Tree Automata for Natural Language Processing

Kevin Knight

notes CS562 fall, 2006

Chomsky [1957]

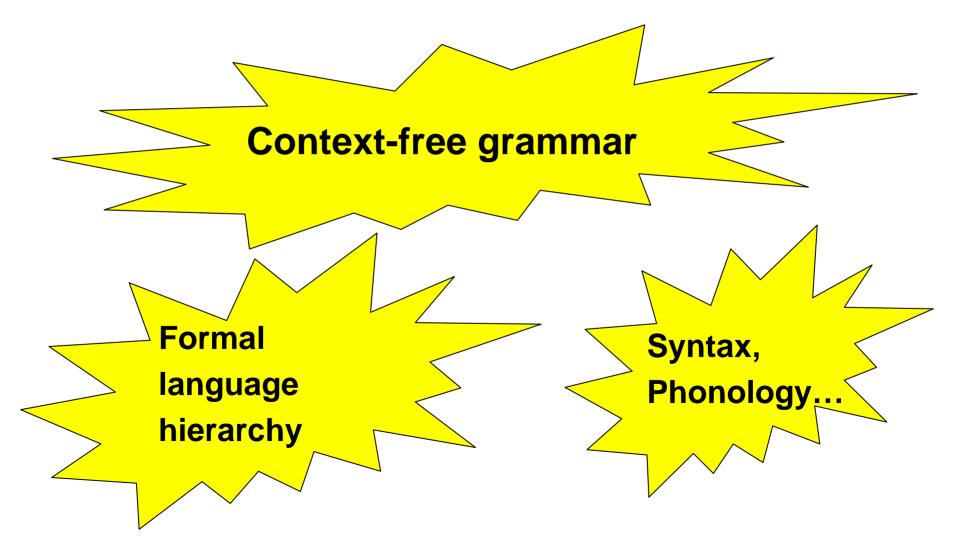
• Distinguish grammatical English from ungrammatical English:

- John thinks Sara hit the boy
- * The hit thinks Sara John boy
- John thinks the boy was hit by Sara
- Who does John think Sara hit?
- John thinks Sara hit the boy and the girl
- * Who does John think Sara hit the boy and?
- John thinks Sara hit the boy with the bat
- What does John think Sara hit the boy with?
- Colorless green ideas sleep furiously.
- * Green sleep furiously ideas colorless.

Chomsky [1957]

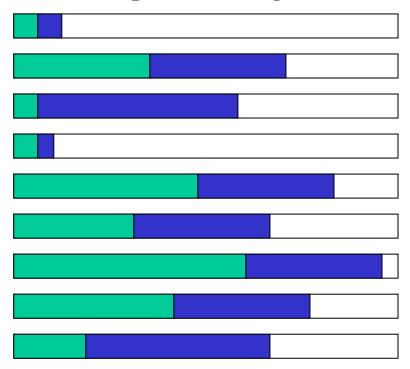
- Can be naturally extended to distinguish sensible vs. nonsense English:
 - * Colorless green ideas sleep furiously.
 - John eats bananas.
 - * Bananas eat John.
- Can be naturally extended to likelihood someone would say X:
 - (VERY LIKELY) Hello, how are you?
 - (VERY VERY UNLIKELY) Sara the Sara boy hit hit India
 - (POSSIBLE) That coyote has long hard teeth
 - (VERY UNLIKELY) Garbage isn't in the mind of the ocean.

This Research Program has Contributed Powerful Ideas!



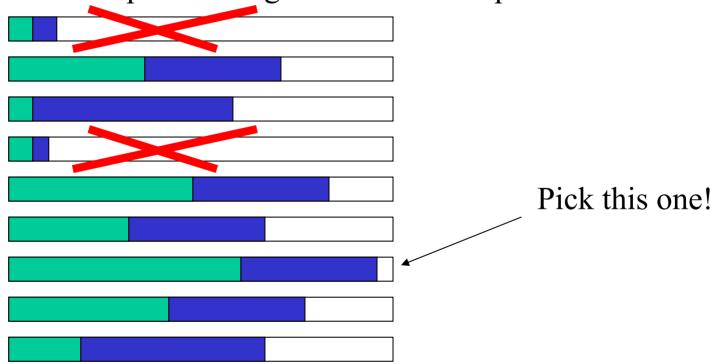
This Research Program has NLP Technology Applications!

Alternative speech recognition or MT outputs:



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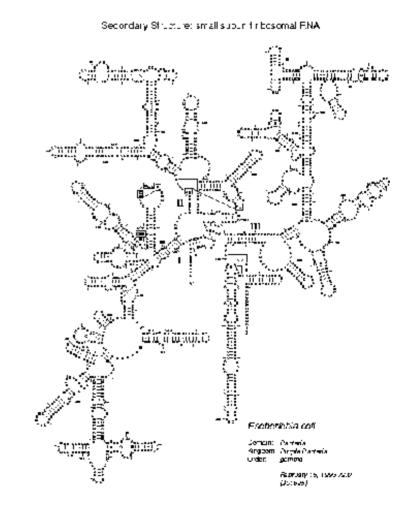


This Research Program Has Wider Reach than Was Expected!

- What makes a legal RNA sequence?
- What is the structure of a given RNA sequence?

For example:

Yasubumi Sakakibara, Michael Brown, Richard Hughey, I. Saira Mian, Kimmen Sjolander, Rebecca C. Underwood and David Haussler. **Stochastic Context-Free Grammars for tRNA**, *Modeling Nucleic Acids Research*, 22(23):5112-5120, 1994.



This Research Program is Really Unfinished!

Type	in	your	English	sentence	here:	

Is this grammatical?

Is this sensible?

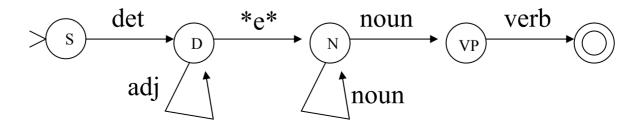
This Research Program is Really Unfinished!

Type	in	your	English	sentence	he	ere:
				(Is th	nis	grammatical?
				Is th	nis	sensible?

Or, check out machine translation output → it grammatical not is really!

Regular Grammar

- Example
 - $-S \rightarrow \det D$
 - $-D \rightarrow adj D$
 - $-D \rightarrow N$
 - $-N \rightarrow noun N$
 - $-N \rightarrow noun VP$
 - VP \rightarrow verb
- Defines a set of *strings*
- Language described by regular grammar can also be described by a finite-state acceptor (FSA):



Regular Grammar

- Can't capture long-distance relationships with a reasonable-sized grammar
 - The toys in that closet are/is fun to play with.
 - The toys in that closet are fun to play with.
- Can't handle aⁿbⁿ constructions?
 - John, Bill, ..., and Jack enjoy
 swimming, kayaking, ..., and slacking, respectively.
- Can't handle deep recursion?
 - The rat died.
 - The rat [that the cat ate] died.

^can a verb come next? yes...

• Example:

• Defines a set of strings

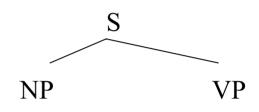
 Language described by CFG can also be described by a push-down acceptor

Generative Process:

S

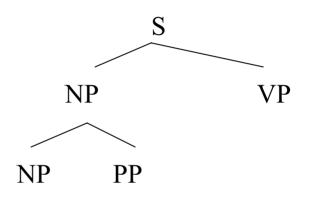
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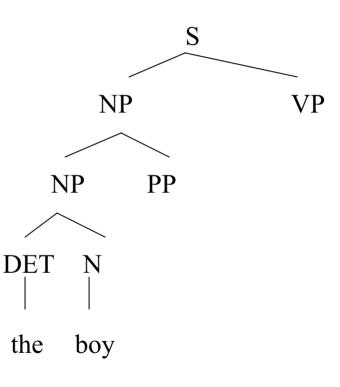
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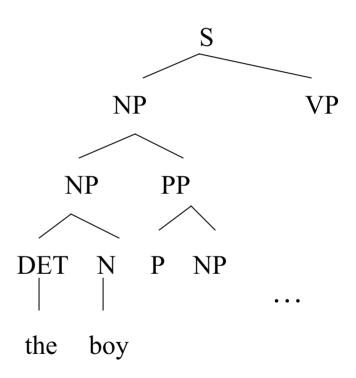
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• Example:

- Defines a set of *strings*
- Language described by CFG can also be described by a push-down acceptor



• Example:

$$-S \rightarrow NP \ VP$$

$$-NP \rightarrow DET \ N$$

$$-NP \rightarrow NP \ PP$$

$$-NP \rightarrow NP \ PP$$

$$-PP \rightarrow P \ NP$$

$$-VP \rightarrow V \ NP$$

$$-DET \rightarrow the$$

$$-NP \rightarrow boy$$

$$-NP \rightarrow boy$$

$$-VP \rightarrow with$$

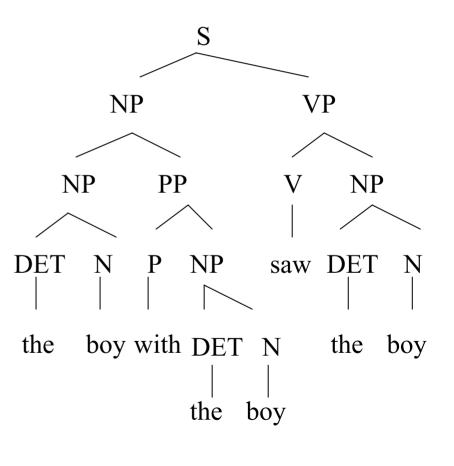
$$[p=1.0]$$

$$-NP \rightarrow with$$

$$[p=1.0]$$

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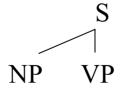
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- Is this what lies behind modern parsers like Collins and Charniak?
- No... they do not have a finite list of productions, but rather infinite.
 - "Markovized" grammar
- Generative process is head-out:



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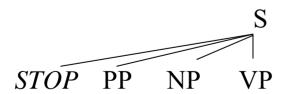


 $P_{left}(NP \mid VP, S)$

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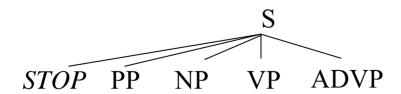


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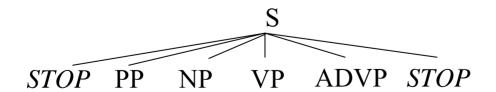


 $P_{left}(STOP \mid VP, S)$

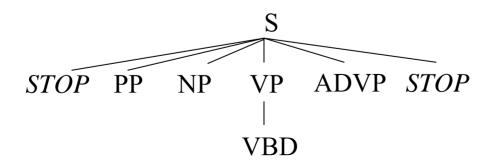
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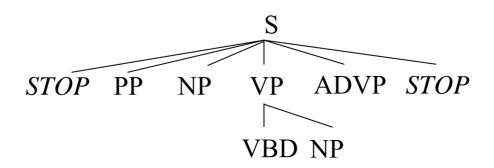
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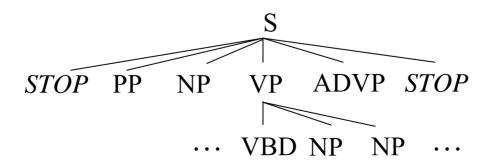
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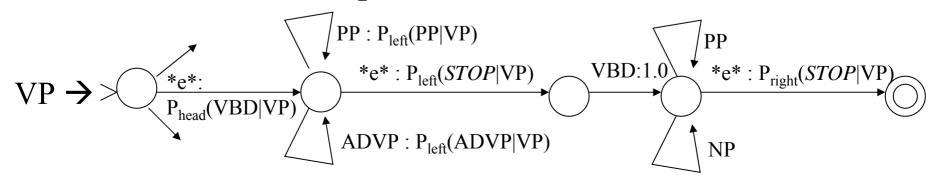


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Extended Context-Free Grammar [Thatcher, 1967]

- Example:
 - $-S \rightarrow ADVP*NPVPPP*$
 - $VP \rightarrow VBD NP [NP] PP*$
- Defines a set of strings
- Can model Charniak and Collins:
 - $\text{ VP} \rightarrow (\text{ADVP} \mid \text{PP})^* \text{ VBD } (\text{NP} \mid \text{PP})^*$
- Can even model probabilistic version:



Extended Context-Free Grammar [Thatcher, 1967]

- Is ECFG more powerful than CFG?
- It is possible to build a CFG that generates the same set of strings as your ECFG
 - As long as right-hand side of every rule is regular
 - Or even context-free ☺

• BUT:

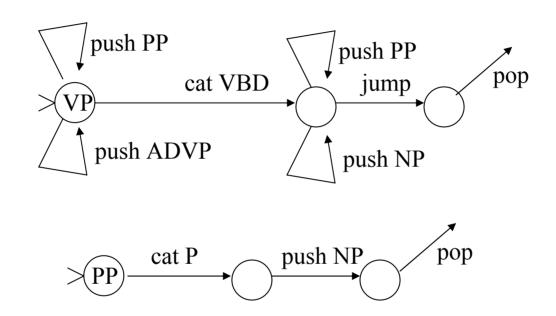
 the CFG won't generate the same derivation trees as the ECFG

Extended Context-Free Grammar [Thatcher, 1967]

• For example:

- ECFG can (of course) accept the string language a*
- Therefore, we can build a CFG that also accepts a*
- But ECFG can do it via this set of derivation trees, if so desired:

Recursive Transition Networks (RTNs)



Collection of separate networks.

