

Reading Aberrations

Lens Design OPTI 517

Reading aberrations

- We cannot intelligently improve a lens system if we cannot recognize its aberrations
- Wave aberration fans
- It is critical that we learn to ‘read’ the aberrations of an optical system

Field of view

- Very small FOV: arc seconds, minutes
- Small FOV: sub-degree to a few degrees
- Small FOV: 5 to 30 degrees
- Medium FOV: 30 to 60 degrees
- Wide angle: > 60 degrees
- Hyper FOV: >180 degrees

Field of view

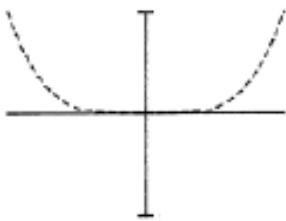
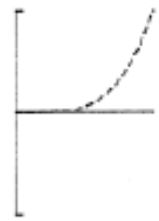
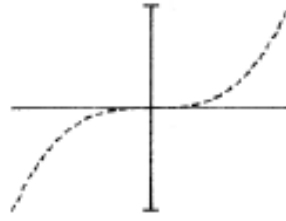
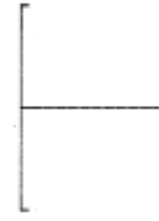
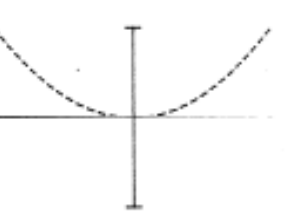

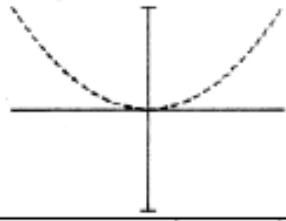
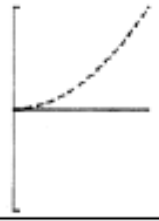
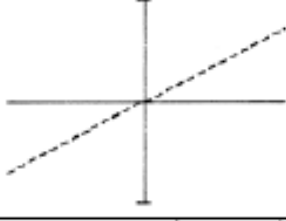

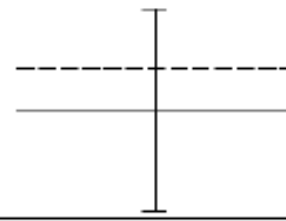

- Eye resolution and field of view
- The Moon
- The Sun
- 35 mm camera ($f=50$ mm)





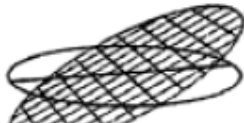
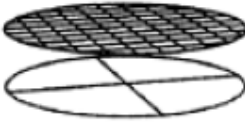
Speed

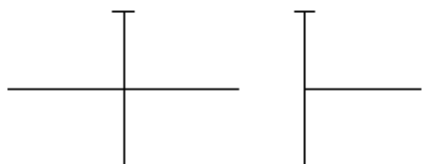
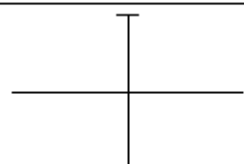
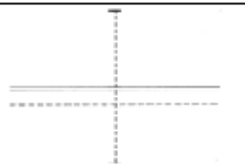
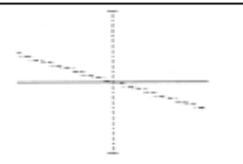
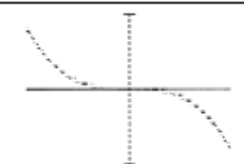
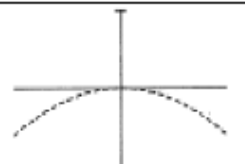
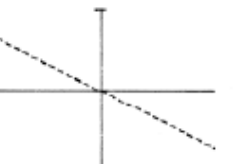
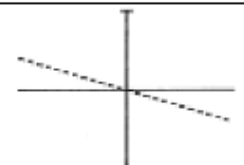
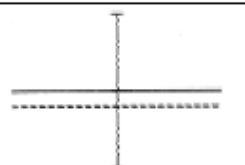
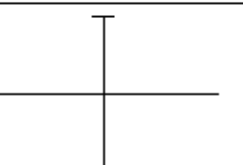
- $F/\# > 10$ slow
- $F/\# < 2.8$ fast
- Eye speed?

