## Verifying Algorithms. Notes.

Ilgiz Mustafin

Innopolis University

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## 1 Installing EVE (0:37)

Since I am using Linux, I took the latest linux build (96960) available at that time.

Unpacking and running run\_eve.py worked (Account example could be verified as expected).

Off topic: I am using a dark GTK theme (Breeze-Dark) on my computer. EiffelStudio has some problems with this (Light grey text on white background, etc.), so I start it with light theme with GTK2\_RC\_FILES=/usr/share/themes/Breeze/gtk-3.20/gtkrc python run\_eve.py.

## 2 Tutorial

Before I could start working on algorithms, I had to complete the tutorial from http://se.inf.ethz.ch/research/autoproof/tutorial/.

## 2.1 Exercise 1 (1:07)

In feature increase\_seconds pre-condition seconds = 59 implies modify\_model ("minutes", Current) gives "Manifest string not supported" and "Manifest tuple in contract not supported" errors, while just modify\_model("minutes",

Current) works. It seems that modify\_model is not supported in logical expressions. Also, in solutions there is no such check, there is just modify\_model (["seconds", "minutes", "hours"], Current).

#### 2.2 Exercise 2 (3:40)

#### 2.2.1 Binary Search

When doing the Binary Search task, I was required to write a precondition to check that array is sorted.

My code was:

```
across 1 | .. | (a.sequence.count - 1) as c all
       a.sequence[c.item] <= a.sequence[c.item + 1]</pre>
2
3
   While the code from the solutions was:
   across 1 |... | a.sequence.count as i all
1
   across 1 | . . | a.sequence.count as j all
2
       i.item <= j.item implies
            a.sequence[i.item] <= a.sequence[j.item]</pre>
4
  end
5
   end
6
```

These two variants give different results of verification. I was able to verify the function with the code from the solutions, but not with my code (not\_in\_lower\_part and not\_in\_upper\_part could be violated).

This could be so, if AutoProof was not considering that  $\leq$  is transitive for integers. Maybe worth pointing out in tutorial.

#### 2.2.2 Permutations

For the Permutations task there was a feature for testing different permutation checking algorithms. I added some more tests.

```
1 feature test_permutation
2 local
3    s1, s2: MML_SEQUENCE [INTEGER]
4    do
5    s1 := << 1, 2, 3, 4 >>
6    s2 := << 1 >>
7    check p1: not is_permutation_1 (s1, s2) end
```

```
8
        s1 := \langle \langle 1, 2, 3, 4 \rangle \rangle
9
        s2 := << 1 >>
10
        check p2: not is_permutation_2 (s1, s2) end
11
12
        s1 := << 1, 2, 2 >>
13
        s2 := << 1, 1, 2 >>
14
        check p2_2: not is_permutation_2 (s1, s2) end
15
16
        s1 := << 1, 2, 3, 4 >>
17
        s2 := << 1 >>
18
        check p3: not is_permutation_3 (s1, s2) end
19
20
        s1 := << 1, 2, 2 >>
21
        s2 := << 1, 1, 2 >>
        check p3_2: not is_permutation_3 (s1, s2) end
23
24
        s1 := << 1, 2, 3, 4 >>
25
26
        s2 := << 1 >>
        check p4: not is_permutation_4 (s1, s2) end
27
28
        s1 := << 1, 2, 2 >>
29
        s2 := << 1, 1, 2 >>
30
        check p4_2: not is_permutation_4 (s1, s2) end
31
    end
32
```

In this version AutoProof reports that checks p1 and p2\_2 may be violated, but check p4\_2 should fail too.

If we comment check p1, only p2 is reported.

If we comment check p2, then both p1 and p4\_2 are reported.

It seems that when AutoProof finds some violation in a feature, it stops checking that feature and several (but *not all!*) violations will be reported. This can be very confusing for people unfamiliar with such behavior.

### 2.3 Excercise 3 (2:17)

Nothing interesting.

