

Lens Design Lecture #1

College of Optical Sciences
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What is imaging?

Photo credit:
Gary Mackender



Prof. Jose Sasian

Imaging with rays: theories

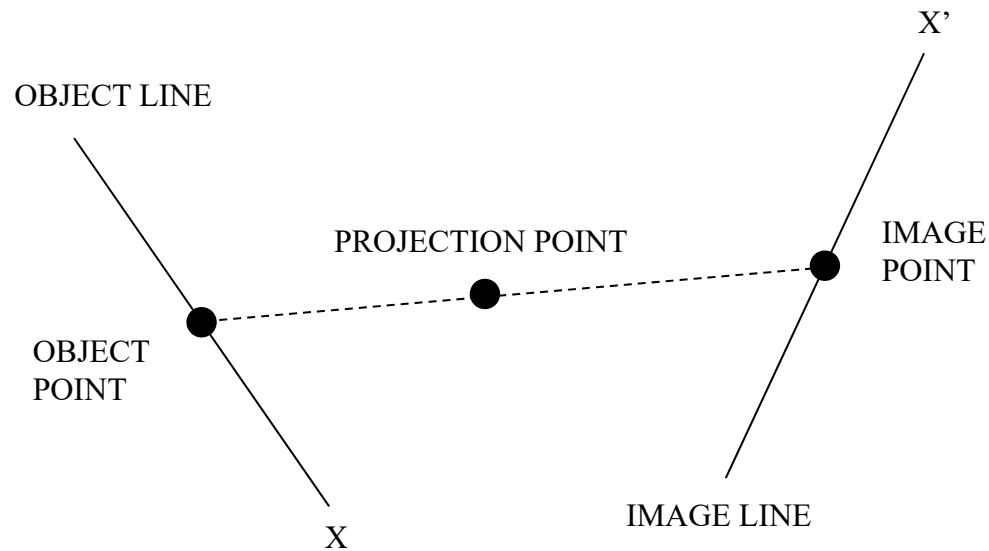
Maxwell's Ideal:

- 1) Each point is imaged stigmatically
- 2) The images of all points in an object plane lie on an image plane
- 3) The ratio of image to heights to object heights is the same for all points.

Collinear transformation

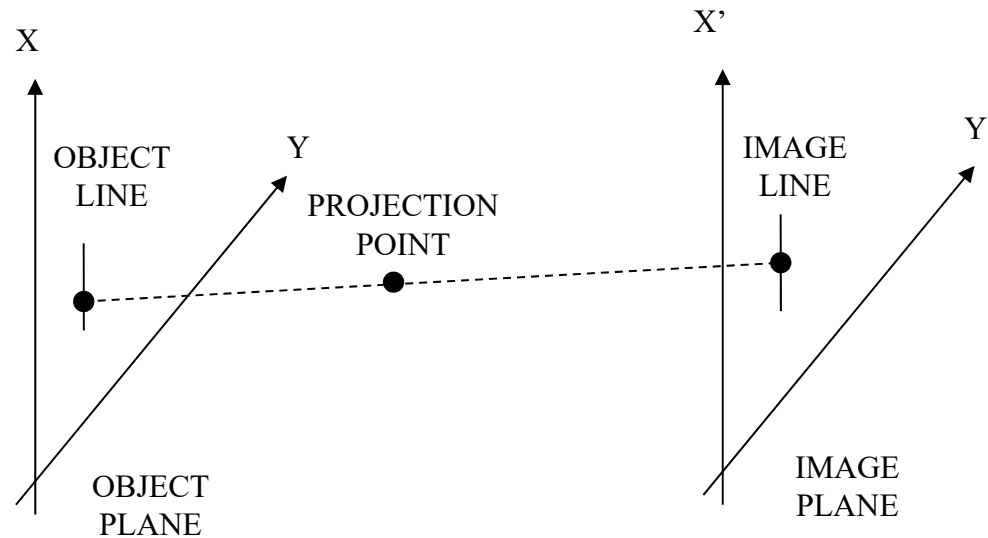
$$X' = \frac{a_1X + b_1Y + c_1Z + d_1}{a_0X + b_0Y + c_0Z + d_0} \quad Y' = \frac{a_2X + b_2Y + c_2Z + d_2}{a_0X + b_0Y + c_0Z + d_0} \quad Z' = \frac{a_3X + b_3Y + c_3Z + d_3}{a_0X + b_0Y + c_0Z + d_0}$$