Display of aberrations

- Historical nature
- Transverse ray aberration fans
- Wave aberration fans
- Field curves
- Aberration coefficients
- Spot diagrams
- Zernike decomposition
- Total aberration vs fourth-order

Fourth-order wave aberrations fans Left plot: meridional. Right plot sagittal.					
					
$W_{040}(\vec{\rho} \cdot \vec{\rho})^2$		$W_{131}(\vec{H} \cdot \vec{\rho})(\vec{\rho} \cdot \vec{\rho})$		$W_{222}(\vec{H} \cdot \vec{\rho})^2$	
					
$W_{220}(\vec{H} \cdot \vec{H})(\vec{\rho} \cdot \vec{\rho})$		$W_{311}(\vec{H} \cdot \vec{H})(\vec{H} \cdot \vec{\rho})$		$W_{400}(\vec{H} \cdot \vec{H})^2$	

Fourth-order wavefront aberration shapes		
		
$W_{040}(\vec{\rho} \cdot \vec{\rho})^2$	$W_{131}(\vec{H} \cdot \vec{\rho})(\vec{\rho} \cdot \vec{\rho})$	$W_{222}(\vec{H} \cdot \vec{\rho})^2$
		
$W_{220}(\vec{H} \cdot \vec{H})(\vec{\rho} \cdot \vec{\rho})$	$W_{311}(\vec{H} \cdot \vec{H})(\vec{H} \cdot \vec{\rho})$	$W_{400}(\vec{H} \cdot \vec{H})^2$

Transverse ray aberration fans Left plot meridional, right plot sagittal.		
Zero-order		
		
$W_{000} = 0$		
First-order		
		
$W_{000} = 0$	$W_{111}\vec{H}$	$2W_{020}\vec{\rho}$
Third-order		
		
$4W_{040}(\vec{\rho} \cdot \vec{\rho})\vec{\rho}$	$W_{131}[(\vec{\rho} \cdot \vec{\rho})\vec{H} + 2(\vec{H} \cdot \vec{\rho})\vec{\rho}]$	$2W_{222}(\vec{H} \cdot \vec{\rho})\vec{H}$
		
$2W_{220}(\vec{H} \cdot \vec{H})\vec{\rho}$	$W_{311}(\vec{H} \cdot \vec{H})\vec{H}$	$W_{400} = 0$

