

PROBABILITY ASSIGNMENT

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1 problem

Two dice are Thrown Simultaneously. if X denotes the number of sixes, find the expectation of X.

The Expectation of X=Mean of the variable X

$$E(X) = \mu = \sum_{i=1}^{n} x_i P(x_i)$$
 (4)

2 solution

Consider each trial results in sucess(getting six on a dices) or failures (not getting sixes on disces)

So,

X may have value 0,1,or 2

Total number of possible outcomes = 36

Number of outcomes n = 2

When a two discs are rolled Once,

$$\mu = 0 \times^{2} C_{0}(\frac{5}{6})^{2} + 1 \times^{2} C_{1}(\frac{5}{36}) + 2 \times^{2} C_{2}(\frac{1}{6})$$
(5)

Mean of
$$X = \mu = \frac{1}{3}$$
 (6)

Probability (p) =
$$\frac{1}{6}$$
 (1)

so,

$$q = 1 - p = 1 - \frac{1}{6} = \frac{5}{6} \tag{2}$$

In Bernoulli trials with X sucess and (n-x) failures, the probability of x sucess in n-Bernoulli trilas can be given as,

$$^{n}C_{x}P^{x}q^{n-x} \tag{3}$$

Therefore, The required probability distribution as follows

X	0	1	2
P(X)	${}^nC_0P^0q^n$	${}^nC_1P^1q^{n-1}$	${}^nC_2P^2q^{n-2}$
P(X)	${}^{2}C_{0}(\frac{5}{6})^{2}$	${}^{2}C_{1}(\frac{5}{26})$	${}^{2}C_{2}(\frac{1}{6})$