

1.

The primal form of the problem is:

$$L = \frac{1}{2} \|\theta\|^2 - \sum_{i=1}^N \alpha^i [y^i (\theta^T x^i + \theta_0) - 1]$$

Applying the  $N$  differentiation on the Lagrangian, we set  $\text{for } \alpha^i \geq 0$

$$\frac{\partial L}{\partial \theta} = 0 - \sum_{i=1}^N \alpha^i y^i x^i = 0 \quad \Rightarrow$$

$$\text{and } \frac{\partial L}{\partial \theta_0} \Rightarrow \sum \alpha^i y^i = 0$$

By Substituting we get:-

$$L = \frac{1}{2} \|\theta\|^2 - \sum_{i=1}^N \alpha^i [y^i (\theta^T x^i + \theta_0) - 1]$$

$$= \frac{1}{2} \|\theta\|^2 - \theta^T \sum_{i=1}^N \alpha^i y^i x^i - \theta_0 \sum_{i=1}^N \alpha^i y^i + \sum_{i=1}^N \alpha^i$$

$$= \frac{1}{2} \|\theta\|^2 - \theta^T \sum_{i=1}^N \alpha^i y^i x^i + \sum_{i=1}^N \alpha^i \quad (\sum \alpha^i y^i = 0)$$

$$= \frac{1}{2} \|\theta\|^2 - \theta^T \theta + \sum_{i=1}^N \alpha^i$$

$$= -\frac{1}{2} \|\theta\|^2 + \sum_{i=1}^N \alpha^i$$

$$\left( \theta = \sum_{i=1}^N \alpha^i y^i x^i \right)$$