$$\vec{\varepsilon} = \bar{y}_I \Delta \vec{H}$$

$$\Delta \vec{H} = -\frac{1}{\mathcal{K}} \vec{\nabla}_{\rho} W$$

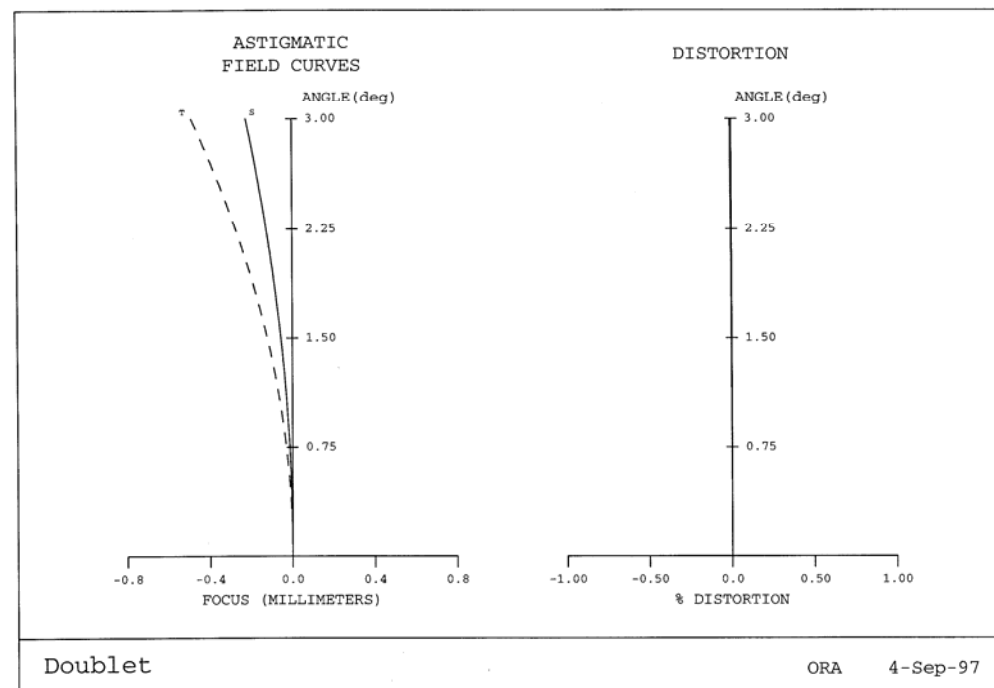
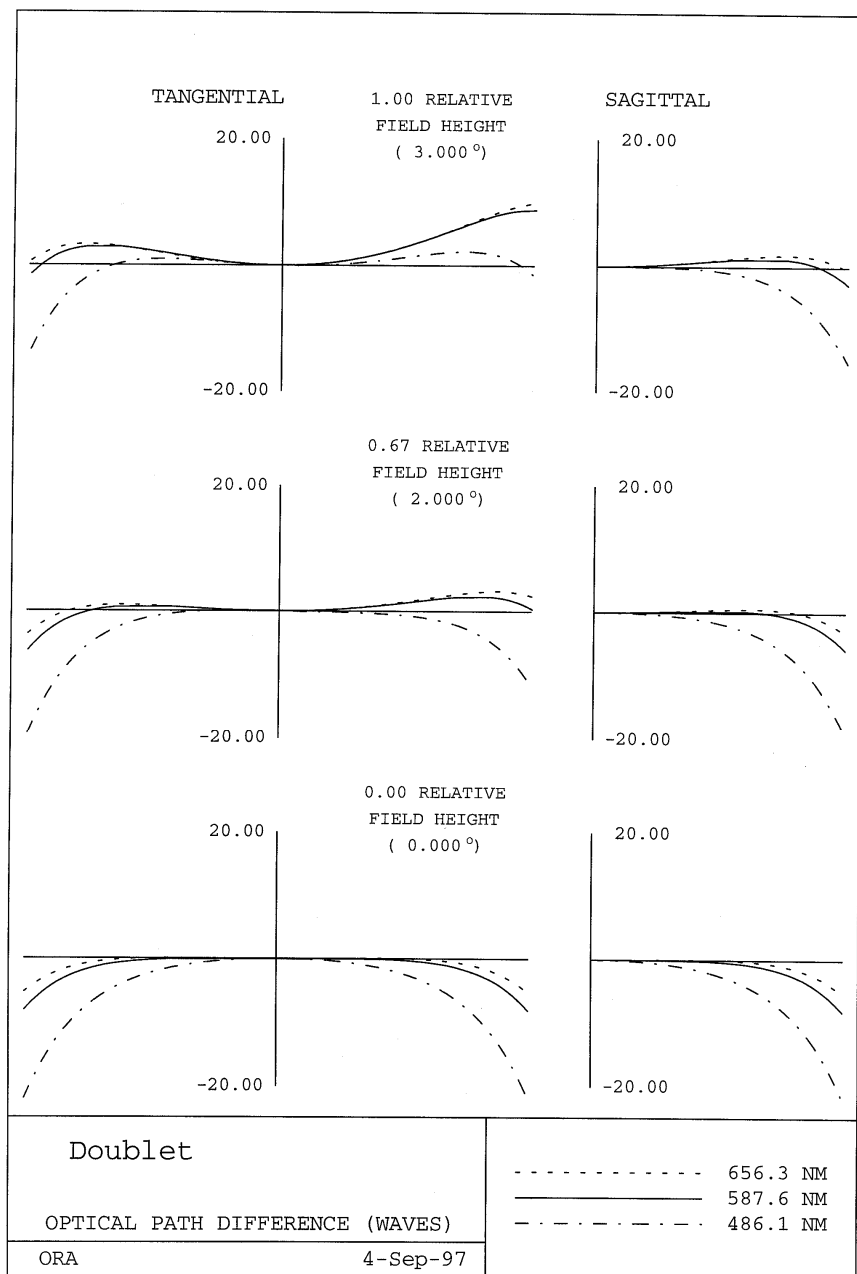
Guide to identifying aberrations from wave-fans

Monochromatic

- 1) Be aware of the speed and field of view
- 2) First, pay attention to the on axis aberrations
 - is it properly in focus ?
 - is there spherical aberration W040?
 - is there higher order spherical?
 - what are the magnitudes?
- 3) Second, take a look at the full field aberrations
 - spherical
 - astigmatism
 - coma
 - Field curvature
 - higher order

