

What I tried

- Redid the correlation with the median rather than average

Correlation Matrix Heatmap - Median pause before tokens



Redid all the correlations with a more robust data structure and checking an “obvious” case – number of tokens vs. number of nodes.

Integrated the data in the existing data structure to handle conll files in order to be able to track back results and check for errors.

Obtained correlation 1.0 between nb of tokens and nb of nodes confirming correctness of data / approach to correlation

Tried different
correlation
formulas: pearson,
spearman and
kendall

At sentence level:

```
#####Pearson Correlations#####  
Correlation head initial: 0.04702515135962086  
Correlation mean hierarchical distance: -0.08967500962164483  
Correlation tree diameter: -0.19661054018754903  
Correlation num crossings: -0.02038021058086742  
Correlation predicted num crossings: -0.1404953846206059  
Correlation expected num crossings: -0.09905873327031321  
Correlation sum edge lengths: -0.1312145012875535  
Correlation expected sum edge lengths: -0.10635647668183107  
Correlation mean dependency distance: -0.0862568382033117  
#####Kendalltau Correlations#####  
Correlation head initial: 0.10839550359403198  
Correlation mean hierarchical distance: -0.05793010688001669  
Correlation tree diameter: -0.07461154114750174  
Correlation num crossings: 0.014604661448358973  
Correlation predicted num crossings: -0.10133165379092222  
Correlation expected num crossings: -0.09731418866865037  
Correlation sum edge lengths: -0.10708153844721391  
Correlation expected sum edge lengths: -0.102646229707907  
Correlation mean dependency distance: -0.11926882328618435  
#####Spearman Correlations#####  
Correlation head initial: 0.15966760097145294  
Correlation mean hierarchical distance: -0.07833112849807591  
Correlation tree diameter: -0.10110665906792915  
Correlation num crossings: 0.018076865627139192  
Correlation predicted num crossings: -0.1543620194453281  
Correlation expected num crossings: -0.15131047253970958  
Correlation sum edge lengths: -0.16974396121790294  
Correlation expected sum edge lengths: -0.15810246739250702  
Correlation mean dependency distance: -0.18100666922750844
```

```

#####Pearson Correlations#####
Correlation head initial: 0.04702515135962086, p-value: 0.00017655604697790125
Correlation mean hierarchical distance: -0.08967500962164483, p-value: 7.932025133079316e-13
Correlation tree diameter: -0.19661054018754903, p-value: 2.0490150663922883e-56
Correlation num crossings: -0.02038021058086742, p-value: 0.10423677816936777
Correlation predicted num crossings: -0.1404953846206059, p-value: 2.198530158080878e-29
Correlation expected num crossings: -0.09905873327031321, p-value: 2.465962939359081e-15
Correlation sum edge lengths: -0.1312145012875535, p-value: 8.244508602277055e-26
Correlation expected sum edge lengths: -0.10635647668183107, p-value: 1.8687573523137835e-17
Correlation mean dependency distance: -0.0862568382033117, p-value: 5.647349499027086e-12
#####Kendalltau Correlations#####
Correlation head initial: 0.10839550359403198, p-value: 2.082843573690224e-37
Correlation mean hierarchical distance: -0.05793010688001669, p-value: 6.980230925769444e-12
Correlation tree diameter: -0.07461154114750174, p-value: 2.833973434252944e-17
Correlation num crossings: 0.014604661448358973, p-value: 0.15022316797120794
Correlation predicted num crossings: -0.10133165379092222, p-value: 8.238997326403826e-33
Correlation expected num crossings: -0.09731418866865037, p-value: 1.1663689966461496e-30
Correlation sum edge lengths: -0.10708153844721391, p-value: 7.447581091377181e-37
Correlation expected sum edge lengths: -0.102646229707907, p-value: 2.4145734938429916e-33
Correlation mean dependency distance: -0.11926882328618435, p-value: 2.175670853370766e-45
#####Spearman Correlations#####
Correlation head initial: 0.15966760097145294, p-value: 1.4567491323436962e-37
Correlation mean hierarchical distance: -0.07833112849807591, p-value: 4.018862606057424e-10
Correlation tree diameter: -0.10110665906792915, p-value: 6.486973168632649e-16
Correlation num crossings: 0.018076865627139192, p-value: 0.1495836038970462
Correlation predicted num crossings: -0.1543620194453281, p-value: 3.426293948537738e-35
Correlation expected num crossings: -0.15131047253970958, p-value: 7.26383983865557e-34
Correlation sum edge lengths: -0.16974396121790294, p-value: 2.688448561530604e-42
Correlation expected sum edge lengths: -0.15810246739250702, p-value: 7.440594330533041e-37
Correlation mean dependency distance: -0.18100666922750844, p-value: 5.999943257075408e-48

```

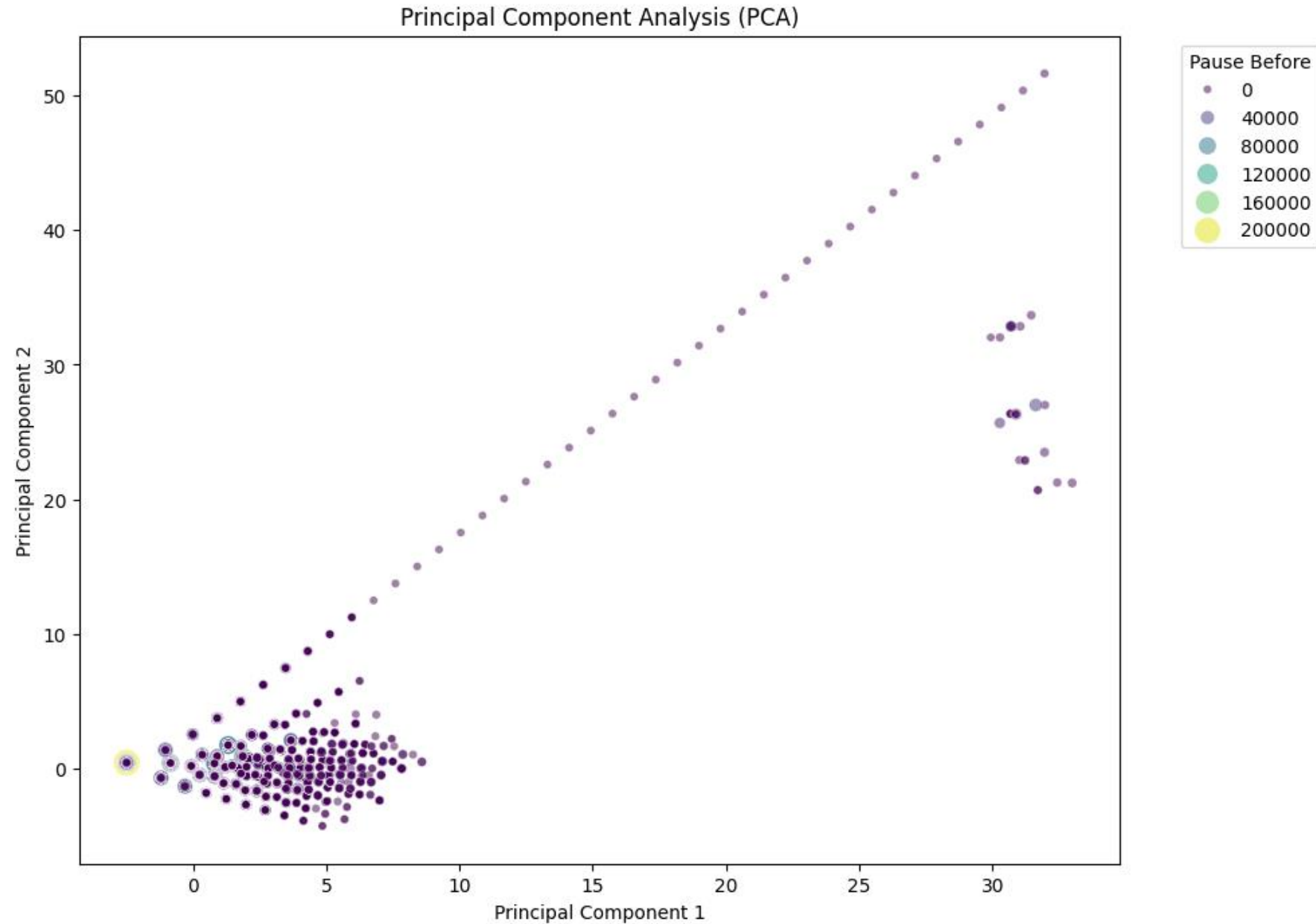
Also added
p-value to
check
significance
of results

