1 Overview

The purpose of a computer graphics system is to enable a user to construct scenes and views to achieve a desired result. Often, speed or real-time performance is also a major concern. Building complex systems requires careful software design in order to minimize complexity, unexpected effects of changes, readability, and expandability. Modularity in computer graphics system design is an important component of achieving these goals.

The following document specifies the data structures, functions, and functionality for a basic 3D rendering system using C. The data types within the system include the following.

- Pixel data structure for holding image data for a single point
- Image data structure for holding the data for a single image
- Z-buffer a depth image, usually part of the Image data structure
- Point a 2D or 3D location in model space
- Line a line segment in 2D or 3D model space
- Circle a 2D circle
- Ellipse a 2D ellipse
- Polygon a closed shape consisting of line segments
- Polyline a sequence of connected line segments
- Color a representation of light energy
- Light a light source
- Vector a direction in 2D or 3D model space
- Matrix a 2D or 3D transformation matrix
- Element a element of a model of a scene
- Module a collection of elements
- View2D information required for a 2D view of a scene
- ViewPerspective information required for a perspective view of a scene
- ViewOrthographic information required for an orthographic view of a scene

Over the course of the semester, you will implement each of the above data structures using a C struct data type. The required fields and their purposes are given in the specification below. For each data type, you will also implement a set of functions. The function prototypes and and a description of the purpose of each required function are also included in the specification, and you are free to add additional functionality. If your code supports the required data types and functionality, then you will be able to run a series of test programs to evaluate and debug your system.

1.1 C versus C++

Many aspects of computer graphics are appropriate for an object-based approach to software design. Primitives such as lines, circles, points and polygons naturally exist as objects that need to be created, manipulated, drawn into an image, and destroyed. We may also want to store a symbolic representation of a scene by saving lists of primitives to a file, which is a natural part of an object-oriented approach.

The ideas of modularity and object-based design are possible to implement in either C or C++. The features of C++ give more structure and flexibility to the object-based approach; C gives the programmer lower-level control of information and forces a deeper understanding of how the information flow occurs. A continuum of possible software system structures are possible between the two extremes of a pure object-based C++ design and a modular, but strict C implementation.

As an example, consider the action of drawing a line into an image. Using C++, we might have a class and method prototyped as below. Creating a Line object and calling line.draw(src, color) would draw a line into the image of the specified color.

```
class Line {
public:
    Point a;
    Point b;

    Line(const Point &a, const Point &b);
    int draw(Image &src, const Color &c);

};

int Line::draw(Image &src, const Color &c) {
    // all of the required information is in the Line class or Image class
    // draw the line from a to b with color c
    return(0);
}
```

The straight C code below has identical functionality and about the same level of modularity. In the main program, calling lineDraw(line, src, color) with a Line structure, an Image and a Color will draw the line in the image.

```
typedef struct {
  Point a;
  Point b;
} Line;

int lineDraw(Line *line, Image *src, Color *b) {
  // all of the required information is in the Line or Image structures
  // draw the line from a to b with color c
  return(0);
}
```

The difference between the two is that in C all of the information required by a function must be explicitly passed through the parameters. In C++, the object on which a method is called can provide some, if not all of the information. Note also that in C passing by reference is not an option: all C parameters are passed by value, which means copies of the parameters get passed to the function. In C++, passing by reference is possible. Note that in both C and C++ we want to avoid passing whole data structures.

2 Image

The image is a basic object in computer graphics. Conceptually, it is a canvas on which object primitives can draw themselves. A useful way of thinking about the image is to treat it as a storage device that holds color data. In graphics we may want our image to also hold depth data—distance from the camera. Other objects can write to or read from the image as necessary, modifying the values stored in the image. An image needs to know how to read from and write itself to a file. Note that the data type of the file does not need to match the internal data type of the image.

Use a float type to represent the RGB, alpha, and depth values in your image. You can organize the data as you see fit. One possible organization method is to create an FPixel type like the following.

```
typedef struct {
  float rgb[3];
  float a;
  float z;
} FPixel;
```

Then you can use a single or double pointer of FPixel type to represent all of the necessary image data.

