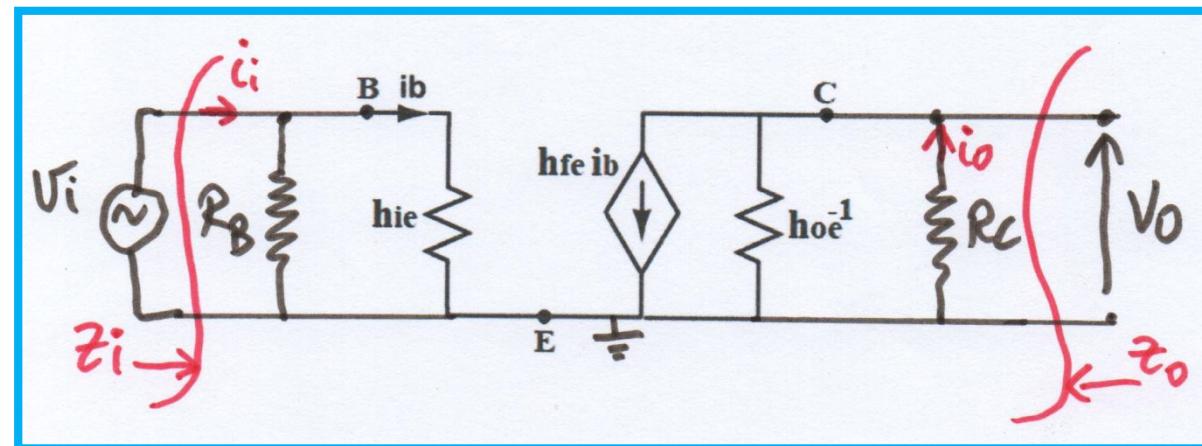
## App 1: Common Emitter Fixed bias amplifier



## App 1: Common Emitter Fixed bias amplifier



## App 1: Common Emitter Fixed bias amplifier



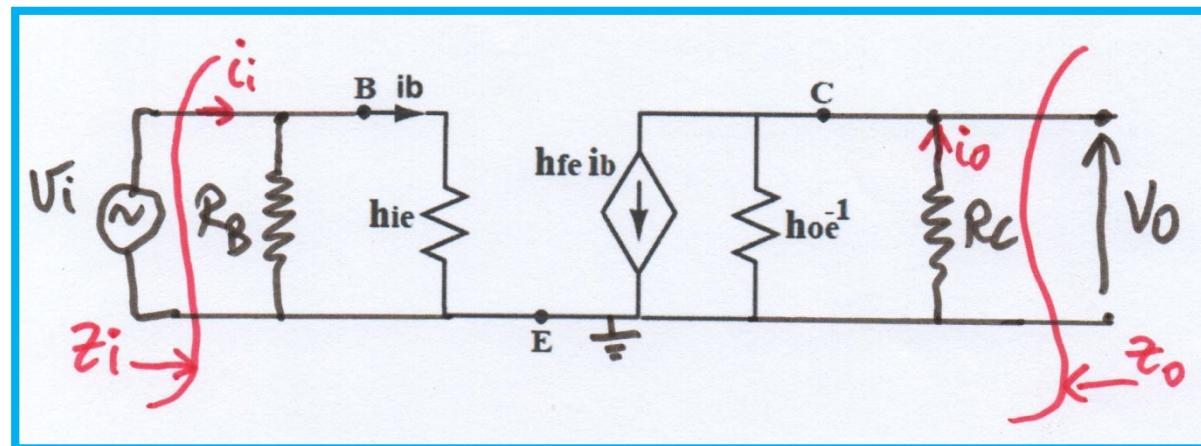
*Input impedance:*

$$Z_i = \frac{V_i}{i_i}$$

$$V_i = i_i (R_B // h_{ie}) \Rightarrow$$

$$Z_i = R_B // h_{ie}$$

## App 1: Common Emitter Fixed bias amplifier



*No loaded voltage Gain:*

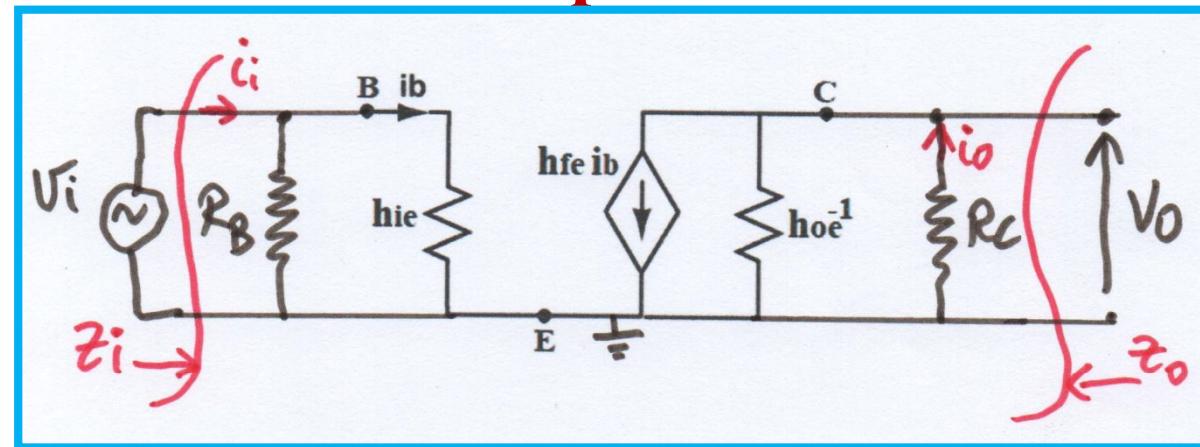
$$\underline{AV_{NL}} = \frac{V_o}{V_i}$$