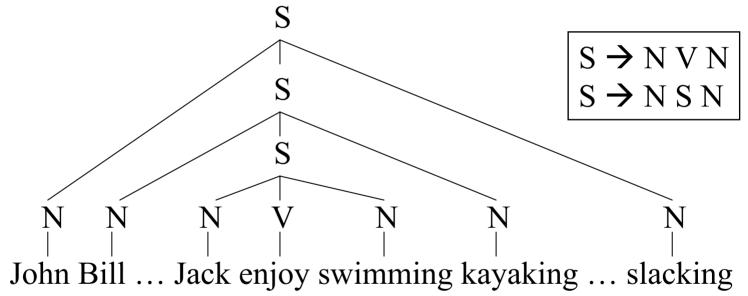
Defines a set of strings.

Usually no one thinks about derivation trees.

Augmented RTNs (ATNs) store pieces of text in register variables as recognition proceeds.

More Trees vs Strings

- Regular grammars can't handle aⁿbⁿ constructions?
- CFGs can:



- We can generate the string ...
- But that's not necessarily the derivation tree we want

Tree Generating Systems

- What if the trees are important?
 - Parsing, RNA structure prediction
 - Tree transformation (active → passive, MT, SBLM, ...)
- We can view CFG or ECFG as a tree-generating system, if we squint real hard ...
- Or, we can look at real tree-generating systems:
 - Regular tree grammar (RTG)
 - More recently in our field called tree substitution grammar (TSG)
 - Tree-adjoining grammar (TAG)
- And at tree-transforming systems:
 - Top-down tree transducers (R, RL, RLN, ...)
 - Bottom-up tree transducers (F, FL, FLN, ...)

What We'd Like to Do

- Device or grammar D for compactly representing possibly-infinite set of trees (possibly with weights)
- Want to support operations like:
 - Membership testing: Is tree X in the set D?
 - Equality testing: Do D1 and D2 contain exactly the same trees?
 - Intersection: Compute (possibly-infinite) set of trees in both D1 and D2
 - Weighted intersection
 - Re-score all weighted trees in D1 by intersecting with weighted set D2
 - E.g.: D1 is a set of candidate translations
 - E.g.: D2 is a language model [Chomsky 1957]

Regular Tree Grammar (RTG)

Generative Process:

Example:

_	$q \rightarrow S(qnp, VP(V(run)))$	[p=1.0]
_	$qnp \rightarrow NP(qdet, qn)$	[p=0.7]
_	$qnp \rightarrow NP(qnp, qpp)$	[p=0.3]
_	$qpp \rightarrow PP(qprep, qnp)$	[p=1.0]
_	$qdet \rightarrow DET(the)$	[p=1.0]
_	$qprep \rightarrow PREP(of)$	[p=1.0]
_	$qn \rightarrow N(sons)$	[p=0.5]
	$qn \rightarrow N(daughters)$	[p=0.5]

• Defines a set of *trees*

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$$- \text{ qpp} \rightarrow \text{PP(qprep, qnp)} \quad [p=1.0]$$

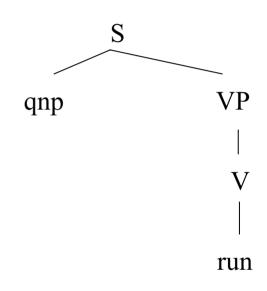
-
$$qdet \rightarrow DET(the)$$
 [p=1.0]

- qprep
$$\rightarrow$$
 PREP(of) [p=1.0]

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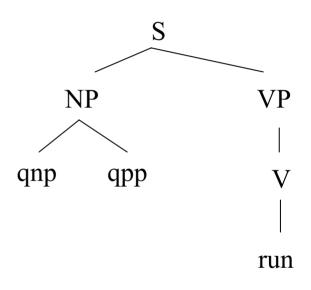
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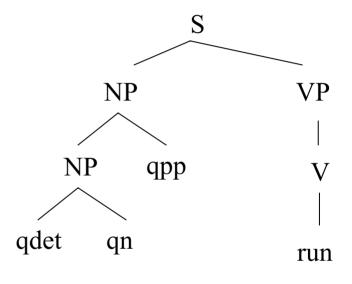
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Generative Process:



• Defines a set of *trees*

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• Example:

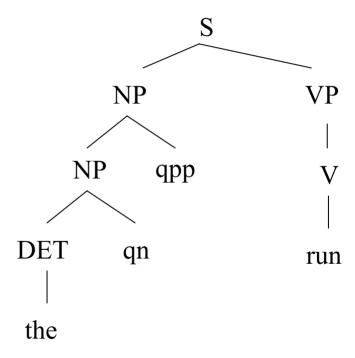
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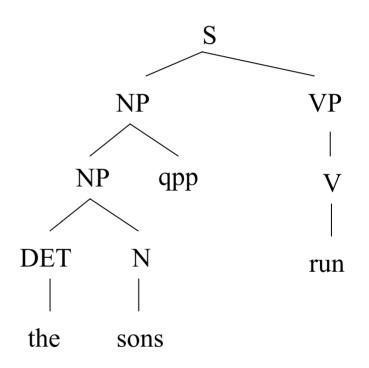
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Generative Process:



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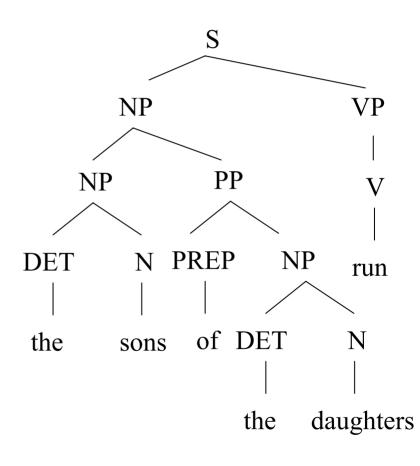
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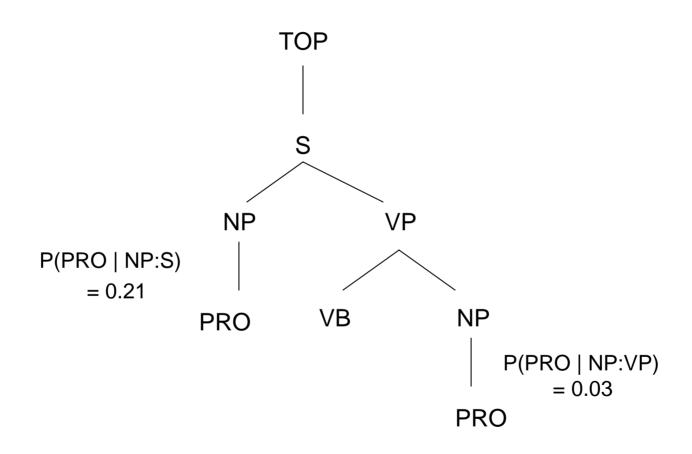
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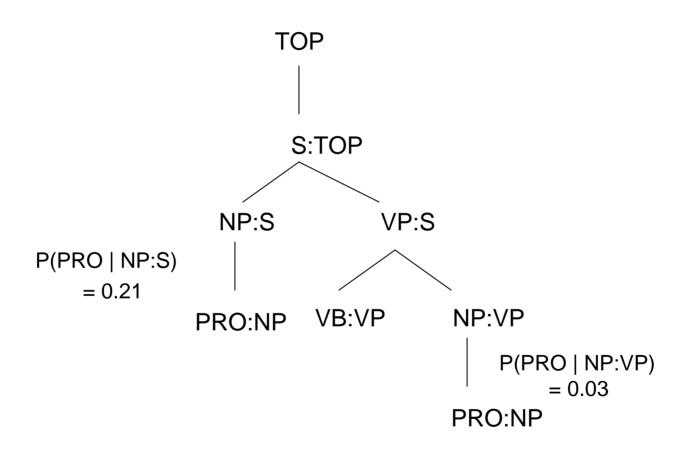


 $P(t) = 1.0 \times 0.3 \times 0.7 \times 0.5 \times 0.7 \times 0.5$

Relation of RTG to Johnson [98] Model

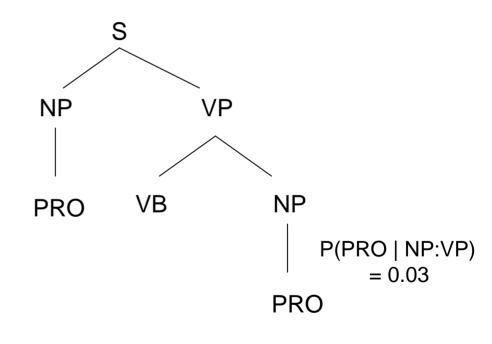


Relation of RTG to Johnson [98] Model



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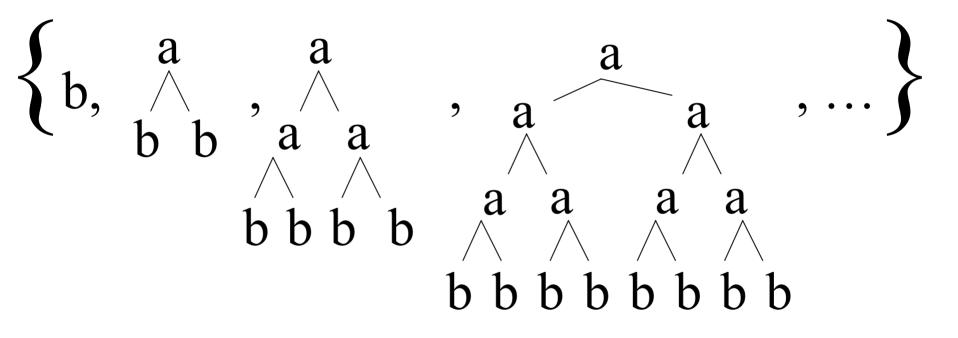
```
RTG:
qstart \rightarrow S(q.np:s, q.vp:s)
q.np:s \rightarrow NP(q.pro:np)
q.np:vp \rightarrow NP(q.pro:np) p=0.03
q.pro:np \rightarrow PRO(q.pro)
q.pro:np \rightarrow he
q.pro:np \rightarrow she
q.pro:np \rightarrow him
q.pro.np \rightarrow her
```



Relation of RTG to Collins Model

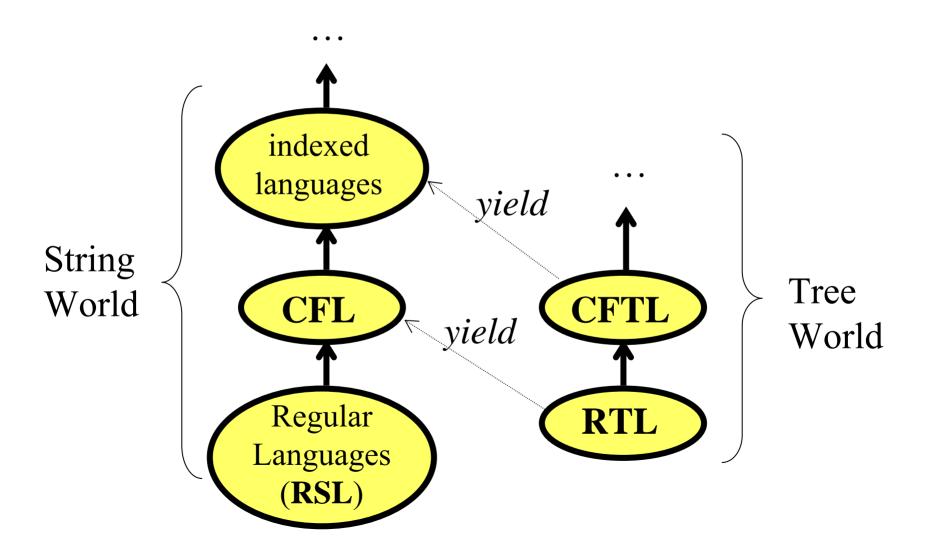
- Collins and Charniak assign P(t) to every tree
- Can weighted RTG (wRTG) implement Collins' P(t) for language modeling?
 - Just like a WFSA can implement smoothed n-gram language model?
- Roughly yes.
 - States encode relevant context that is passed up and down the tree.
- Two technical problems:
 - "Markovized" grammar ("Extended" RTG?)
 - Collins' model requires keep head-word information, and if we "back off" to a state that forgets head-word, we can't get it back.

