

# Report

## Question 1

Question-1

The given dissimilarity matrix:

	a	b	c	d
a	0	0.3	0.4	0.7
b	0.3	0	0.5	0.8
c	0.4	0.5	0	0.45
d	0.7	0.8	0.45	0

(a) Using complete linkage

$D_1$

	a	c	(b,d)
(a)	0	0.4	0.7
(c)	0.4	0	0.5
(b,d)	0.7	0.5	0

$D_2 = (C)$

	(c)	(a,b,d)
(c)	0	0.5
(a,b,d)	0.5	0

$P_3 = (a,b,c,d)$

(b) Using complete linkage

$D_1 = (a,b)$

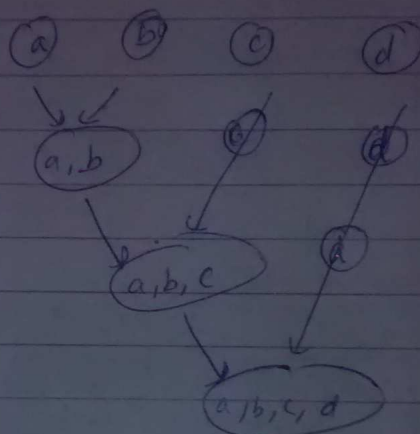
	(a,b)	(c)	(d)
(a,b)	0	0.4	0.7
(c)	0.4	0	0.45
(d)	0.7	0.45	0

Date :

Page No.

$$D_2 = \begin{matrix} & (a,b,c) & d \\ \begin{matrix} (a,b,c) \\ (d) \end{matrix} & \begin{bmatrix} 0 & 0.45 \\ 0.45 & 0 \end{bmatrix} \end{matrix}$$

$$P_3 = \begin{matrix} (a,b,c,d) \\ [0] \end{matrix}$$



(c) Results of two clusters in complete linkage,  
 $\{a,b,d\}$  and  $\{c\}$ .

(d) Results of two clusters in single linkage,  
 $\{a,b,c\}$  and  $\{d\}$ .

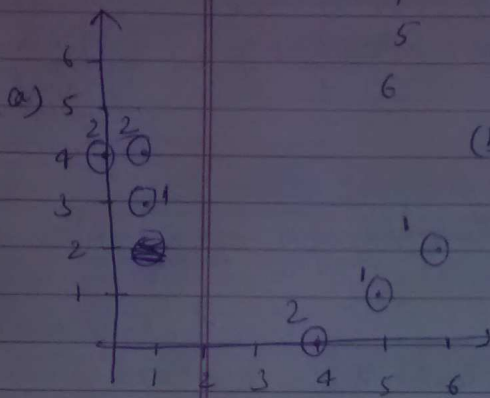


Date :

Page No

(1)  $K=2$   
 $M=6$   
 $p=2$

Obs.	$X_1$	$X_2$
1	1	4
2	1	3
3	0	4
4	6	2
5	5	1
6	4	0



(b) Random initialization of clusters

$(6, 2) \rightarrow$

Cluster (1)

$(6, 2), (5, 1), (1, 3)$

Cluster (2)

$(0, 4), (1, 4), (4, 0)$

(c) Centroid of (1)  $\left( \frac{6+5+1}{3}, \frac{2+1+3}{3} \right) = (4, 2)$

" (2)  $\rightarrow \left( \frac{0+1+4}{3}, \frac{4+4+0}{3} \right) = \left( \frac{5}{3}, \frac{8}{3} \right)$

(d) Closest distance for  $(6, 2) = (1) \sqrt{(6-4)^2 + (2-2)^2} = 2$   
 Cluster (2)  $\sqrt{\left(6 - \frac{5}{3}\right)^2 + \left(2 - \frac{8}{3}\right)^2}$

Distance for cluster (2) > Distance for cluster 1

So  $(6, 2)$  in cluster (1)

Similarly  $(5, 1)$  in cluster (1)

$(1, 3)$  in cluster (2)

$(0, 4)$  " (2)

$(1, 4)$  " (2)

$(4, 0)$  " (1)

Date :

Page No.