$$V_i = h_{ie} i_b \dots \textcircled{1}$$

$$V_o = (R_C \parallel h_{oe}^{-1}) (-h_{fe} i_b)$$

$$V_o = - (R_C \parallel h_{oe}^{-1}) h_{fe} i_b \dots \textcircled{2}$$

## App 1: Common Emitter Fixed bias amplifier



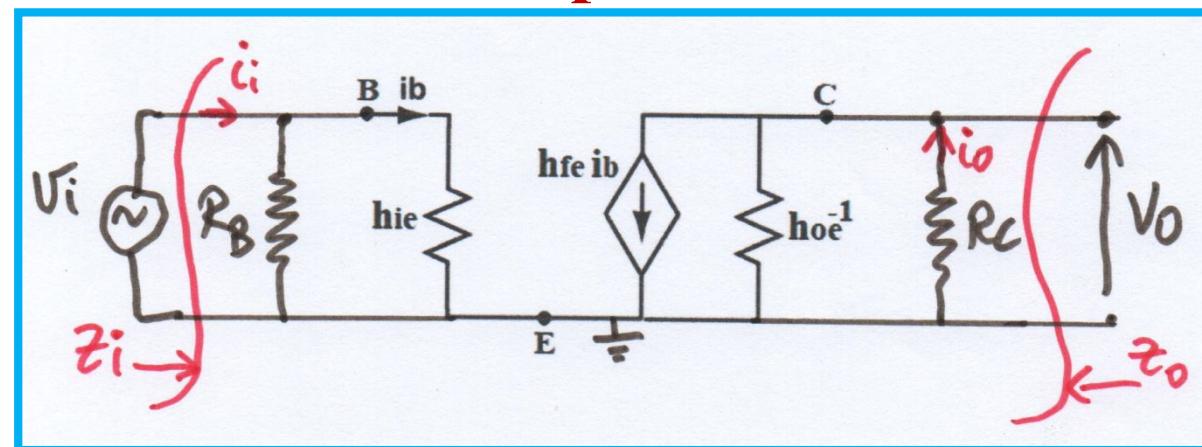
*No loaded voltage Gain:*

$$AV_{NL} = \frac{2}{1} = -\frac{(R_C \parallel h_{oe}^{-1}) h_{fe}}{h_{ie}}$$

$$AV_{NL} = -\frac{(R_C \parallel h_{oe}^{-1}) h_{fe}}{h_{ie}}$$

phase of  $180^\circ$  ( $V_i, V_o$ )

