Your Daily Dose of Fiber (Bundles)

GSAW Research Symposium

Isaac M. Craig

3 April 2018

Bryn Mawr College

Products

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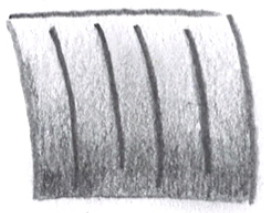

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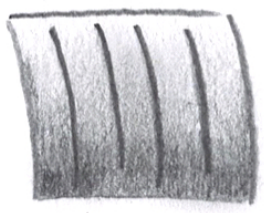

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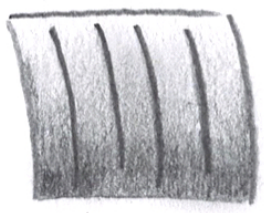

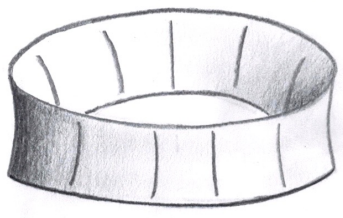

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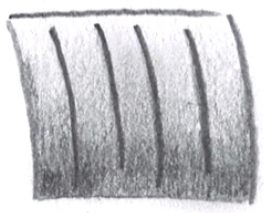

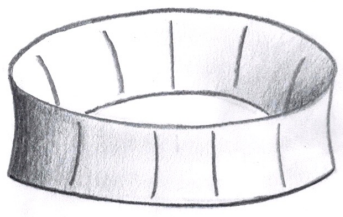

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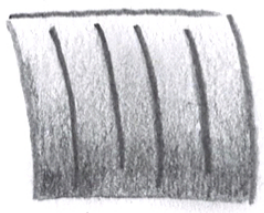

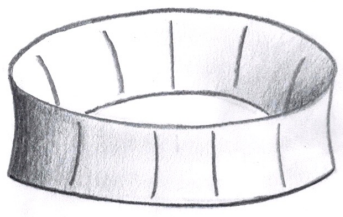

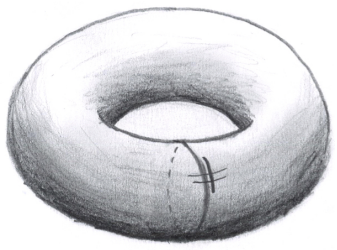

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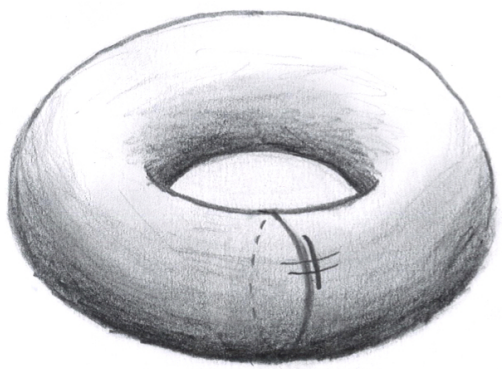

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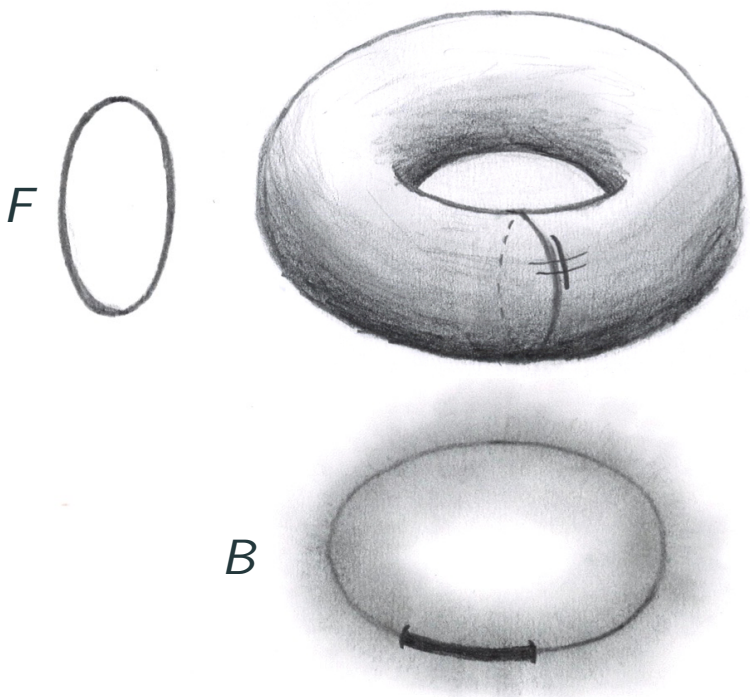