(e) New centroids for

Cluster(1)  $(6, 2), (5, 1), (4, 0)$

$$\Rightarrow \left( \frac{6+5+4}{3}, \frac{2+1+0}{3} \right) = (5, 1)$$

Cluster(2)  $= (0, 4), (1, 4), (1, 3)$

$$= \left( \frac{0+1+1}{3}, \frac{4+4+3}{3} \right) = \left( \frac{2}{3}, \frac{11}{3} \right)$$

Now calculating the nearest centroids.

$$(6, 2) \text{ in cluster(1)} \quad \sqrt{\left(\frac{2}{3}-6\right)^2 + \left(\frac{11}{3}-2\right)^2}$$

Similarly.

$(5, 1)$  in cluster (2)

$(4, 0)$  " " (1)

and

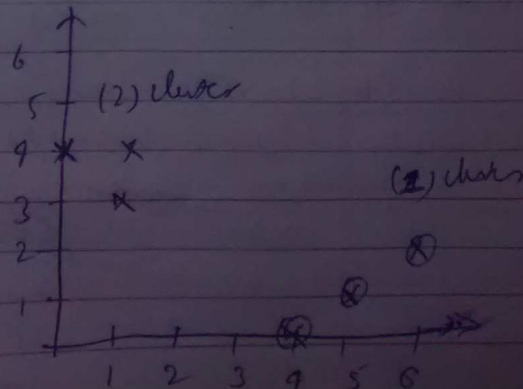
$(0, 4)$  in cluster 2

$(1, 4)$  in cluster 2

$(1, 3)$  in cluster 2.

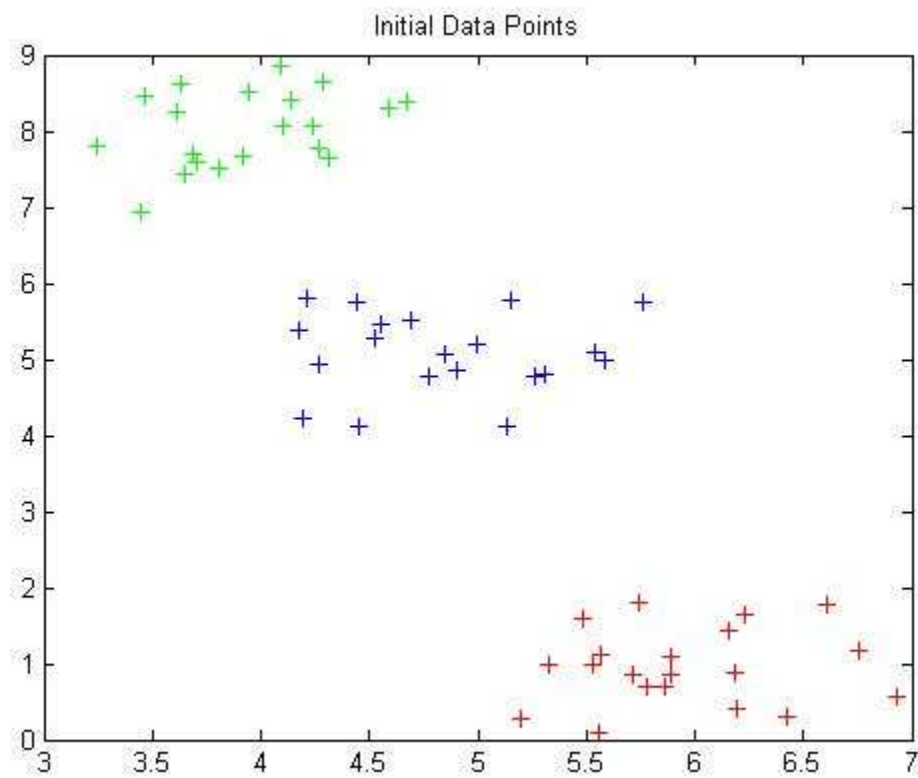
Since the clusters are not changing we can stop here.

(f) Final clusters.