A Tree Language Accepted by No RTG



Note also that the *yield language* is $\{b^{2^n} : n \ge 1\}$, which is not context-free.

Language Classes in String World and Tree World



More on RTG and CFG

- For every CFG, there is an RTG that directly generates its derivation trees
 - TRUE (just convert the notation)
- For every RTG, there is a CFG that generates the same trees as derivations
 - $\begin{array}{c} \textbf{-FALSE} \\ q \rightarrow S(X(A), Y(B)) \\ q \rightarrow S(X(B), Y(A)) \end{array} \quad \text{accepts} \quad \left\{ \begin{array}{c} S \\ X \\ Y \\ A \end{array} \right. , \quad \begin{array}{c} X \\ Y \\ B \end{array} \right. \right\}$

Picture So Far

	String	Tree
	Languages	Languages
Grammars	Regular grammar (RG)	Regular tree grammar (RTG)
Acceptors	Finite-state acceptor (FSA)	?

FSA Analog: Top-Down Tree Acceptor [Rabin, 1969; Doner, 1970]

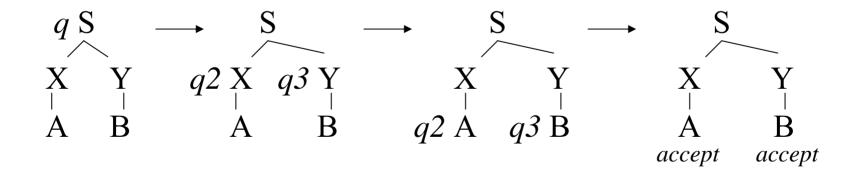
RTG:

$$q \rightarrow S(X(A), Y(B))$$

 $q \rightarrow S(X(B), Y(A))$

TDTA:

$$q S \rightarrow q2 q3$$
 $q3 X \rightarrow q3$
 $q S \rightarrow q3 q2$ $q3 Y \rightarrow q3$
 $q2 X \rightarrow q2$ $q2 A \rightarrow accept$
 $q2 Y \rightarrow q2$ $q3 B \rightarrow accept$



For any RTG, there is a TDTA that accepts the same trees. For any TDTA, there is an RTG that accepts the same trees.

FSA Analog: Bottom-Up Tree Acceptor [Thatcher, 1967]

• A similar story...

Properties of Language Classes

String World

Tree World

	RSL	CFL	RTL
	(FSA, rexp)	(PDA, CFG)	(TDTA, RTG)
Closed under union	YES	YES	YES
Closed under intersection	YES	NO	YES
Closed under complement	YES	NO	YES
Membership testing	O(n)	$O(n^3)$	O(n)
Emptiness decidable?	YES	YES	YES
Equality decidable?	YES	NO	YES

(references: Hopcroft & Ullman 79, Gécseg & Steinby 84)

• Example:

Generative Process:

S

- S(NP \downarrow , VP(V(hit), NP \downarrow))

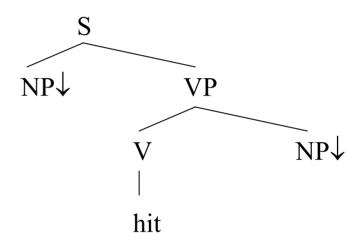
- NP(D \downarrow , N(boy))
- NP(D↓, N(dragon))
- NP(John)
- D(the)
- VP(VP*, ADV(today))
- ADJ(ADV(very), ADJ*)
- N(ADJ(funny), N*)

• Example:

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• Defines a set of *trees*

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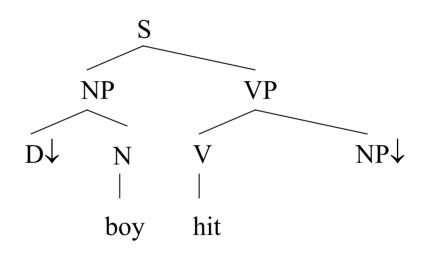


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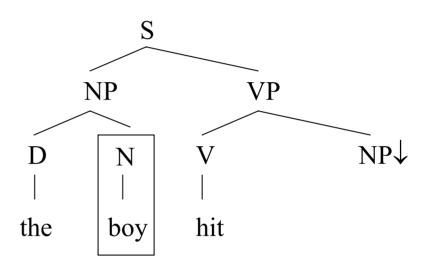
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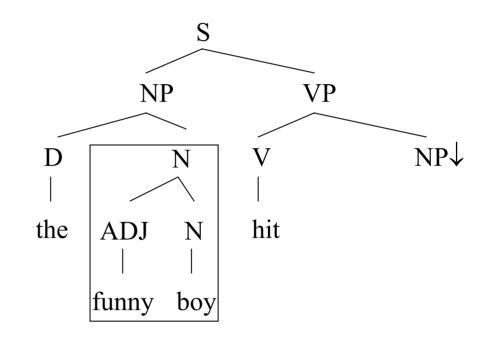


So far, just like RTG/TSG.

Example:

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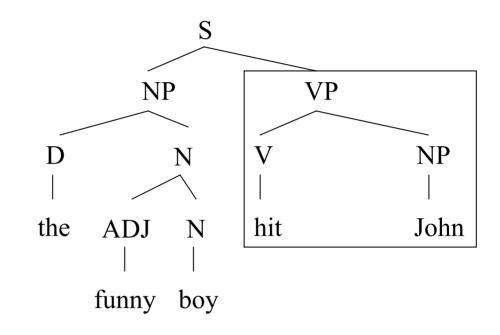
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- $NP(D\downarrow, N(dragon))$
- NP(John)
- D(the)
- VP(VP*, ADV(today))
- ADJ(ADV(very), ADJ*)
- N(ADJ(funny), N*)

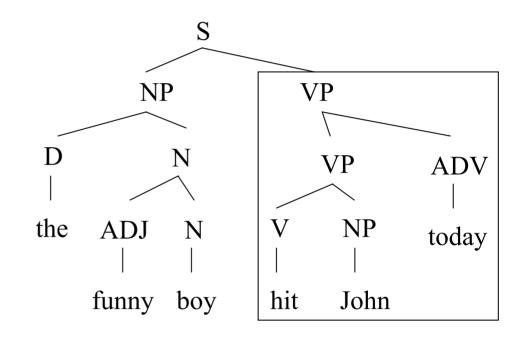
Generative Process:



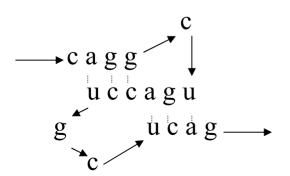
• Example:

- $S(NP\downarrow, VP(V(hit), NP\downarrow))$
- $NP(D\downarrow, N(boy))$
- NP(D↓, N(dragon))
- NP(John)
- D(the)
- VP(VP*, ADV(today))
- ADJ(ADV(very), ADJ*)
- N(ADJ(funny), N*)

Generative Process:



- Can generate tree sets that RTG cannot
- Elements far apart in the tree can depend on each other.
 - Mary attacked.
 - Mary had attacked.
 - Mary had attacked yesterday. [now Mary & attacked are far apart]
- Has recently been used to model RNA structure
 - Observed string: ... caggcugaccugcucag...
 - Most likely folding structure according to grammar:



[Uemura, Hasegawa, Kobayashi, Yokomori, 1999] [Rivas and Eddy, 2000]

Picture So Far

String Language

- FSA compactly represents a possibly-infinite set of strings
- Probabilistic FSA assigns a P(s) to every string
- Can ask: Is s grammatical & sensible?

Tree Language

- RTG compactly represents a possiblyinfinite set of trees
- Probabilistic RTG assigns a P(t) to every tree
- Can ask: Is t grammatical & sensible?

Picture So Far

String Language

- FSA compactly represents a possibly-infinite set of strings
- Probabilistic FSA assigns a P(s) to every string
- Can ask: Is s grammatical & sensible?

String Transducer

- FST compactly represents a possiblyinfinite set of *string pairs*
- Probabilistic FST assign P(s2 | s1) to every *string pair*
- Can ask: What's the best transformation of string s1?

Tree Language

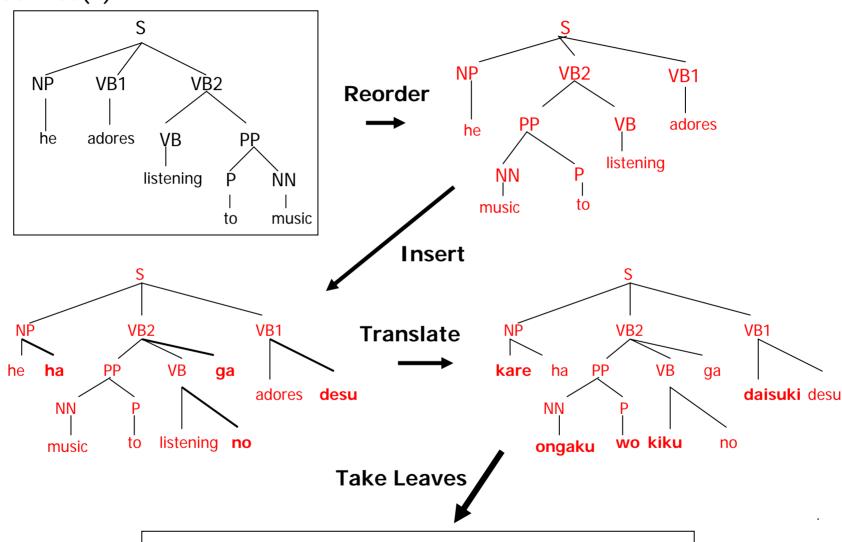
- RTG compactly represents a possiblyinfinite set of trees
- Probabilistic RTG assigns a P(t) to every tree
- Can ask: Is t grammatical & sensible?

Tree Transducer

- Tree transducers compactly represent a possibly-infinite set of *tree pairs*
- Probabilistic tree transducers assign
 P(t2 | t1) to every tree pair
- Can ask: What's the best transformation of tree t1?

Example 1: Machine Translation (Yamada & Knight 2001)

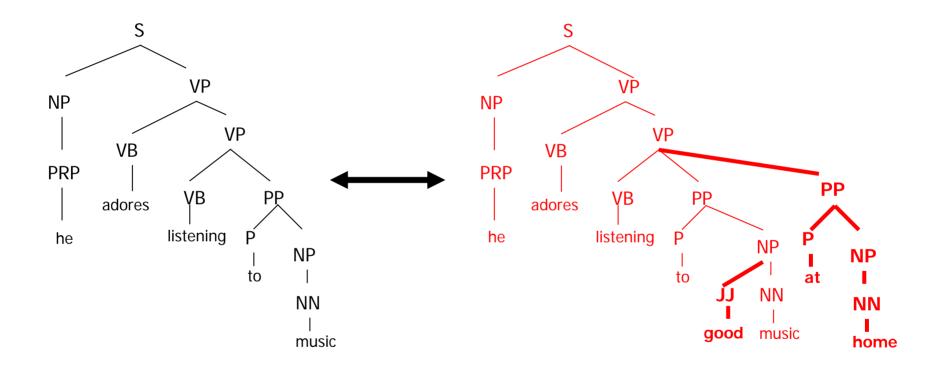
Parse Tree(E)



Sentence(J)

Kare ha ongaku wo kiku no ga daisuki desu

Example 2: Sentence Compression Knight & Marcu (2000)



What We'd Like to Do

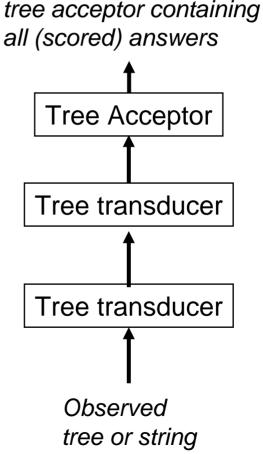
- Device T for compactly representing possiblyinfinite set of tree pairs (possibly with weights)
- Want to support operations like:
 - Forward application: Send input tree X through T,
 get all possible output trees, represented as an RTG.
 - Backward application: What input trees, when sent through T, would output tree X?
 - Composition: Given a sequence of T1 and T2, can we build a transducer T3 that does the work of both?
 - Equality testing: Do T1 and T2 contain exactly the same tree pairs?
 - **Training**: How to set weights given a corpus?