At sentence level:

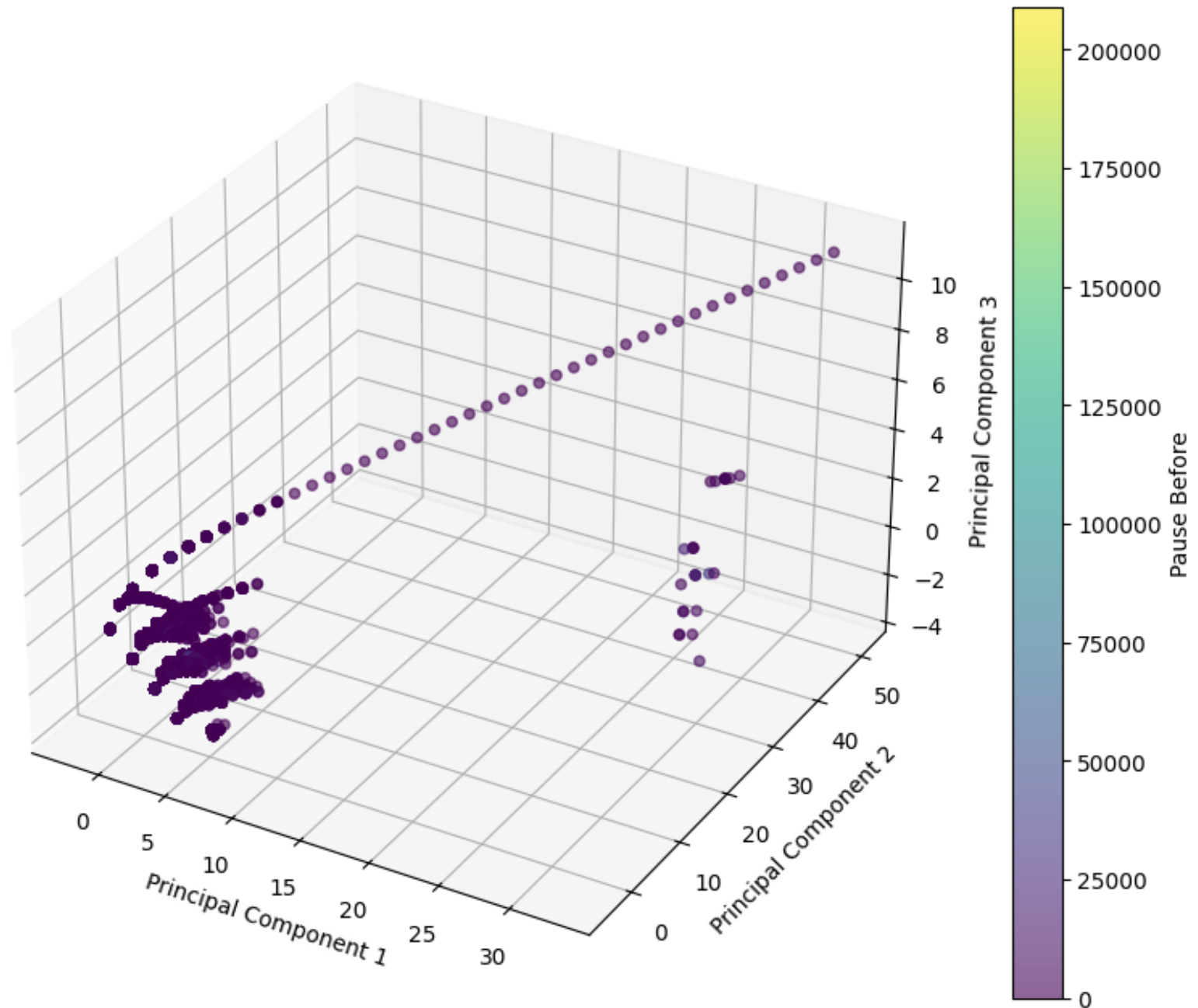
At token level:

```
#####Pearson Correlations#####
Correlation flux size and pause: -0.07533748772499355 (p-value: 1.023299614348079e-148)
Correlation flux left span and pause: -0.08768835513242718 (p-value: 6.015495282380408e-201)
Correlation flux right span and pause: -0.029256564249771157 (p-value: 7.211245124491826e-24)
Correlation flux weight and pause: -0.060784076515618186 (p-value: 2.105961155967122e-97)
Correlation flux RL ratio and pause: 0.023787276374464934 (p-value: 2.611982979904057e-16)
Correlation flux WS ratio and pause: 0.08035440210992414 (p-value: 5.73444750506293e-169)
#####Spearman Correlations#####
Correlation flux size and pause: -0.13017354007609247 (p-value: 0.0)
Correlation flux left span and pause: -0.14311833292972578 (p-value: 0.0)
Correlation flux right span and pause: -0.06919606587491443 (p-value: 1.0228729185292302e-125)
Correlation flux weight and pause: -0.1083801325023214 (p-value: 1.8130226874648306e-306)
Correlation flux RL ratio and pause: 0.08262920988725748 (p-value: 1.3849377658786898e-178)
Correlation flux WS ratio and pause: 0.06695104993213218 (p-value: 8.442803664036185e-118)
#####Kendall Correlations#####
Correlation flux size and pause: -0.0952418733981384 (p-value: 0.0)
Correlation flux left span and pause: -0.10624543225828688 (p-value: 0.0)
Correlation flux right span and pause: -0.052812552797325 (p-value: 5.127137096268854e-126)
Correlation flux weight and pause: -0.08561289349154574 (p-value: 1.120601956365336e-306)
Correlation flux RL ratio and pause: 0.059157534887426894 (p-value: 4.456168879563216e-176)
Correlation flux WS ratio and pause: 0.048424603781632984 (p-value: 1.6009458956031436e-116)
```

Principal component analysis of fluxes with 2 principal components (variance ratio of 0.77)



Principal
component
analysis of
fluxes with 3
principal
components
(variance ratio of
0.96)



Log normalization

- The purpose is to bring variances closer together
- If we check the variance of the columns, we can see that column 2 has a significantly higher variance than column 1, which makes it a clear candidate for log normalization.

```
print(df)
```

```
   col1  col2
0  1.00   3.0
1  1.20  45.5
2  0.75  28.0
3  1.60 100.0
```

```
print(df.var())
```

```
col1    0.128958
col2   1691.729167
dtype: float64
```