Image Fields

- data: pointer or double pointer to space for storing Pixels
- rows: number of rows in the image
- cols: number of columns in the image
- maxval: (optional) maximum value for a pixel
- filename: (optional) char array to hold the filename of the image

2.1 Image Functions

Constructors and destructors:

- Image *image_create(int rows, int cols) Allocates an Image structure and initializes the top level fields to appropriate values. Allocates space for an image of the specified size, unless either rows or cols is 0. Returns a pointer to the allocated Image structure. Returns a NULL pointer if the operation fails.
- void image_free (Image *src) de-allocates image data and frees the Image structure.
- void image_init (Image *src) given an uninitialized Image structure, sets the rows and cols fields to zero and the data field to NULL.
- int image_alloc(Image *src, int rows, int cols) allocates space for the image data given rows and columns and initializes the image data to appropriate values, such as 0.0 for RGB and 1.0 for A and Z. Returns 0 if the operation is successful. Returns a non-zero value if the operation fails. This function should free existing memory if rows and cols are both non-zero.
- void image_dealloc(Image *src) de-allocates image data and resets the Image structure fields. The function does not free the Image structure.

I/O functions:

- Image *image_read(char *filename) reads a PPM image from the given filename. An optional extension is to determine the image type from the filename and permit the use of different file types. Initializes the alpha channel to 1.0 and the z channel to 1.0. Returns a NULL pointer if the operation fails.
- int image_write(Image *src, char *filename) writes a PPM image to the given filename. Returns 0 on success. Optionally, you can look at the filename extension and write different file types.

Access

- FPixel image_getf(Image *src, int r, int c) returns the FPixel at (r, c).
- float image_getc(Image *src, int r, int c, int b) returns the value of band b at pixel (r, c).
- float image_geta(Image *src, int r, int c) returns the alpha value at pixel (r, c).
- float image_getz(Image *src, int r, int c) returns the depth value at pixel(r, c).
- void image_setf(Image *src, int r, int c, FPixel val) sets the values of pixel (r, c) to the FPixel val.
- void image_setc(Image *src, int r, int c, int b, float val) sets the value of pixel(r, c) band b to val.
- void image_seta(Image *src, int r, int c, float val) sets the alpha value of pixel (r, c) to val.
- void image_setz(Image *src, int r, int c, float val) sets the depth value of pixel (r, c) to val.
- The programmer can also access to the image data directly. You may choose whether to organize the image data as a 1-D single pointer or a 2-D double-pointer.

Utility

- void image_reset (Image *src) resets every pixel to a default value (e.g. Black, alpha value of 1.0, z value of 1.0).
- void image_fill(Image *src, FPixel val) sets every FPixel to the given value.
- void image_fillrgb(Image *src, float r, float g, float b) sets the (r, g, b) values of each pixel to the given color.
- void image_filla(Image *src, float a) sets the alpha value of each pixel to the given value.
- void image_fillz(Image *src, float z) sets the z value of each pixel to the given value.

3 Color

As we move into shading and 3D color calculations, it will be important to use floating point math rather than integer math to represent colors. The Color type is the same as the RGB component of an FPixel. You may also want to create functions that convert between an integer and a float representation, doing appropriate scaling. Colors, which are used for calculating shading, use a range of [0, 1], while Pixels for writing to an integer-based file format generally use a range of [0, 255], although 16-bits per pixel is becoming more common.

A simple way to define a Color in C is as an array of floats.

```
typedef float Color[3];
```

However, this representation can also be cumbersome for some tasks (like copying). So the recommended method of making a Color type in C is as below.

```
typedef struct {
float c[3];
} Color;
```

A simple assignment will copy a color if you use the struct definition.

3.1 Color Functions

Define the following functions for the Color type.

```
void color_copy(Color *to, Color *from)
- copies the Color data.

void color_set(Color *to, float r, float g, float b)
- sets the Color data.

In addition, add the following functions for an Image.

void image_setColor( Image *src, int r, int c, Color val )
- copies the Color data to the proper pixel.

Color image_getColor( Image *src, int r, int c)
- returns a Color structure built from the pixel values.
```

4 Primitive Objects

Primitive objects like pixels, lines, circles, and polygons must hold enough information to know where and how to draw themselves in an image. The primitives Point, Line, Circle, and Ellipse are required for this assignment. The minimum fields required for each type are listed below. Note that on this assignment all z-values will be ignored. However, we'll need them for 3D in a few weeks. Why we're using 4-element vectors for 3D will become clear soon.