Transducer Cascades

modeling direction:

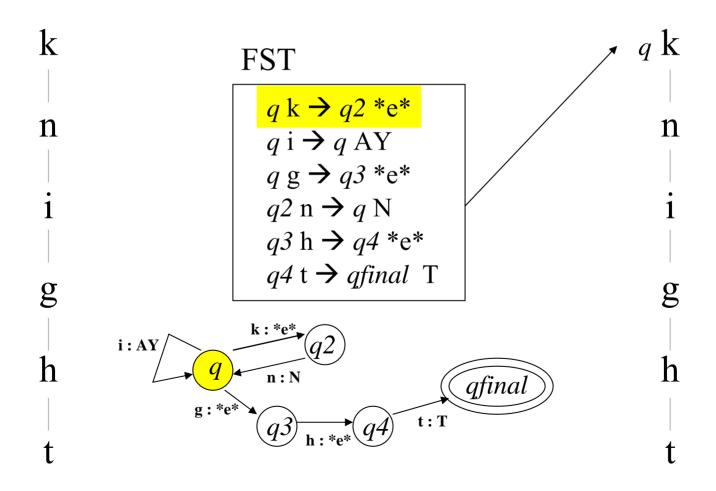
decoding direction:

Tree Acceptor Tree transducer Tree transducer Observed tree or string

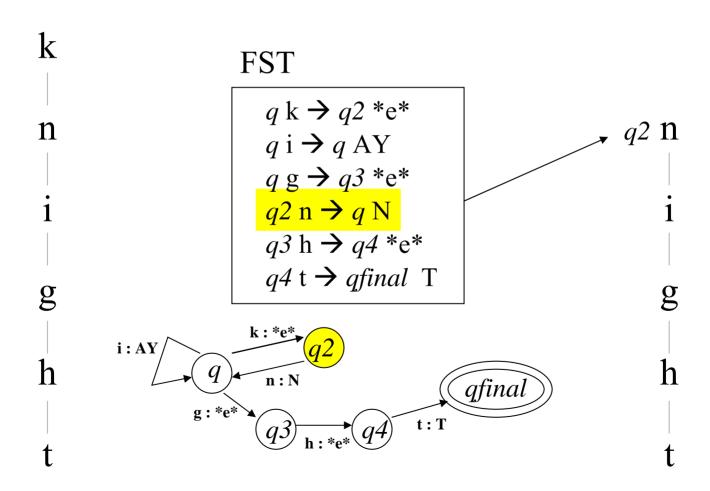


Finite-State Transducer (FST)

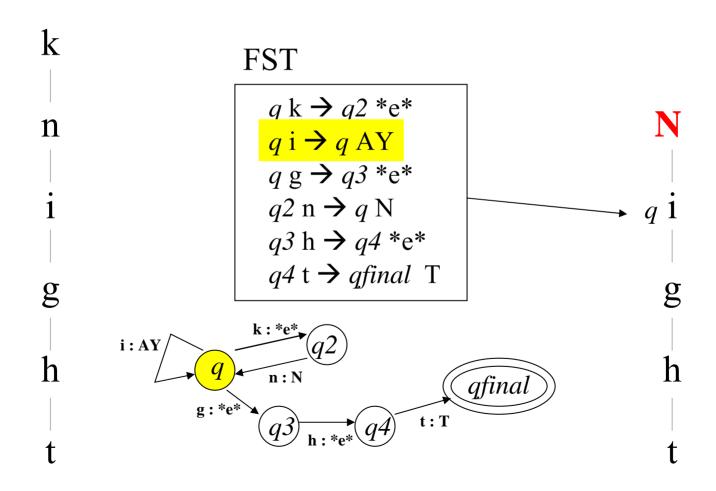
Original input:



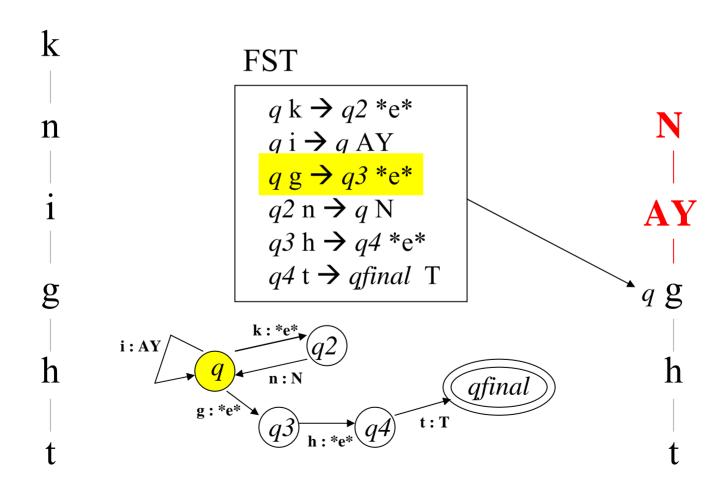
Original input:



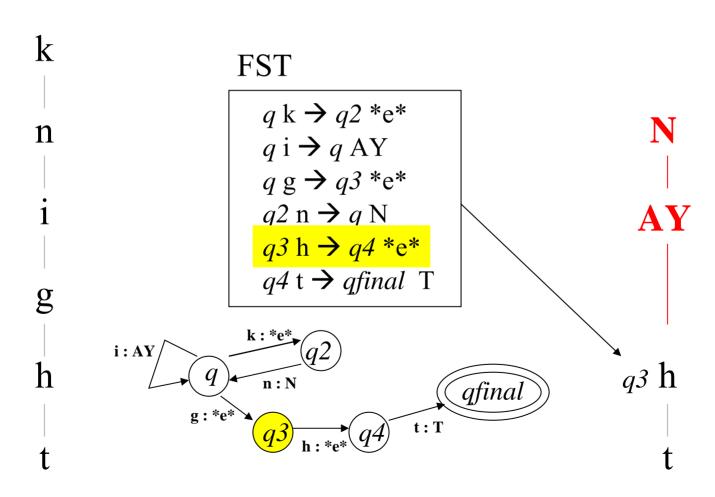
Original input:



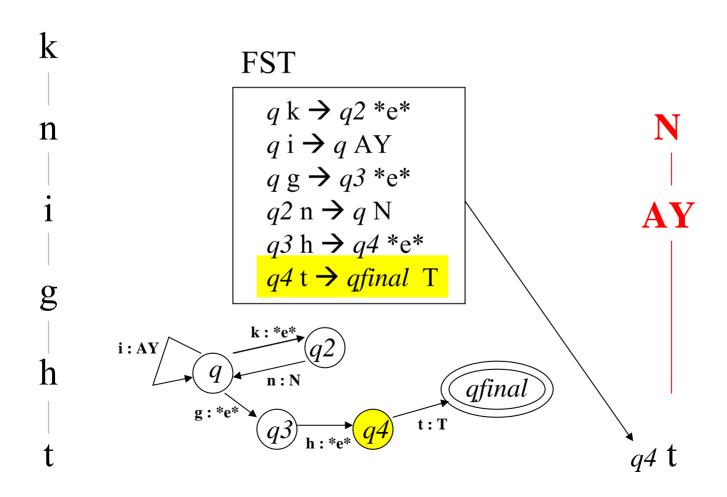
Original input:



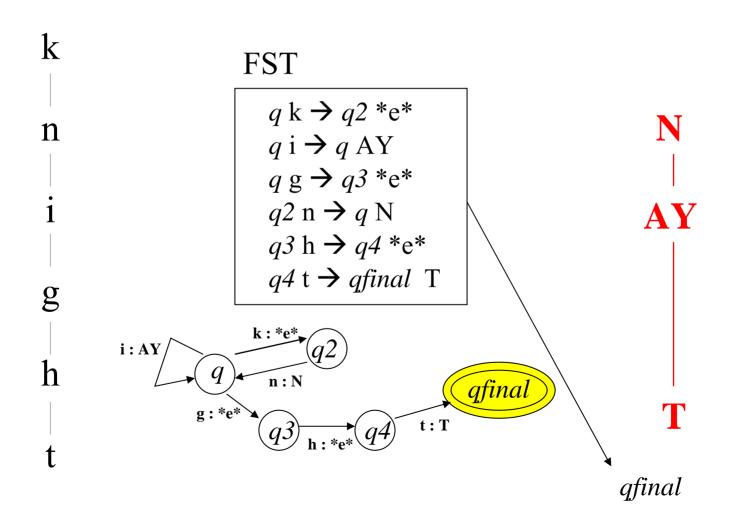
Original input:



Original input:



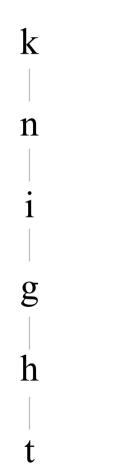
Original input:



Finite-State (String) Transducer

Original input:

Final output:



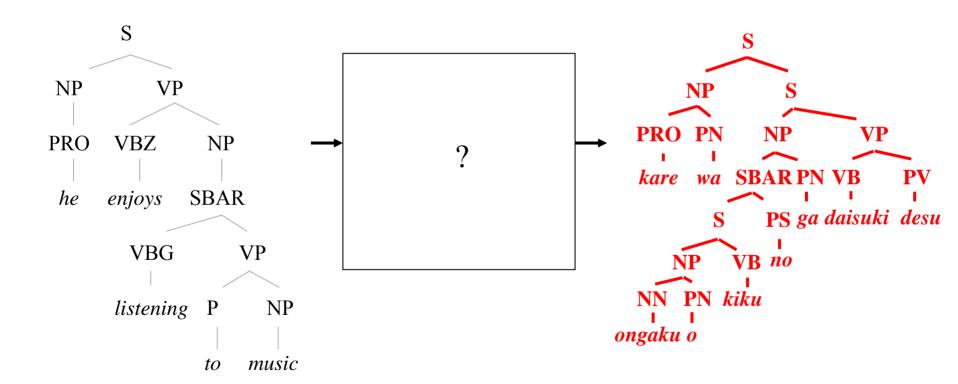
FST $q k \rightarrow q2 *e*$ $q i \rightarrow q AY$ $q g \rightarrow q3 *e*$ $q2 n \rightarrow q N$ $q3 h \rightarrow q4 *e*$ $q4 t \rightarrow qfinal T$



Trees

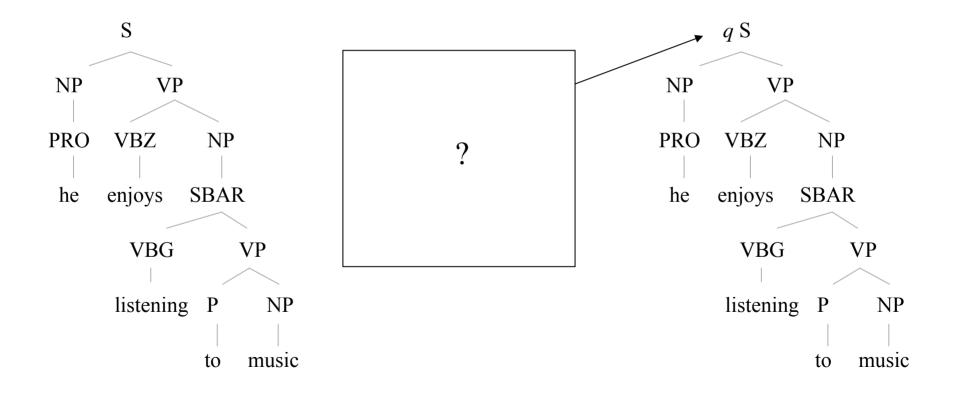
Original input:

Target output:



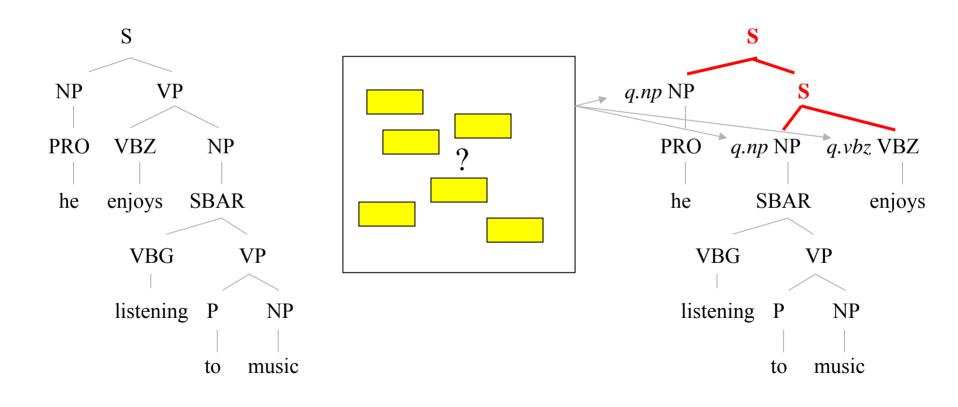
Tree Transformation

Original input:



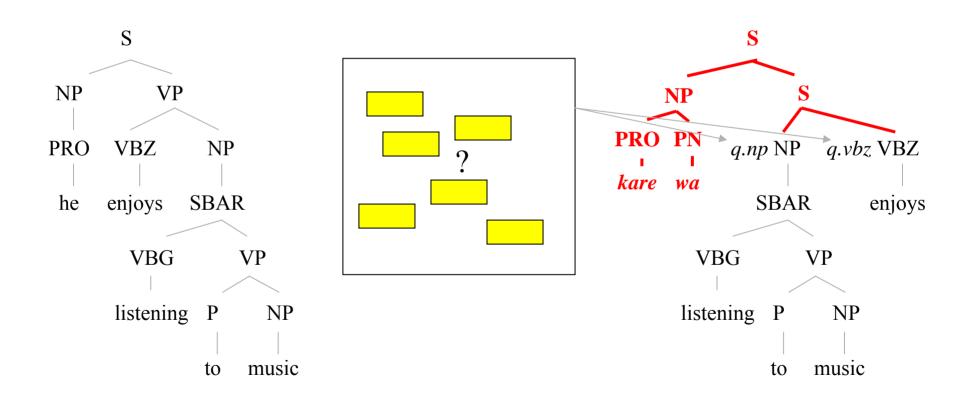
Tree Transformation

Original input:



Trees

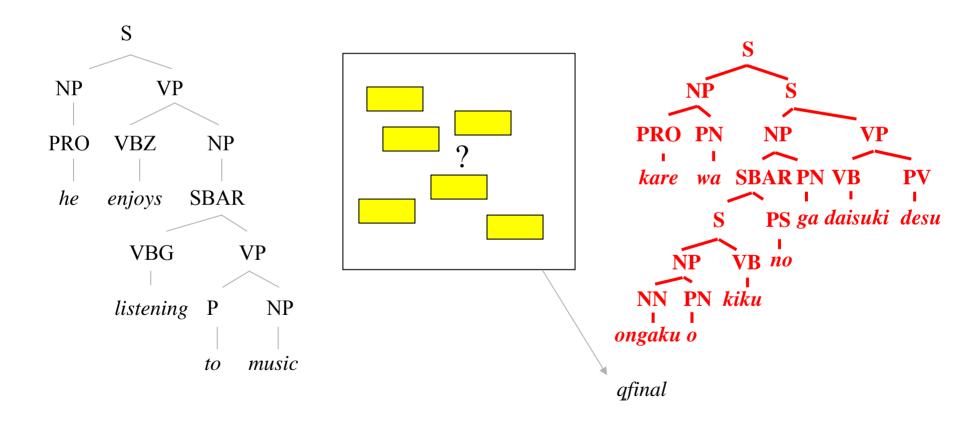
Original input:



Trees

Original input:

Final output:

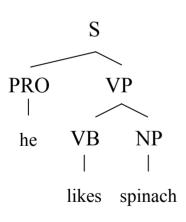


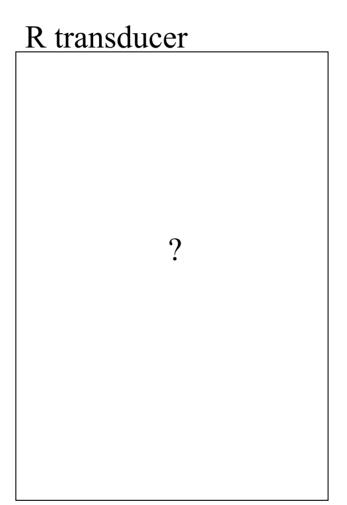
• Introduced by Rounds (1970) & Thatcher (1970)

"Recent developments in the theory of automata have pointed to an extension of the domain of definition of automata from strings to trees ... parts of mathematical linguistics can be formalized easily in a tree-automaton setting ... Our results should clarify the nature of syntax-directed translations and transformational grammars ..." (Mappings on Grammars and Trees, *Math. Systems Theory* 4(3), Rounds 1970)

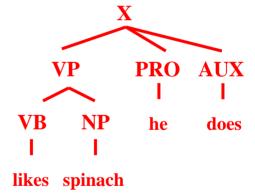
- "FST for trees"
- Large theory literature
 - e.g., Gécseg & Steinby (1984), Comon et al (1997)
- Many classes of transducers
 - Top-down: **R** ("root-to-frontier"), RL, RLN...
 - Bottom-up: F, FL, FLN...

Original Input:

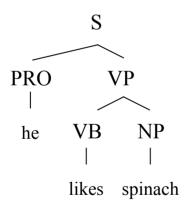




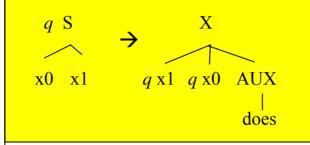
Target Output:



Original Input:

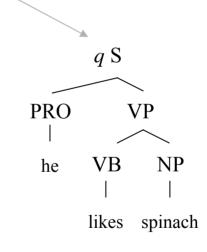


R transducer

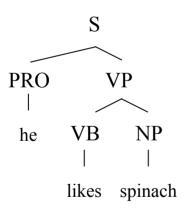


Or in computer-speak:

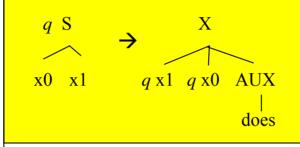
$$q S(x0, x1) \rightarrow X(q x1, q x0, AUX(does))$$



Original Input:

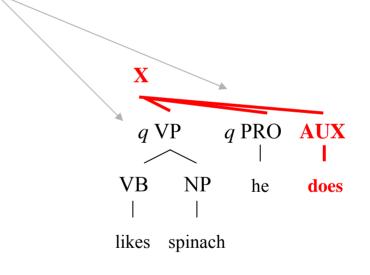


R transducer



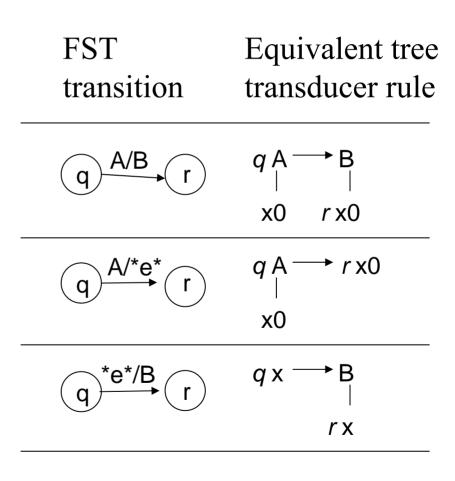
Or in computer-speak:

$$q S(x0, x1) \rightarrow X(q x1, q x0, AUX(does))$$



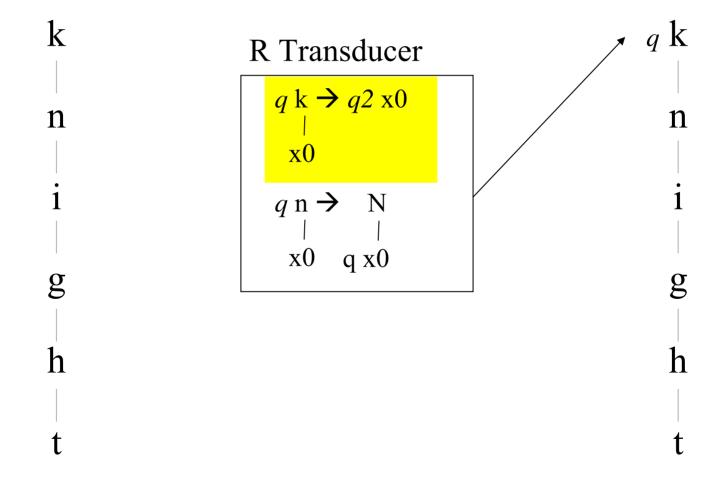
Tree Transducers and FSTs

 Tree transducers generalize FST (strings are "monadic trees")



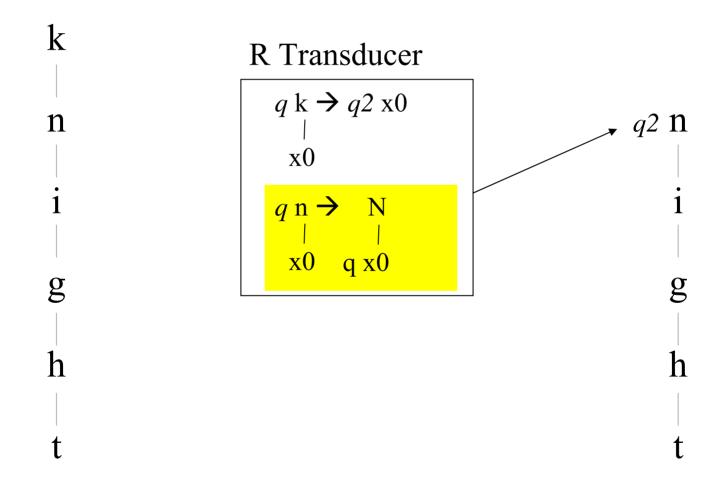
Tree Transducer Simulating FST

Original input:



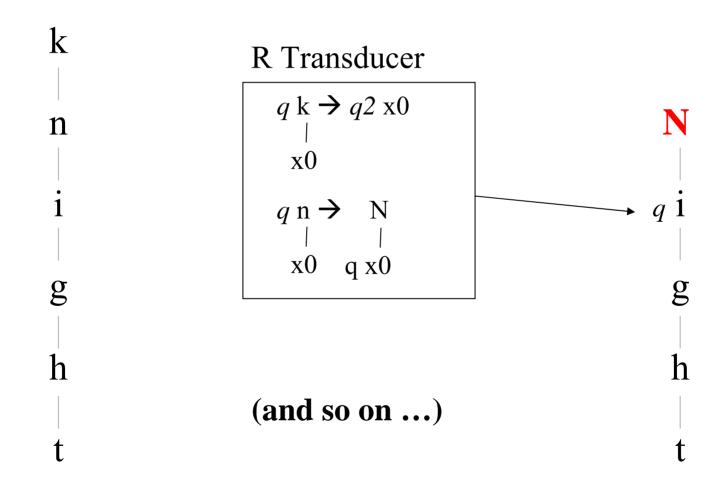
Tree Transducer Simulating FST

Original input:



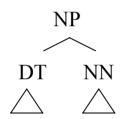
Tree Transducer Simulating FST

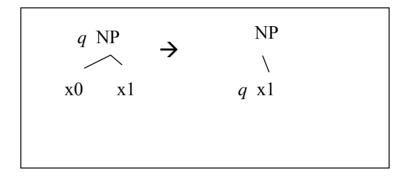
Original input:



R can Copy and/or Delete

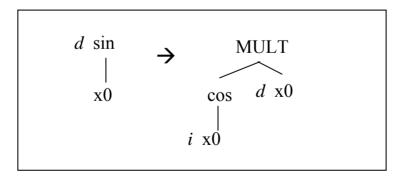
R transducer

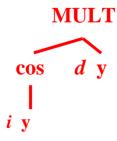




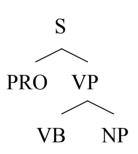




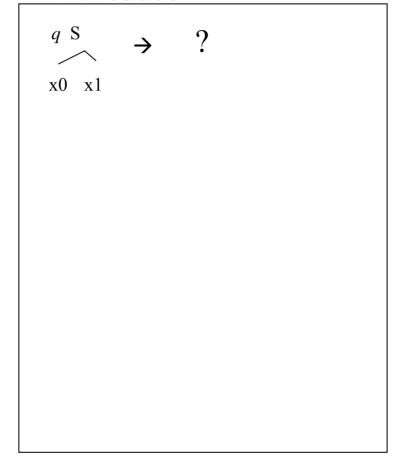




Original Input:



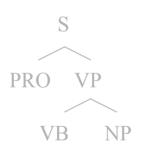
R transducer



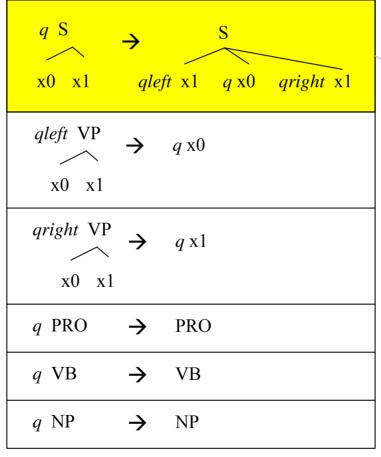
Target Output:

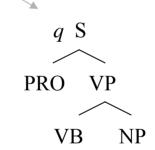


Original Input:

