

Autonomous Navigation and Perception for Aerial Vehicles

Assistant Prof. Vadim Indelman



ANPL | Autonomous Navigation & Perception Lab

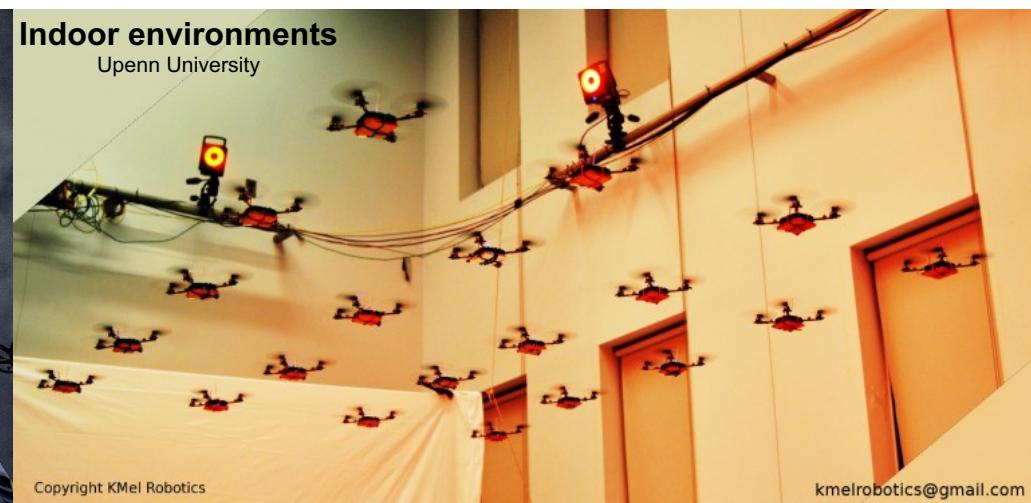
Aerial Autonomy

- Autonomous operation in complex, uncertain and ambiguous scenarios
 - Independent of infrastructure and prior information
 - Within static and dynamic environments

Urban environments
IROS 2013 workshop



Indoor environments
Upenn University



Amazon Prime Air



Google X Project Wing

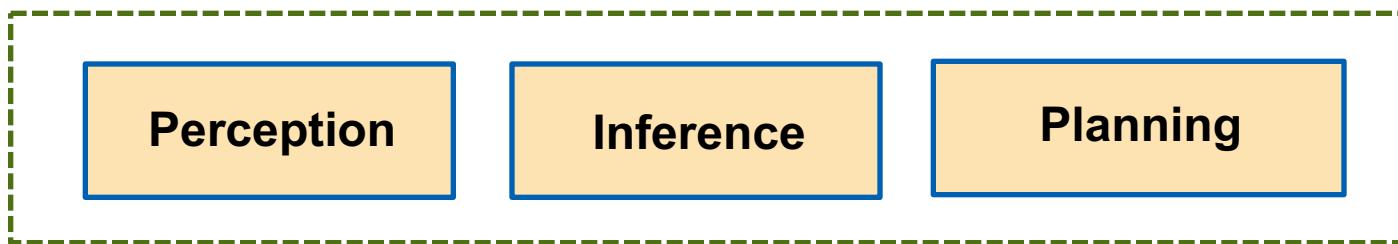


Upenn & CMU



Aerial Autonomy

- Key required components
 - **Perception & inference:** Where am I? What is the surrounding environment?
 - **Planning:** What to do next?



- Required online
- Additional complexity for multiple robots

Perception and Inference

- Where am I?
- What is the surrounding environment?

Perception

Inference

■ What if neither is known?

- Need to estimate **both** robot pose and observed structure
- **Robotics:** simultaneous localization and mapping (SLAM)
- **Computer vision:** structure from motion, bundle adjustment

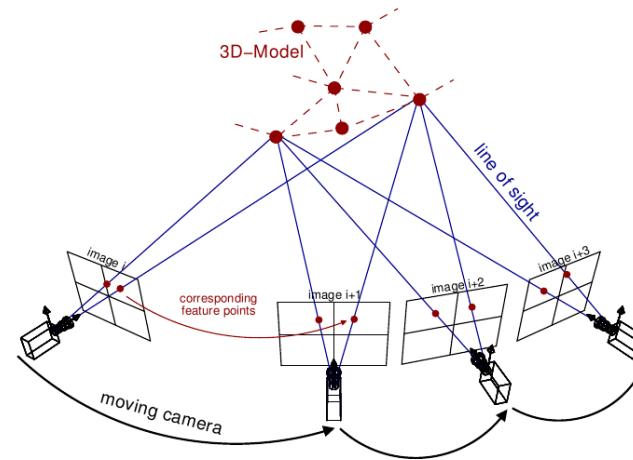


Image from: <http://www.tnt.uni-hannover.de/project/motionestimation>

Notations and Formulation

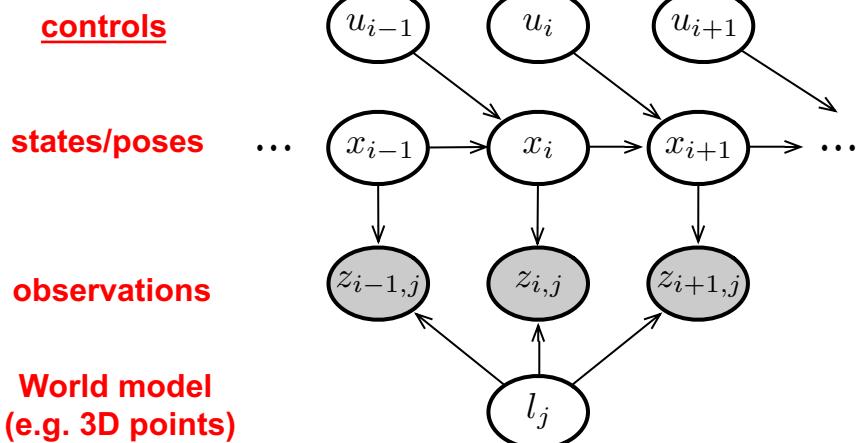
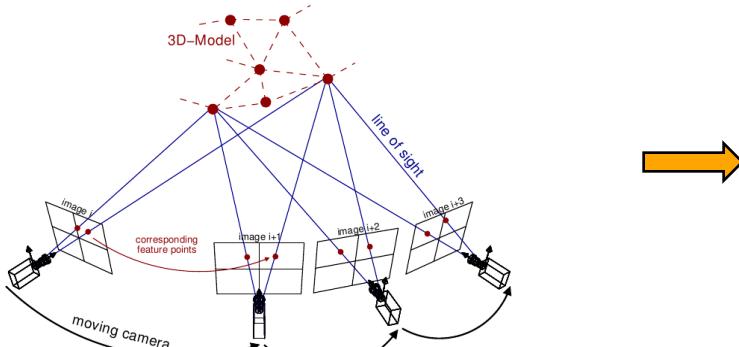
- Joint state vector

$$X_k \doteq \underbrace{\{x_0, \dots, x_k\}}_{\text{Past & current robot states}} \underbrace{L_k}_{\text{Mapped environment}}$$