Central Projection 1D



$$X' = \frac{a_1 X}{a_0 X + b_0}$$

Central Projection 2D



$$X' = \frac{a_1 X}{a_0 X + b_0 Y + c_0} \quad Y' = \frac{a_2 Y}{a_0 X + b_0 Y + c_0}$$

Central Projection 3D

$$X' = \frac{a_1X + b_1Y + c_1Z + d_1}{a_0X + b_0Y + c_0Z + d_0}$$

$$Y' = \frac{a_2X + b_2Y + c_2Z + d_2}{a_0X + b_0Y + c_0Z + d_0}$$

$$Z' = \frac{a_3X + b_3Y + c_3Z + d_3}{a_0X + b_0Y + c_0Z + d_0}$$

Point into points, lines into lines, and planes into planes.

Axial symmetry I

$$\rho = \sqrt{x^2 + y^2} \quad \rho' = \sqrt{x'^2 + y'^2}$$

ρ' and Z' must be only a function of ρ and Z , leads to:

$$X' = \frac{a_1 X}{c_0 Z + d_0} \quad Y' = \frac{a_1 Y}{c_0 Z + d_0} \quad Z' = \frac{c_3 Z + d_3}{c_0 Z + d_0}$$

- Origins transform into the origins: $d_3=0$
- Origins located at the planes of unit magnification implies: a_1 equal to d_0

Axial Symmetry II

$$X' = \frac{X}{c_0 Z + 1} \quad Y' = \frac{Y}{c_0 Z + 1} \quad Z' = \frac{c_3 Z}{c_0 Z + 1}$$

$$m = \frac{1}{c_0 Z + 1} \quad Z' = f' = \frac{c_3}{c_0} \quad Z = f = \frac{-1}{c_0}$$

Gaussian equations

$$\frac{Z}{f} = 1 - \frac{1}{m}$$

$$m = \frac{1}{1 - Z \setminus f}$$

$$\frac{Z}{f'} = 1 - m$$

$$m = 1 - \frac{Z}{f'}$$

$$\frac{f'}{Z} + \frac{f}{Z} = 1$$

Newtonian Equations

$$\frac{Z}{f} = - \frac{1}{m}$$

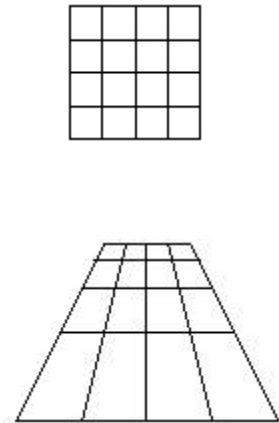
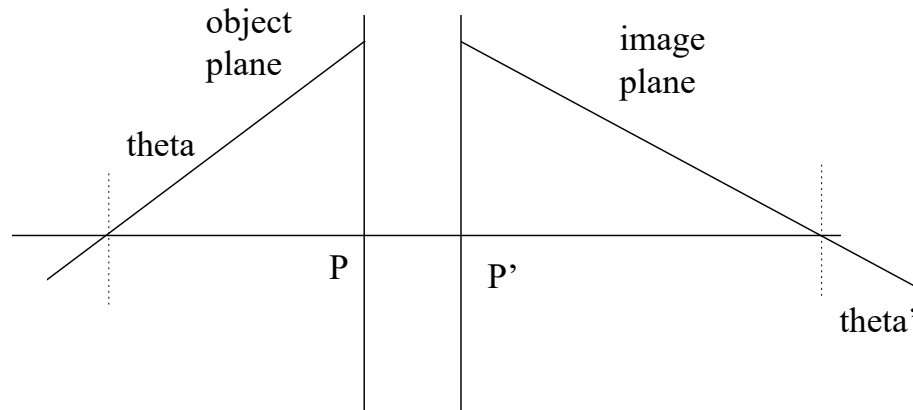
$$ZZ' = ff'$$