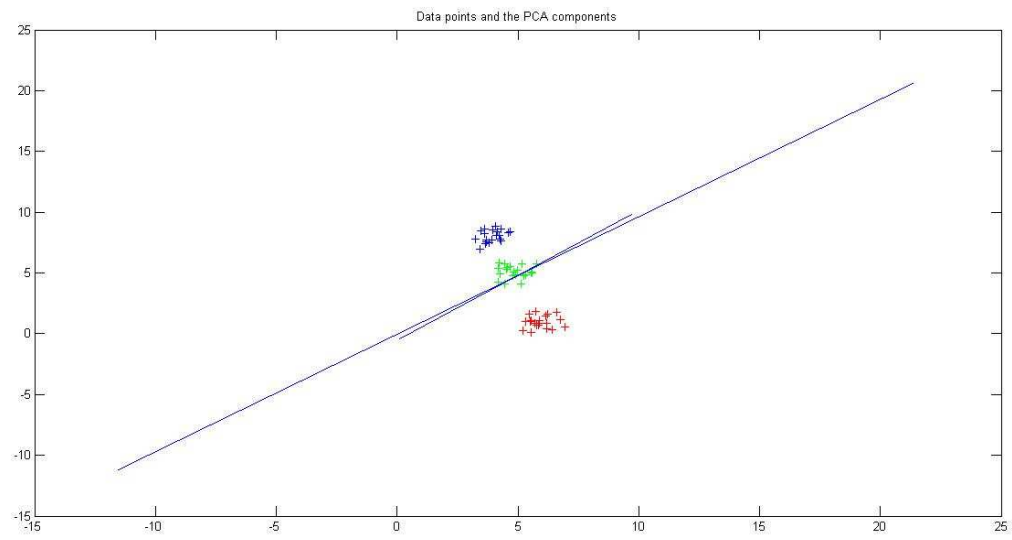


3.

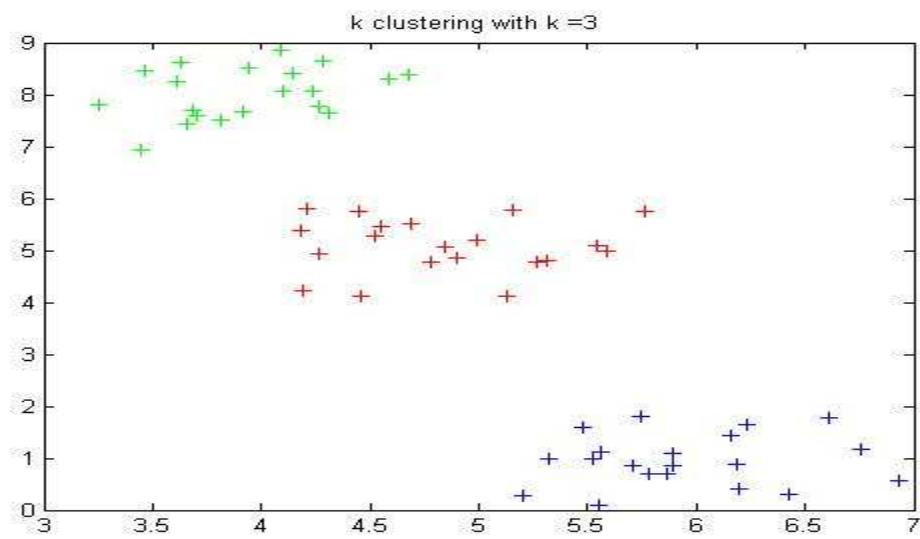
(a) The 60 observation initially with the data labels



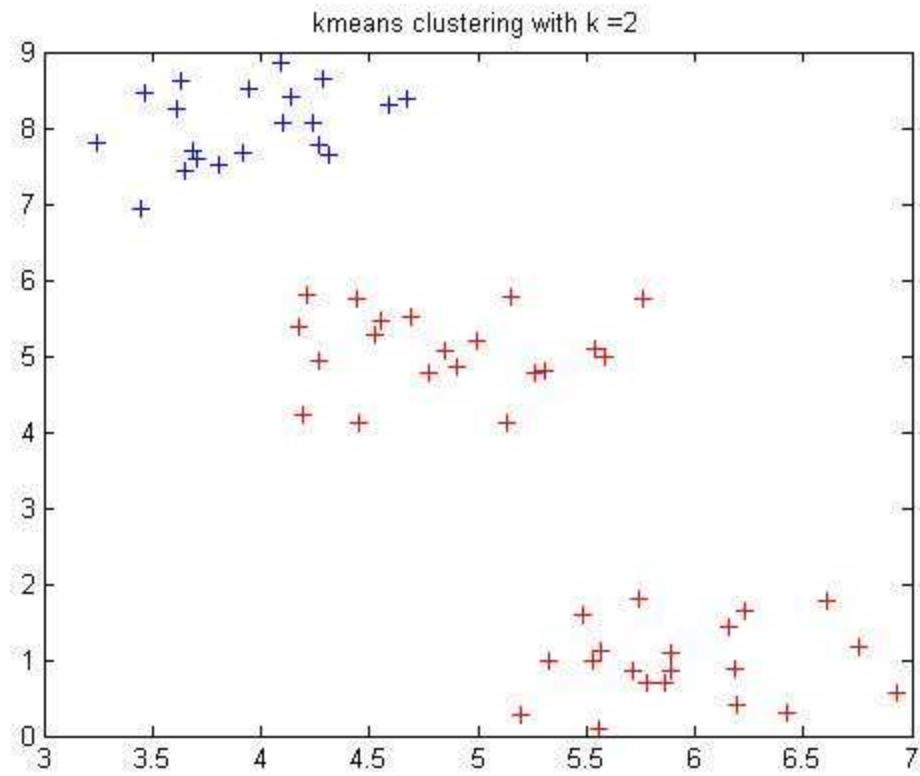
3(b) The data points with the PCA vector shown