# 3 Real development

### 3.1 Generics, int and ref

class

2

12 13

end

VALUE [G]

Suppose we have class VALUE which stores one non-void object.

```
3
   create
4
        make
6
   feature
7
8
        make (v: G)
9
            require
10
                 value_exists: v /= Void
11
12
            do
                 value := v
            end
14
15
        value: G
16
18
    We want to use it to store an integer.
   class
        TEST
2
3
   feature
4
5
6
        test
7
            local
                 value: VALUE[INTEGER]
8
9
            do
                 create value.make (123)
10
            end
11
```

Trying to verify this system gives invalid argument types (int and ref) to binary operator !=.

After quick inspection of AutoProof \*.bpl output in EIFGENs/.../Proofs I suspect several facts.

```
type ref; // Type definition for reference types
const Void: ref; // Constant for Void references
```

Eiffel Void is translated into a Boogie constant of reference type.

Eiffel INTEGER is translated into Boogie int. There is some code about integer boxing, but both these functions are never used.

```
function unboxed_int(r: ref) returns (int);
These suspicions are supported by the following code.

procedure VALUE_ANY_.make(Current: ref, v: ref);

requires (v) != (Void); // type:pre tag:v_exists line:11

procedure VALUE_INTEGER_32_.make(Current: ref, v: int);

free requires is_integer_32(v); // info:type property for argument v

requires (v) != (Void); // type:pre tag:v_exists line:11

requires (v) != (Void); // type:pre tag:v_exists line:11
```

While the assertion  $(v) \mathrel{!=} (Void)$  is valid in the ANY variant because argument v is of type ref, the code in the INTEGER is invalid because v is of type int.

The first naive solution was to add an axiom axiom (forall i:int :: (Void) != i); to the theory files, but this is not even a valid Boogie construction (invalid argument types (ref and int) to binary operator!=).

For now, I will make less generic code as a workaround for this problem.

# 3.2 Using object comparison to find objects in MML containers, is\_equal vs is\_model\_equal

Suppose we have class TS\_PAIR which is just a pair of integers.

const unique INTEGER: Type;

function boxed\_int(i: int) returns (ref);

```
redefine
10
                 is_equal,
11
                 is_model_equal
12
            end
13
14
   create
15
16
        make
17
   feature -- Initialization
18
19
        make (a_left, a_right: INTEGER)
20
21
            note
                 status: creator
22
            require
23
                 modify_model (["left", "right"], Current)
            do
25
                 left := a_left
26
                 right := a_right
^{27}
28
            ensure
29
                 left = a_left
                 right = a_right
30
31
            end
32
   feature -- Data
33
34
        left: INTEGER assign set_left
35
36
        right: INTEGER assign set_right
37
38
    feature -- Modification
39
40
        set_left (a_left: INTEGER)
41
            require
42
                 modify_model ("left", Current)
43
            do
44
                 left := a_left
45
46
            ensure
47
                 left = a_left
            end
48
49
        set_right (a_right: INTEGER)
50
51
            require
                 modify_model ("right", Current)
52
            do
53
                 right := a_right
55
                 right = a_right
56
            end
57
```

```
feature -- Comparison
59
60
        is_equal, is_model_equal (a_other: like Current): BOOLEAN
61
62
                 status: functional
63
            require else
64
                 reads_model (["left", "right"], [Current, a_other])
65
66
                 Result := left = a_other.left and right = a_other.right
67
            end
68
69
70
```

How to check if there is already an object-equal pair in a, say, MML\_SEQUENCE? This code will not work (Check s\_has\_object\_b may be violated.):

```
local
2
        a, b: TS_PAIR
        s: MML_SEQUENCE [TS_PAIR]
3
   do
4
        create a.make (1, 1)
5
        create b.make (1, 1)
6
        create s
7
        s := s & a
8
        check
9
            s_has_object_b: across s as i some i.item.is_equal (b) end
10
        end
11
12
   end
```

While trying to find the root of the problem I added some random checks which made verification successful.

```
local
1
        a, b: TS_PAIR
2
        s: MML_SEQUENCE [TS_PAIR]
3
   do
4
        create a.make (1, 1)
5
        create b.make (1, 1)
6
        create s
7
        s := s & a
8
        check
9
            a_equals_b: a.is_equal (b)
10
        end
11
        check
12
             s_has_a: s.has (a)
13
        end
14
        check
15
            s_has_object_b: across s as i some i.item.is_equal (b) end
16
17
        end
18
    end
```

Changing a\_equals\_b check into b.is\_equal (a) invalidates s\_has\_object\_b. This makes sense because ANY.is\_equal does not have symmetric contract as ANY.is\_model\_equal does.