- Joint probability distribution function $p(X_k | \mathcal{Z}_k, \mathcal{U}_{k-1})$

$$p(X_k | \mathcal{Z}_k, \mathcal{U}_{k-1}) = \text{priors} \cdot \prod_{i=1}^k p(x_i | x_{i-1}, u_{i-1}) p(z_i | X_i^o)$$

General observation model $X_i^o \subseteq X_i$



Notations and Formulation

- Joint state vector

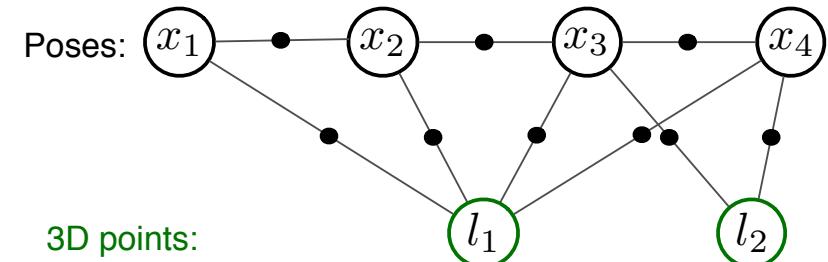
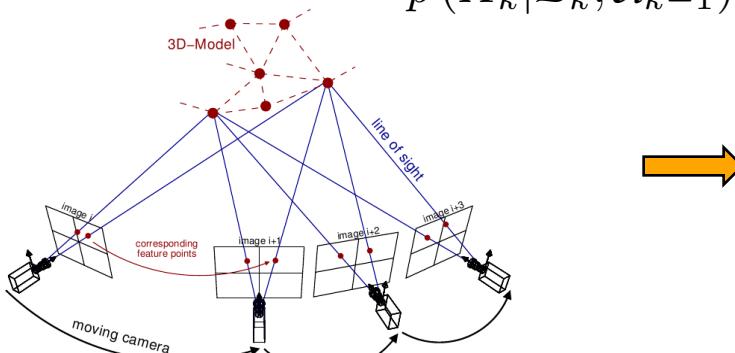
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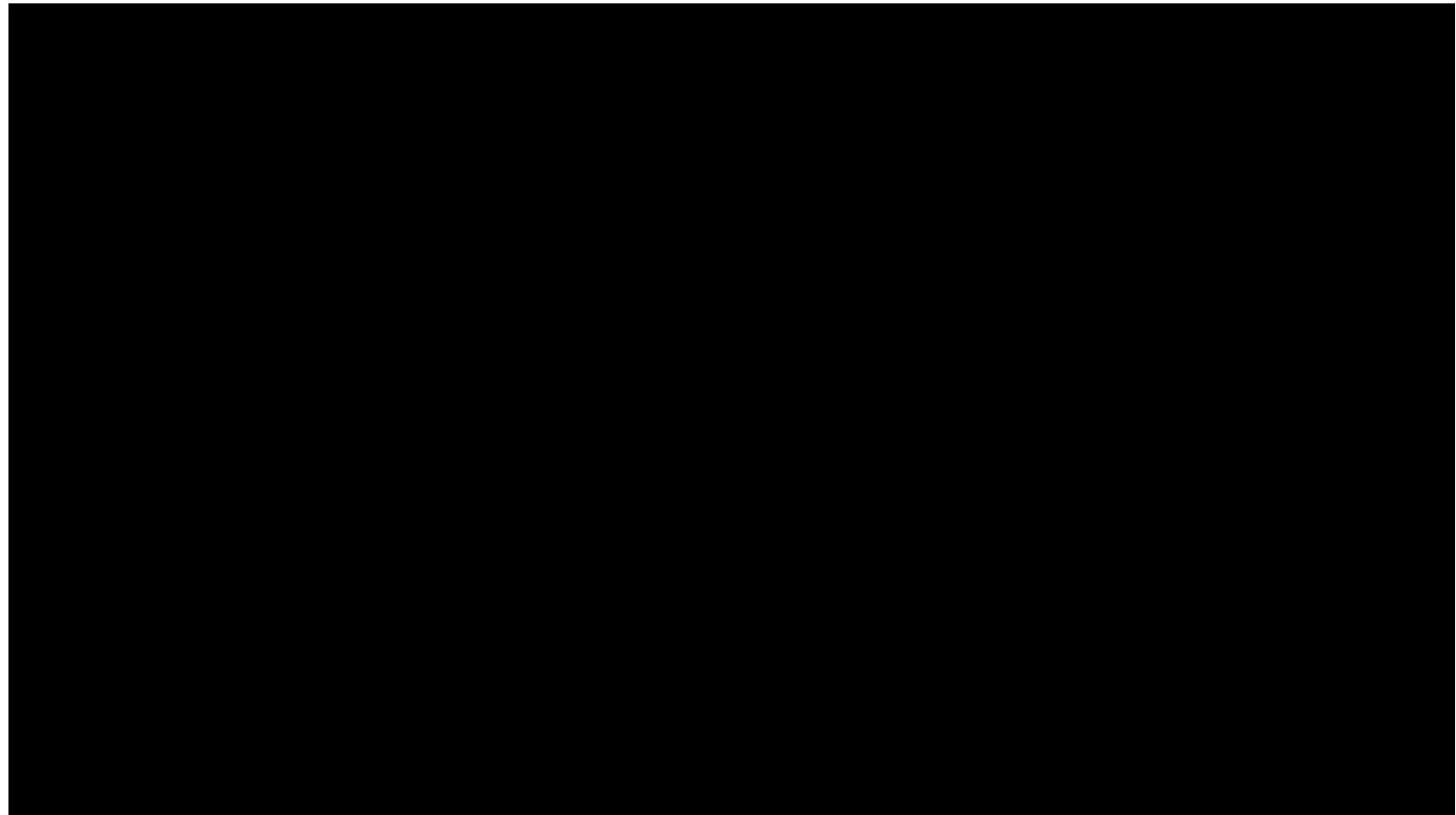
$$p(X_k | \mathcal{Z}_k, \mathcal{U}_{k-1}) = \text{priors} \cdot \prod_{i=1}^k p(x_i | x_{i-1}, u_{i-1}) p(z_i | X_i^o) \quad \text{General observation model } X_i^o \subseteq X_i$$

