

408.0

Q1. Polynomial

1	2
3	4
5	6
7	8

Answer: Here,

$$f(x) = a_0x + a_1x + a_2x^2 + a_3x^3 + a_4x^4 + \dots$$

$$f(1) = 2 \quad f(5) = 6$$

$$f(3) = 4 \quad f(7) = 8$$

Following polynomial satisfies those point

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$$f(x) = \frac{(x-5)(x-3)(x-7)(x-10)}{(1-5)(1-3)(1-7)(1-10)} + \frac{(x-8)(x-2)(x-10)}{(3-8)(3-2)(3-10)}$$

$$f(x) =$$

Q2) Taylor series e^{10x}

$$f(x) = \frac{d}{dx} e^{ax} = a e^{ax}$$

$$f'(x) = \frac{d}{dx} (e^{10}) = 10 e^{10x}$$

$$f''(x) = 10^2 e^{10x}$$

$$f'''(x) = 10^3 e^{10x}$$

$$f(x) = \frac{f'(0)}{1!} + \frac{f''(0)}{2!} + \frac{f'''(0)}{3!} + \frac{f^{(4)}(0)}{4!} + \dots$$

$$f(x) = 10 + \frac{10^2}{2!} + \frac{10^3}{3!} + \dots$$