

Sprawozdanie lab2 Agnieszka Pierzcha?a

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In [1]: import numpy as np
import time

#ZADANIE 1

def gauss_jordan(a):

    n = a.shape[0]
    x= np.zeros(n)
    #print("Array before pivoting")
    #print(a)

    for i in range(n):
        for k in range(i+1,n):
            if(a[i][i]<a[k][i]):
                for j in range(n+1):
                    tmp = a[i][j];
                    a[i][j]=a[k][j];
                    a[k][j]=tmp;

    #print("Array after pivoting")
    #print(a)

    for i in range(n-1):
        for k in range(i+1,n):
            t = a[k][i]/a[i][i];
            for j in range(n+1):
                a[k][j] = a[k][j] - t*a[i][j];

    #print("Array after gaussian elimination")
    #print(a)

    for i in range(n-1,0,-1):
        for k in range(i-1,-1,-1):
            t = a[k][i]/a[i][i];
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        for j in range(n+1):
            a[k][j] = a[k][j] - t*a[i][j];

    #print("Array after gaussian elimination up")
    #print(a)

    for s in range(n):
        for j in range(n,-1,-1):
            a[s][j] = a[s][j]/a[s][s];
        x[s] = a[s][n]

    #print(x)
    return x

In [2]: a= np.array([[0.,2.,1.,-8.],[1.,-2.,-3.,0.],[-1.,1.,2.,3.]]);
        z=gauss_jordan(a)

In [3]: print(z)

[-4. -5.  2.]

In [9]: n=500
        b= np.random.rand(n,n+1);

In [10]: #measure time
        start = time.time()
        x=gauss_jordan(b)
        end = time.time()
        print('My solver time:',end - start)

        b=np.random.rand(n,n);
        y=np.random.rand(n,1);
        start = time.time()
        x=np.linalg.solve(b,y)
        end = time.time()
        print('Library solver time',end - start)

My solver time: 227.91824388504028
Library solver time 0.016000986099243164

In [11]: #ZAD 2
        def scale_matrix(matrix):
            scale_coefficient = matrix.max()
            return matrix/ scale_coefficient, scale_coefficient

        def create_pivot_matrix(a):

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n = a.shape[0]
x = np.identity(n)

for i in range(n):
    maxrow = a[i][i];
    row = i;
    for j in range(i,n):
        if(a[j][i]>maxrow):
            maxrow = a[j][i];
            row = j;
    if i != row :
        for k in range(n):
            tmp = x[i][k];
            x[i][k]=x[row][k];
            x[row][k]=tmp;

return x

def lu_decomposition(a, scaled= True ):
    n=a.shape[0]
    if(scaled):
        a, coefficient = scale_matrix(a)

    s=(n,n)
    L=np.zeros(s)
    U=np.zeros(s)
    P=create_pivot_matrix(a)
    PA = np.dot(P,a)

    for j in range(n):
        L[j][j] = 1.
        for i in range(j+1):
            s1 = 0.
            for k in range(i):
                s1+=U[k][j] * L[i][k]
            U[i][j] = PA[i][j] - s1;

        for i in range(j,n):
            s2 = 0.
            for k in range(j):
                s2+= U[k][j] * L[i][k]
            L[i][j] = (PA[i][j] - s2) / U[j][j]

    return (L,U,P)

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In [12]: d= np.array([[1.,3.,5.],[2.,4.,7.],[1.,1.,0.]])
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e= np.array([[11.,9.,24.,2.],[1.,5.,2.,6.],[3.,17.,18.,1.],[2.,5.,7.,1.]));

In [15]: (a,b) = scale_matrix(d)
          print(b)
          print(a)

          (l,u,p)=lu_decomposition(d,True)
          print('printing l')
          print(l)
          print('printing u')
          print(u)
          print('printing p')
          print(p)

7.0
[[ 0.14285714  0.42857143  0.71428571]
 [ 0.28571429  0.57142857  1.         ]
 [ 0.14285714  0.14285714  0.         ]]
printing l
[[ 1.  0.  0. ]
 [ 0.5 1.  0. ]
 [ 0.5 -1.  1. ]]
printing u
[[ 0.28571429  0.57142857  1.         ]
 [ 0.         0.14285714  0.21428571]
 [ 0.         0.         -0.28571429]]
printing p
[[ 0.  1.  0.]
 [ 1.  0.  0.]
 [ 0.  0.  1.]]

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