- Computationally-efficient maximum a posteriori inference e.g. [Kaess et al. 2012]

$$p(X_k | \mathcal{Z}_k, \mathcal{U}_{k-1}) \sim N(X_k^*, \Sigma_k)$$

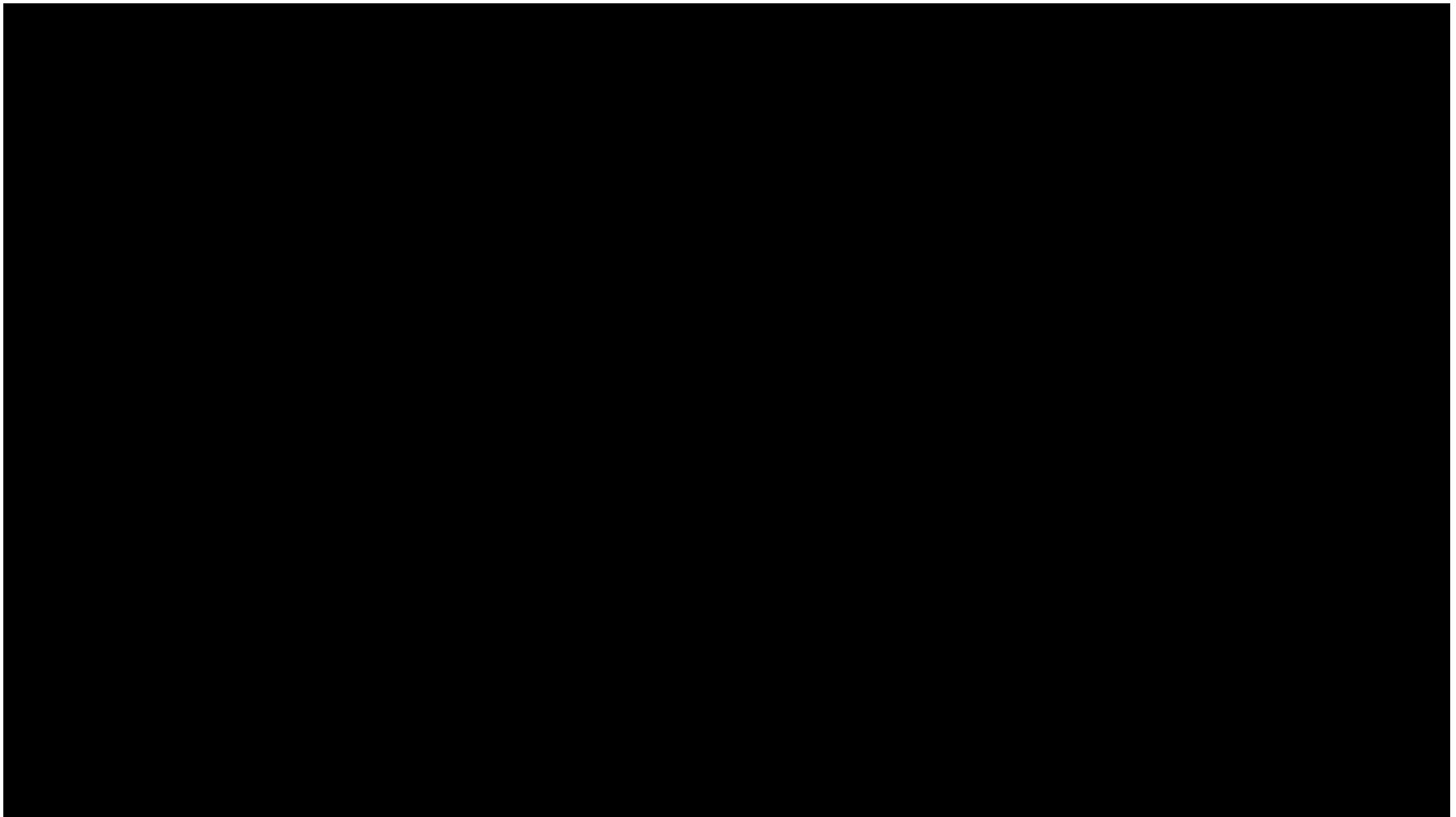


Vision Aided Quadrotor Navigation



MARS Lab, University of Minnesota

RGBD Mapping

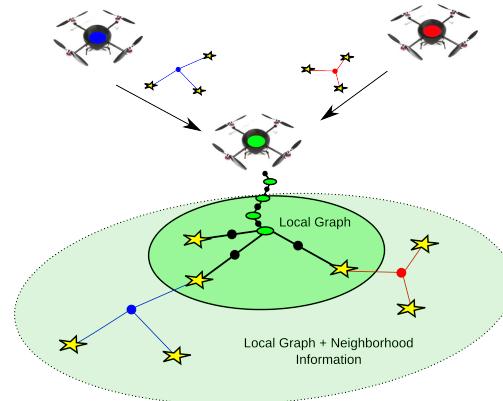
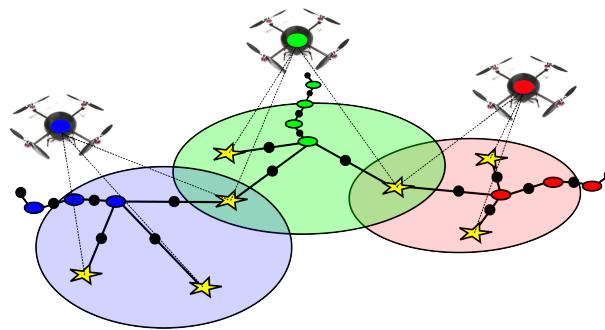


ANPL, Technion

Collaborative Navigation & Mapping

Collaborative Inference & Perception - Why?

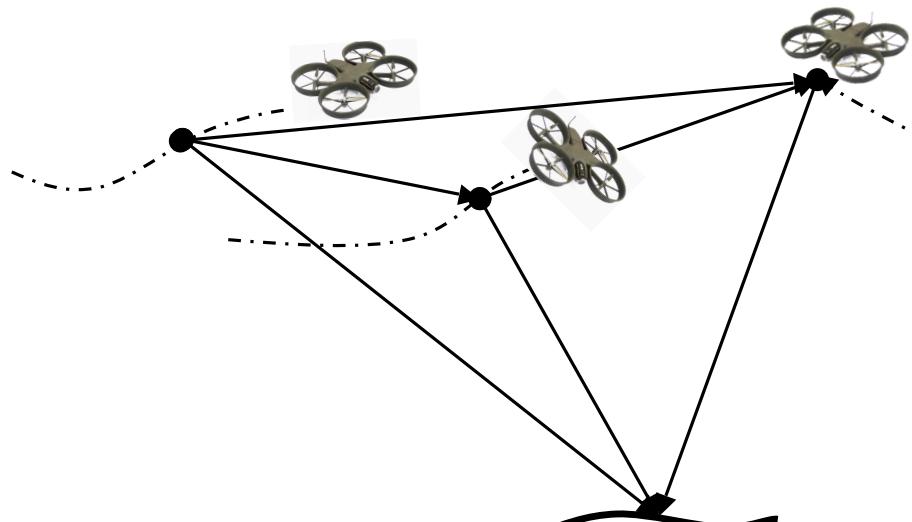
- Key capability:
 - By **sharing information** between robots and formulating **multi-robot constraints**, performance of individuals in the group can be greatly improved
 - Additional advantages, according to application (e.g. mapping - extend sensing horizon)



Images from “DDF-SAM 2.0: Consistent Distributed Smoothing and Mapping”, ICRA, 2013

Distributed Multi-View Geometry

- Exploit mutually observed scenes:
 - Share image observations and appropriate navigation information
 - Distributed information fusion using **multi-view geometry constraints**



[Indelman et al., IJRR 2012]

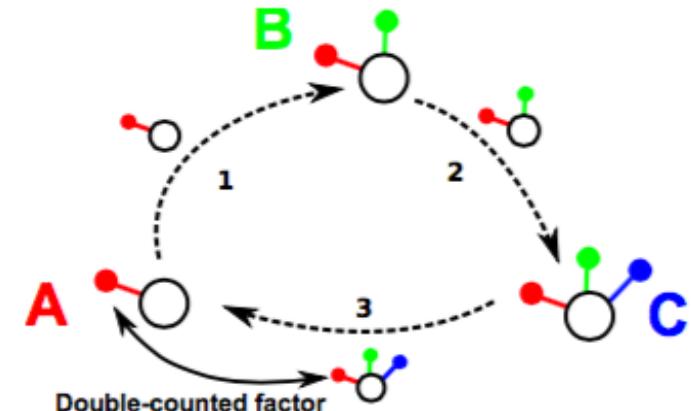
Challenges

- How to guarantee **consistent** information fusion?
- How to determine **data association**?
- How to determine next actions **autonomously & online**?