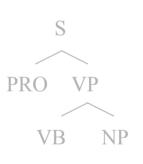


Transformation:

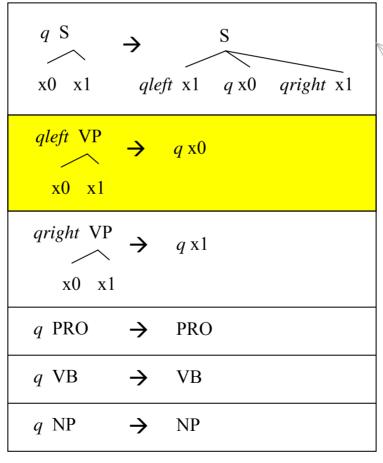


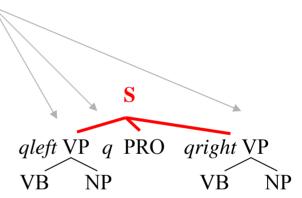


Original Input:

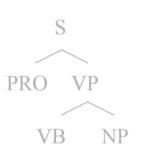


Transformation:

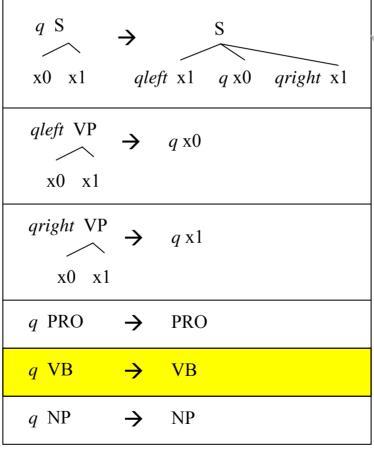


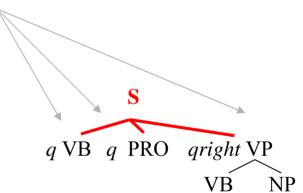


Original Input:

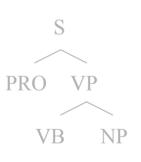


Transformation:

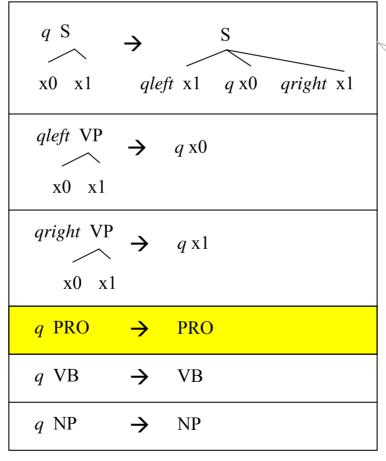


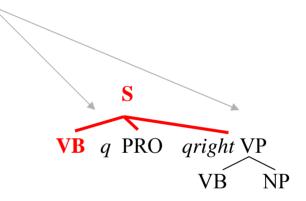


Original Input:

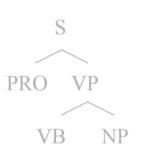


Transformation:

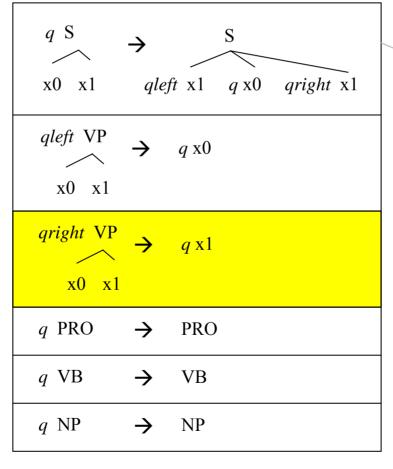


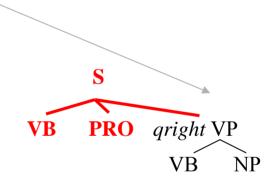


Original Input:

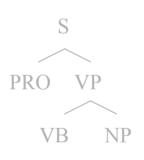


Transformation:

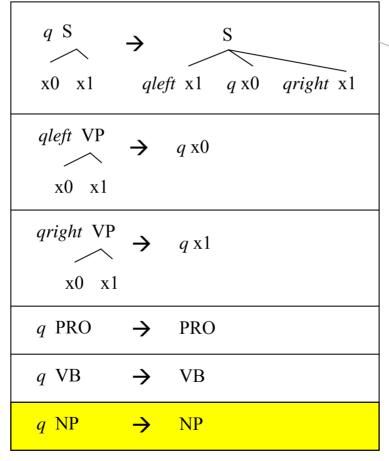


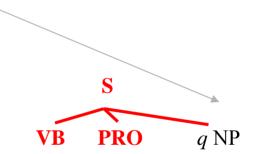


Original Input:

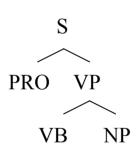


Transformation:

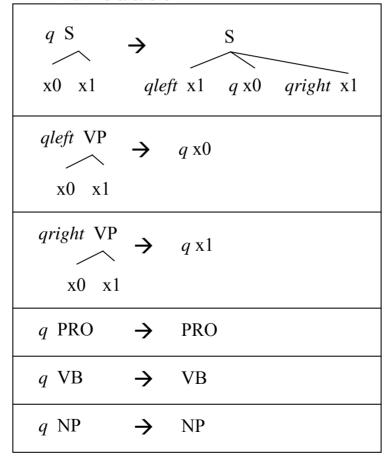




Original Input:



R transducer

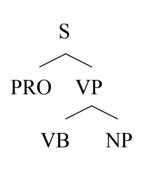


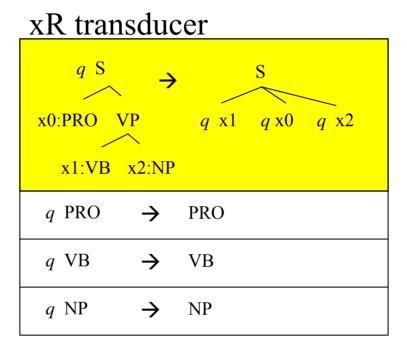
Final Output:



Extended Left-Hand Side: xR

Original Input:





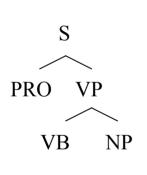
Final Output:

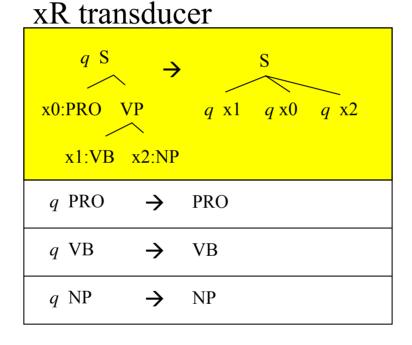


Mentioned already in Section 4, Rounds 1970. Not defined or used in proofs.

Extended Left-Hand Side: xR

Original Input:



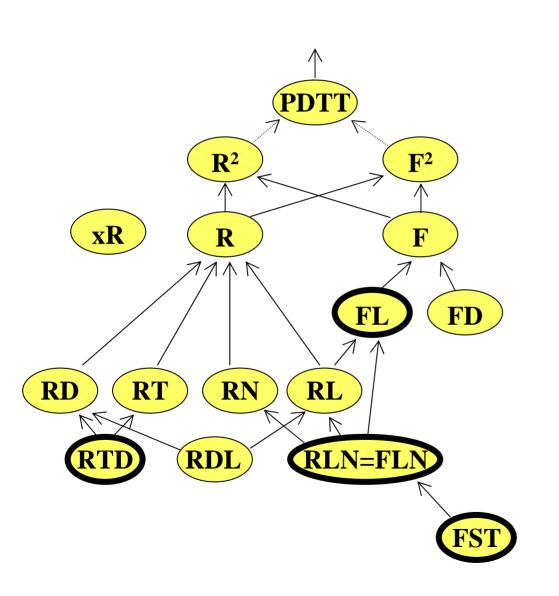


Final Output:



NOTE: This "extended" is not the same kind of "extended" as Thatcher's [1967] Extended Context Free Grammar (ECFG)! Is there such a thing as an ER transducer that works over its children one by one??

Tree Transducer Classes

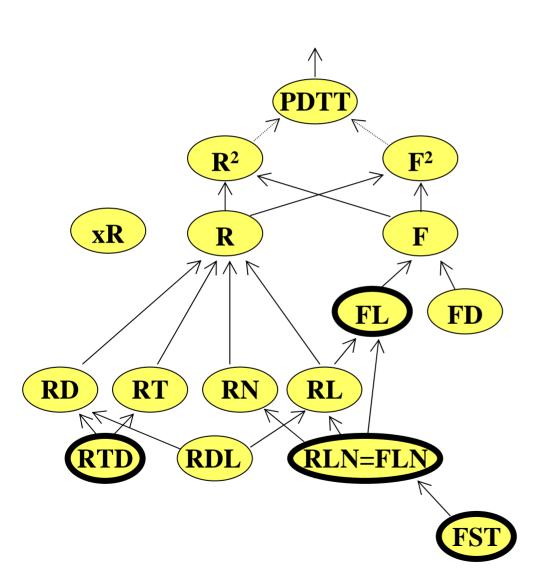


Abbreviations:

- **R** top-down tree transducer
- **F** bottom-up tree transducer
- L linear (non-copying)
- N non-deleting
- **D** deterministic
- T total (non-rejecting)
- x extended left-hand side

PDTT push-down transducer

Tree Transducer Classes

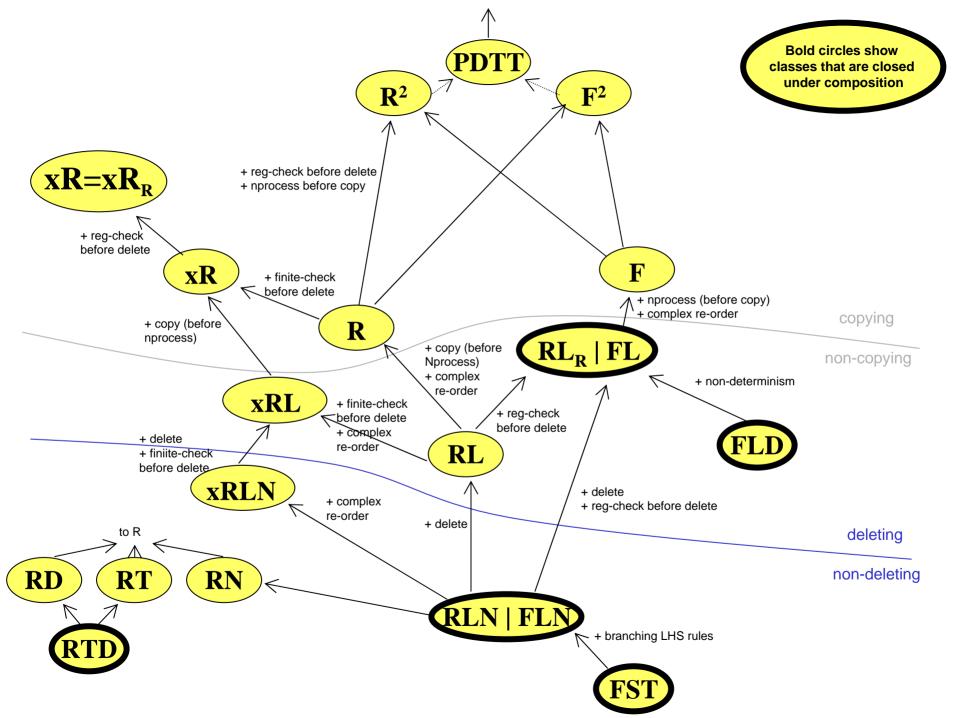


Abbreviations:

- **R** top-down tree transducer
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- L linear (non-copying)
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- x extended left-hand side

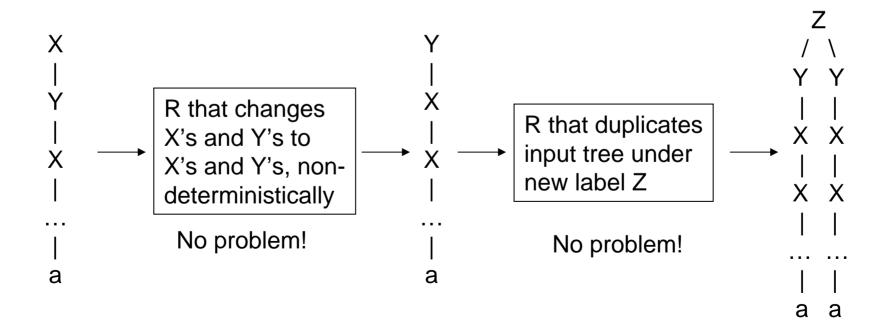
PDTT push-down transducer

Bold circles show classes that are closed under composition!