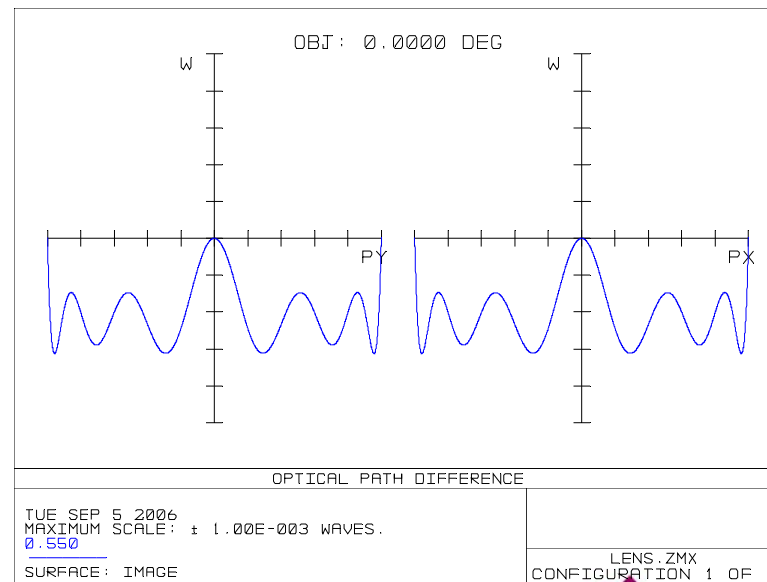
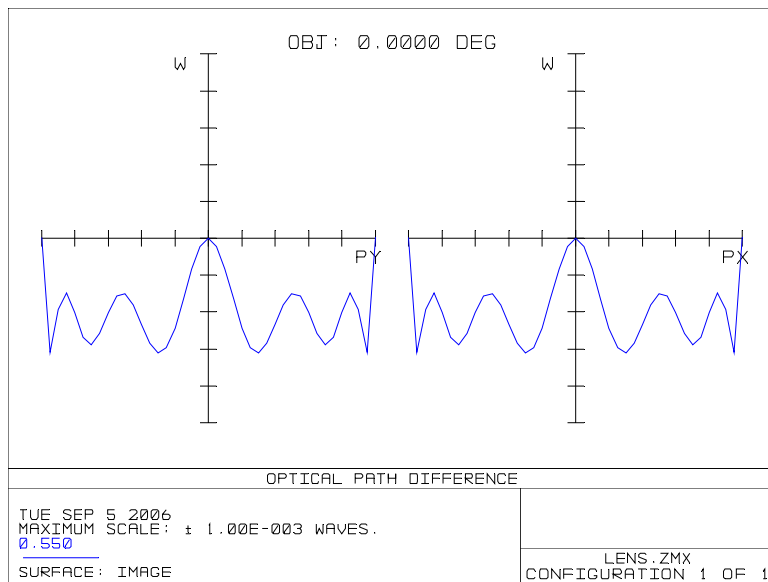
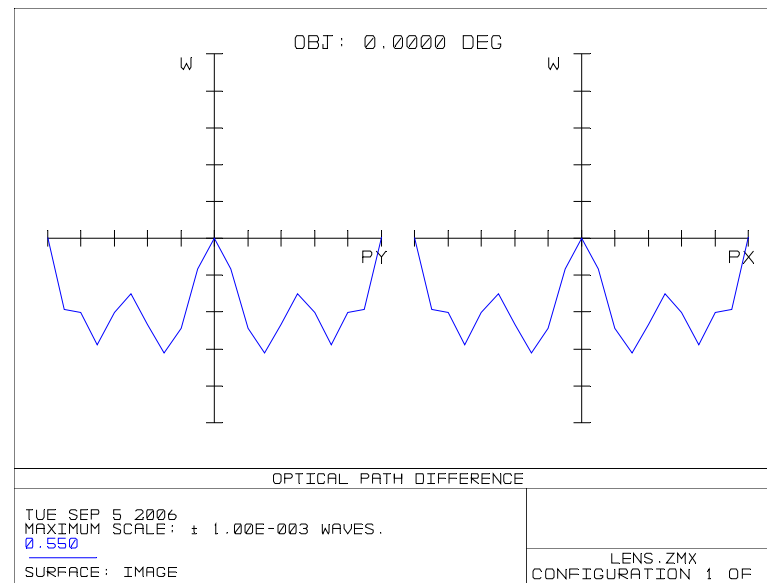
Guide to identifying aberrations from wave-fans

- 4) Take a look at the 7/10 field
- 5) Verify with field curves, spot diagrams, and fourth-order coefficients
 - Note: Real ray wavefront fans have fourth-order aberrations as components.
 - Slow systems with small fields may be well described by fourth-order theory.

