Experiment No: 01

Experiment Name: Find out the point estimate of the population mean and interval estimation of the population mean. where 30 students quiz test marks is

(2, 4, 3, 23, 25, 27, 28, 13, 15, 16, 20, 14, 35, 33, 32, 21, 35, 40, 42, 22, 33, 13, 17, 20, 25, 29, 27, 40, 38, 31).

Total marks 50. Here population size N=30 and sample size n=10.

Also illustrate the sample size determination, sampling distribution for mean and check the unbiasednes of the population mean.

Objectives:

1. To calculate the point estimation and interval estimation.

2. To calculate sampling distribution for mean.

3. To check the unbiasedness of the population mean.

4. To comment on the data.

Procedure:

Step-1: First of all we find out the population mean and population variance. Population length is N.

$$\text{mean}, \ \bar{x} = \frac{\Sigma x_i}{N}$$

$$\text{variance}, \ s^2 = \frac{1}{N-1}\left[\Sigma x_i^2 - \frac{(\Sigma x_i)^2}{N}\right]$$

Step-2: To calculate point estimation and interval estimation.

interval estimation:

$$\left(\bar{x} - z_{\alpha/2}\frac{\sigma}{\sqrt{n}}, \ \bar{x} + z_{\alpha/2}\frac{\sigma}{\sqrt{n}}\right)$$

Step-3: Sampling Distribution for mean.
We choose the sample size $n=10$ from the population size $N=30$
Then we calculate the mean and unbiasedness.

bias = mean(nsample) - mean(population)

= 0

When bias is 0 then we can say the mean is unbiasedness.

Step-4: Sampling Distribution for median. We choose the sample size $n=10$ from the population size $N=30$
The we calculate the median and unbiasedness.

bias = median(nsample) - median(population)

When bias is 0 then we can say the median is unbiasedness.

step-5: Efficiency check

we calculate the mean and the median of sampling distribution.

Mean and median to be two unbiased estimator then which variance is ~~more~~ less than other then we say that this is more efficient than other.

R-Source code:

```
IQ<-c(2,4,3,23,25,27,28, 13,15,16,20,14,
35,33,32,21,35,40,42,22,33,13,17,20,25,
29,27,40,38,31)
mean(IQ)
var(IQ)
length(IQ)

set.seed(1246)
x<-sample(IQ,10, replace=TRUE)
mean(x)
sd(IQ)

qnorm(0.025,0,1)
```

```
## lower class interval

21.6 -((1.96*11)/sqrt(10))

## upper class interval

21.6 + ((1.96*11)/sqrt(10))

##Sampling Distribution for mean

choose (30,10)
nsample <- req(0, 300000)
for(i in 1:300000){
    nsample [i] <- (mean(sample (IQ, 10,
                    replace = TRUE)))

}
mean(nsample)
bias = mean(nsample) - mean(IQ)

## Sampling Distribution for median

choose(30,10)
nsample2 <- req(0,300000)
for (i in 1:300000){
    nsample[i] <- (median(sample (IQ,10,
                    replace = TRUE)))

}
```

```
median(IQ)
median(nsample2)
bias = median(nsample2)-median(IQ)

### Efficiency check ###
L1<-length(nsample)
V1<-Sum((nsample-mean(IQ))^2)/L1
V1
L2<-length(nsample2)
V2<-Sum((nsample2-median(IQ))^2)/L2
V2
```

Input and output:

```
mean(IQ) = 24.1
var(IQ) = 121.2655
length(IQ) = 30
mean(x) = 21.6
sd(IQ) = 11.012
qnorm = -1.96
14.78  # lower class interval
28.41  # upper class interval
```

mean(nsample) = 24.097

bias = -0.0024

median(IQ) = 25

median(nsample2) = 25

bias = 0

L1 = 300000

V1 = 11.69

L2 = 300000

V2 = 19.97

Comment : From the R code we can see that the mean is a unbiased estimator and the median also unbiased estimator. The variance of ~~mean is~~ nsample is less then the variance of nsample2. So, the mean is more efficient ~~the~~ than median.

Experiment No: 02

Experiment Name: Two dice rolled, S is the sum of both faces, Find the expectation of S, E(S) and variance of S, V(S). Plot the distribution of S and dice D.

