Show all of your work on this assignment and answer each question fully in the given context.

Please staple your assignment!

- 1. Chapter 5, Exercise 35 (page 330)
- 2. Chapter 5, Exercise 37 (page 331)
- 3. Suppose that X and Y are two independent random variables with probability density functions given by:

$$f_X x = \begin{cases} 5e^{5x} & x > 0\\ 0 & \text{otherwise} \end{cases}$$

and

$$f_Y y = \begin{cases} 2e^{2y} & y > 0\\ 0 & \text{otherwise} \end{cases}$$

respectively.

Further, define random variable U as

$$U = \begin{cases} 1 & Y > X \\ 0 & \text{otherwise} \end{cases}$$

Meaning that if the observed value of the random variable Y is larger than the observed value of the random variable X then U = 1 and if the observed value of the random variable X is larger than the observed value of the random variable Y then U = 0.

- (a) Find the probability that X is greater than 3.
- (b) Find the probability that Y is greater than 3.
- (c) Provide the joint probability of (X, Y).
- (d) Find the probability that U = 1.
- 4. Suppose that Z_1, Z_2, \ldots, Z_n are n independent standard normal random variables. Find the expected value and variance of each of the following:
- 5. Find the expected value of variance of X where $X = 3Z_1 + 5$
- 6. Find the expected value of variance of Y where $Y = Z_1 Z_2$
- 7. Find the expected value of variance of U where $U = Z_1 Z_1$
- 8. Find the expected value of variance of W where $W = \sum_{i=1}^{n} \frac{i}{n} Z_i$

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