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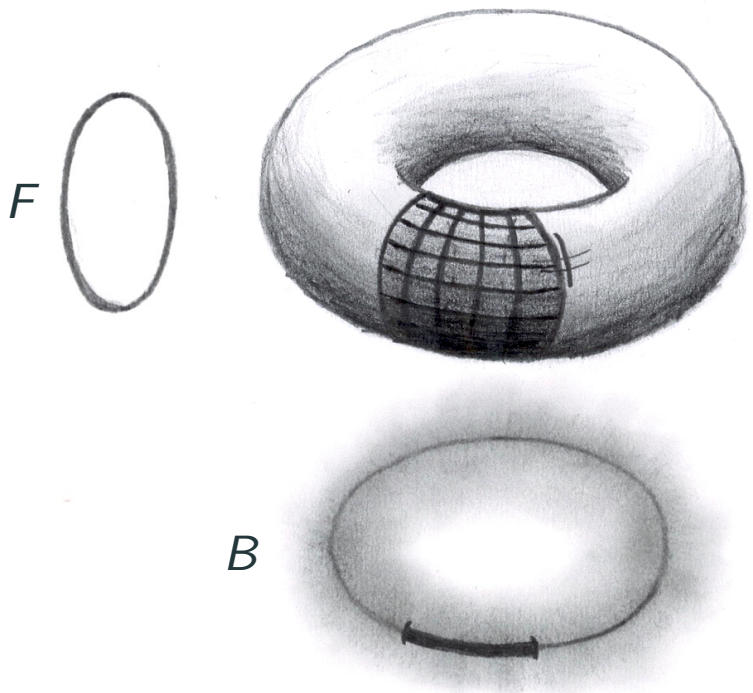

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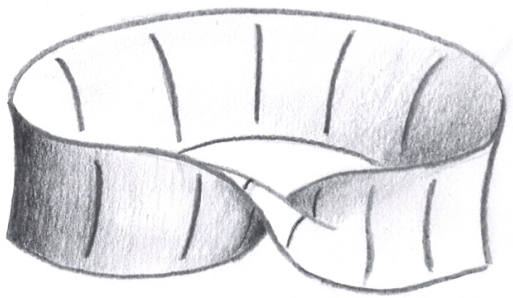

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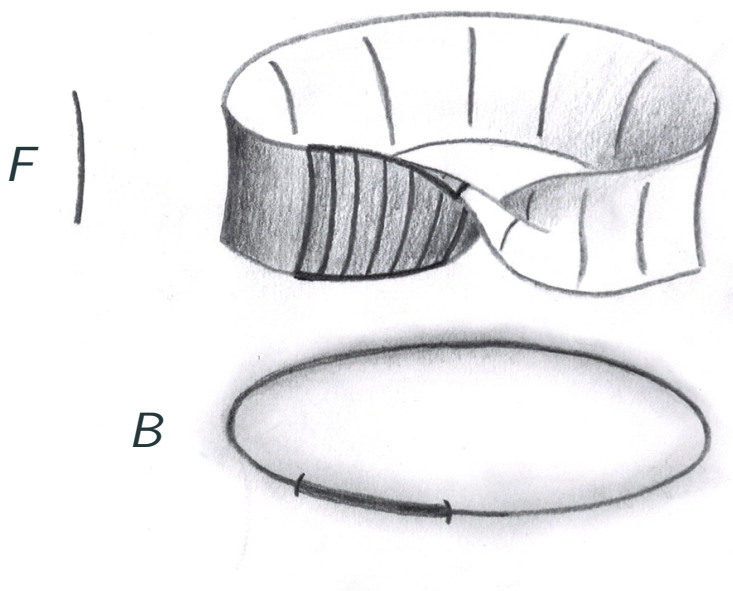

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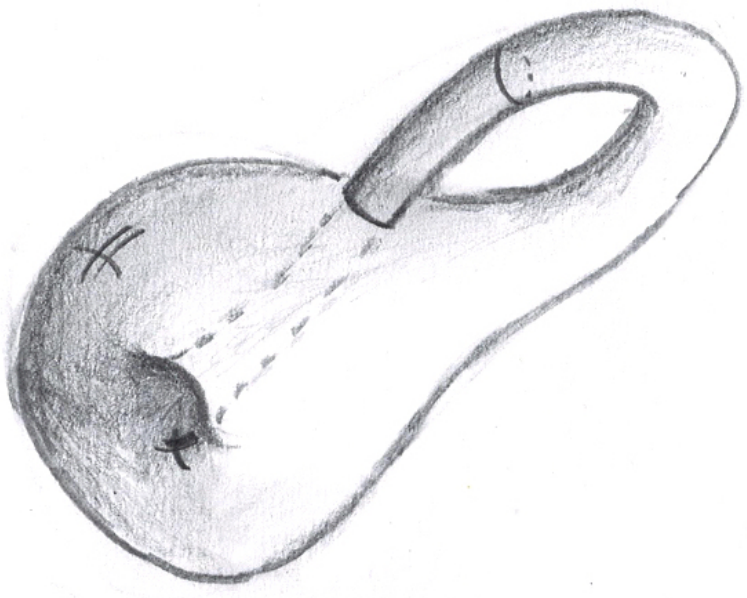