Objectives:

1. To find the expectation of S.
2. To find the variance of S.
3. To plot the distribution of S and dice D.
4. To comment on the data.

Procedure:

step-1: Two dice rolled, S is the sum of both faces. To calculate the expectation of S, E(S).

Step-2: To calculate the variance of S, V(S).

$$V(S) = \frac{\left[\Sigma x_i^2 - \frac{(\Sigma x_i)^2}{n}\right]}{n-1}$$

Step-3: To plot the distribution of S and dice D.

R- Source code:

```
S<- 2:12
A <-c(1:6,5:1)
PS<-C(1:6,5:1)/36
ES<-Sum (S*PS)
varS<-Sum((S-C(ES))^2*PS)

## plot distribution of S
barplot (PS, ylim=c(0,0.2),
         ylab="Probability",
         xlab="S",
         col=" steelblue",
         Space=0,
         main="Sum of two dice rolls")
```

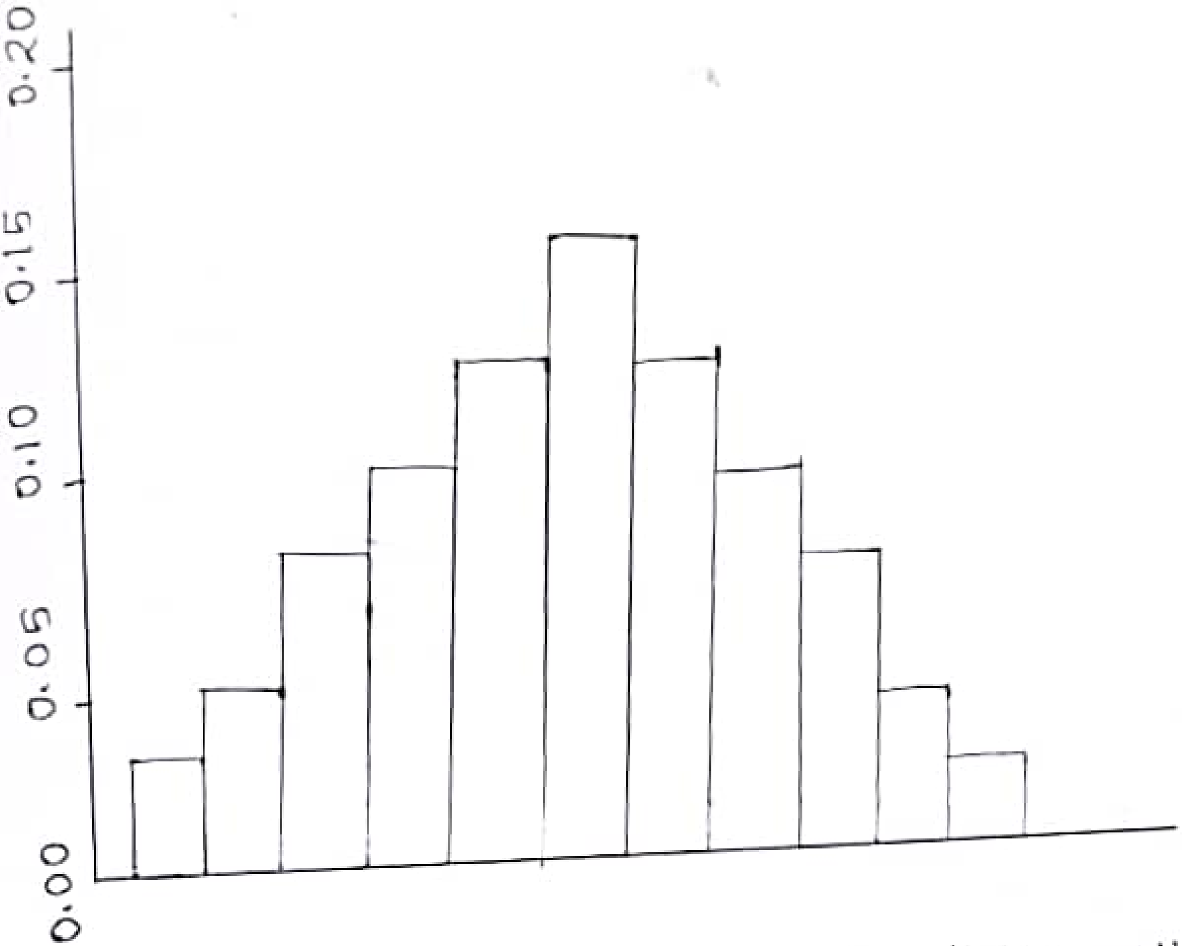
```
### plot distribution of D
Probability <- rep(1/6,6)
names(Probability) <-1:6

barplot(probability,
        ylim=c(0,0.2),
        xlab = "D"
        col = "steelblue",
        Space = 0,
        main= "outcomes of a single
                         dice roll")
```

