MS – E2112 – Multivariate statistical analysis – Home exercise 5

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Problem 1

Data: A 2-dimensional frequency table SMOKING.txt data was provided, where the details of smoking of employees in a company was tabulated. The employees were categorized into Senior Managers (SM), Junior managers (JM), Senior Employee (SE), Junior Employee (JE), Secretaries (SC), which were further categorized into None, Light, Medium and Heavy smokers.

a) The theoretical frequencies for the given data under independence is given in the table below. Each element is the product of its corresponding row and columns' marginal relative frequency. But the margin remain same as the observed frequencies.

	None	Light	Medium	Heavy
SM	3.476684	2.564767	3.533679	1.42487
JM	5.689119	4.196891	5.782383	2.331606
SE	16.119171	11.891192	16.38342	6.606218
JE	27.813472	20.518135	28.26943	11.398964
sc	7.901554	5.829016	8.031088	3.238342

b) The attraction repulsion matrix for the data is given below. It tells about the relationship between two modalities. If two modalities have a value greater than 1, it means they are attracted, less than 1, they are repulsed (unattracted) and if 1, it means they not related.

	None	Light	Medium	Heavy
SM	1.1505216	0.779798	0.8489736	1.4036364
JM	0.7030965	0.7148148	1.2105735	1.7155556
SE	1.5509482	0.8409586	0.7324478	0.6054902
JE	0.6471684	1.169697	1.1673387	1.1404545
sc	1.2655738	1.0293333	0.8716129	0.6176

- c) From the attraction repulsion matrix given above, the following analysis can be made.
 - 1. Junior Managers are the most frequent smokers (here, in heavy category) of all and Secretaries
 - are least frequent smokers (also in heavy category!).

 The smoking group of Junior Employees is most frequent of all the groups this is also highlighted by the fact they are repulsed in 'None' category with 0.64, denoting most of them
 - The Senior Employees are least frequent smokers which is also substantiated by more frequency in 'None' category.

Appendix

The code for the problem solved above.

```
setwd("~/Documents/OneDrive/Aalto/Sem2/MSA/Ex 5")
data <- read.table("SMOKING.txt", header = T, row.names = 1)</pre>
data <- data[,-5]</pre>
data <- data[-6,]</pre>
D <- as.matrix(data)</pre>
\# standardizing the row and columns so that they add to 1
prop.table(D,1) #row profile
prop.table(D,2) #col profile
v1 \leftarrow margin.table(D,1) \# Gives you the sum of all the rows
v2 \leftarrow margin.table(D,2) # Gives you the sum of all columns
n1 = length(v1)
n2 = length(v2)
V1 = matrix(v1, ncol = 1)
V2 = matrix(v2, ncol=n2)
E = V1 %*% V2 / sum(D)
AR.matrix <- D/E \# D = original data (number of observations)
# E = expected number of observations under independence
round(AR.matrix,2) # Round off to two digits
```