$$\frac{Z}{f'} = - m$$

Scheimpflug condition

(Plane symmetry)

$$\tan(\theta') - (Z'/Z) \tan(\theta) = 0$$



Scheimpflug construction

$$X' = m \frac{X}{1 + KY}$$

$$Y' = m \frac{Y}{1 + KY}$$

$$K = -m \frac{\tan(\theta)}{f} = \frac{\tan(\theta')}{f'}$$

Civil War 1859

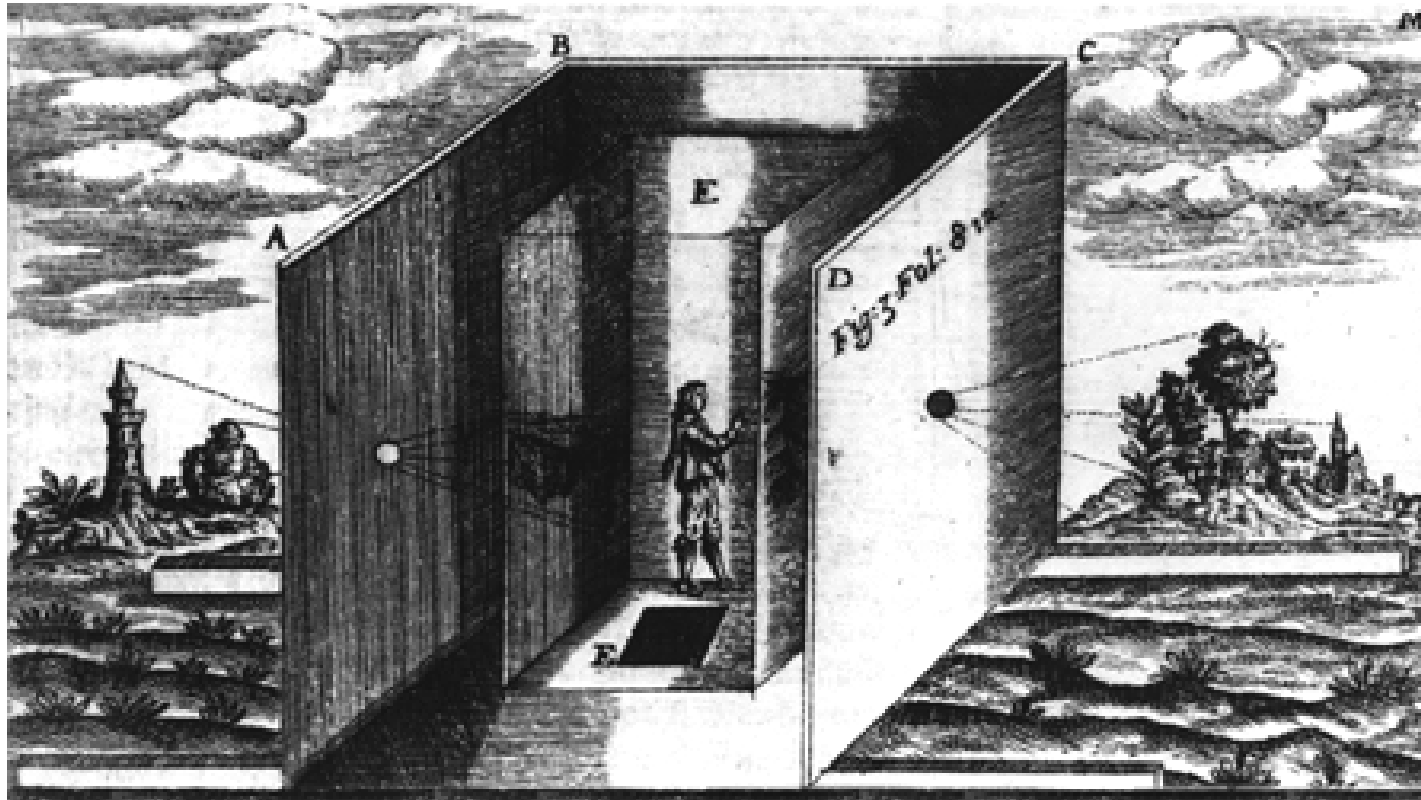