Consistent Decentralized Estimation

- Intuitive example:

- Consider 3 robots: **A**, **B** and **C**, and a cyclic communication
- Each robot estimates the variable x based on available data
- Assume **A** transmits to **B** message $p(x|Z_A)$
- **B** then passes to **C** the message $p(x|Z_B, Z_A)$
- **C** sends to **A** the message $p(x|Z_C, Z_B, Z_A)$



- If **A** treats $p(x|Z_C, Z_B, Z_A)$ as independent wrt its local belief - it will double count information

Images from “DDF-SAM 2.0: Consistent Distributed Smoothing and Mapping”, ICRA, 2013

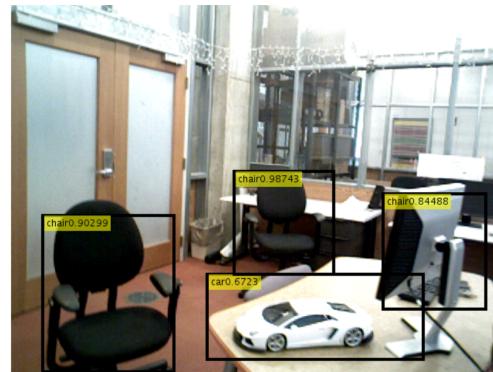
Challenges

- How to guarantee **consistent** information fusion?
- How to determine **data association**?
 - Example: two matched images, same scene?
- How to determine next actions **autonomously & online**?

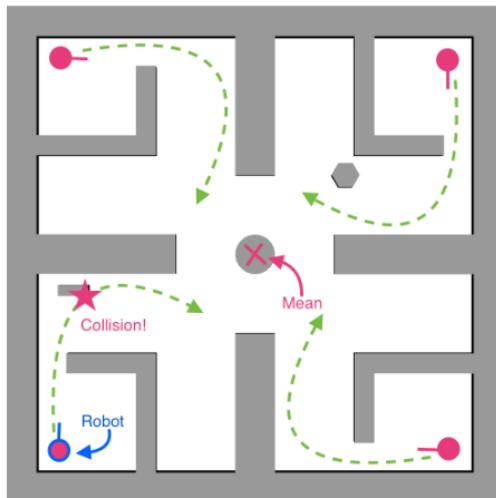
Ambiguous Environments



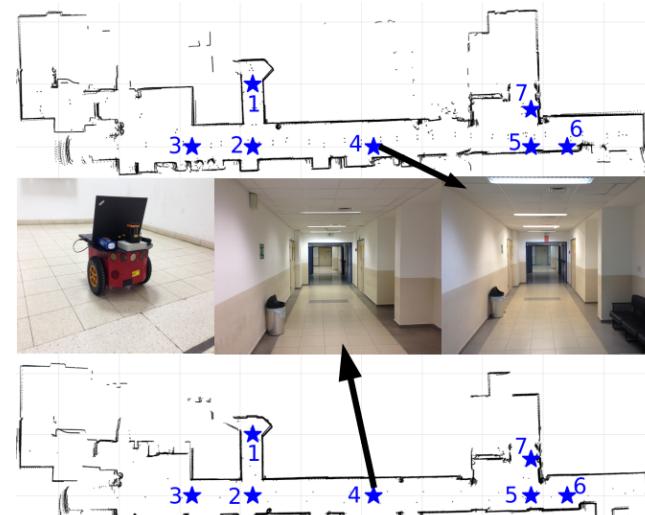
Angeli et al., TRO'08



Mu et al., IROS'16



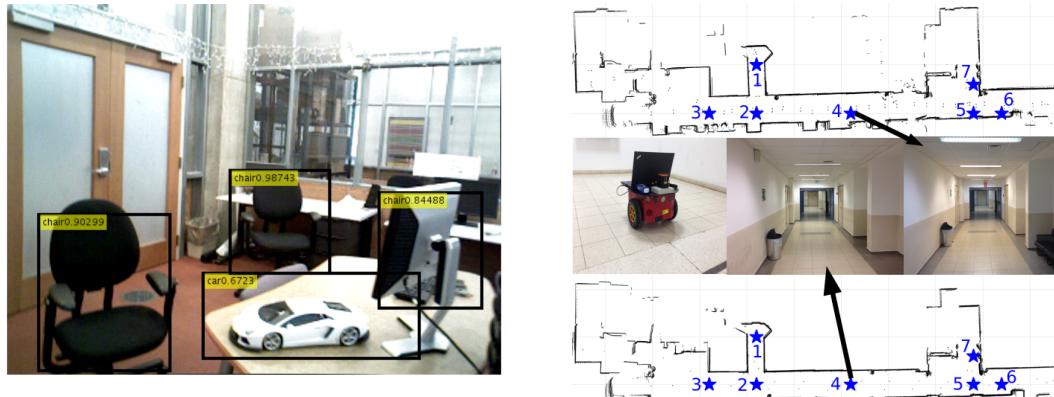
Agarwal et al., arXiv 2015



Pathak et al., arXiv 2016

Ambiguous Environments

- Ambiguity can be due to (combination of):
 - Perceptually aliased scenes (two similar objects)
 - Limited/imperfect sensing (limited sensing range)