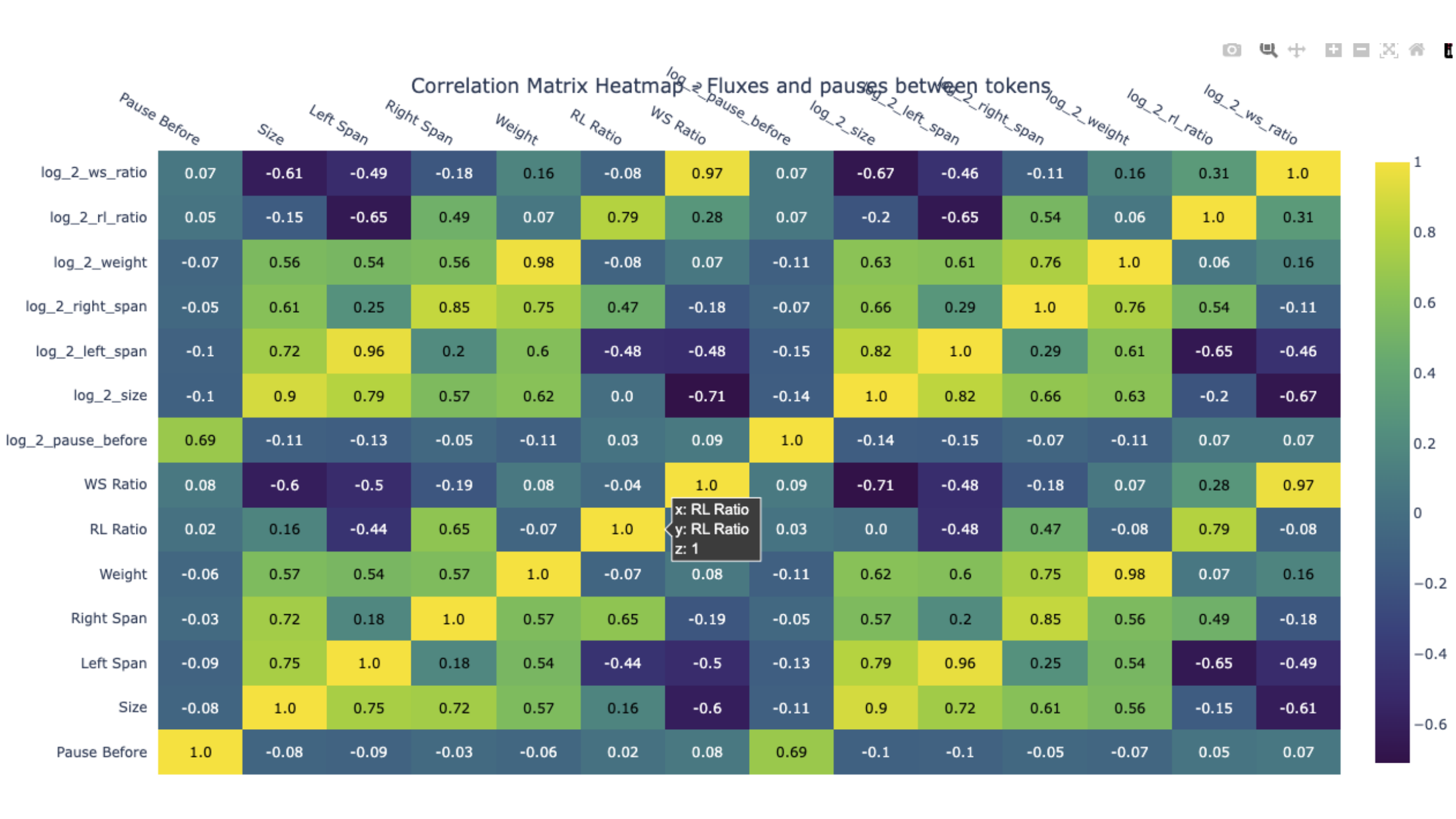

But in our case...

- Variance is very small in all cases so there isn't a column that it would make sense to do log normalization on.

```
Pause Before    2.425359e+07
Size            2.739876e+00
Left Span       1.594734e+00
Right Span      1.498890e+00
Weight          4.882483e-01
RL Ratio        6.862192e-01
WS Ratio        6.199889e-02
dtype: float64
```

If we apply log normalization to all columns

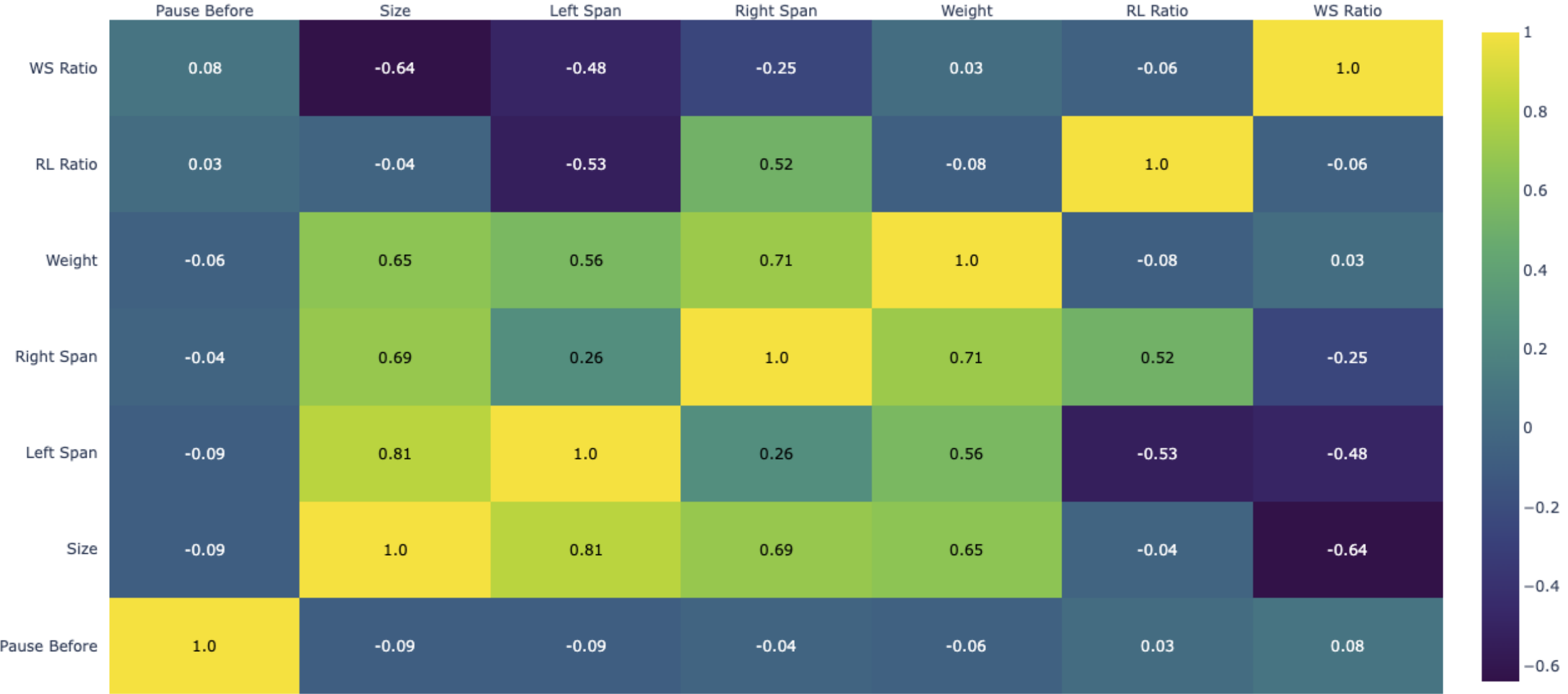
index	Pause B...	Size	Left Span	Right S...	Weight	RL Ratio	WS Ratio	log_2_...	log_2_s...	log_2_l...	log_2_r...	log_2_...	log_2_r...	log_2_...
0	2589	1	1	1	1	1	1	7.8590269...	0	0	0	0	0	0
1	2074	1	1	1	1	1	1	7.6372343...	0	0	0	0	0	0
2	3557	1	1	1	1	1	1	8.1766727...	0	0	0	0	0	0
3	281	2	2	1	1	0.5	0.5	5.638354...	0.6931471...	0.6931471...	0	0	-0.693147...	-0.693147...
4	1997	3	3	1	1	0.333333...	0.333333...	7.5994013...	1.0986122...	1.0986122...	0	0	-1.098612...	-1.098612...
5	436	4	4	1	1	0.25	0.25	6.0776422...	1.3862943...	1.3862943...	0	0	-1.386294...	-1.386294...
6	1466	2	1	2	1	2	0.5	7.2902928...	0.6931471...	0	0.6931471...	0	0.6931471...	-0.693147...
7	593	2	2	2	2	1	1	6.3851943...	0.6931471...	0.6931471...	0.6931471...	0.6931471...	0	0
8	21731	1	1	1	1	1	1	9.986495...	0	0	0	0	0	0
9	2074	1	1	1	1	1	1	7.6372343...	0	0	0	0	0	0
10	3557	1	1	1	1	1	1	8.1766727...	0	0	0	0	0	0