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And much more...

- Gaussian equations
- Newtonian equations
- Anamorphic systems
- Focal and afocal systems
- Scheimpflug condition
- Cardinal points
- Keystone distortion
- ...and much more!

Collinear transformation, camera obscura and lenses



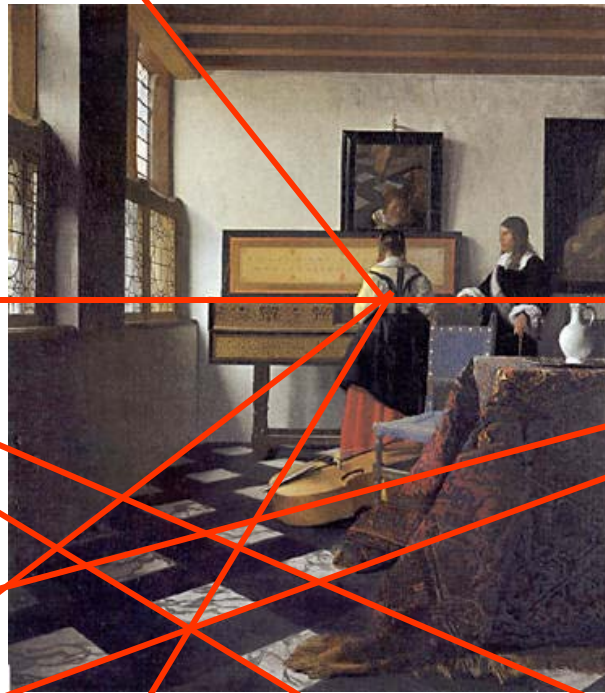
Camera Obscura, Athanasius Kircher, 1646