In C, while you could use typedef double Point[4];, it is probably easier to use a struct.

Point fields

• double val[4] - four element vector of doubles.

Line fields

- int zBuffer; whether to use the z-buffer, should default to true (1).
- Point a starting point
- Point b ending point

Circle fields

- double r-radius,
- Point c center

Ellipse fields

- double ra major axis radius
- double rb minor axis radius
- Point c center
- double a (optional) angle of major axis relative to the X-axis

Polyline fields (C)

- int zBuffer; whether to use the z-buffer; should default to true (1).
- int numVertex Number of vertices
- Point *vertex vertex information

4.1 Primitive Functions

Point

- void point_set2D (Point *p, double x, double y)

 set the first two values of the vector to x and y. Set the third value to 0.0 and the fourth value to 1.0.
- void point_set3D(Point *p, double x, double y, double z) set the point's values to x and y and z. Set the homogeneous coordinate to 1.0.
- void point_set(Point *p, double x, double y, double z, double h) set the four values of the vector to x, y, z, and h, respectively.
- void point_normalize (Point *p) - normalize the x and y values of a point by its homogeneous coordinate: x = x/h, y = y/h.
- void point_copy(Point *to, Point *from)
 copy the point data structure.
- void point_draw(Point *p, Image *src, Color c)
 draw the point into src using color c.
- void point_drawf(Point *p, Image *src, FPixel c)
 draw the p into src using FPixel c.
- void point_print(Point *p, FILE *fp)
 - use fprintf to print the contents of the Point to the stream fp. The FILE pointer fp can be an actual file opened using fopen or a standard output stream like stdout or stderr, both defined in stdio.h. The point_print function doesn't care which it is, it just uses fprintf, which takes a FILE pointer as the first argument.

Line

- void line_set2D(Line *1, double x0, double y0, double x1, double y1) initialize a 2D line.
- void line_set(Line *1, Point ta, Point tb)
 initialize a line to ta and tb.
- void line_zBuffer(Line *1, int flag)
 set the z-buffer flag to the given value.
- void line_normalize(Line *1)
 - normalize the x and y values of the endpoints by their homogeneous coordinate.
- void line_copy (Line *to, Line *from)
 copy the line data structure.
- void line_draw(Line *1, Image *src, Color c) draw the line into src using color c.

Circle

- void circle_set(Circle *c, Point tc, double tr) initialize to center tc and radius tr.
- void circle_draw(Circle *c, Image *src, Color p)
 draw the circle into src using color p.
- void circle_drawFill(Circle *c, Image *src, Color p) draw a filled circle into src using color p.

Ellipse

- void ellipse_set(Ellipse *e, Point tc, double ta, double tb)
 initialize an ellipse to location tc and radii ta and tb.
- void ellipse_draw(Ellipse *e, Image *src, Color p)
 draw into src using color p.
- void ellipse_drawFill(Ellipse *e, Image *src, Color p)
 draw a filled ellipse into src using color p.

Polyline

The functions polyline_create and polyline_free manage both the Polyline data structure and the memory required for the vertex list.

- Polyline *polyline_create()
 returns an allocated Polyline pointer initialized so that numVertex is 0 and vertex is NULL.
- Polyline *polyline_createp(int numV, Point *vlist)

 returns an allocated Polyline pointer with the vertex list initialized to the points in vlist.
- void polyline_free (Polyline *p)
 frees the internal data and the Polyline pointer.

The functions polyline_init, polyline_set, and polyline_clear work on a pre-existing Polyline data structure and manage only the memory required for the vertex list.