Also tried the correlation only taking into account the final sentence(s) in each file

```
#####Pearson Correlations#####
Correlation head initial: 0.20817386124677179, p-value: 0.007475036696129296
Correlation mean hierarchical distance: -0.07655131158207834, p-value: 0.3299238868947745
Correlation tree diameter: -0.15987698094945174, p-value: 0.040861073837752775
Correlation num crossings: -0.06133656833362801, p-value: 0.43526242241819296
Correlation predicted num crossings: -0.20248302626240977, p-value: 0.009316791576977804
Correlation expected num crossings: -0.14521499303551716, p-value: 0.06355600680324376
Correlation sum edge lengths: -0.15305130168755784, p-value: 0.05039870664248668
Correlation expected sum edge lengths: -0.15046032754486394, p-value: 0.05447296928642393
Correlation mean dependency distance: -0.09389400674545449, p-value: 0.23174468222766847
#####Kendalltau Correlations#####
Correlation head initial: 0.12083941980411914, p-value: 0.02273754655527359
Correlation mean hierarchical distance: -0.03233685004954308, p-value: 0.5399116241641282
Correlation tree diameter: -0.08834811780207219, p-value: 0.11113584986095865
Correlation num crossings: -0.05419428142496544, p-value: 0.39175042428785567
Correlation predicted num crossings: -0.10519269514052805, p-value: 0.04627257600255736
Correlation expected num crossings: -0.1016240315911081, p-value: 0.053980897644696414
Correlation sum edge lengths: -0.10469472217494083, p-value: 0.04741832544103585
Correlation expected sum edge lengths: -0.1077995166550254, p-value: 0.04326994916779795
Correlation mean dependency distance: -0.09175172250913728, p-value: 0.08197376681757479
#####Spearman Correlations#####
Correlation head initial: 0.17102808987004314, p-value: 0.02855074408597388
Correlation mean hierarchical distance: -0.04226816971308679, p-value: 0.5909936450126618
Correlation tree diameter: -0.11667936149272957, p-value: 0.13678182652170445
Correlation num crossings: -0.06764608162029578, p-value: 0.3894292939609185
Correlation predicted num crossings: -0.15170636203579807, p-value: 0.052480848099376594
Correlation expected num crossings: -0.14991531518344076, p-value: 0.05536375508322784
Correlation sum edge lengths: -0.15735120153053514, p-value: 0.044196907075453075
Correlation expected sum edge lengths: -0.15865096777474333, p-value: 0.042452901961527297
Correlation mean dependency distance: -0.135804208446436, p-value: 0.08293902441826316
```

Correlation Matrix Heatmap - Fluxes and pauses between tokens for final sentences only



Mixed effects analysis

- Also known as a hierarchical linear model, which is useful when you want to account for both fixed effects and random effects in your data.
- In mixed-effects models:
- **Fixed effects** are the main effects you're interested in. For example, in our case, the fixed effect might be the size of the flux.
- **Random effects** account for variations between individual subjects or groups.

When looking at the pause and size of the flux:

Interpretation:

- Intercept (4654.007): This is the estimated average value of `Pause_Before` when `Size` is zero. The positive coefficient indicates that, on average, the `Pause_Before` is 4654.007 ms when `Size` is zero. The p-value (0.000) indicates that this coefficient is statistically significant.

- Size (-228.013): This coefficient represents the change in Pause_Before for a one-unit increase in Size. The negative value (-228.013) suggests that as Size increases, Pause_Before decreases. The p-value (0.000) indicates that this relationship is statistically significant.

- Group Variance (5,729,316.888): This value represents the variance of the random intercepts for the groups (Person). A higher variance indicates more variability in Pause_Before between different persons.

```

Mixed Linear Model Regression Results
=====
Model:                MixedLM   Dependent Variable:  Pause_Before
No. Observations:    118513   Method:              REML
No. Groups:          45       Scale:               21888804.4026
Min. group size:     104      Log-Likelihood:      -1169807.6671
Max. group size:     14463    Converged:           Yes
Mean group size:     2633.6

=====
              Coef.      Std.Err.      z      P>|z|      [0.025      0.975]
-----
Intercept    4654.007    358.647    12.977  0.000    3951.073    5356.942
Size         -228.013     8.484   -26.877  0.000   -244.641   -211.386
Group Var 5729316.888    267.224
=====

```

Next steps:

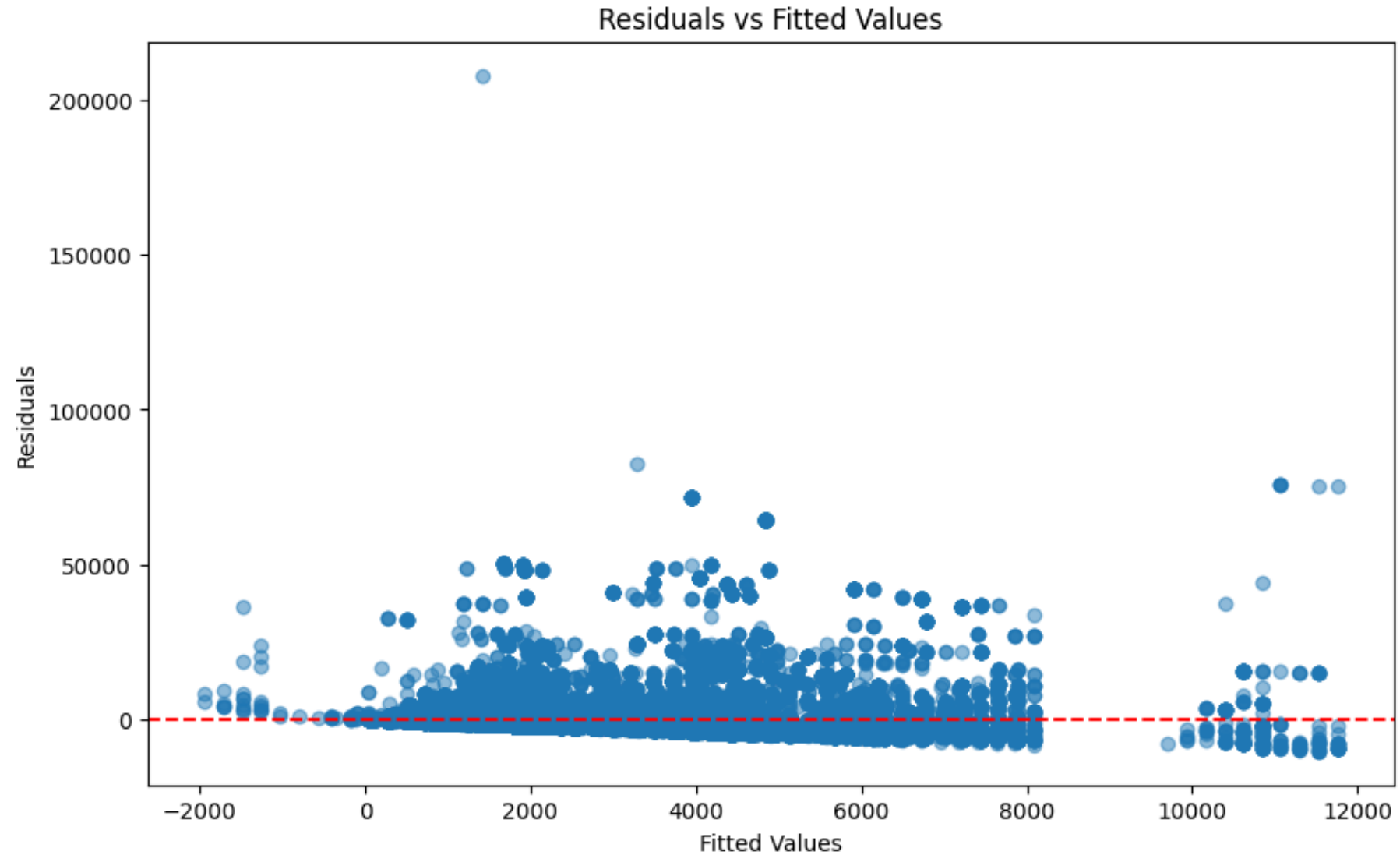
- **Model Validation:** The model should be validated by checking residuals and performing diagnostic checks to ensure the assumptions of the mixed-effects model are met.
- **Further Exploration:** Explore the effects of the other measures on `Pause_Before` by including them in the model.

Validating the model

- Validating the model involves checking the residuals and ensuring that the assumptions of the mixed-effects model are met. Here are the key steps you can take for model validation:
 - 1. Plotting Residuals:** Check for normality and homoscedasticity.
 - 2. QQ Plot:** Check if the residuals follow a normal distribution.
 - 3. Random Effects:** Inspect the random effects to ensure they are normally distributed.
 - 4. Influence of Random Effects:** Check if random effects significantly improve the model fit.

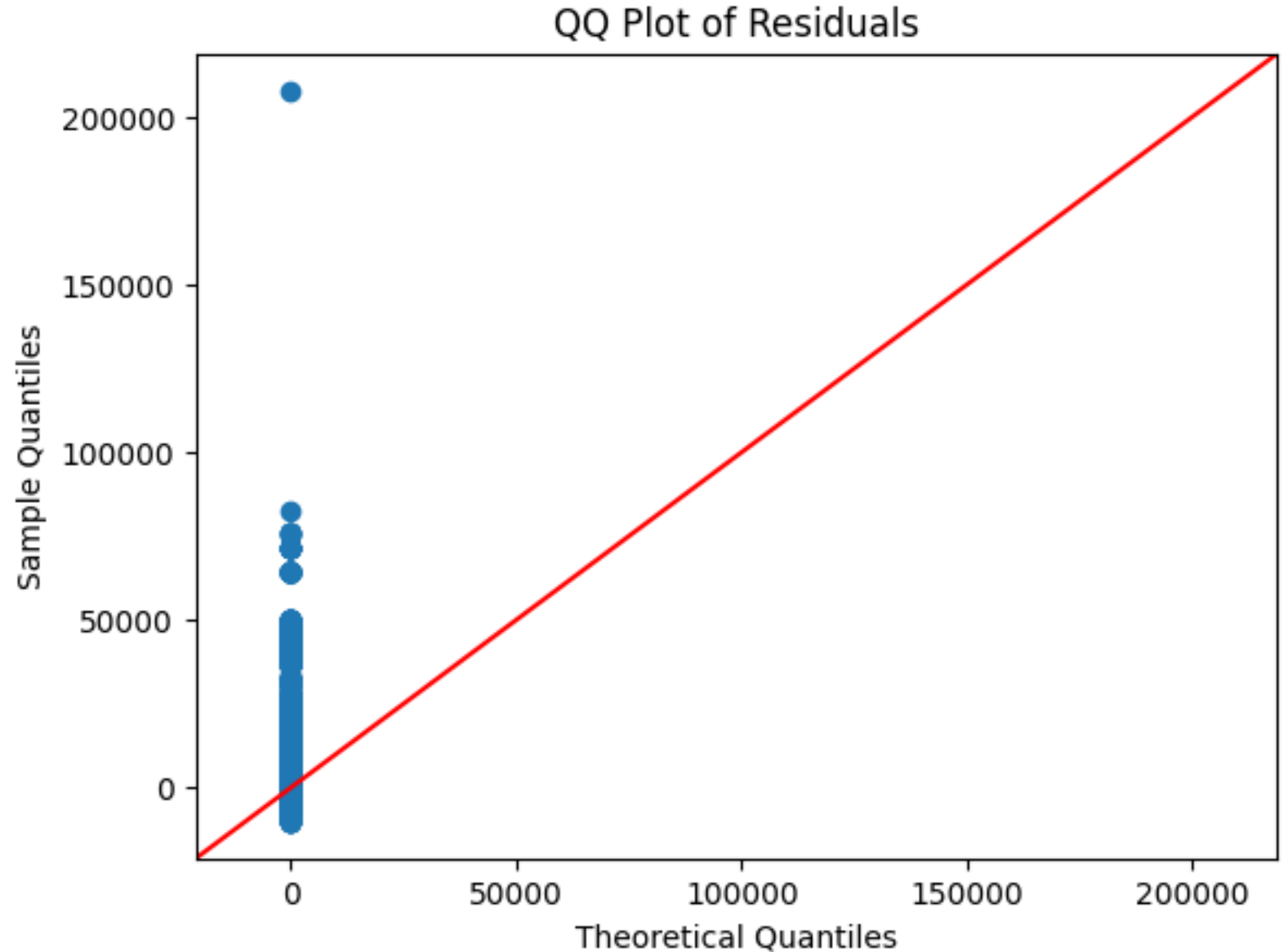
Plotting residuals

This plot helps check for homoscedasticity (constant variance of residuals). Ideally, the residuals should be randomly scattered around zero without any discernible pattern.