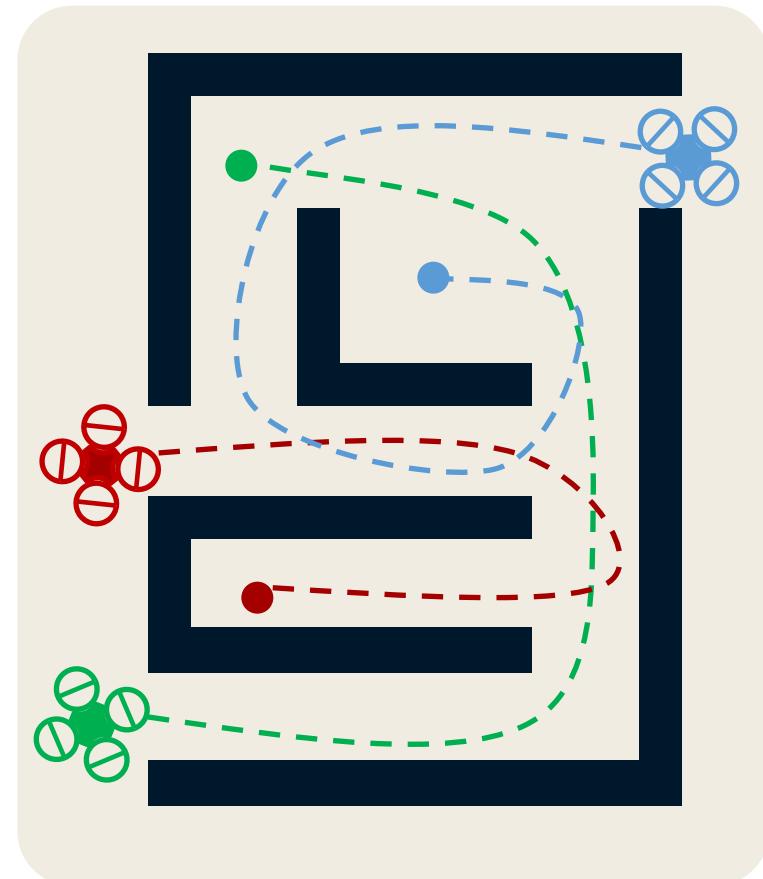


- Data association and SLAM/localization are inherently coupled
- Can we incorporate these aspects within **inference** and **decision making?**

Robust Perception

Possible Application

- Robots scattered in an unknown **perceptually aliased** environment
- Initially **unaware** of each others' location
- How to establish collaboration?
 - **Unknown** multi-robot data association
 - **Unknown** initial relative poses between robots



Robust Collaborative Perception

- Multi-robot collaborative localization and mapping – **distributed, online**
- **Robust perception** (cope with perceptual aliasing)

Distributed Real-time Cooperative Localization and Mapping
using an Uncertainty-Aware Expectation Maximization Approach

Jing Dong, Erik Nelson, Vadim Indelman,
Nathan Michael, Frank Dellaert

Georgia Tech Institute for Robotics
and Intelligent Machines

Carnegie
Mellon
University

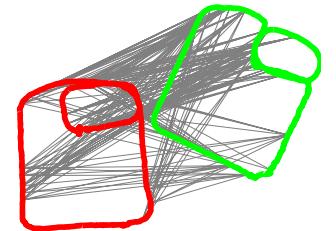
 TECHNION
Israel Institute
of Technology

Probabilistic Formulation

- Notations:
 - \mathcal{F} : Multi-robot correspondences set
 - \mathcal{J} : Latent variables to indicate inliers/outliers
- Joint pdf over robot trajectories and multi-robot data association:

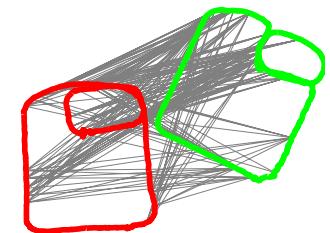
$$p(X, \mathcal{J}|Z) \propto \prod_r p(X^r|Z^r) \prod_{(r_1, r_2, k, l) \in \mathcal{F}} p(j_{k,l}^{r_1, r_2}) p(u_{k,l}^{r_1, r_2} | x_k^{r_1}, x_l^{r_2}, j_{k,l}^{r_1, r_2})$$

Only local measurements Data association Multi-robot measurement likelihood, given data association
 ↑
 Each multi-robot correspondence

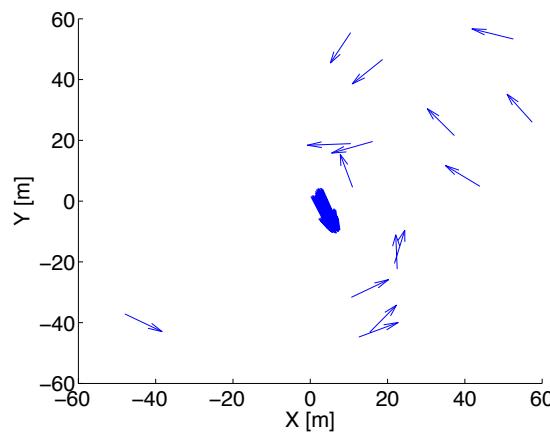


Key Observation

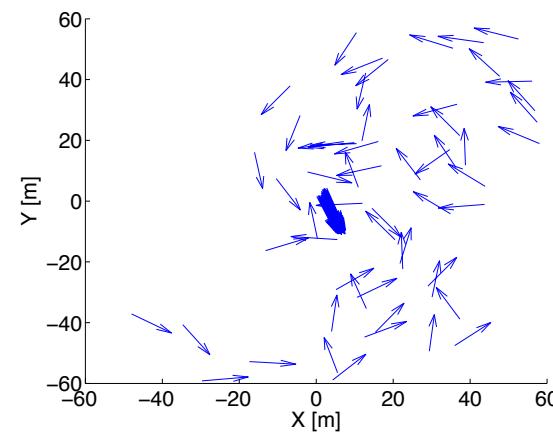
- Given robot local trajectories, relative initial pose can be calculated from **each** candidate multi-robot correspondence
 - Only** inliers produce similar transformations
 - Objective: identify cluster



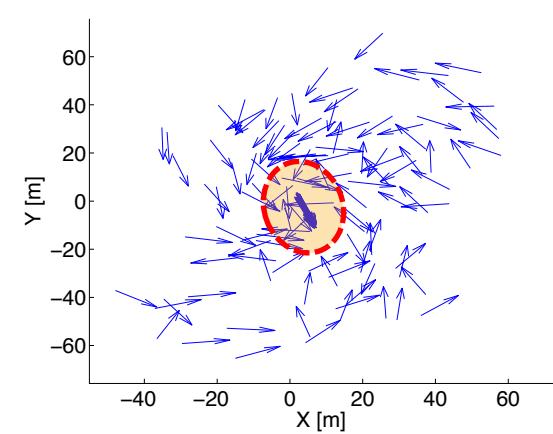
Initial relative pose between two robots (planar case: x, y, θ)
[synthetic data]



10% outliers



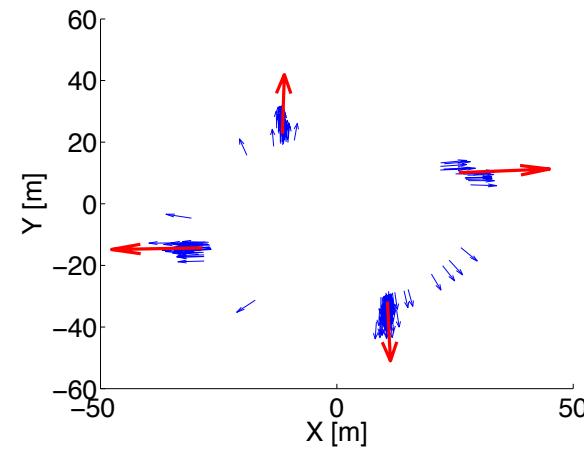
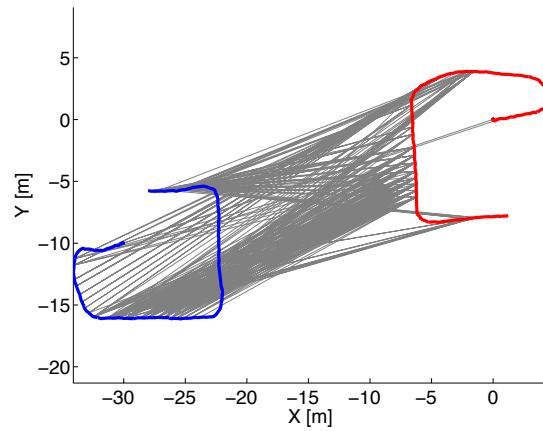
40% outliers