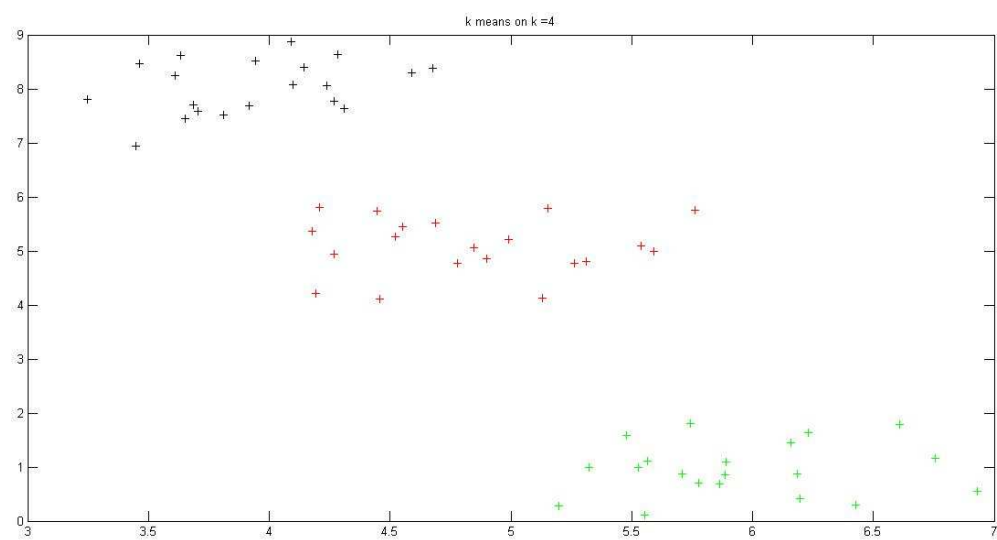
3(c) K means clustering on the data with  $k=3$



