Algorithm 1 Insertion tache

```
1: function ADD_TASK(du_t, cpu_t)
                                                                                                                    \triangleright duration, number of cpu
         start \ key \leftarrow [0, du \ t, cpu \ t]
         end\_key \leftarrow [+\infty, +\infty, +\infty]
 3:
         profile\ tree \rightarrow \mathbf{node}\ \mathbf{loop}(start\ key, end\ key, \{
 4:
               starting\_time\_min \leftarrow (freespace \rightarrow \{starting\_time\})
 5:
               processor\_range\_t \leftarrow (freespace \rightarrow \{cpu\})
 6:
 7:
               return 1
         })
 8:
                                                                                               \triangleright Remove the number of cpu for the range
 9:
         processor\_range\_t \leftarrow (processor\_range\_t \rightarrow reduce\_to\_basic(cpu\_t))
10:
11:
         start key \leftarrow [0, 0, 0]
         end\_key \leftarrow [starting\_time\_min + du\_t, +\infty, +\infty]
12:
         profile\ tree \rightarrow \mathbf{node}\ \mathbf{loop}(start\ key, end\ key, \{
                                                                                                                    \rhd Research with contraints
13:
               {\bf push}\ free space\_impacted, free space
14:
               return 0
15:
         })
16:
         \mathbf{for}\ \mathit{freespace} \leftarrow \mathit{freespace}\ \mathit{impacted}\ \mathbf{do}
17:
              \mathbf{cut} \quad \mathbf{freespace}(freespace, starting\_time\_min, du\_t, processor\_range\_t)
18:
         end for
19:
20: end function
```

Algorithm 2 Decoupage Freespace

```
1: function CUT FREESPACE(freespace, start\ time, duration, processor\ range)
                          if Intersection(freespace \rightarrow \{cpu\}, processor\ range) > 0 then
   2:
                                       profile\ tree \rightarrow \mathbf{remove}(freespace)
   3:
   4:
                                       if freespace \rightarrow \{starting\ time\} < start\ time\ then
                                                    new freespaceright freespace \leftarrow (freespace \rightarrow {starting time}, start time - freespace \rightarrow
   5:
              \{starting\ time\}, freespace \rightarrow \{cpu\}\}
                                                   profile\ tree \rightarrow \mathbf{add}(right\ freespace)
   6:
   7:
                                       end if
                                      if freespace \rightarrow \{starting\ time\} < (start\ time + duration) then
   8:
   9:
                                                   \mathbf{new} \ free space eft\_free space \leftarrow (free space \rightarrow \{starting\_time\}, start\_time - free space \rightarrow \{start\_time\}, start\_time - free space \rightarrow \{sta
              \{starting\ time\}, freespace \rightarrow \{cpu\}\}
                                                   profile\ tree \rightarrow \mathbf{add}(left\ freespace)
10:
                                      end if
11:
                                       range\ test \leftarrow (freespace \rightarrow \{cpu\} \rightarrow \mathbf{copy}())
12:
13:
                                       range test \rightarrow \mathbf{remove}(processor range)
                                       if range\ test \rightarrow size() > 0 then
14:
                                                    new freespacenew freespace
                                                                                                                                                                                                                          (free space)
                                                                                                                                                                                                                                                                                                            \{starting\ time\}, freespace
15:
              \{duration\}, range\ test)
                                                   profile tree \rightarrow add(new freespace)
16:
17:
                                       end if
                          end if
18:
19: end function
```

Algorithm 3 Suppression tache

```
1: function REMOVE TASK(st t, d t, cpu t)
                                                                                                    ▷ Starting time, duration, cpu range
         et \ t \leftarrow (st \ t + d \ t)
                                                                                                                             ▶ End time of job
         start key \leftarrow [0, 0, 0]
 3:
         end\_key \leftarrow [st\_t + d\_t, +\infty, +\infty]
 4:
         profile\ tree \rightarrow \mathbf{node}\ \mathbf{loop}(start\ key, end\ key, \{
 5:
 6:
         push freespace impacted, freespace
 7:
         st t2 \leftarrow (freespace \rightarrow \{starting\ time\})
 8:
         et \ t2 \leftarrow (freespace \rightarrow \{starting \ time\} + freespace \rightarrow \{duration\})
         if (st \ t \leq st \ t2 \text{ and } st \ t2 \leq et \ t) then
 9:
             direction\{freespace\} \leftarrow -1
10:
         else if (st \ t2 \le st \ t \ and \ st \ t \le et \ t2) then
11:
12:
             direction\{freespace\} \leftarrow 1
         end if
13:
         if exist direction{freespace} then
14:
             \mathbf{for}\ t \leftarrow st\ \ t2\ \mathbf{to}\ et\ \ t2\ \mathbf{do}
15:
                  if exist tab\{t\} then
16:
                      add tab\{t\} \leftarrow (freespace \rightarrow \{cpu\} inter \ tab\{t\})
17:
18:
                      add tab\{t\} \leftarrow (freespace \rightarrow \{cpu\})
19:
20:
                  end if
             end for
21:
         end if
22:
23:
         for freespace \leftarrow freespace impacted do
24:
             extend freespace(freespace)
25:
         end for
26:
27: end function
```

Algorithm 4 Augmentation Freespace

```
1: function EXTEND FREESPACE(freespace)
        if direction\{freespace\} = 1 then
            t\_next \leftarrow (freespace \rightarrow \{starting\_time\} + freespace \rightarrow \{duration\})
 3:
        else
 4:
            t next \leftarrow freespace \rightarrow \{starting time\}
 5:
        end if
 6:
        new \quad t \leftarrow t \quad next
 7:
        while (exist tab\{new\_t\} and (tab\{new\_t\} inter freespace \rightarrow \{cpu\}) \geq freespace \rightarrow \{cpu\} \rightarrow \mathbf{size}())
 8:
    do
 9:
            t \quad max \leftarrow new \quad t
            new \ t \leftarrow (new \ t + direction\{freespace\})
10:
        end while
11:
        if direction\{freespace\} = 1 then
12:
             freespace \rightarrow \{duration\} \leftarrow (t\_next - freespace \rightarrow \{starting\_time\})
13:
14:
             freespace \rightarrow \{duration\} \leftarrow (freespace \rightarrow \{starting\ time\} - new\ t + freespace \rightarrow \{duration\})
15:
16:
             freespace \rightarrow \{starting\_time\} \leftarrow new\_t
        end if
17:
        TODO :VERIFIER SI L'ESPACE N'EST PAS COMPRIS DANS UN AUTRE
19: end function
```