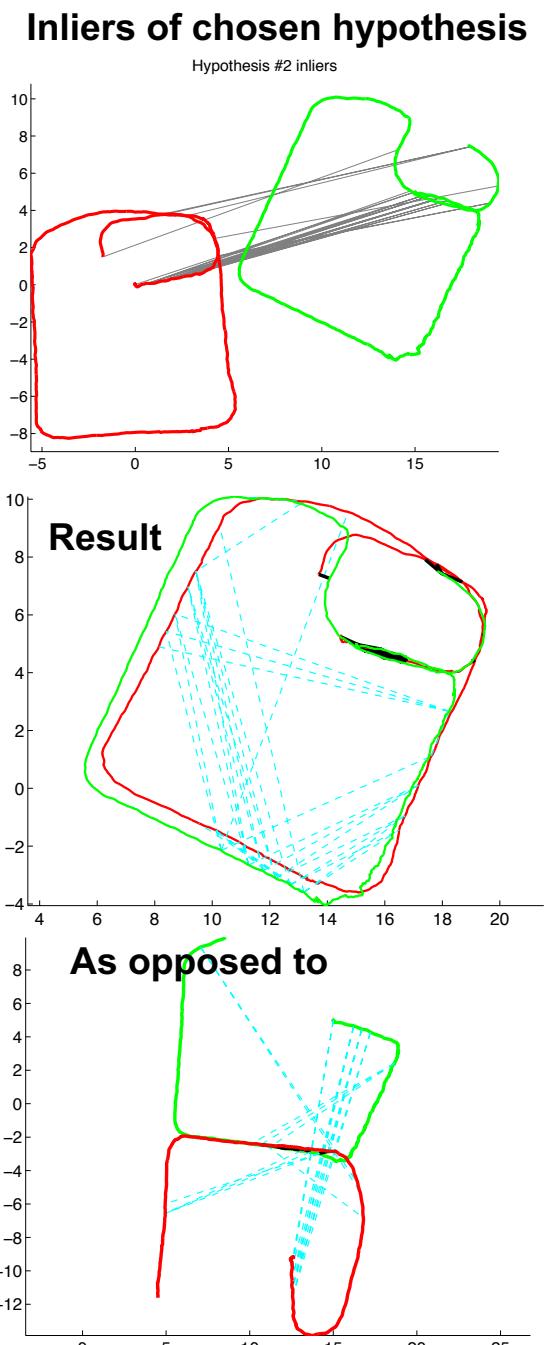
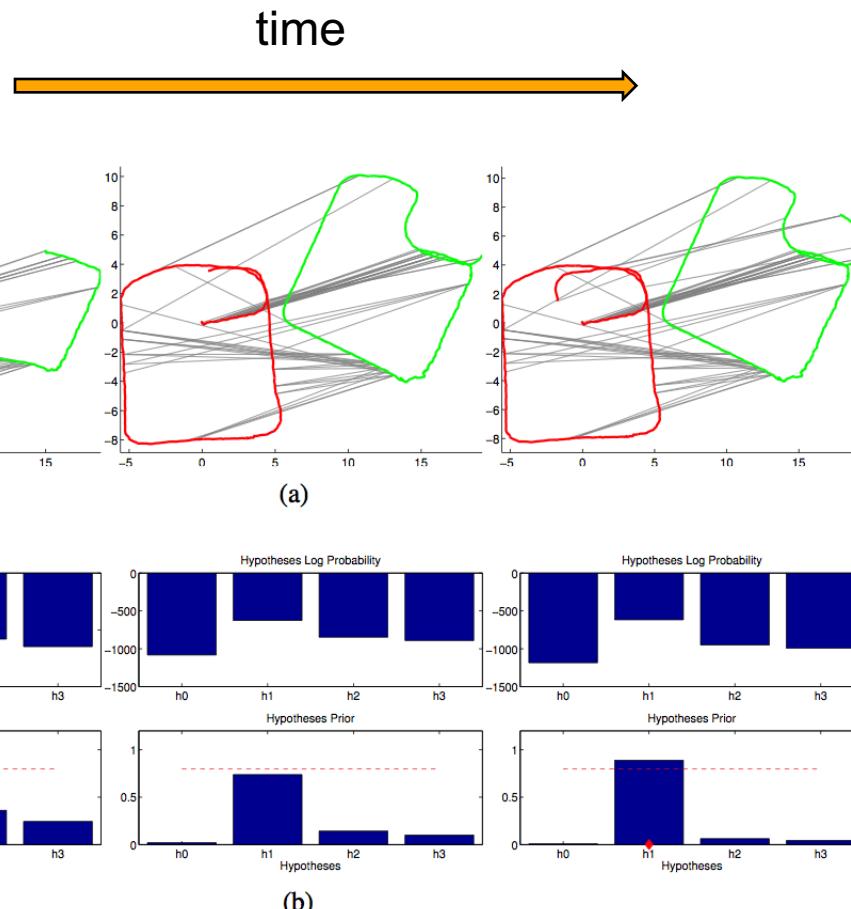
85% outliers

In Presence of Perceptual Aliasing

- Multiple hypotheses/clusters
- Which one to choose?



Incorporating Chinese Restaurant Process



Challenges

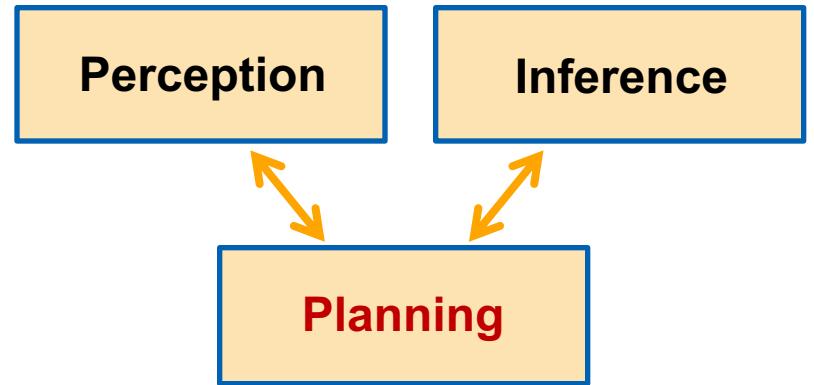
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- How to determine **data association**?
- How to determine next actions **autonomously & online**?