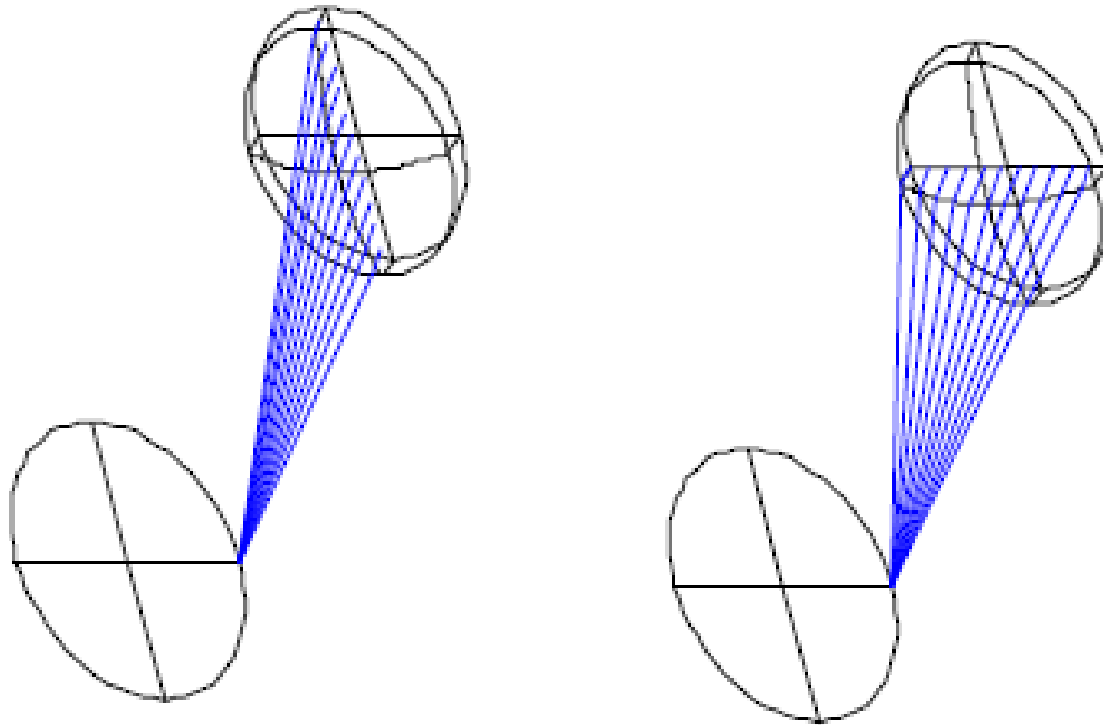


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OPTI 517

What is going on here?



Meridional and Sagittal planes

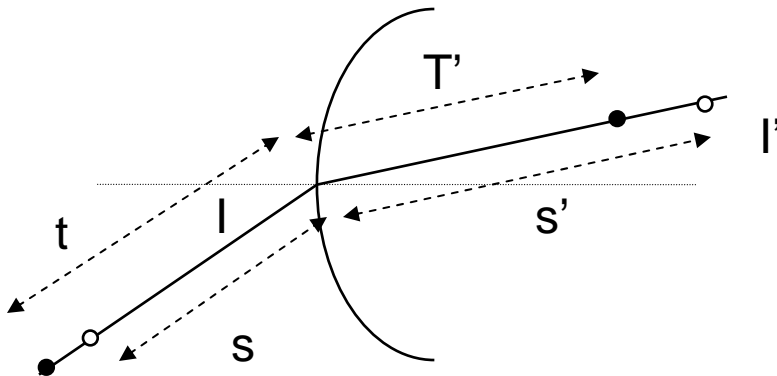


- A meridional plane contains the optical axis
- Sagittal from the Latin meaning arrow

