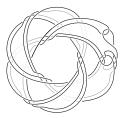
## Khovanov homology and surfaces in the 4-ball

#### Isaac Sundberg

Max-Planck-Institut für Mathematik

Low-dimensional Topology Seminar

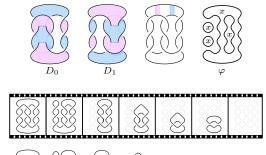
22 September 2022



#### Example 1

#### Proposition (S.-Swann 20, Hayden-S. 21)

The knot  $9_{46}$  bounds a pair of slice disks  $D_{0,1}$  distinguished up to boundary-preserving isotopy by their maps on Khovanov homology.

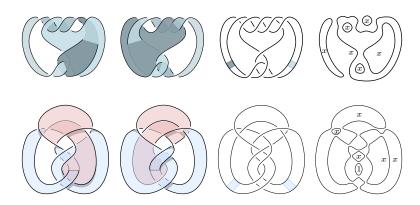


$$\mathsf{Kh}(D_1)(\varphi): \quad \bigotimes \left\{ -\bigotimes \left\{ -\bigotimes \left\{ -\bigotimes \right\} \right\} \right\} = \left\{ -\bigotimes \right\} - \left\{ -\bigotimes \right\} = \left\{ -\bigotimes$$

# Example 2

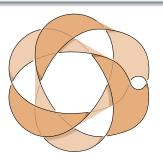
#### Proposition (Hayden-S. 21)

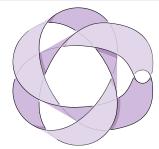
The knots  $15n_{103488}$  and  $17nh_{73}$  bound slice disks distinguished up to boundary-preserving isotopy by their maps on Khovanov homology.



#### Theorem (Hayden-Miller-Kim-Park-S. 22)

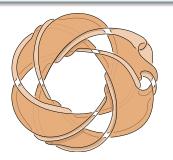
There are knots bounding pairs of non-isotopic Seifert surfaces, which remain non-isotopic when pushed into  $B^4$ .

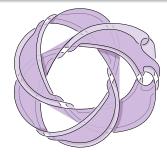




## Theorem (Hayden-Miller-Kim-Park-S. 22)

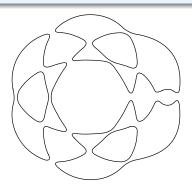
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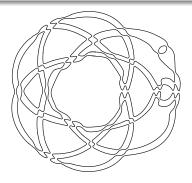
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(All x labels)

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# Thank You!

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