Active Robust Perception - Data Association Aware Belief Space Planning

Planning and Decision Making Under Uncertainty

- Given partial and uncertain knowledge, determine:
 - Next actions, given a task

- Also known as (or related to):
 - Active perception/vision
 - Belief space planning
 - Autonomous navigation



Notations and Formulation

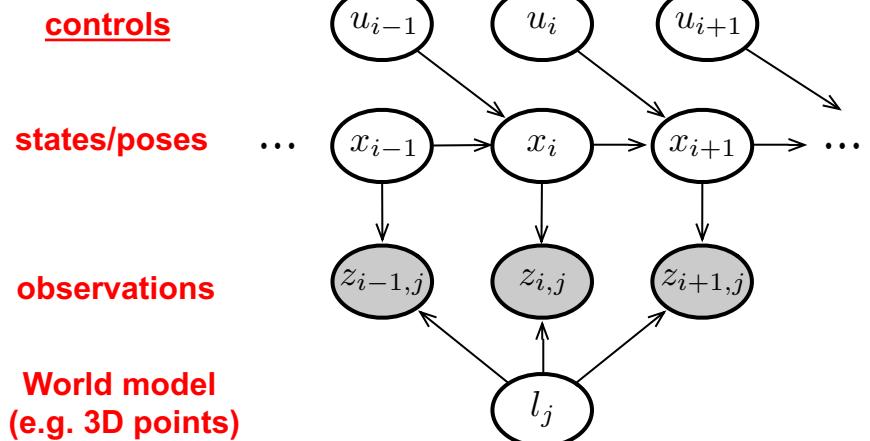
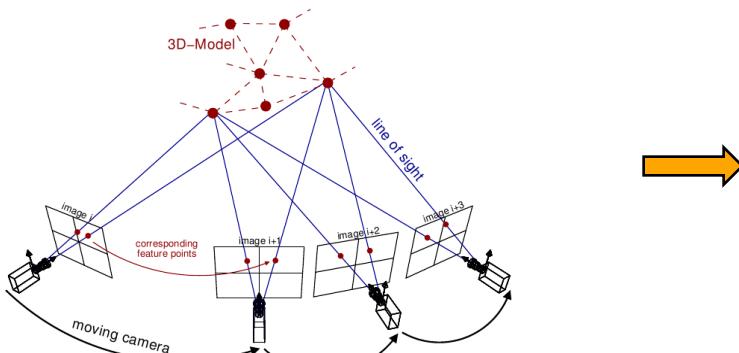
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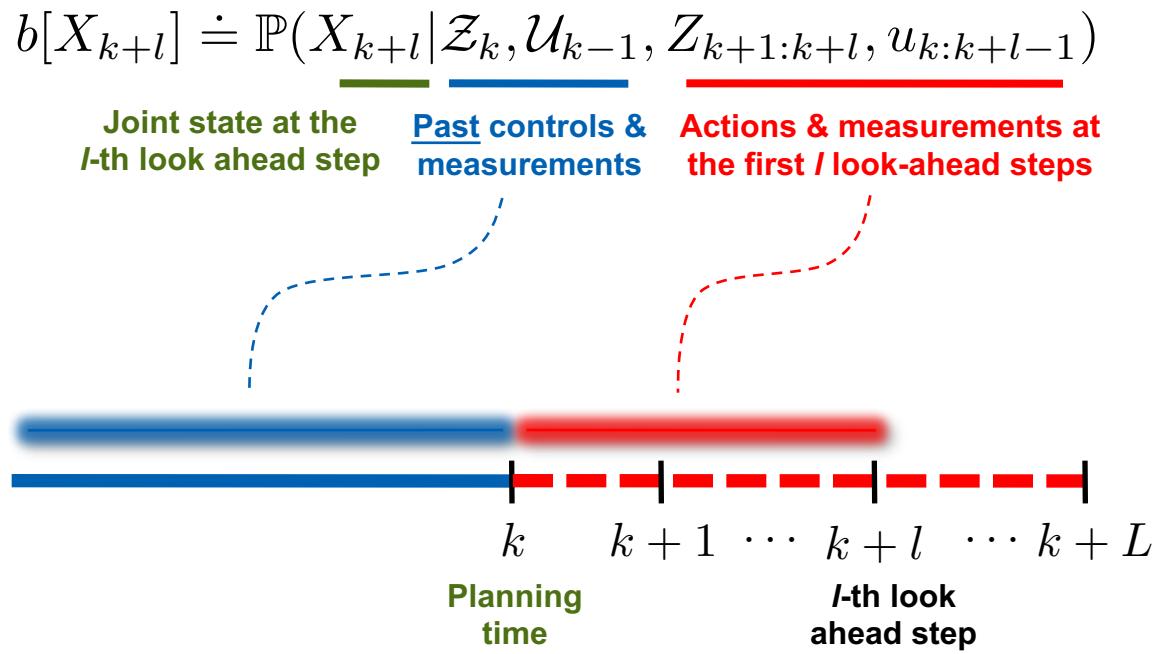
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General observation model $X_i^o \subseteq X_i$



Belief Space Planning

- Belief at the l -th look-ahead step
 - Describes the joint pdf (e.g. robot/camera poses and environment states) at that future time



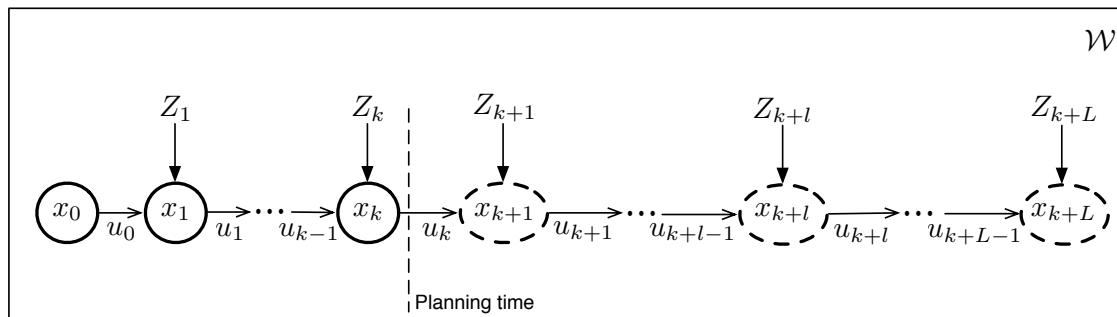
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$$b[X_{k+l}] \doteq \mathbb{P}(X_{k+l} | \mathcal{Z}_k, \mathcal{U}_{k-1}, Z_{k+1:k+l}, u_{k:k+l-1})$$

- Objective function can now involve **uncertainty** aspects

$$J_k(u_{k:k+L-1}) \doteq \mathbb{E}_{Z_{k+1:k+L}} \left\{ \sum_{l=0}^{L-1} c_l(b[X_{k+l}], u_{k+l}) + c_L(b[X_{k+L}]) \right\}$$



Active Robust Perception

- Incorporate data association (DA) aspects within belief space planning
- Can be used for active disambiguation (for example)
- Relax common assumption in belief space planning that DA is given and perfect