Using is\_model\_equal instead of is\_equal requires a\_equals\_b and s\_has\_a checks to verify s\_has\_object\_b, but we can swap left and right sides in a\_equals\_b.

What function should I use in my code? Let us compare contracts.

```
is_model_equal (other: like Current): BOOLEAN
1
           -- Is the abstract state of `Current' equal to that of `other'?
2
      require
3
               other /= Void
               reads (Current, other)
5
       ensure
6
           reflexive: other = Current implies Result
           symmetric: Result = other.is_model_equal (Current)
8
  is_equal (other: like Current): BOOLEAN
           -- Is `other' attached to an object considered
2
           -- equal to current object?
3
4
       require
           other_not_void: other /= Void
```

We can see that is\_equal has neither reflexivity nor symmetricity properties, which are natural properties to assume while designing code.

is\_model\_equal, on the other hand, should only be used in contracts for verification. Normal Eiffel class ANY does not have this function.

We could try to mix them like this:

```
if x.is_equal(y) then -- for behavior, we may assume symmetricity, etc.
check x.is_model_equal (y) end -- Verify symmetricity, etc.
```

But there is no guarantee that for all x and y x.is\_equal (y) = x.is\_model\_equal (y). Adding such contract can be a solution.

For the first versions of algorithm I will use is\_model\_equal in custom classes, until we come up with something better.

#### 3.3 Instantiation of V\_ARRAY2

```
1 items: INTEGER
2
3 data: V_ARRAY2[BOOLEAN]
```

```
4
   make (a_items: INTEGER)
5
       require
6
            a_items >= 0
7
8
9
            items := a_items
            create data.make_filled (a_items, a_items, False)
            check rows: data.row_count = items end
11
            check columns: data.column_count = items end
12
13
        end
```

First of all, check rows could not be verified, but check columns is verified. Maybe this is because V\_ARRAY2#make and #make\_filled have a post-condition that #column\_count is set, but they do not have a post-condition that #row\_count is set. Maybe this is because it can be derived from invariant row\_count\_definition: row\_count \* column\_count = sequence.count.

#### 4 Installation 2

I had to switch to a new computer. This required me to install EVE to a fresh system. I was using ArchLinux. I did the same installation steps: download the freshest EVE build for linux, unpack the archive, run EVE.

However, issuing AutoProof verification from EVE produced no output in EVE, EIFGENs/v\_topsort/Proofs/autoproof\*.txt files were created but were empty. bpl files are created and contain Boogie code, they seem ok. Nothing is written to STDOUT/STDERR of EVE.

Following EVE installation instructions from https://trac.inf.ethz.ch/trac/meyer/eve/#Setup1 is not working too. Executing python eve.py update produces errors (python2 is for running python 2):

```
$ python2 eve.py update
Updating EiffelStudio
Traceback (most recent call last):
   File "eve.py", line 1196, in <module>
        main()
   File "eve.py", line 1161, in main
        update_EiffelStudio()
   File "eve.py", line 591, in update_EiffelStudio
        name, filename, version, url = get_nightly_build(d_ise_platform, d_archive_e
   File "eve.py", line 614, in get_nightly_build
```

```
response = urllib2.urlopen(download_page)
  File "/usr/lib/python2.7/urllib2.py", line 154, in urlopen
    return opener.open(url, data, timeout)
 File "/usr/lib/python2.7/urllib2.py", line 429, in open
    response = self._open(req, data)
 File "/usr/lib/python2.7/urllib2.py", line 447, in _open
    '_open', req)
  File "/usr/lib/python2.7/urllib2.py", line 407, in _call_chain
    result = func(*args)
 File "/usr/lib/python2.7/urllib2.py", line 1413, in ftp_open
    fw = self.connect_ftp(user, passwd, host, port, dirs, req.timeout)
 File "/usr/lib/python2.7/urllib2.py", line 1435, in connect_ftp
    persistent=False)
 File "/usr/lib/python2.7/urllib.py", line 877, in __init__
    self.init()
 File "/usr/lib/python2.7/urllib.py", line 889, in init
    self.ftp.cwd(_target)
 File "/usr/lib/python2.7/ftplib.py", line 562, in cwd
    return self.voidcmd(cmd)
 File "/usr/lib/python2.7/ftplib.py", line 254, in voidcmd
    return self.voidresp()
 File "/usr/lib/python2.7/ftplib.py", line 229, in voidresp
    resp = self.getresp()
 File "/usr/lib/python2.7/ftplib.py", line 224, in getresp
    raise error_perm, resp
URLError: <urlopen error ftp error: 550 Failed to change directory.>
However, the installation instructions mentioned that Mono is required. I
installed it and AutoProof started to work.
```