The secret in Vermeer's paintings



Johannes Vermeer, XVII century

Perspective of the painting



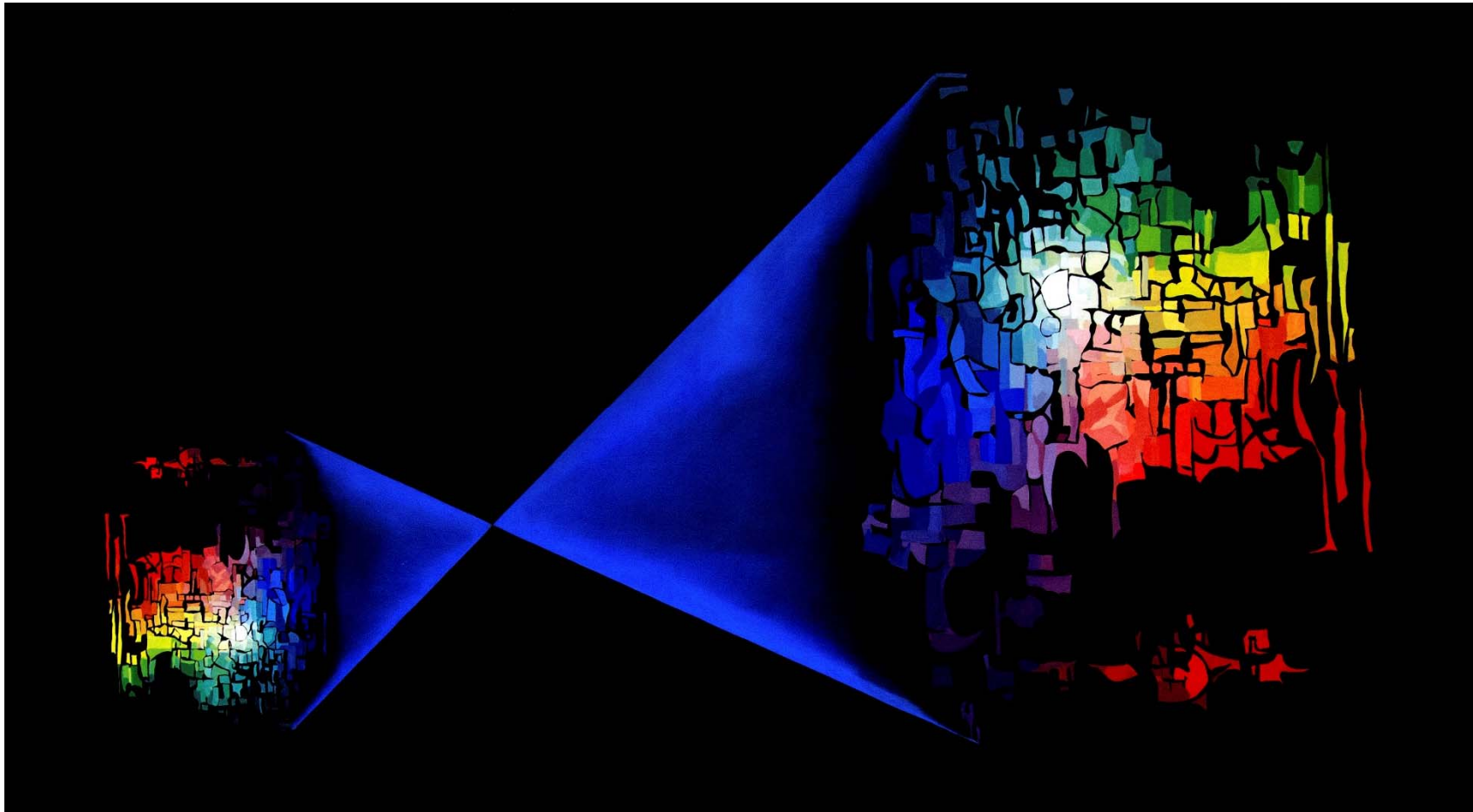
$$f = 68 \text{ cm}$$

$$D = f \times \tan(\theta) = f \tan(45^\circ)$$

However...

- Image parity issues
- Needed a flat mirror or
- To copy again the image

Central projection



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By Don Cowen

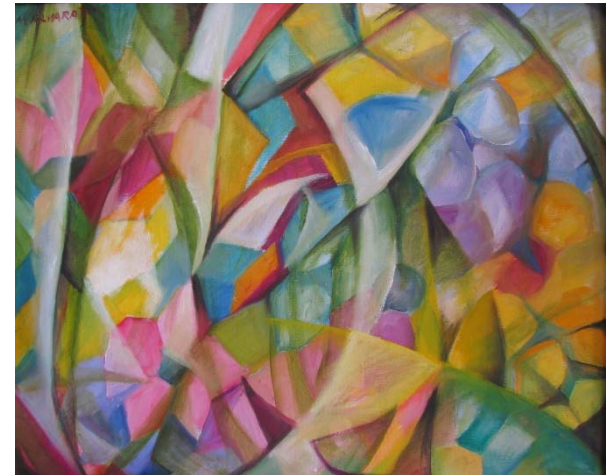
Other “perspectives”