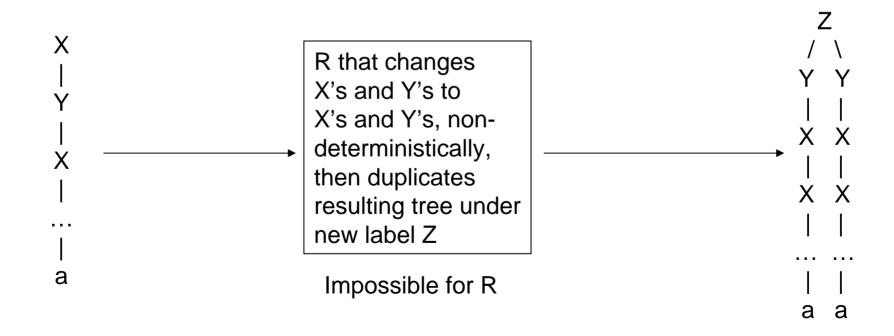
Composability of R

- Deterministic R-transducers are composable.
- Non-deterministic R transducers are not!



Composability of R

- Deterministic R-transducers are composable.
- Non-deterministic R transducers are not!



Properties of Transducer Classes

String World

Tree World

						•
	FST	R	RL	RLN=FLN	F	FL
Closed under composition	YES	NO	NO	YES	NO	YES
Closed under intersection	NO	NO	NO	NO	NO	NO
Image of tree (or finite forest) is:	RSL	RTL	RTL	RTL	Not RTL	RTL
Image of RTL is:	RSL	Not RTL	RTL	RTL	Not RTL	RTL
Inverse image of tree is:	RSL	RTL	RTL	RTL	RTL	RTL
Inverse image of RTL is:	RSL	RTL	RTL	RTL	RTL	RTL
Efficiently trainable	YES	YES	YES	YES		

(references: Hopcroft & Ullman 79, Gécseg & Steinby 84, Baum & Welch 71, Graehl & Knight 04)

Are Tree Transducers Expressive Enough?

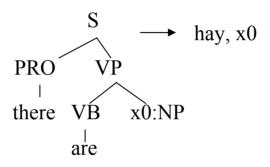
- MT model (Yamada & Knight, 2001) can be cast as a tree transducer.
 - Details in [Graehl & Knight, 2004]
- Good for elucidating the model, as in:
 - Knight & Al-Onaizan, 1998 IBM Model 3
 - Kumar & Byrne, 2003 Phrase-based SMT
- With tree transducer framework, these models can be extended with additional transitions.

Lots of Extensions Possible

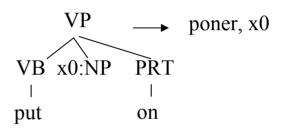
Phrasal Translation

VP — está, cantando VBZ VBG is singing

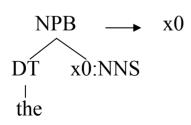
Non-constituent Phrases



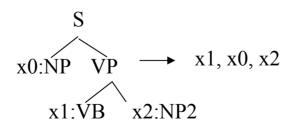
Non-contiguous Phrases



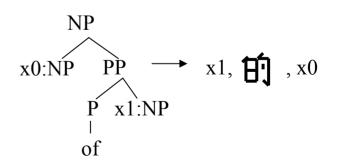
Context-Sensitive Word Insertion



Multilevel Re-Ordering



Lexicalized Re-Ordering

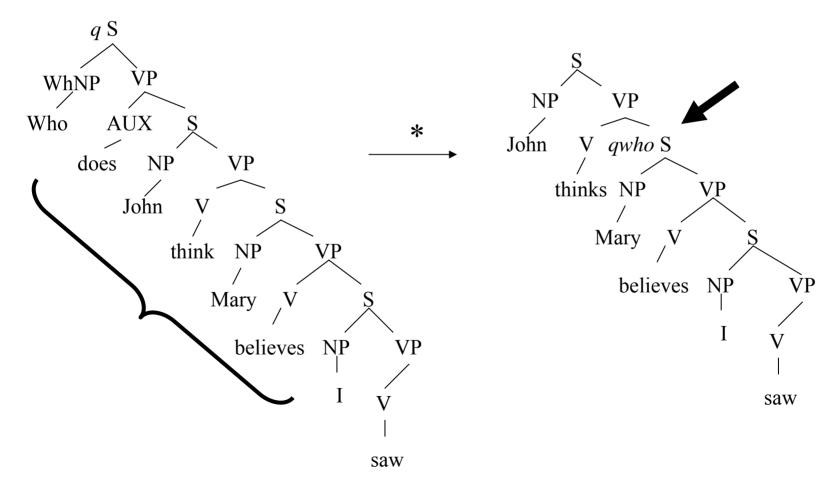


In fact, these are all learned by GHKM

Limitations of R Model

Long-distance Re-Ordering

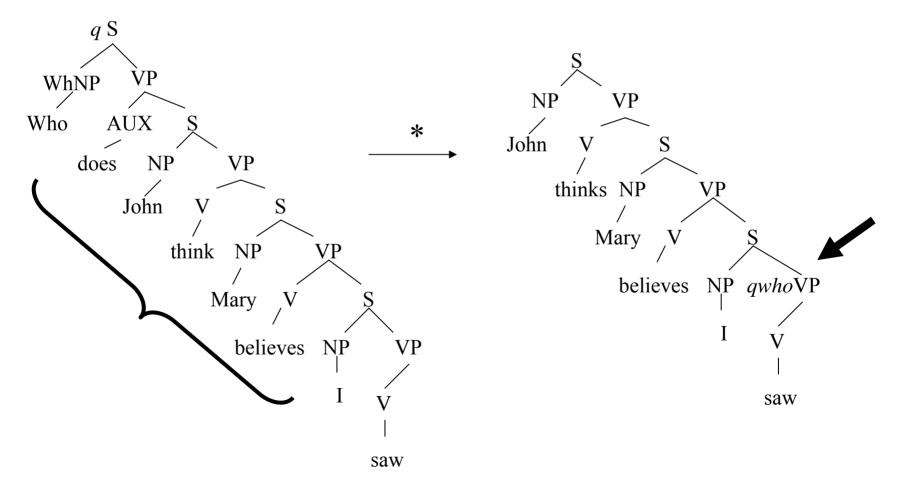
Who does John think Mary believes I saw? → John thinks Mary believes I saw *who*?



Limitations of R Model

Long-distance Re-Ordering

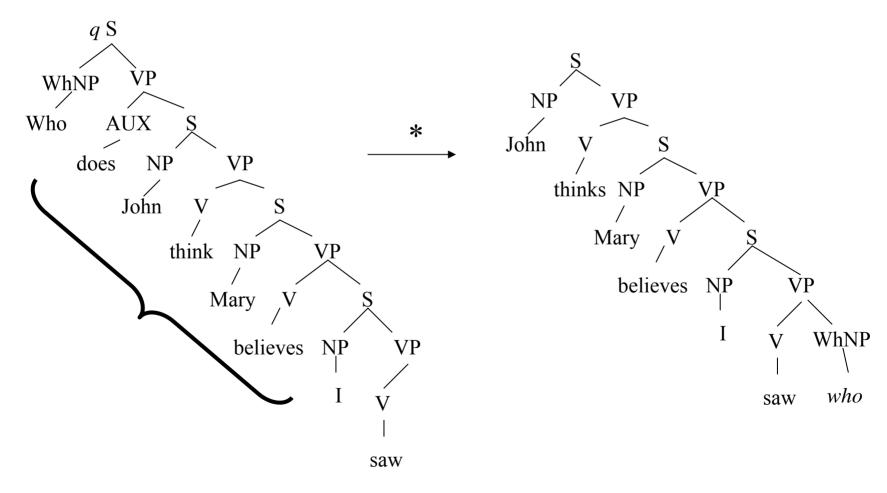
Who does John think Mary believes I saw? → John thinks Mary believes I saw *who*?



Limitations of R Model

Long-distance Re-Ordering

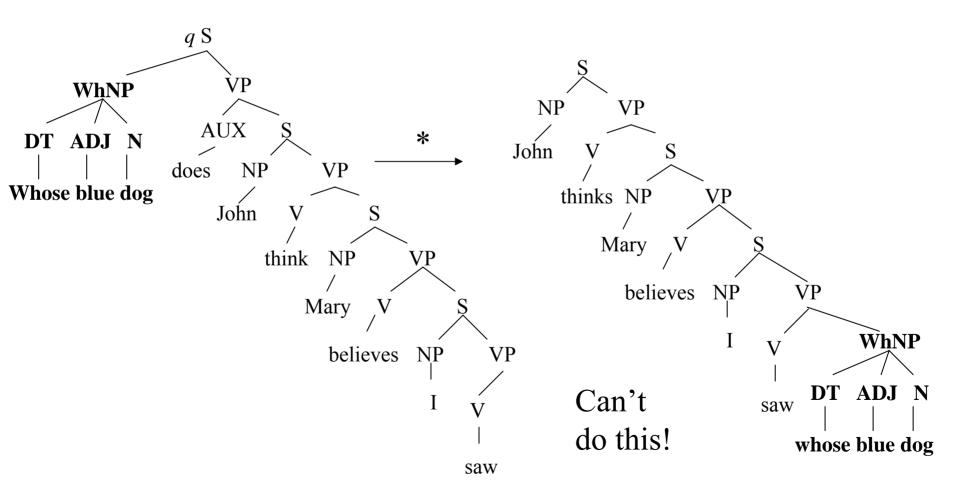
Who does John think Mary believes I saw? → John thinks Mary believes I saw *who*?



Limitations of R Model

Long-distance Re-Ordering

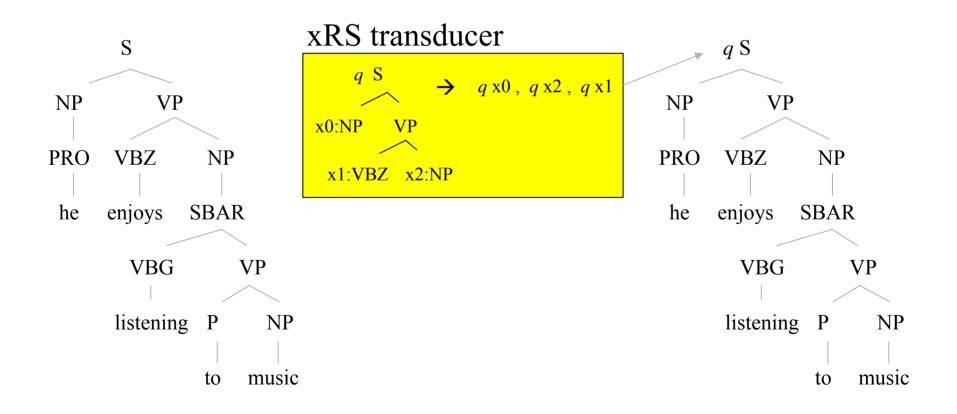
Whose blue dog does John think Mary believes I saw? → John thinks Mary believes I saw whose blue dog?



