#### STAT 105 Exam I Reference Sheet

### Numeric Summaries

 $\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$ 

population standard deviation 
$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^{n} \left(x_i - \bar{x}\right)^2}$$

$$\sigma^2 = \frac{1}{n} \sum_{i=1}^{n} (x_i - \bar{x})^2$$

ard deviation 
$$\sigma = \sqrt{\epsilon}$$

deviation 
$$\sigma = \sqrt{}$$

sample variance 
$$s^2 = \frac{1}{n-1} \sum_{i=1}^n \left( x_i - \bar{x} \right)^2$$

sample standard deviation

$$s = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (x_i - \bar{x})^2}$$

## Linear Relationships

$$y \approx \beta_0 + \beta_1 x$$

Fitted linear relationship 
$$\hat{y} = b_0 + b_1 x$$

$$b_1 = \frac{\sum_{i=1}^{n} (x_i - \bar{x})(y_i - \bar{y})}{\sum_{i=1}^{n} (x_i - \bar{x})^2}$$

$$b_1 = \frac{\sum_{i=1}^n x_i y_i - n\bar{x}\bar{y}}{\sum_{i=1}^n x_i^2 - n\bar{x}^2}$$

$$b_0 = \bar{u} - b_1 \bar{x}$$

$$b_0 = \bar{y} - b_1 \bar{x}$$

Residuals 
$$e_i=y_i-\hat{y}_i$$
 sample correlation coeffecient 
$$r=\frac{\sum_{i=1}^n(x_i-\bar{x})(y_i-\bar{y})}{\sqrt{\sum_{i=1}^n(x_i-\bar{x})^2\sum_{i=1}^n(x_i-\bar{x})^2}}$$

Residuals

$$r = \frac{\sum_{i=1}^{n} x_i y_i - nxy}{\sqrt{\left(\sum_{i=1}^{n} x_i^2 - n\bar{x}^2\right)\left(\sum_{i=1}^{n} y_i^2 - n\bar{y}^2\right)}}$$

 $\sum_{i=1}^n x_i y_i - n \bar{x} \bar{y}$ 

coeffecient of determination 
$$R^2 = (r)^2$$

$$R^2 = \frac{\sum_{i=1}^{n} (y_i - \bar{y})^2 - \sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{\sum_{i=1}^{n} (y_i - \bar{y})^2}$$

# Multivariate Relationships

$$y \approx \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \ldots + \beta_k x_k$$

Fitted relationship 
$$\hat{y} \approx b_0 + b_1 x_1 + b_2 x_2 + \ldots + b_k x_k$$

relationship 
$$\hat{y} \approx b_0 + b_1 x_1 + b_2 x_2 +$$

$$e_i = y_i - \hat{y}_i$$

$$SSTO = \sum_{i=1}^{n} (y_i - \bar{y})^2$$

Sums of Squares

Residuals

$$SSE = \sum_{i=1}^{n} (y_i - \hat{y}_i)^2$$

$$SSR = SSTO - SSE = \sum_{i=1}^{n} (\hat{y}_i - \bar{y})^2$$

coeffecient of determination 
$$R^2 = \frac{\sum_{i=1}^{n} (y_i - \bar{y})^2 - \sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{\sum_{i=1}^{n} (y_i - \bar{y})^2}$$

$$R^2 = \frac{\text{SSTO} - \text{SSE}}{\text{SSTO}}$$

$$R^2 = rac{ ext{SSR}}{ ext{SSTO}}$$

$$R^2 = \frac{\sum_{i=1}^{n} (y_i - \bar{y})^2 - \sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{\sum_{i=1}^{n} (y_i - \bar{y})^2}$$

#### Functions

**Quantile Function** Q(p) For a dataset consisting of n values that are ordered so that  $x_1 \le x_2 \le \ldots \le x_n$  and value p where  $0 \le p \le 1$ , let  $i = \lfloor n \cdot p + 0.5 \rfloor$ . Then the quantile function at p is:

$$Q(p) = x_i + (n \cdot p + 0.5 - i)(x_{i+1} - x_i)$$