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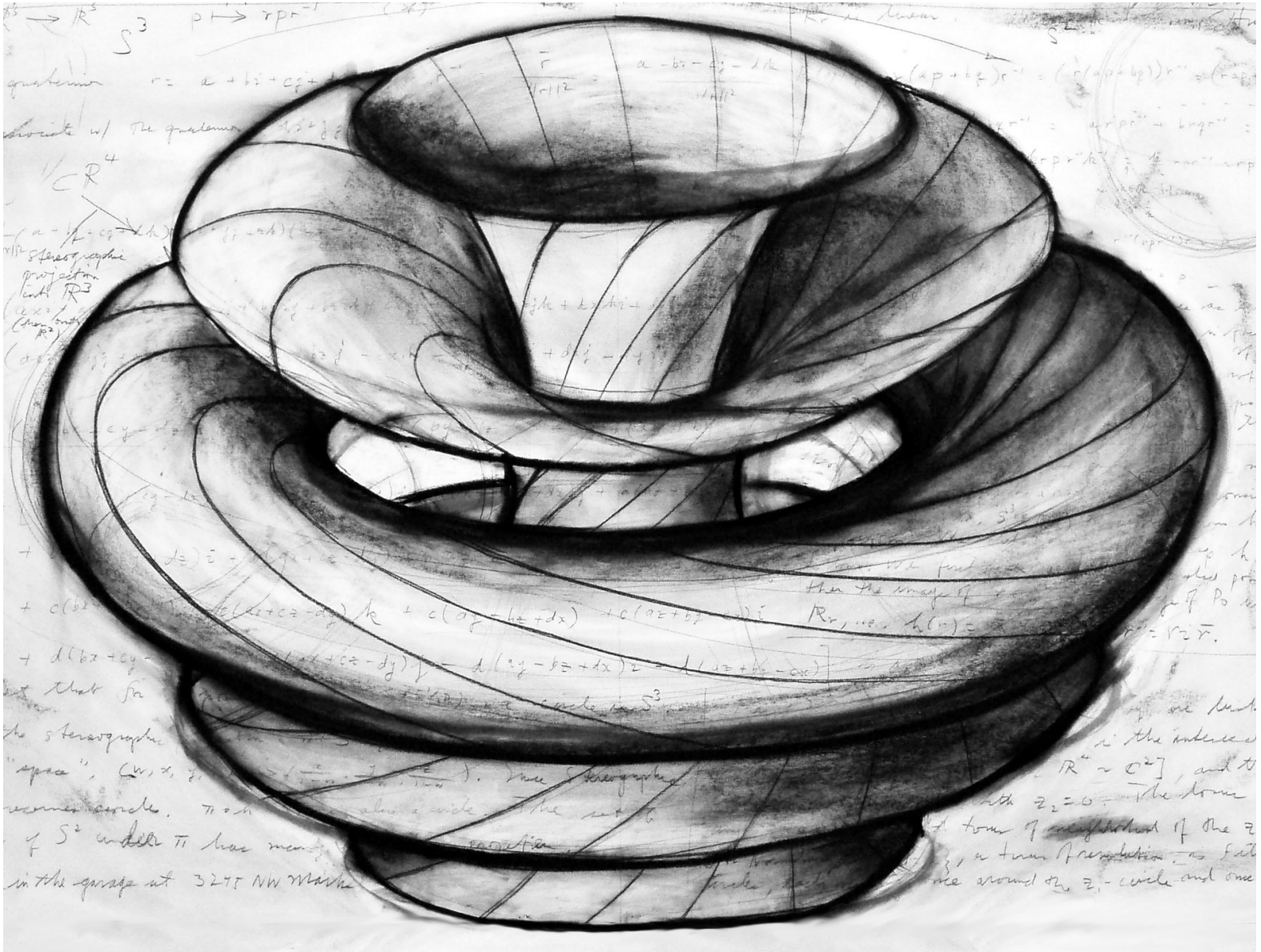

Photo cred: Lun-Yi Tsai

Thank you!