Coddington Equations

$$\frac{n'}{s'} - \frac{n}{s} = \frac{n' \cos I' - n \cos I}{R_s}$$

$$\frac{n' \cos^2 I'}{t'} - \frac{n \cos^2 I}{t} = \frac{n' \cos I' - n \cos I}{R_t}$$



s is the distance along the ray from the object point to the surface vertex

s' is the distance along the ray from the surface vertex to the image point

t is the distance along the ray from the object point to the surface vertex

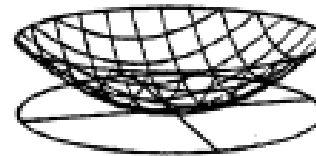
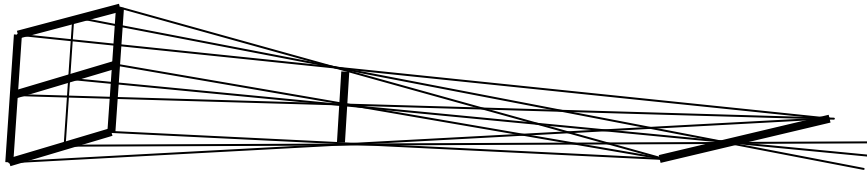
t' is the distance along the ray from the surface vertex to the image point

R_s is the sagittal radius of curvature at the intersection point

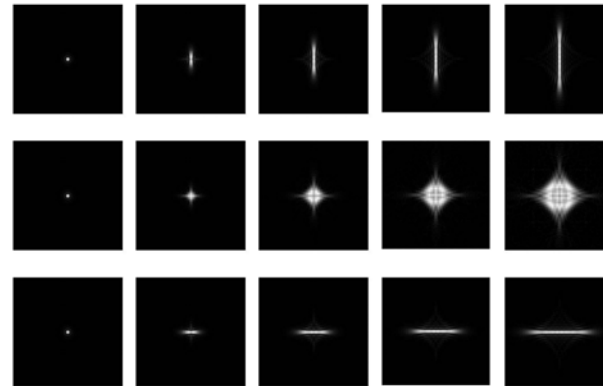
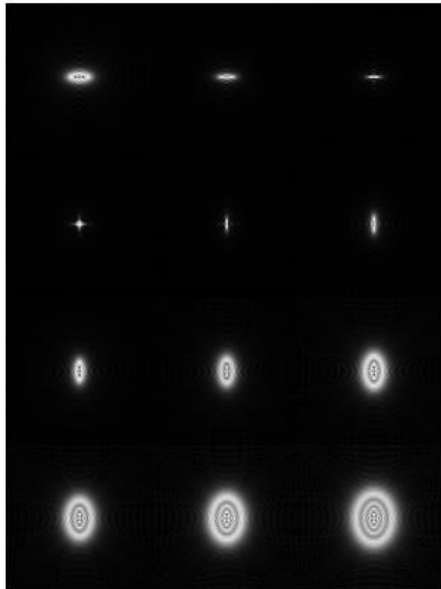
R_t is the tangential radius of curvature at the intersection point

- Actually Thomas Young equations
- Note change of aberration metric: longitudinal