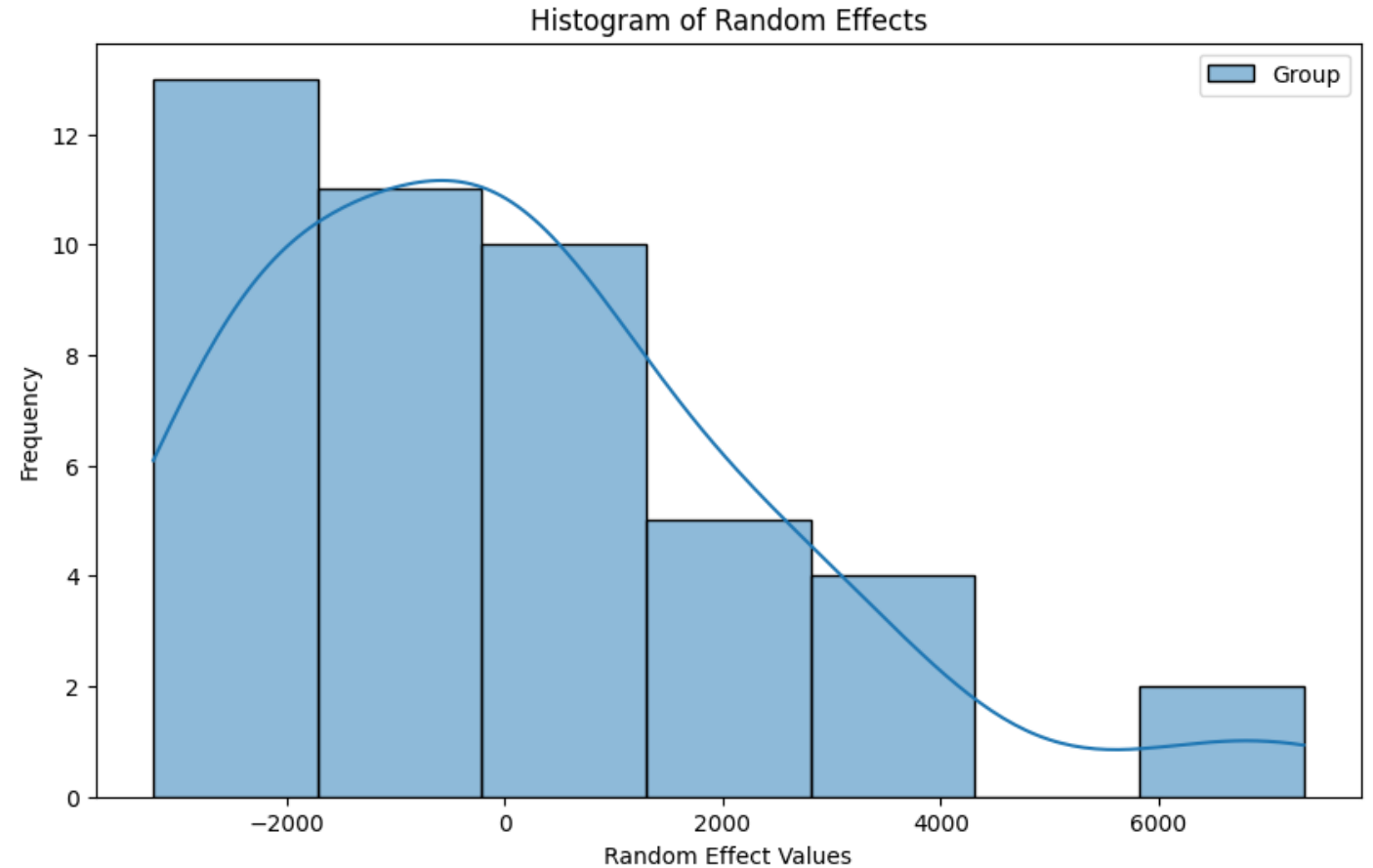
QQ Plot

- If the residuals follow the line closely, they are approximately normally distributed. Deviations from the line suggest departures from normality.



Distribution of Random Effects

The histogram should approximate a normal distribution if the random effects are normally distributed.



Model Comparison with and without Random Effects

- Comparing AIC and BIC values helps determine if including random effects improves the model. Lower AIC and BIC values indicate a better model fit.

```

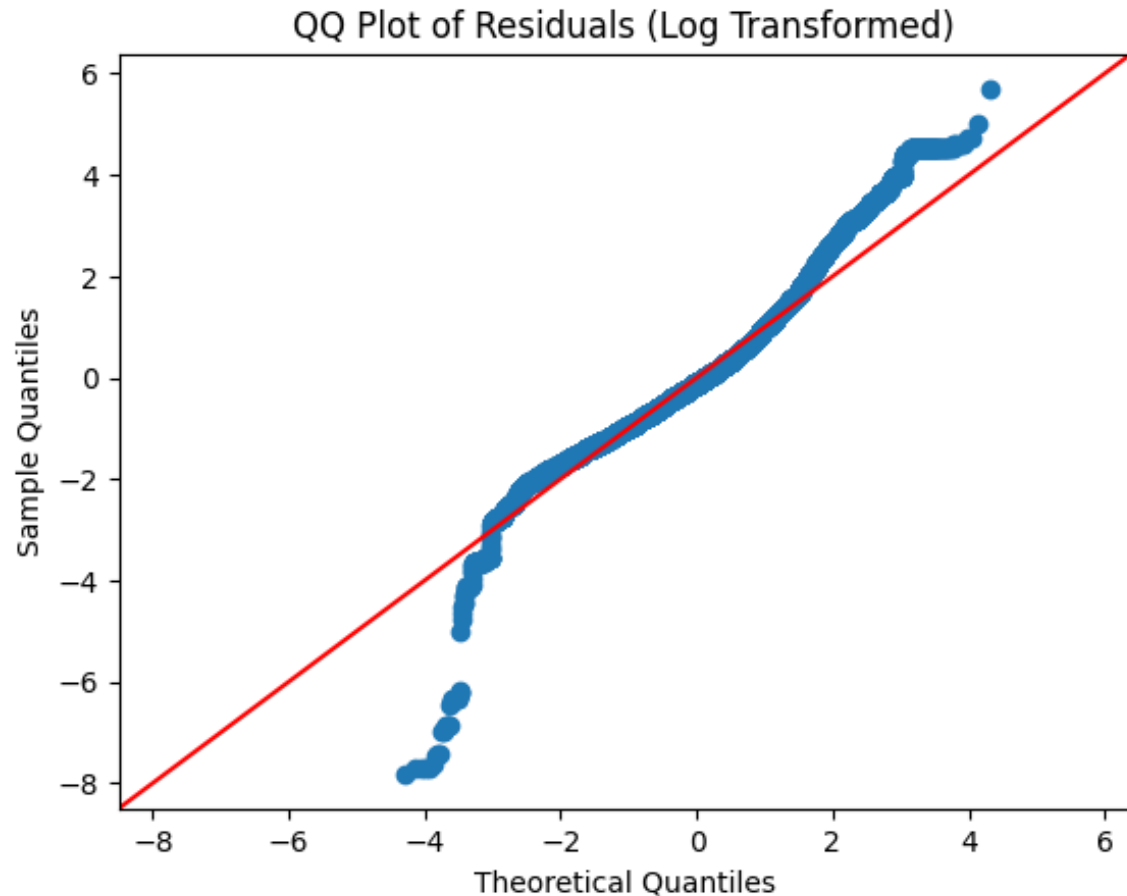
=====
OLS Regression Results
=====
Dep. Variable:          Pause_Before    R-squared:                0.006
Model:                  OLS             Adj. R-squared:           0.006
Method:                 Least Squares    F-statistic:              676.5
Date:                  Mon, 29 Jul 2024  Prob (F-statistic):      1.02e-148
Time:                  11:37:53         Log-Likelihood:          -1.1754e+06
No. Observations:      118513          AIC:                     2.351e+06
Df Residuals:          118511          BIC:                     2.351e+06
Df Model:               1
Covariance Type:       nonrobust
=====
               coef    std err          t      P>|t|      [0.025      0.975]
-----
Intercept    2928.1244     30.046     97.453     0.000     2869.234     2987.015
Size        -224.1474      8.618    -26.009     0.000    -241.039    -207.256
=====
Omnibus:                 151190.846    Durbin-Watson:           1.910
Prob(Omnibus):            0.000    Jarque-Bera (JB):        36097172.006
Skew:                     7.005    Prob(JB):                0.00
Kurtosis:                 87.343    Cond. No.                7.82
=====

Notes:
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
AIC (Mixed-Effects Model): nan
BIC (Mixed-Effects Model): nan
AIC (Simple Model): 2350857.7351698596
BIC (Simple Model): 2350877.100725736