Input and output:

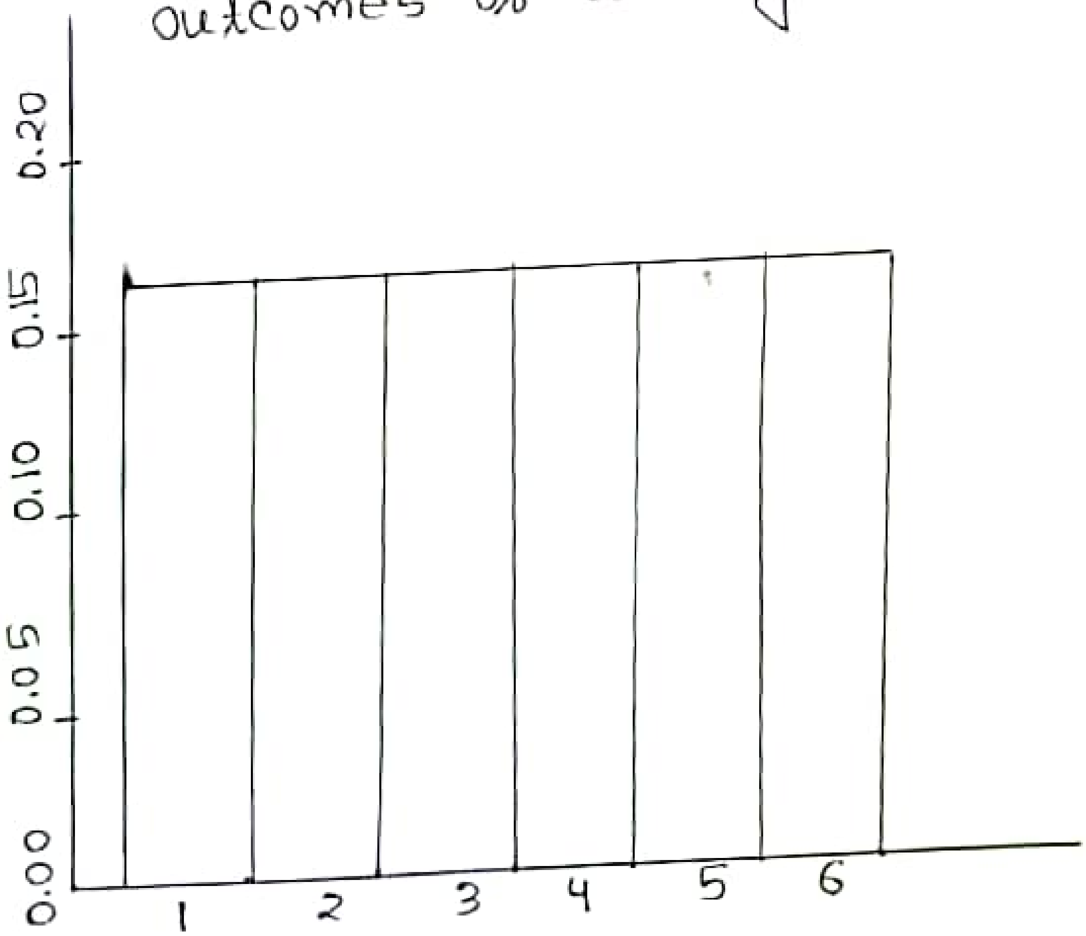
Es = 7

vars = 5.833

Sum of two dice rolls



outcomes of a single dice roll



Comment : Two dic rolled, S is the sum of both faces, the expectation of S, $E(S) = 7$ and variance of S, $V(S) = 5.833$