- void polyline_init (Polyline *p)
 initializes the pre-existing Polyline to an empty Polyline.
- void polyline_set (Polyline *p, int numV, Point *vlist)
 initializes the vertex list to the points in vlist. De-allocates/allocates the vertex list for p, as necessary.
- void polyline_clear (Polyline *p)

 frees the internal data for a Polyline, if necessary, and sets numVertex to 0 and vertex to NULL.
- void polyline_zBuffer(Polyline *p, int flag)
 sets the z-buffer flag to the given value.
- void polyline_copy(Polyline *to, Polyline *from)
 - De-allocates/allocates space as necessary in the destination Polyline data structure and copies the vertex data from the source polyline (from) to the destination (to).
- void polyline_print (Polyline *p, FILE *fp)
 prints Polyline data to the stream designated by the FILE pointer.
- void polyline_normalize (Polyline *p)
 normalize the x and y values of each vertex by the homogeneous coordinate.
- void polyline_draw(Polyline *p, Image *src, Color c)
 - draw the polyline using color c.

5 Polygon

Polygons require a more complex type than the other primitive objects because they are variable sized structures. Polygons are very similar to Polylines, but they can also be filled with a color. It is assumed that the last vertex of a polygon connects back to the first. As you develop your system, you may want to add more fields into your polygon than the required fields listed below.

Polygon fields (C)

- int nVertex Number of vertices
- Point *vertex vertex information
- int zBuffer; whether to use the z-buffer; should default to true (1)

5.1 Polygon Functions

Polygon

The functions polygon_create and polygon_free manage both the Polygon data structure and the memory required for the vertex list.

- Polygon *polygon_create()
 - returns an allocated Polygon pointer initialized so that numVertex is 0 and vertex is NULL.
- Polygon *polygon_createp(int numV, Point *vlist)
 - returns an allocated Polygon pointer with the vertex list initialized to a copy of the points in vlist.
- void polygon_free(Polygon *p)
 - frees the internal data for a Polygon and the Polygon pointer.

The functions polygon_init, polygon_set, and polygon_clear work on a pre-existing Polygon data structure and manage only the memory required for the vertex list.

- void polygon_init(Polygon *p)
 - initializes the existing Polygon to an empty Polygon.
- void polygon_set(Polygon *p, int numV, Point *vlist)
 - initializes the vertex array to the points in vlist.
- void polygon_clear(Polygon *p)
 - frees the internal data and resets the fields.
- ullet void polygon_zBuffer(Polygon *p, int flag)
 - sets the z-buffer flag to the given value.
- void polygon_copy(Polygon *to, Polygon *from)
 - De-allocates/allocates space and copies the vertex and color data from one polygon to the other.
- void polygon_print(Polygon *p, FILE *fp)
 - prints polygon data to the stream designated by the FILE pointer.

- void polygon_normalize (Polygon *p)
 normalize the x and y values of each vertex by the homogeneous coord.
- void polygon_draw(Polygon *p, Image *src, Color c) draw the outline of the polygon using color c.
- void polygon_drawFill (Polygon *p, Image *src, Color c)

 draw the filled polygon using color c with the scanline rendering algorithm.
- void polygon_drawFillB(Polygon *p, Image *src, Color c)

 draw the filled polygon using color c with the Barycentric coordinates algorithm.

6 Transformation Matrices

Transform matrices should be 4x4 matrices of doubles. Use a structure (C) with a 4x4 array in the structure. In C, the type could be declared as below.

```
typedef struct {
    double m[4][4];
} Matrix;
```

You will also need a Vector type. You can make your Vector type be identical in form to your Point type, but they have different mathematical meanings. A Vector is a direction, while a Point is a location.

```
typedef Point Vector;
```

Vectors should have a zero as their homogeneous coordinate so they do not undergo translations. You can get away with only three values as part of the Vector class (because h=0). The implementation details are up to you, but avoid any dynamic memory allocation. Note that the vector_set function only takes three arguments (x, y, z).