```

- The QQ plot of the residuals shows a significant deviation from the reference line (the red line), which indicates that the residuals do not follow a normal distribution. Here are some key observations from the plot:
 - 1. Heavy Tail and Outliers:** The points are clustered near the origin, with some points deviating significantly from the line. This suggests the presence of heavy tails or outliers in the data.
 - 2. Non-Normality:** The extreme deviation of points from the line indicates that the residuals are not normally distributed. In a QQ plot, if the residuals were normally distributed, the points would fall along the red line.
 - 3. Potential Skewness:** The concentration of points at the lower end and the spread at the upper end suggest possible skewness in the residuals.
- **Steps to Address Non-Normality**
 - 1. Transform the Dependent Variable:** Apply transformations such as log, square root, or Box-Cox transformation to the dependent variable to stabilize variance and make the distribution more normal.
 - 2. Check for Outliers:** Identify and handle outliers, which can disproportionately affect the normality of residuals.
 - 3. Use Robust Methods:** Consider using robust regression methods that are less sensitive to violations of assumptions.
 - 4. Model Diagnostics:** Perform further diagnostics to understand the source of non-normality. Check for patterns or trends in residual plots.

So I applied a log transformation to the pause and refit the model



Mixed Linear Model Regression Results

```
=====
Model:                MixedLM Dependent Variable: log_Pause_Before
No. Observations: 118513 Method:                REML
No. Groups:           45      Scale:              1.1019
Min. group size: 104      Log-Likelihood:    -174064.6335
Max. group size: 14463    Converged:          Yes
Mean group size: 2633.6
=====
```

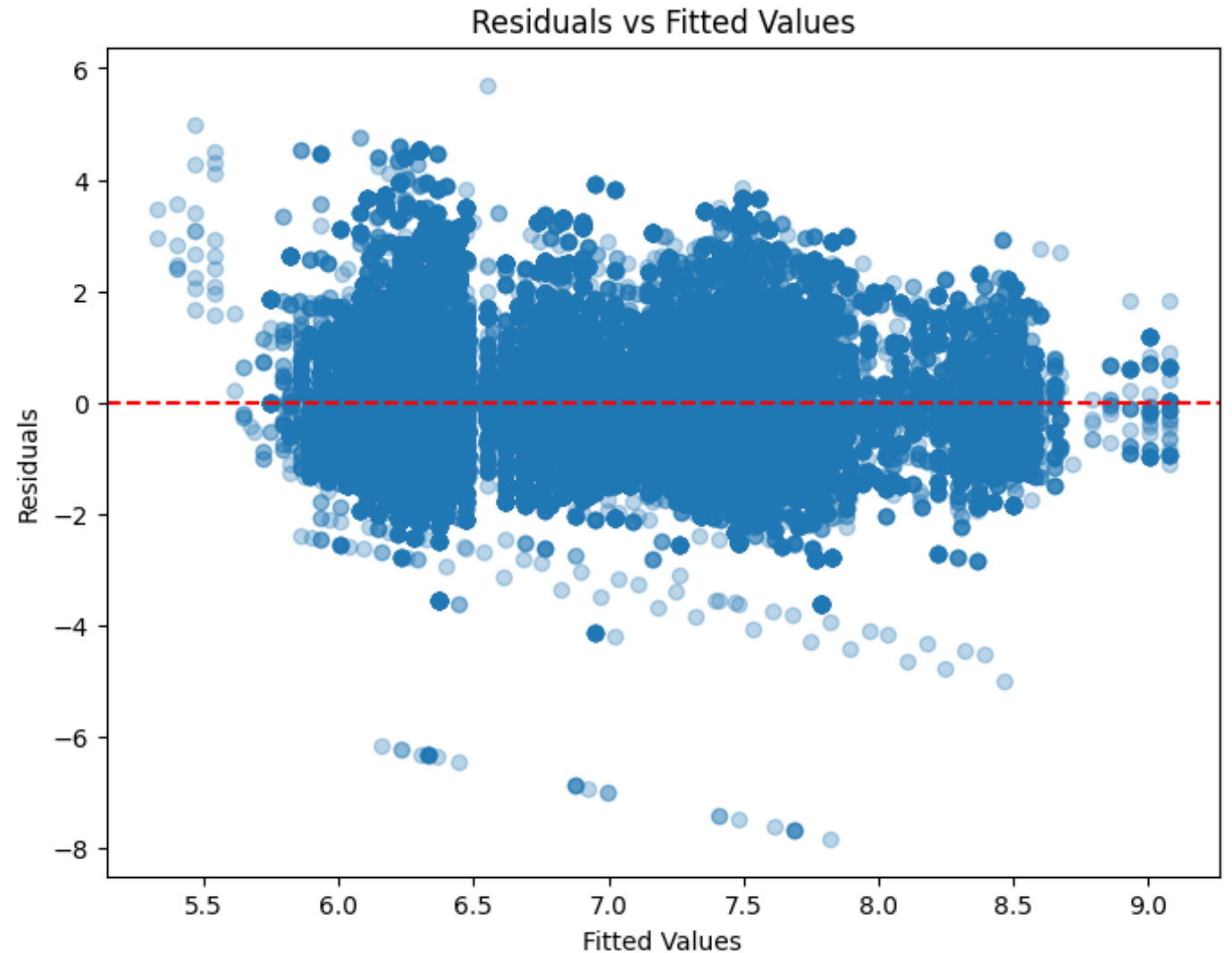
	Coef.	Std.Err.	z	P> z	[0.025	0.975]
Intercept	7.648	0.109	70.166	0.000	7.434	7.861
Size	-0.071	0.002	-37.471	0.000	-0.075	-0.068
Group Var	0.532	0.109				

```
=====
```

- Interpretation:
- Intercept (7.648): This is the estimated average value of `log_Pause_Before` when `Size` is zero. The positive coefficient indicates that, on average, the log-transformed `Pause_Before` is 7.648 units when `Size` is zero. The p-value (0.000) indicates that this coefficient is statistically significant.
- Size (-0.071): This coefficient represents the change in `log_Pause_Before` for a one-unit increase in `Size`. The negative value (-0.071) suggests that as `Size` increases, the log-transformed `Pause_Before` decreases. The p-value (0.000) indicates that this relationship is statistically significant.
- Group Variance (0.532): This value represents the variance of the random intercepts for the groups (Person). A higher variance indicates more variability in `log_Pause_Before` between different persons.
- Conclusion:
- The model suggests that `log_Pause_Before` is significantly influenced by `Size`, with larger sizes leading to shorter pauses on a logarithmic scale. There is also significant variability in `log_Pause_Before` across different persons, as indicated by the group variance. The model has converged, indicating that the fitting process was successful. The log transformation has likely improved the model fit, as indicated by the lower scale value (1.1019) compared to the untransformed model.