## App 1: Common Emitter Fixed bias amplifier



*No loaded Current Gain:*

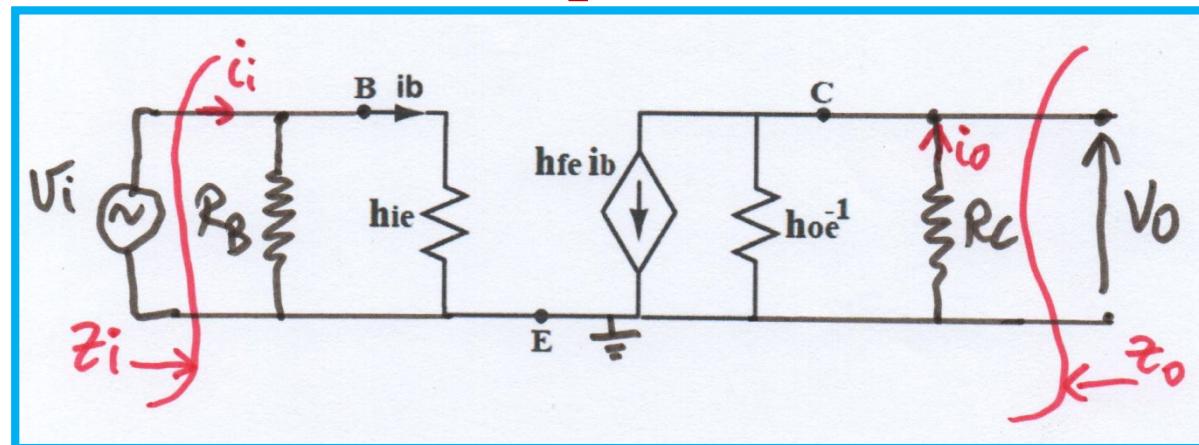
$$A_i = \dot{i}_o / \dot{i}_i$$

$$V_i = z_i \cdot \dot{i}_i = (R_B \parallel h_{ie}) \cdot \dot{i}_i$$

$$V_i = (R_B \parallel h_{ie}) \cdot \dot{i}_i \dots \textcircled{1}$$

$$V_o = -R_C \cdot \dot{i}_o \dots \textcircled{2}$$

## App 1: Common Emitter Fixed bias amplifier

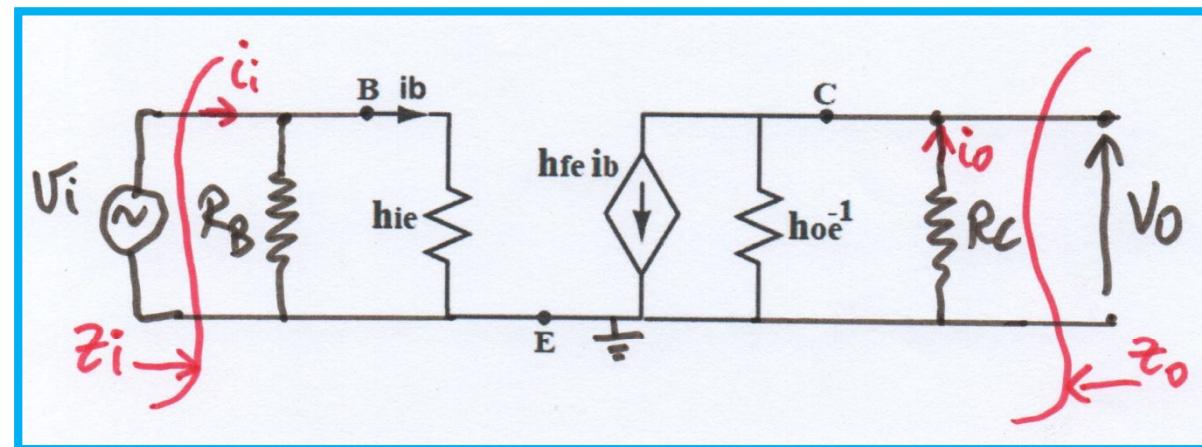


*No loaded Current Gain:*

$$\textcircled{1} \quad A_v = \frac{V_o}{V_i} = -\frac{R_C}{R_B \parallel h_{ie}} \frac{\dot{I}_O}{\dot{I}_I}$$

$A_{vNL}$        $A_I$

## App 1: Common Emitter Fixed bias amplifier

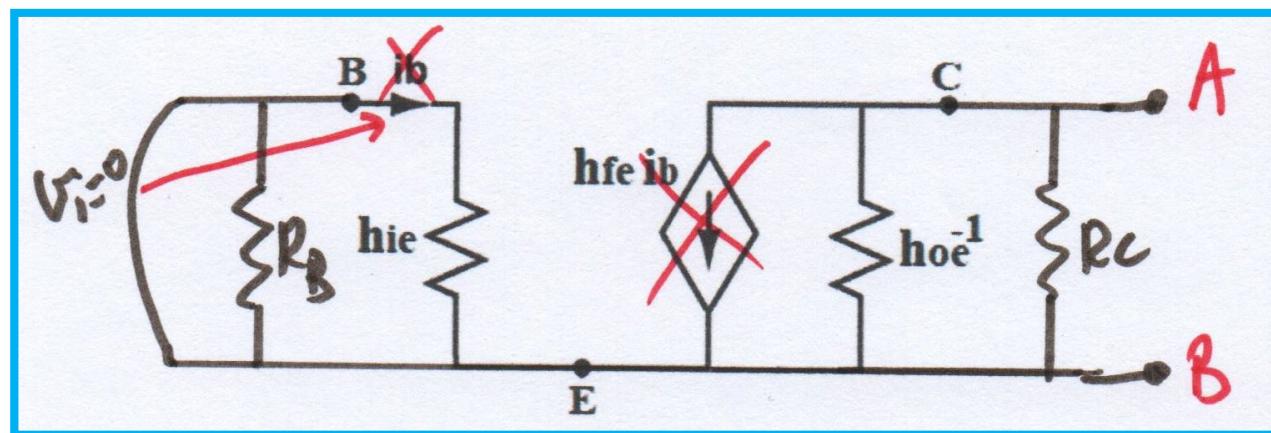


*No loaded Current Gain:*

$$A_i = - \frac{R_B \parallel h_{ie}}{R_C} A_{VNL}$$

$$A_{VNL} < 0, A_i > 0$$

## App 1: Common Emitter Fixed bias amplifier



*Output impedance:*

$$z_o = \frac{V_s}{i_s} \mid V_i = 0$$

if  $V_i = 0 \Rightarrow i_b = 0 \Rightarrow$

$$z_o = R_C \parallel h_{oe}^{-1}$$