## 5 Progress!

Nearly 40 hours were required to get started. I am using *explicit wrapping*, *contracts* so that I am really understanding what is happening. Making AutoProof display collaborated code could be really helpful.

## 6 Left-right scrolling

Using touchpad to scroll up and down works, using touchpad to scroll left and right does not. It works in other applications like Firefox.

## 7 Changing behavior for easier verification

Let us look at an implementation of is\_subset\_of.

```
is_subset_of (a_other: TS_INTEGER_RELATION): BOOLEAN
   require
2
3
        closed
        a_other.closed
4
   local
        i: INTEGER
6
        k: INTEGER
   do
9
        Result := True
       from
10
           i := 1
11
        invariant
12
           Result implies across 1 | . . | (i - 1) as j all a_other.has_pair
13
            Result implies k = 0
14
            (not Result) implies across 1 |..| (i - 1) as j some not
            → a_other.has_pair (data.sequence[j.item]) end
            (not Result) implies (1 \leq k and k \leq data.sequence.count)
16
            (not Result) implies not a_other.has_pair (data.sequence[k])
17
        variant
            data.sequence.count - i
19
        until
20
            i > data.count or not Result
^{21}
        loop
            if not a_other.has_pair (data[i]) then
23
                check not a_other.has_pair (data.sequence[i]) end
24
                Result := False
25
                k := i
26
            end
27
            i := i + 1
28
        end
29
    ensure
30
        closed
31
        a_other.closed
32
        is_empty implies Result
        a_other.is_empty implies (Result = is_empty)
34
```

```
Result implies across data.sequence as s all a_other.has_pair (s.item)

original end

not Result) implies across 1 | . . | (data.sequence.count) as j some not

original a_other.has_pair (data.sequence[j.item]) end

red
```

In this example, variable k is not needed to compute the result of this function. But it helps to verify this function. All usages of k seem to be extractable into some ghost function, but I did not do this.

# 8 Studying AutoProof Verified Code Repository

In some paper I found the link to http://se.inf.ethz.ch/research/autoproof/repo/index.html. Here are some comments.

#### 8.1 Weak specifications

Many of the example specifications seem to be too weak. This fact makes these examples somewhat useless. In particular:

sum\_and\_max Feature sum\_and\_max, according to the comment description of the feature should find the sum of elements in array and find
the greatest value in array. However, the postcondition and loop invariants do not even check that max is a value present in the array. For
any array tuple [sum = X, max = X\*LENGTH] will be a valid result for
postcondition.

master\_clock Feature tick in class MASTER has comment Increment time,
however postcondition is just time > old time but strangely not time
= old time + 1.

#### 8.2 Pattern to own container and everything in it

Suppose we want an object to own a container and all items in it.

First idea would be to write invariant owns = container.sequence.range.extended (container) end. This will not work. AutoProof will say that on this line container.sequence might not be readable.

What I see in the Repository and what I randomly did once is to add owns.has (container). So, one of the correct codes to achieve this is this:

```
invariant
owns.has (container)
owns = container.sequence.range.extended (container)
end
```

#### 8.3 Using ghost attributes

Due to the fact that I found very few examples of using AutoProof with Eiffel it was really unclear to me how to properly use ghost attributes. The most common usage is assigning a value in invariant like owns = [a, b, c].

However, in treemax example we can see another usage: ghost attribute sequence is assigned values in creator procedures.

#### 8.3.1 Ghost result for non-ghost functions

In map example functions extend (add key-value to map) and remove (remove key from map) have comment *Returns index of [removed] key 'k' (ghost value)*. While the returned value should be useless for the clients of the class, it is used in the post-condition of these functions.