(d) k means clustering on  $K=2$

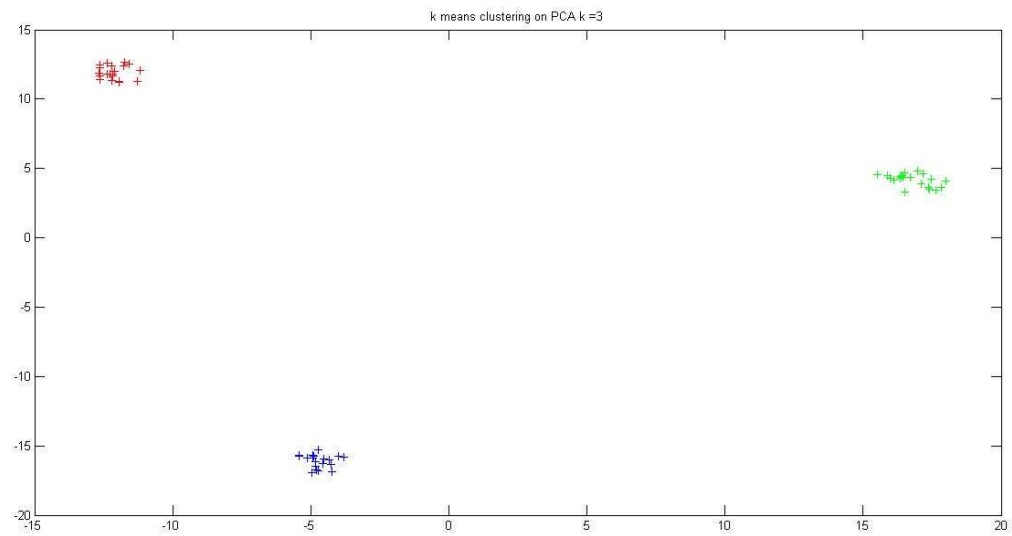


(e) k means clustering on the data with  $k=4$  on the original data



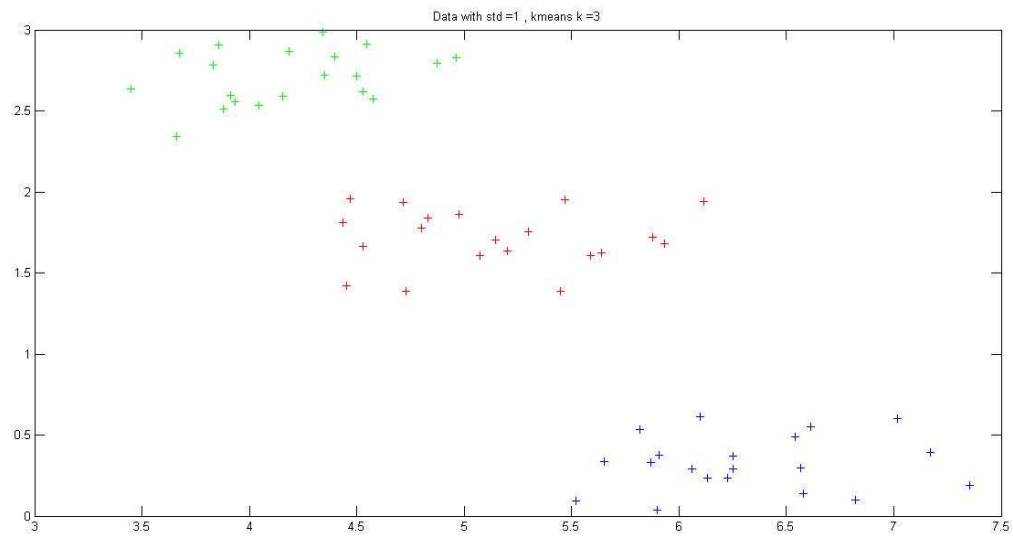


(f) k means clustering on the PCA points with  $k = 3$ .

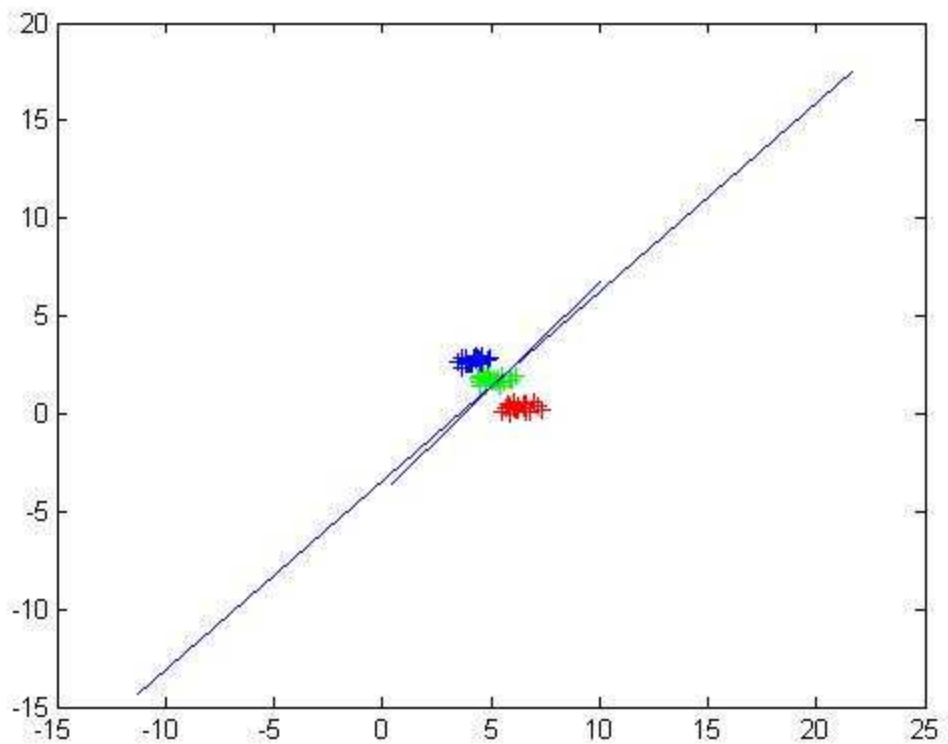


It can be seen in the PCA of the data points the points are more far separated than the original data .