6.1 Vector Functions

- void vector_set(Vector *v, double x, double y, double z) Set the Vector to (x, y, z, 0.0).
- void vector_print(Vector *v, FILE *fp)
 - Print out the Vector to stream fp in a pretty form.
- void vector_copy(Vector *dest, Vector *src)
 - Copy the src Vector into the dest Vector.
- double vector_length(Vector *v)
 - Returns the Euclidean length of the vector, assuming the homogeneous coordinate is 1.0.

$$L = \|\vec{v}\| = \sqrt{v_x^2 + v_y^2 + v_z^2} \tag{1}$$

- void vector_normalize(Vector *v)
 - Normalize the Vector to unit length. Do not modify the homogeneous coordinate.

$$\hat{v} = \vec{v} \left(\frac{1}{L} \right) \tag{2}$$

- double vector_dot(Vector *a, Vector *b)
 - Returns the scalar product of \vec{a} and \vec{b} .

$$d(a,b) = a_x b_x + a_y b_y + a_z b_z \tag{3}$$

- void vector_cross(Vector *a, Vector *b, Vector *c)
 - Calculates the the cross product (vector product) of \vec{a} and \vec{b} and puts the result in \vec{c} .

$$\begin{bmatrix} c_x \\ c_y \\ c_z \end{bmatrix} = \vec{a} \times \vec{b} = \begin{bmatrix} a_y b_z - a_z b_y \\ a_z b_x - a_x b_z \\ a_x b_y - a_y b_x \end{bmatrix}$$
(4)

6.2 2D and Generic Matrix Functions

The following functions should be defined for matrices.

- void matrix_print(Matrix *m, FILE *fp)
 - Print out the matrix in a nice 4x4 arrangement with a blank line below.
- void matrix_clear (Matrix *m)
 - Set the matrix to all zeros.
- void matrix_identity(Matrix *m)
 - Set the matrix to the identity matrix.

$$M = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \tag{5}$$

- double matrix_get(Matrix *m, int r, int c)
 - Return the element of the matrix at row r, column c.
- void matrix_set(Matrix *m, int r, int c, double v)
 - Set the element of the matrix at row r, column c to v.
- void matrix_copy (Matrix *dest, Matrix *src)
 - Copy the src matrix into the dest matrix.
- void matrix_transpose (Matrix *m)
 - Transpose the matrix m in place.
- void matrix_multiply(Matrix *left, Matrix *right, Matrix *m)
 - Multiply left and right and put the result in m.

$$[M] = [left] [right] \tag{6}$$

Make sure that the function is written so that the result matrix can also be the left or right matrix.

- void matrix_xformPoint(Matrix *m, Point *p, Point *q)
 - Transform the point p by the matrix m and put the result in q. For this function, p and q need to be different variables.

$$\vec{q} = M\vec{p} \tag{7}$$

- void matrix_xformVector(Matrix *m, Vector *p, Vector *q)
 - Transform the vector p by the matrix m and put the result in q. For this function, p and q need to be different variables.
- void matrix_xformPolygon(Matrix *m, Polygon *p)
 - Transform the points and surface normals (if they exist) in the Polygon p by the matrix m.
- void matrix_xformPolyline(Matrix *m, Polyline *p)
 - Transform the points in the Polyline p by the matrix m.
- void matrix_xformLine(Matrix *m, Line *line)
 - Transform the points in line by the matrix m.

- ullet void matrix_scale2D(Matrix *m, double sx, double sy)
 - Premultiply the matrix by a scale matrix parameterized by s_x and s_y .

$$M = S(s_x, s_y)M = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} M$$
 (8)

- void matrix_rotateZ(Matrix *m, double cth, double sth)
 - Premultiply the matrix by a Z-axis rotation matrix parameterized by $cos(\theta)$ and $sin(\theta)$, where θ is the angle of rotation about the Z-axis.

$$M = R_Z(\cos(\theta), \sin(\theta))M = \begin{bmatrix} \cos(\theta) & -\sin(\theta) & 0 & 0\\ \sin(\theta) & \cos(\theta) & 0 & 0\\ 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 1 \end{bmatrix} M$$
 (9)

- void matrix_translate2D(Matrix *m, double tx, double ty)
 - Premultiply the matrix by a 2D translation matrix parameterized by t_x and t_y .

$$M = T(t_x, t_y)M = \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} M$$
 (10)

- void matrix_shear2D (Matrix *m, double shx, double shy)
 - Premultiply the matrix by a 2D shear matrix parameterized by sh_x and sh_y .

