



PROBABILITY ASSIGNMENT

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1 problem

Two dice are thrown simultaneously. If X denotes the number of sixes, find the expectation of X .

2 solution

consider each trial results in success (getting six on a dice) or failures (not getting sixes on dices)

so,

X may have value 0, 1, or 2

Total number of possible outcomes = 36

number of outcomes $n = 2$

when a two dice are rolled once,

probability $P = \frac{1}{6}$

so, $q = 1 - P = 1 - \frac{1}{6} = \frac{5}{6}$

In Bernoulli trials with X success and $(n - x)$ failures, the probability of x success in n Bernoulli trials can be given as,

$${}^nC_x P^x q^{n-x} \quad (1)$$

Therefore, The required probability distribution as follows

X	0	1	2
$P(X)$	${}^nC_0 P^0 q^n$	${}^nC_1 P^1 q^{n-1}$	${}^nC_2 P^2 q^{n-2}$
$P(X)$	${}^2C_0 (\frac{5}{6})^2$	${}^2C_1 (\frac{5}{6})$	${}^2C_2 (\frac{1}{6})^2$

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The Expectation of X = Mean of the variable X

$$E(X) = \mu = \sum_{i=1}^n x_i P(x_i)$$

$$\mu = 0 \times {}^2C_0 (\frac{5}{6})^2 + 1 \times {}^2C_1 (\frac{5}{6}) + 2 \times {}^2C_2 (\frac{1}{6})^2$$

$$\text{Mean of } X = \mu = \frac{1}{3}$$