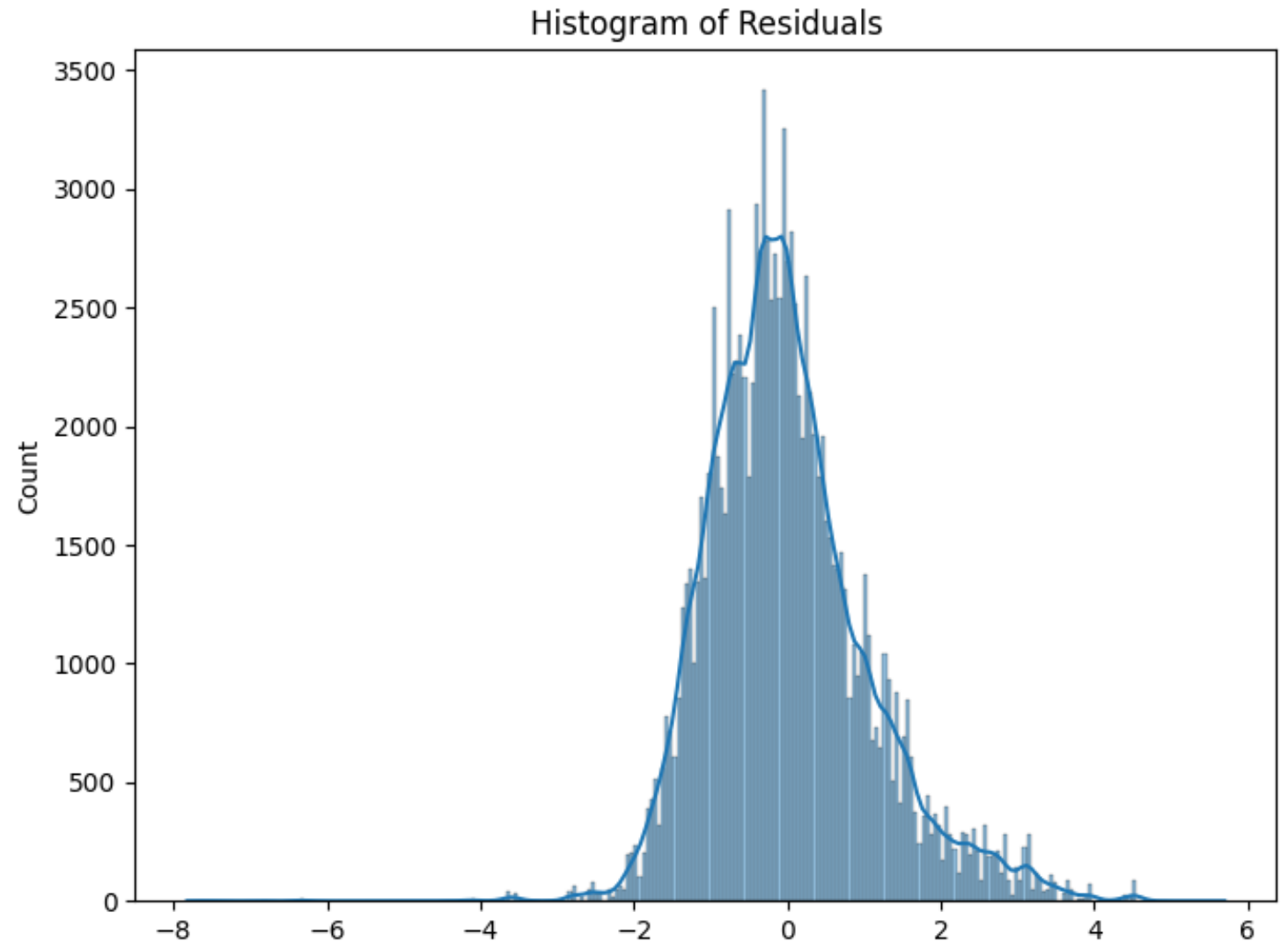
Same as before: validating the model

This plot helps check for homoscedasticity (constant variance of residuals). Ideally, the residuals should be randomly scattered around zero without any discernible pattern.



Distribution of Random Effects

The histogram should approximate a normal distribution if the random effects are normally distributed.



Model Comparison with and without Random Effects

- Comparing AIC and BIC values helps determine if including random effects improves the model. Lower AIC and BIC values indicate a better model fit.

```

                                OLS Regression Results
=====
Dep. Variable:          log_Pause_Before      R-squared:                0.011
Model:                  OLS                  Adj. R-squared:           0.011
Method:                 Least Squares        F-statistic:              1345.
Date:                   Mon, 29 Jul 2024     Prob (F-statistic):       1.01e-292
Time:                   14:14:31             Log-Likelihood:           -1.9132e+05
No. Observations:       118513              AIC:                     3.827e+05
Df Residuals:           118511              BIC:                     3.827e+05
Df Model:                1
Covariance Type:        nonrobust
=====
                                coef      std err          t      P>|t|      [0.025      0.975]
-----
Intercept              7.0703         0.007    950.435      0.000         7.056         7.085
Size                  -0.0782         0.002   -36.669      0.000        -0.082        -0.074
=====
Omnibus:               4849.665      Durbin-Watson:           1.498
Prob(Omnibus):          0.000      Jarque-Bera (JB):        5567.255
Skew:                   0.493      Prob(JB):                0.00
Kurtosis:               3.395      Cond. No.                7.82
=====

Notes:
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
AIC (Mixed-Effects Model): nan
BIC (Mixed-Effects Model): nan
AIC (Simple Model): 382650.4268990078
BIC (Simple Model): 382669.79245488415

```

En conclusion:

- Intercept : 7.648 -> Cette valeur représente la moyenne de la log_pause lorsque la taille du flux (size) est à 0.
- Effet de la taille du flux (size) : -0.071 -> Ce coefficient indique que pour chaque augmentation d'une unité dans la taille du flux, la log_pause diminue en moyenne de 0.071. Comme le coefficient est négatif, cela signifie qu'une augmentation de la taille du flux est associée à une diminution de la log_pause. **En d'autres termes, une augmentation de 1 unité de size est associée à une diminution de 0.071 ms dans la valeur logarithmique de la pause.**
- Variance du groupe : 0.532 -> Cette valeur suggère qu'il existe une variabilité significative de la log_pause entre les différents sujets. Autrement dit, il y a des différences importantes entre les sujets en ce qui concerne leurs pauses.