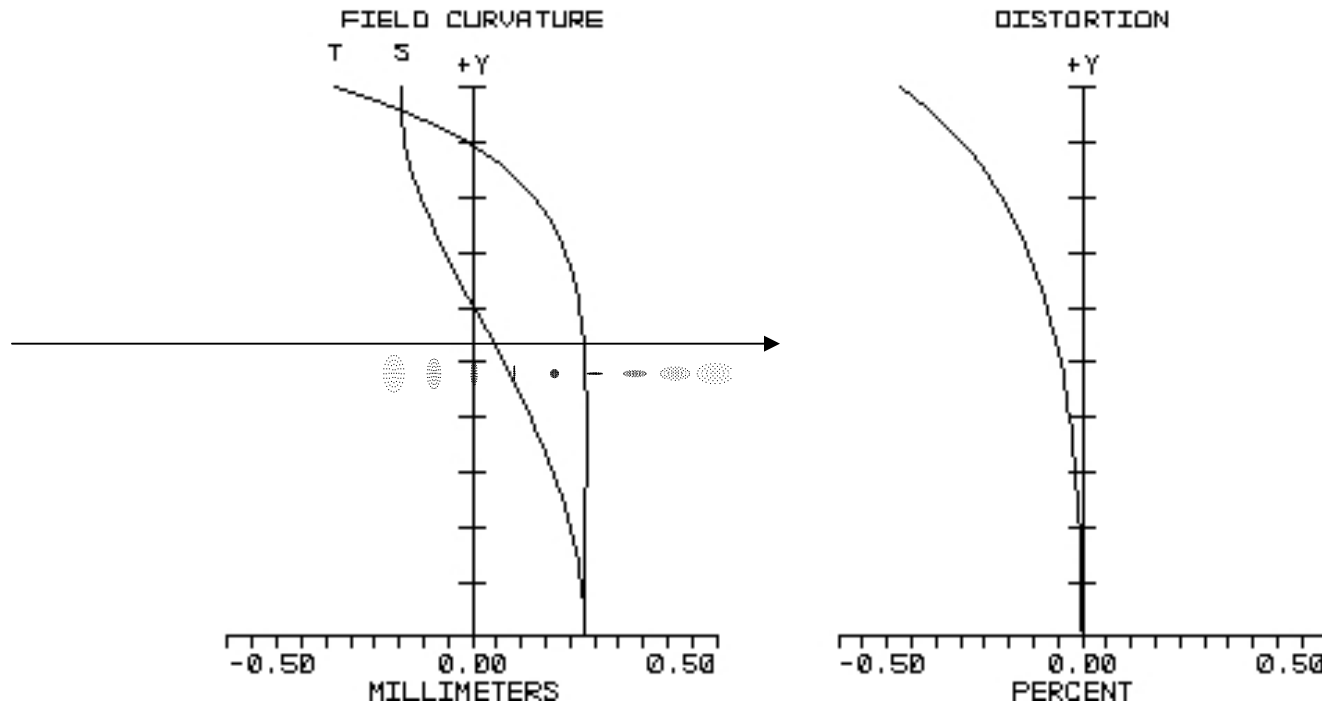
Astigmatism



Minimum defocus $\Delta d = -2$ Defocus unit step $= 0.5$

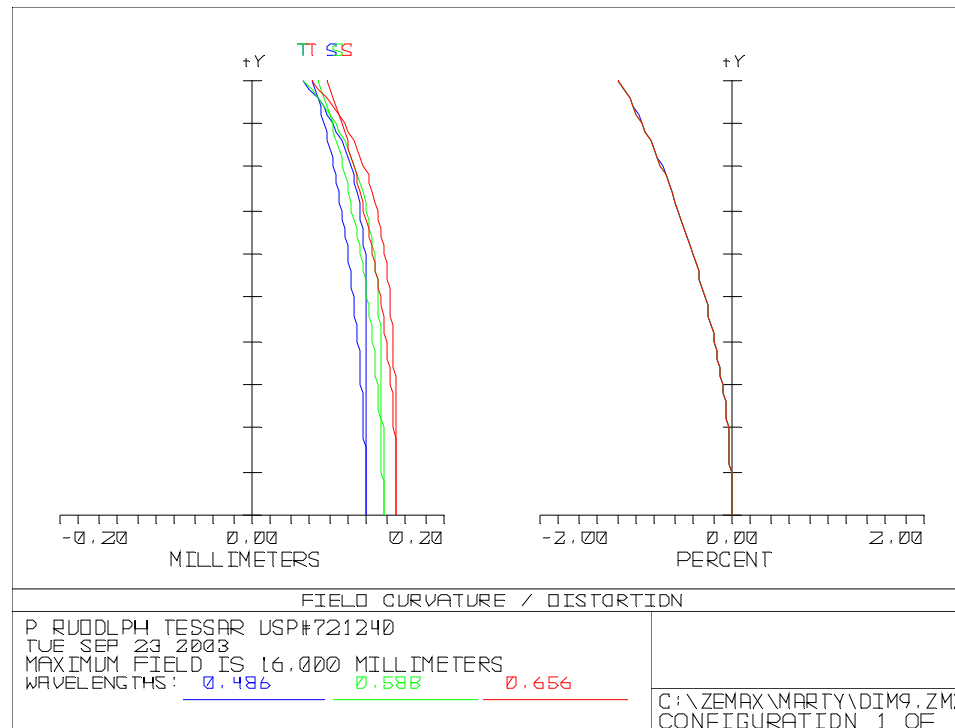


Field curves



$$\text{Distortion} = (H-h) \cdot 100/h$$

Field curves



Program may trace two close real rays

$$\text{Distortion} = (H-h) * 100/h$$

Summary

- Being aware of the system speed and FOV
- Knowing how to read/identify aberrations
- Coddington/Thomas Young equations
- Article by R. Kingslake

WHO DISCOVERED CODDINGTON'S Equations?

Optics and Photonics News, Vol. 5, Issue 8, pp. 20-23 (1994)