(g) k means cluster on the points with std deviation = 1



With std deviation and PCA

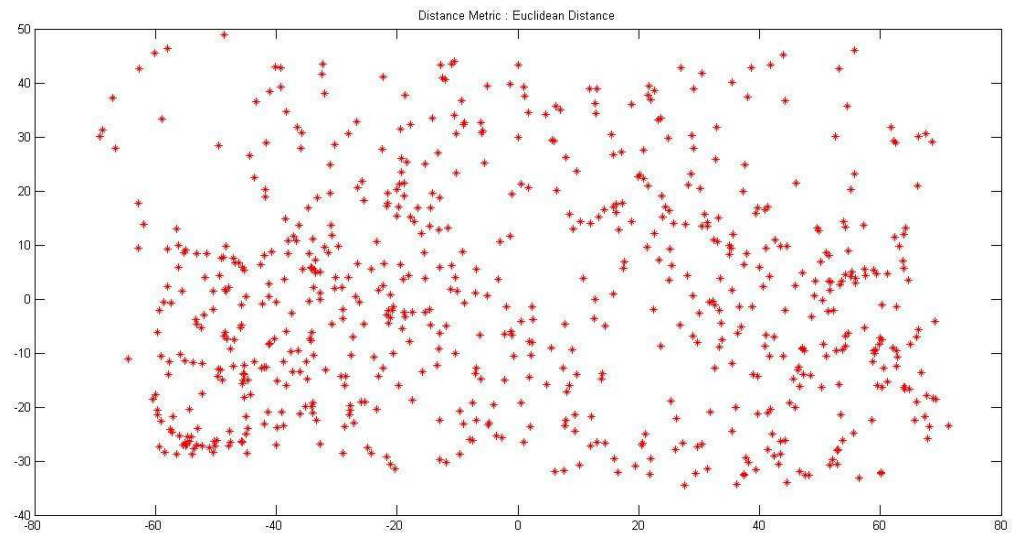


It can be seen by changing the standard deviation of the data to 1 the data points are more closer as the in the original data standard deviation was 0.5.

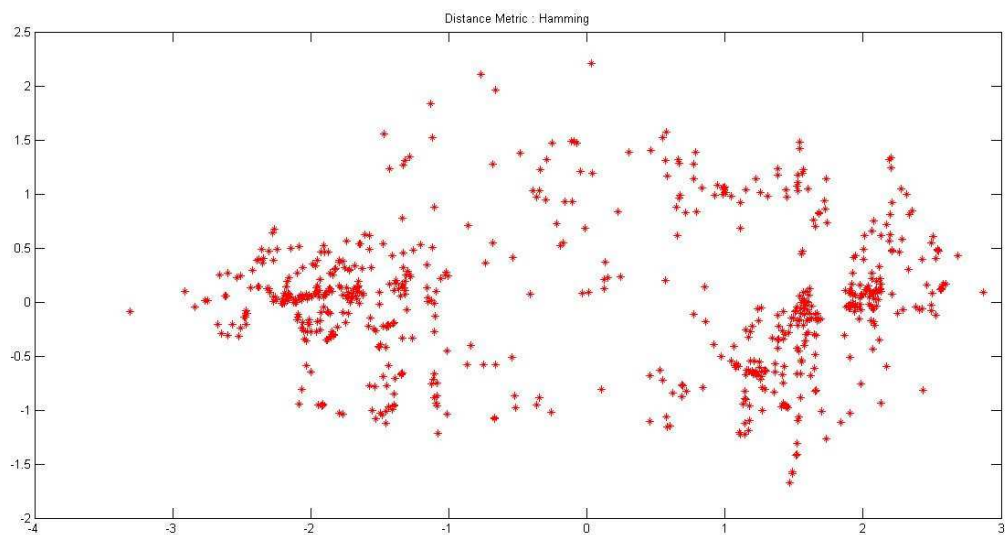
4.

(b)

The 2D embedding with euclidean distance



(c) Embedding with distance metric as hamming



Embedding with distance metric as cityblock