$$M = Sh(sh_x, sh_y)M = \begin{bmatrix} 1 & sh_x & 0 & 0 \\ sh_y & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} M$$
 (11)

6.3 3D Matrix Functions

- void matrix_translate(Matrix *m, double tx, double ty, double tz)
 - Premultiply the matrix by a translation matrix parameterized by t_x , t_y , and t_z .

$$M = T(t_x, t_y, t_z)M = \begin{bmatrix} 1 & 0 & 0 & t_x \\ 0 & 1 & 0 & t_y \\ 0 & 0 & 1 & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} M$$
(12)

- void matrix_scale(Matrix *m, double sx, double sy, double sz)
 - Premultiply the matrix by a scale matrix parameterized by s_x , s_y , s_z .

$$M = S(s_x, s_y, s_z)M = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} M$$
(13)

- void matrix_rotateX(Matrix *m, double cth, double sth)
 - Premultiply the matrix by a X-axis rotation matrix parameterized by $cos(\theta)$ and $sin(\theta)$, where θ is the angle of rotation about the X-axis.

$$M = R_X(\cos(\theta), \sin(\theta))M = \begin{bmatrix} 1 & 0 & 0 & 0\\ 0 & \cos(\theta) & -\sin(\theta) & 0\\ 0 & \sin(\theta) & \cos(\theta) & 0\\ 0 & 0 & 0 & 1 \end{bmatrix} M$$
 (14)

- void matrix_rotateY(Matrix *m, double cth, double sth)
 - Premultiply the matrix by a Y-axis rotation matrix parameterized by $cos(\theta)$ and $sin(\theta)$, where θ is the angle of rotation about the Y-axis.

$$M = R_Y(\cos(\theta), \sin(\theta))M = \begin{bmatrix} \cos(\theta) & 0 & \sin(\theta) & 0\\ 0 & 1 & 0 & 0\\ -\sin(\theta) & 0 & \cos(\theta) & 0\\ 0 & 0 & 0 & 1 \end{bmatrix} M$$
 (15)

- void matrix_rotateXYZ(Matrix *m, Vector *u, Vector *v, Vector *w)
 - Premultiply the matrix by an XYZ-axis rotation matrix parameterized by the vectors \vec{u} , \vec{v} , and \vec{w} , where the three vectors represent an orthonormal 3D basis.

$$M = R_{XYZ}(\vec{u}, \vec{v}, \vec{w})M = \begin{bmatrix} u_x & u_y & u_z & 0 \\ v_x & v_y & v_z & 0 \\ w_x & w_y & w_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} M$$
 (16)

- void matrix_shearZ(Matrix *m, double shx, double shy)
 - Premultiply the matrix by a shear Z matrix parameterized by shx and shy.

$$M = Sh_z(sh_x, sh_y)M = \begin{bmatrix} 1 & 0 & shx & 0 \\ 0 & 1 & shy & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} M$$
(17)

- void matrix_perspective(Matrix *m, double d)
 - Premultiply the matrix by a perspective matrix parameterized by d.

$$M = Persp(d)M = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 1/d & 0 \end{bmatrix} M$$
(18)

7 Viewing

7.1 2D Viewing

Define a 2D View structure View2D that converts world Cartesian coordinates (y-axis up, x-axis right) into screen coordinates. The structure should have fields for the following data.

- The **center** of the view rectangle V_0 in world coordinates
- The width of the view rectangle du in world coordinates
- The orientation angle θ_v or the x-axis of the view window expressed as a normalized vector (n_x, n_y) . The relationship between the two is given by $(n_x, n_y) = (\cos(\theta_v), \sin(\theta_v))$.
- \bullet The number of columns C in the output image
- The number of rows R in the output image

Define a function to generate a view transformation matrix VTM. The function should set the VTM to the view specified by the structure.

void matrix_setView2D (Matrix *vtm, View2D *view) — Sets vtm to be the view transformation defined by the 2DView structure.