Classical



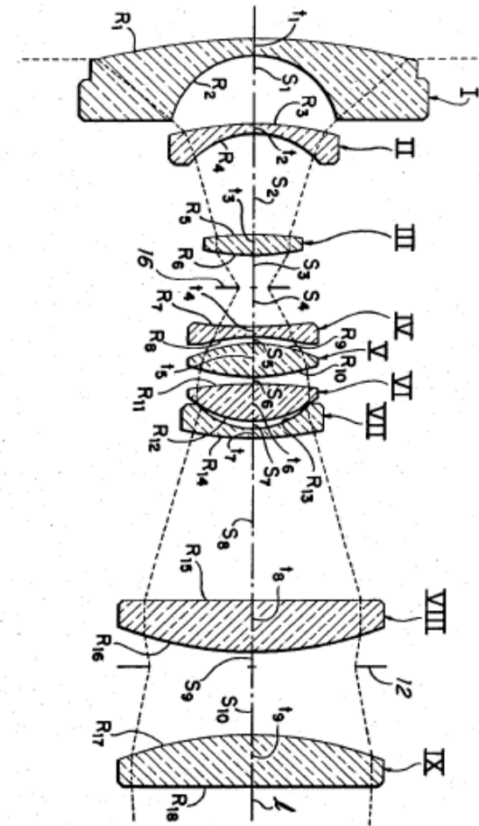
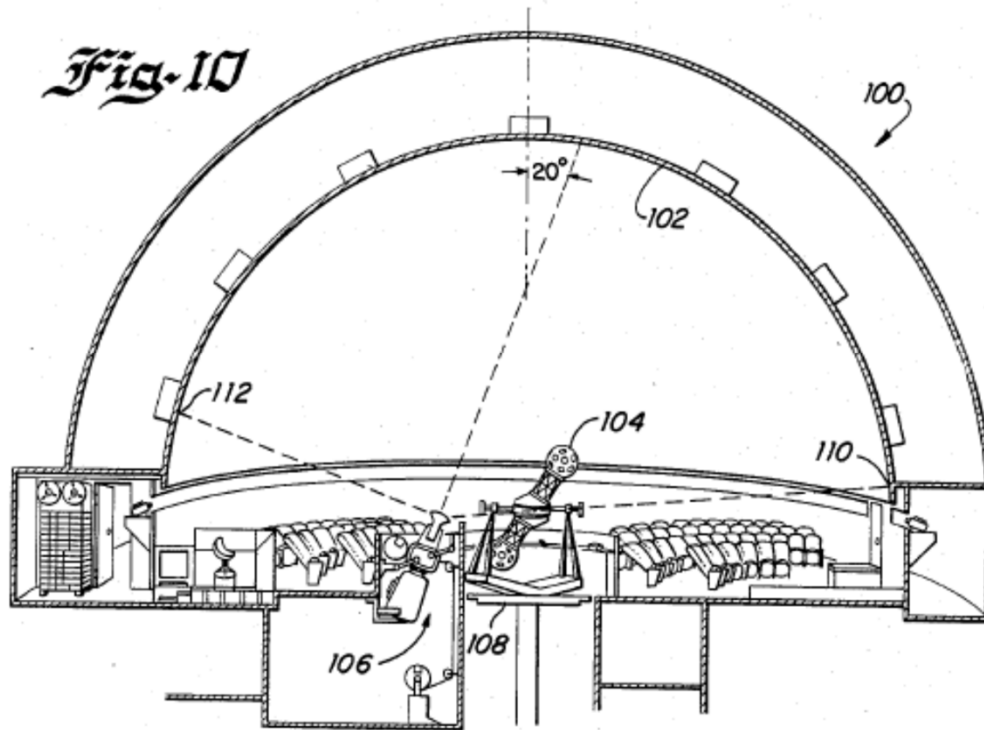
Impressionism



Cubism

A plurality of new and exciting
new concepts in imaging

Imaging on the sphere



IPAD Imaging



Class summary

- Syllabus
 - Imaging
 - Collinear transformation
 - Art application
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- Codev, OSLO, Zemax
 - Review of first-order optics