Syntax-directed translation for compilers (Aho & Ullman, 1971)

Original input:

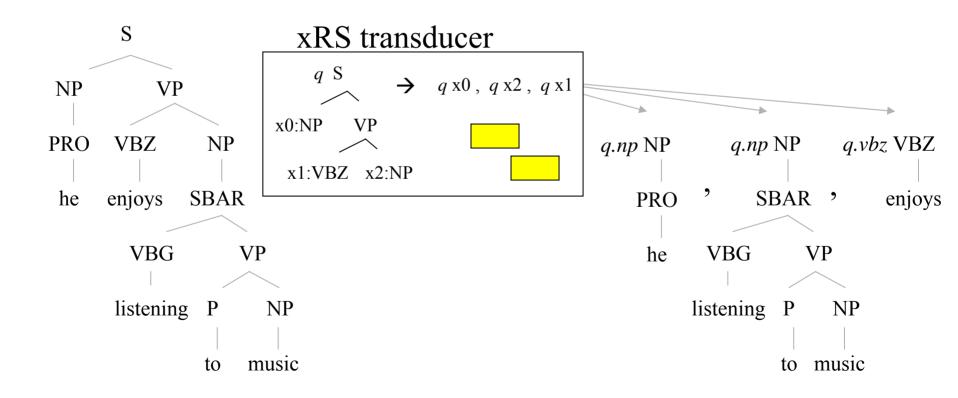
Transformation:



Syntax-directed translation for compilers (Aho & Ullman, 1971)

Original input:

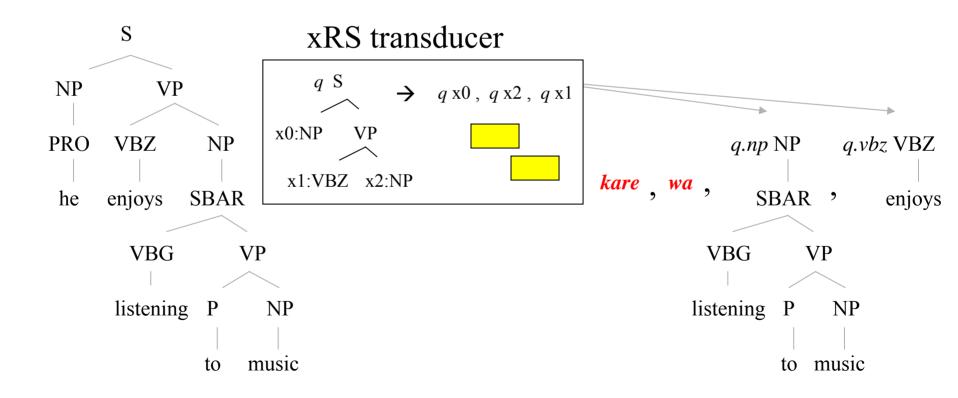
Transformation:



Syntax-directed translation for compilers (Aho & Ullman, 1971)

Original input:

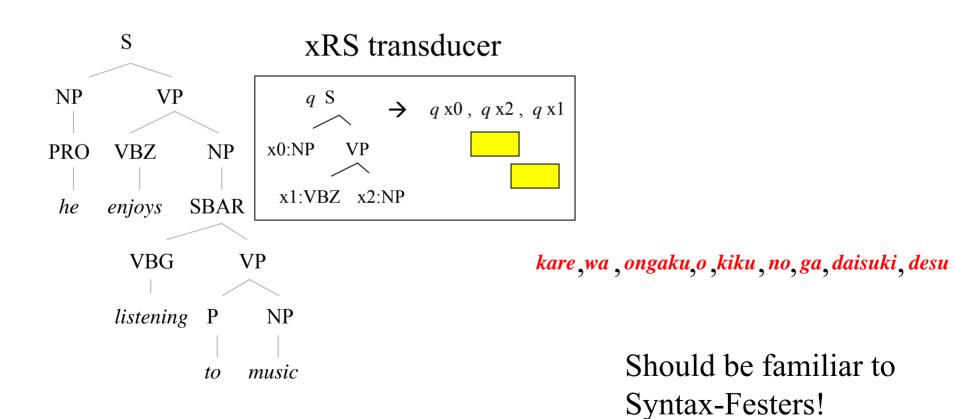
Transformation:



Syntax-directed translation for compilers (Aho & Ullman, 1971)

Original input:

Final output:



The Training Problem [Graehl & Knight, 2004]

• Given:

- an xR transducer with a set of non-deterministic rules $(r_1...r_m)$
- a training corpus of input-tree/output-tree pairs

• Produce:

– conditional probabilities $p_1...p_m$ that maximize

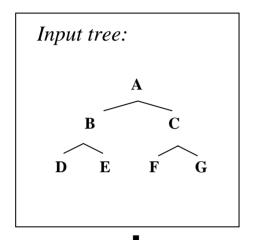
P(output trees | input trees)

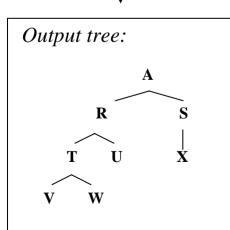
$$= \Pi_{i,o} P(o \mid i) \qquad \text{input/output trees} < i, o >$$

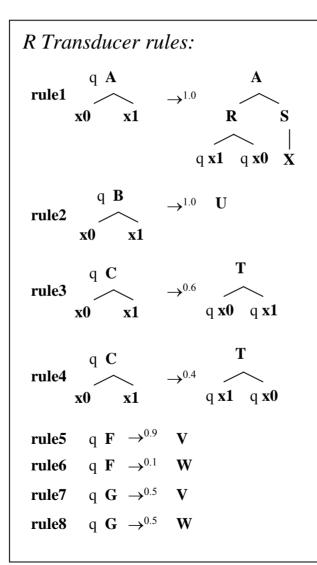
$$= \Pi_{i,o} \Sigma_d P(d, o \mid i) \qquad \text{derivations d mapping i to o}$$

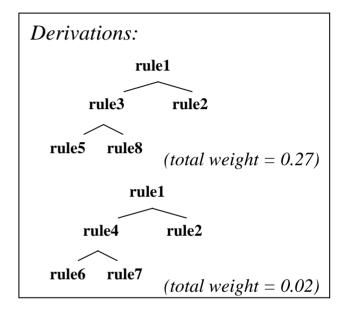
$$= \Pi_{i,o} \Sigma_d \Pi_r p_r \qquad \text{rules r in derivation d}$$

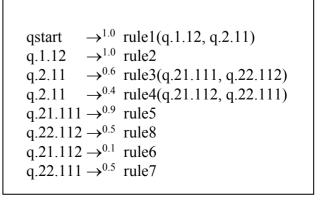
Derivations in R





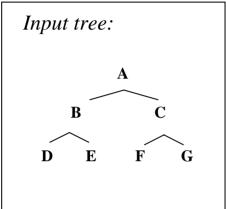




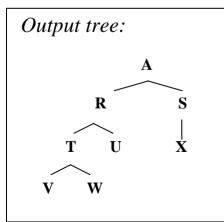


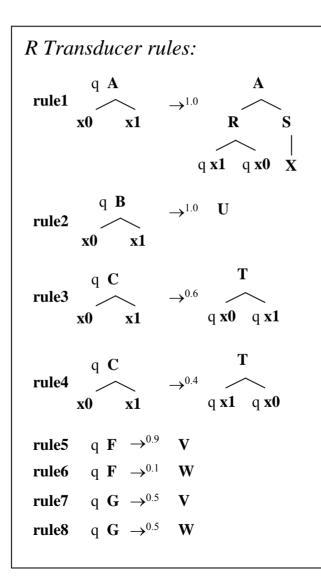
Packed Derivations:

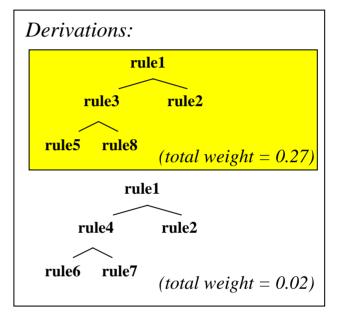
Derivations in R

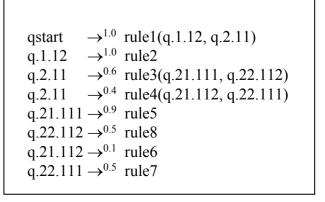






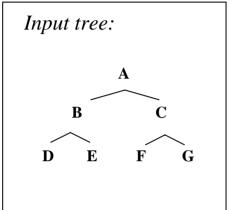




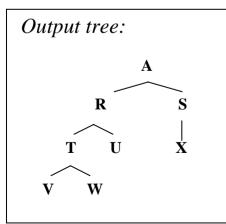


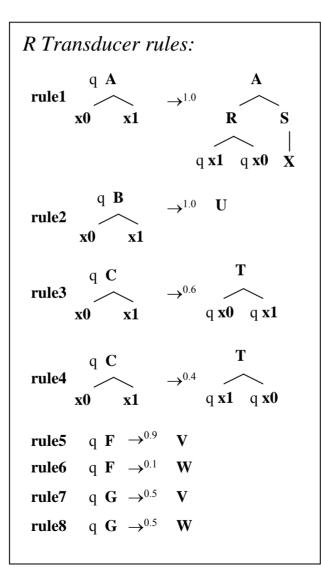
Packed Derivations:

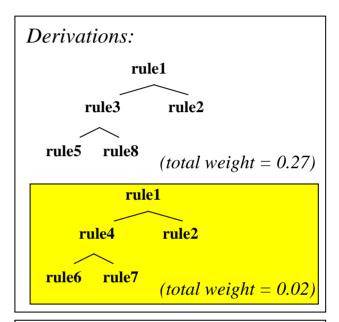
Derivations in R

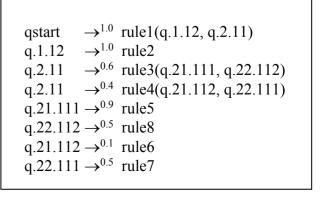












Packed Derivations:

Naïve EM Algorithm for xR

Initialize uniform probabilities

Until tired do:

Make zero rule count table

For each training case <i, o>

Compute P(o | i) by summing over derivations d

For each derivation d for <i, o> /* exponential! */

Compute $P(d \mid i, o) = P(d, o \mid i) / P(o \mid i)$

For each rule r used in d

 $count(r) += P(d \mid i, o)$

Normalize counts to probabilities

Packed Derivation Forest

Build packed derivation forest using dynamic programming (Yamada & Knight 2001, Eisner 2003)

Hit each triple <q, i-node, o-node> at most once:

For each <q, i-node, o-node>

For each rule r matching subtrees at i-node & o-node Can r kick off a mapping from subtree at i-node to subtree at o-node?

Bottom-up, or top-down memo-ized

 $O(q n^2 r)$ time

O(q n² r) space (therefore max size of derivation forest)

Efficient EM for xR

Initialize uniform probabilities Until tired do:

Make zero rule count table

For each training case <i, o>

Build packed derivation forest O(q n² r) time/space

Use inside-outside algorithm to collect rule counts

Inside pass $O(q n^2 r) time/space$

Outside pass $O(q n^2 r) time/space$

Count collection pass $O(q n^2 r)$ time/space

Normalize counts to probabilities (joint or conditional)

Per-example training complexity is O(n²) x "transducer constant" -- same as forward-backward training for string transducers (Baum & Welch, 1971).

EM for Tree/String Transducer (xRS)

Build packed derivation forest using dynamic programming. Hit each <**q**, **i-node**, **o-***span*> at most once:

For each <q, i-node, o-*span*>
For each rule r (*with* |*RHS*| = *k*) matching at i-node

For each break-up b of o-span into k pieces

Can r kick off a mapping from subtree at i-node to substring at o-*span*, *via break-up b*?

 $O(q n^4 r)$ time (if k = 2). $O(q n^3 r)$ space (therefore max size of derivation forest)

Followed by same inside-outside rule counting as for xR.

Training: Related Work

- Generalizes MT training in Appendix of (Yamada/Knight, 2001)
 - xR training not tied to particular MT model, or to MT at all
- Generalizes forward-backward HMM training (Baum/Welch, 1971)
 - Write strings vertically, and use xR training
- Generalizes inside-outside PCFG training (Lari/Young, 1990)
 - Attach fixed input tree to each "output" string, and use xRS training
- Generalizes synchronous tree-substitution grammar training (Eisner, 2003)
 - xR and xRS allow copying of subtrees

Best-Tree Search

• Given an input, what's the most likely output?

• FSA

- Best path through FSA can be found with [Dijkstra, 1959]
- Carmel lists k-best paths (incl. cycles), using [Eppstein 1999]
 - $O(n + m \log m + k \log k)$ running time
- Regular Tree Grammar (RTG)
 - Knuth [1977] solved the related grammar problem: efficiently extracts best tree from a forest
 - Can be viewed as hypergraph search
 - Look forward to hearing more from Liang on Friday!

Alternative Formulation of Transducers

- Synchronous Tree Grammars
 - Synchronous Tree Substitution Grammar (STSG)
 [Shieber, 1992; Eisner 2003 for training]

$$\begin{cases} q \to S(CC(if), S(qnp, qvp), CC(then), q) \\ q \to S(qnp, ifthen, q, qvp) \end{cases}$$

- Synchronous Tree Adjoining Grammar (STAG)[Shieber & Schabes, 1990]
- STSG same power as RLN [Eisner, 2003]
- Not true, says [Shieber, 2004]

Why Worry About Formal Languages?

- Is it a pretty dead field?
- They already figured out most everything back in the 1960s...
- If that's true, lucky us!

Why Worry About Formal Languages?

- Is there an extended version of R-style transducers, with ECFG-like processing of children?
- Are there transducers that can move material across a longer distance in the tree? Are they trainable?
 - [Johnson, 2004, ms]
- Is there an automata version of TAG? What properties?
- What about tree-based models that could train on string/string data? (SxRS...)
- What about "parent-less left-hand-side" rules like
 - NP(x0:DT, x1:JJ, x2:NN) \rightarrow x0, x1, x2
 - DT(the) \rightarrow el
 - JJ(big) NN(cheese) → jefe /* parent-less LHS rule */
- Can "cloning" operation of [Gildea 03] be captured by a tree transducer?
- Is xR closed under composition? Where is it in the transducer-power hierarchy?
- Can we build tree transducer toolkits as powerful and ubiquitous as string transducer toolkits?

the end beginning