The height of the view rectangle in world coordinates is given by:

$$dv = \frac{duR}{C} \tag{19}$$

The VTM is the multiplication of four matrices. The process involves translating the origin of the view window to the origin, orienting the view window with the x-axis, scaling the view window and flipping the y-axis, then shifting the range of y-values back to [0, R].

$$VTM = T(\frac{C}{2}, \frac{R}{2})S(\frac{C}{du}, -\frac{R}{dv})R_z(n_x, -n_y)T(-V_{0x}, -V_{0y})$$
(20)

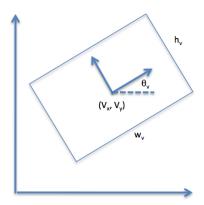


Figure 1: 2D view parameters shown in a world coordinate system.

7.2 Perspective Viewing

Define a View3D structure/class as below.

```
typedef struct {
   Point vrp;
   Vector vpn;
   Vector vup;
   double d;
   double du;
   double f;
   double b;
   int screenx;
   int screeny;
} View3D;
```

- View Reference Point [VRP]: 3-D vector indicating the origin of the view reference coordinates.
- View Plane Normal [VPN]: 3-D vector indicating the direction in which the viewer is looking.
- View Up Vector [VUP]: 3-D vector indicating the UP direction on the view plane. The only restriction is that it cannot be parallel to the view plane normal.
- Projection Distance [d]: distance in the negative VPN direction at which the center of projection is located.
- View Window Extent [du, dv]: extent of view plane around the VRP, expressed in world coordinate distances.
- Front and Back Clip Planes [F, B]: front and back clip planes expressed as distances along the positive VPN. F > 0 and F < B.
- Screen Size [screenX, screenY]: Size of the desired image in pixels.

void matrix_setView3D (Matrix *vtm, View3D *view) - Implement the 3D perspective pipeline. When the function returns, the vtm should contain the complete view matrix. Inside the function, begin by initializing VTM to the identity. Do not modify any of the values in the PerspectiveView structure inside the function (no side-effects).

8 Hierarchical Modeling

A module is primarily a linked list of elements. Example definitions of a Module and an Element type in C are given below. If you wish, you can create a union that can be any of the basic primitive types {Point, Line, Polygon, Polyline, Matrix, Pixel, and void * (for a Module *)} and use it instead of a void pointer in the Element structure.

```
typedef enum { // example of an enumerated type
 ObjNone,
 ObjLine,
 ObjPoint,
 ObjPolyline,
 ObjPolygon,
 ObjIdentity,
  ObjMatrix,
  ObjColor,
  ObjBodyColor,
  ObjSurfaceColor,
 ObjSurfaceCoeff,
 ObjLight,
 ObjModule
} ObjectType;
// option 1 for Element structure (void * option)
typedef struct {
   ObjectType type; // Type of object stored in the obj pointer
    void *obj;  // pointer to the object
void *next;  // next pointer
} Element;
// option 2 for Element structure (union option)
typedef union {
 Point point;
 Line line;
 Polyline polyline;
 Polygon polygon;
 Matrix matrix;
 Color color;
 float coeff;
 void *module;
} Object;
// Module structure
typedef struct {
 ObjectType type;
 Object obj;
 void *next;
} Element;
typedef struct {
   Element *head;  // pointer to the head of the linked list
    Element *tail; // keep around a pointer to the last object
} Module;
```

8.1 2D and Generic Module Functions

The following set of functions create, add items to, manipulate, draw, and destroy Modules and Elements. Note that most of the module_functions will be similar.

- Element *element_create()
 - Allocate and return an initialized but empty Element.
- Element *element_init(ObjectType type, void *obj)
 - Allocate an Element and store a **duplicate** of the data pointed to by obj in the Element. Modules do not get duplicated. The function needs to handle each type of object separately in a case statement.
- void element_delete(Element *e)
 - free the element and the object it contains, as appropriate.
- Module *module_create()
 - Allocate an empty module.
- void module_clear(Module *md)
 - clear the module's list of Elements, freeing memory as appropriate.
- void module_delete(Module *md)
 - Free all of the memory associated with a module, including the memory pointed to by md.
- void module_insert(Module *md, Element *e)
 - Generic insert of an element into the module at the tail of the list.
- void module_module (Module *md, Module *sub)
 - Adds a pointer to the Module sub to the tail of the module's list.
- void module_point(Module *md, Point *p)
 - Adds p to the tail of the module's list.
- void module_line(Module *md, Line *p)
 - Adds p to the tail of the module's list.
- void module_polyline(Module *md, Polyline *p)
 - Adds p to the tail of the module's list.
- void module_polygon (Module *md, Polygon *p)
 - Adds p to the tail of the module's list.
- void module_identity(Module *md)
 - Object that sets the current transform to the identity, placed at the tail of the module's list.
- void module_translate2D (Module *md, double tx, double ty)
 - Matrix operand to add a translation matrix to the tail of the module's list.
- void module_scale2D(Module *md, double sx, double sy)
 - Matrix operand to add a scale matrix to the tail of the module's list.
- void module_rotateZ(Module *md, double cth, double sth)
 - Matrix operand to add a rotation about the Z axis to the tail of the module's list
- void module_shear2D(Module *md, double shx, double shy)
 - Matrix operand to add a 2D shear matrix to the tail of the module's list.

- void module_draw(Module *md, Matrix *VTM, Matrix *GTM, DrawState *ds, Lighting *lighting, Image *src)
 - Draw the module into the image using the given view transformation matrix [VTM], Lighting and DrawState by traversing the list of Elements. (For now, Lighting can be an empty structure.)

8.2 3D Module functions

- void module_translate(Module *md, double tx, double ty, double tz) Matrix operand to add a 3D translation to the Module.
- void module_scale(Module *md, double sx, double sy, double sz) Matrix operand to add a 3D scale to the Module.
- void module_rotateX(Module *md, double cth, double sth)
 - Matrix operand to add a rotation about the X-axis to the Module.
- void module_rotateY(Module *md, double cth, double sth)
 - Matrix operand to add a rotation about the Y-axis to the Module.
- void module_rotateXYZ (Module *md, Vector *u, Vector *v, Vector *w) Matrix operand to add a rotation that orients to the orthonormal axes $\vec{u}, \vec{v}, \vec{w}$.
- void module_cube (Module *md, int solid)
 Adds a unit cube, axis-aligned and centered on zero to the Module. If solid is zero, add only lines.
 If solid is non-zero, use polygons. Make sure each polygon has surface normals defined for it.

8.3 Shading/Color Module Functions

- void module_color(Module *md, Color *c)
 - Adds the foreground color value to the tail of the module's list.

9 DrawState

The DrawState structure specifies how an object is to be drawn into the image. The draw state can affect both color and the manner of shading/drawing. The DrawState structure should have the following fields, although for this week we will use only the color and shade fields.

- color the foreground color, used in the default drawing mode.
- flatColor the color to flat-fill a polygon based on a shading calculation.
- body the body reflection color, used for shading calculations.
- surface the surface reflection color, used for shading calculations.
- surfaceCoeff a float that represents the shininess of the surface.
- shade an enumerated type ShadeMethod.
- zBufferFlag whether to use z-buffer hidden surface removal.
- viewer a Point representing the view location in 3D (identical to the VRP in View3D).

The ShadeMethod enumerated type will determine how an object is drawn into the image. It should have (at least) the following values. ShadePhong is optional.

- ShadeFrame draw only the borders of objects, including polygons.
- ShadeConstant draw objects using the current foreground color, fill polygons.
- ShadeDepth draw objects using their depth value.
- ShadeFlat draw objects using shading calculations, but each polygon is a constant value.
- ShadeGouraud draw objects using Gouraud shading.
- ShadePhong draw objects using Phong shading.

9.1 DrawState functions

- void drawstate_create (void)
 -create a new DrawState structure and initialize the fields.
- void drawstate_setColor(DrawState *s, Color c)
 set the color field to c.
- void drawstate_setBody (DrawState *s, Color c)
 set the body field to c.
- void drawstate_setSurface(DrawState *s, Color c)
 set the surface field to c.
- void drawstate_setSurfaceCoeff(DrawState *s, float f)
 set the surfaceCoeff field to f.
- void drawstate_copy(DrawState *to, DrawState *from)
 copy the DrawState data.