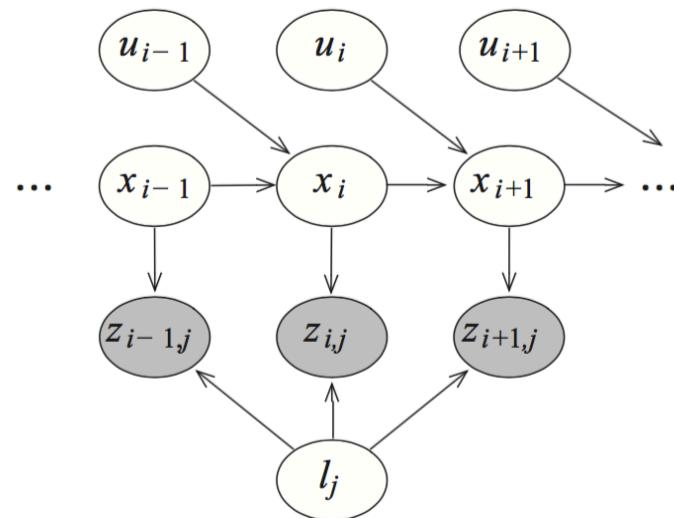
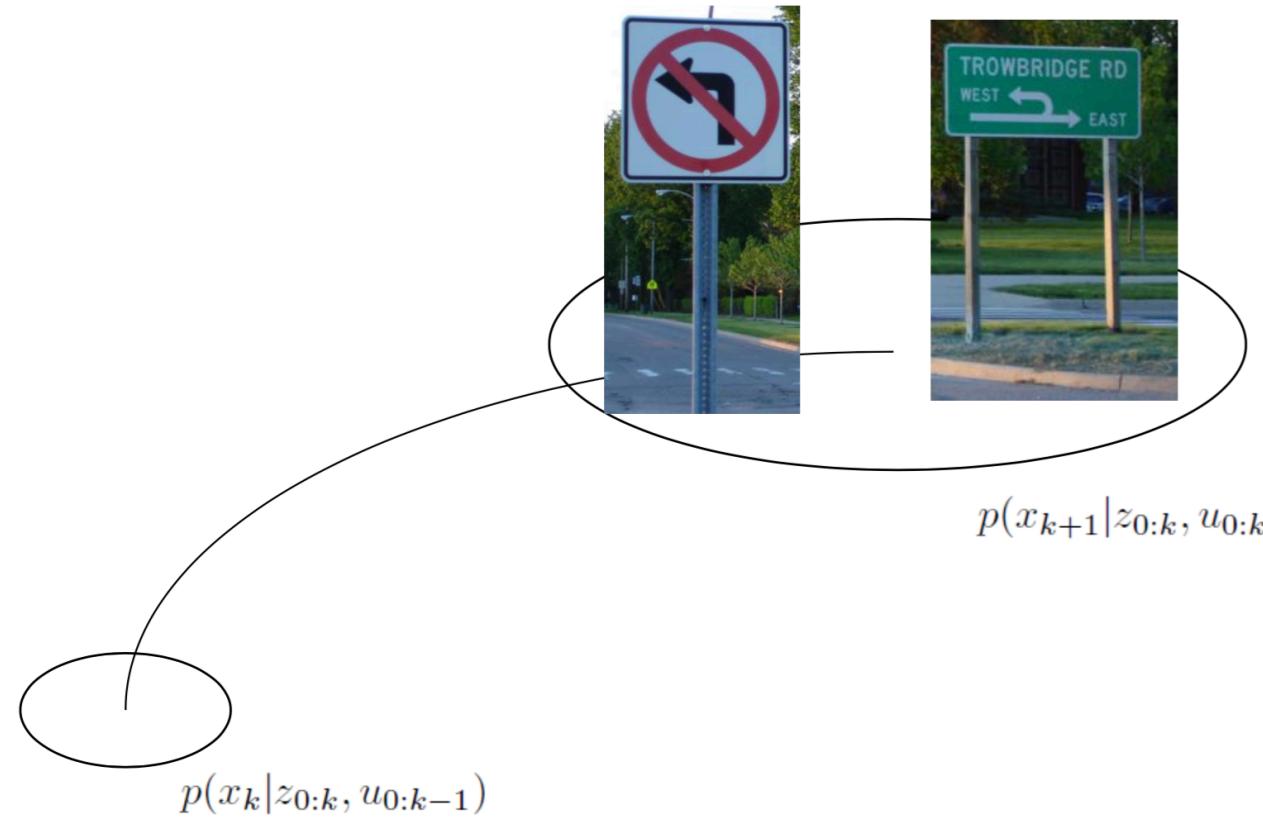


Image from Indelman et al., IJRR'15

Active Robust Perception

- Intuition

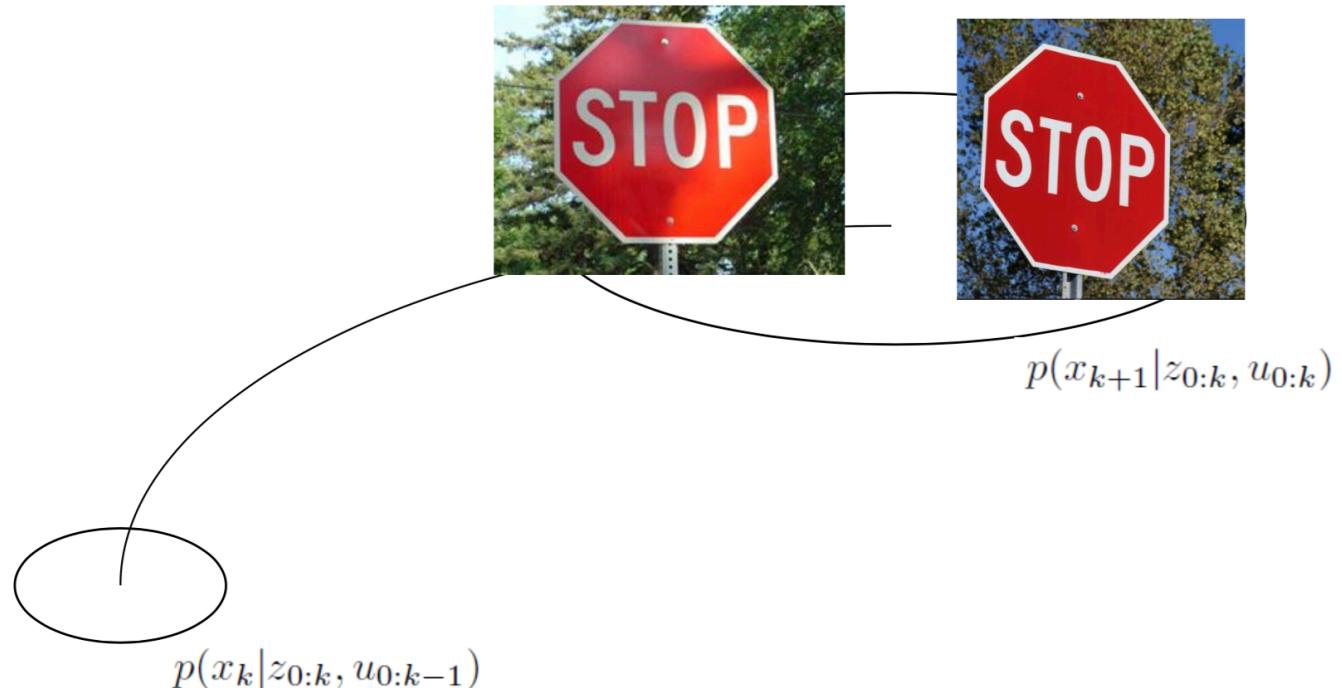
Distinct scenes



Active Robust Perception

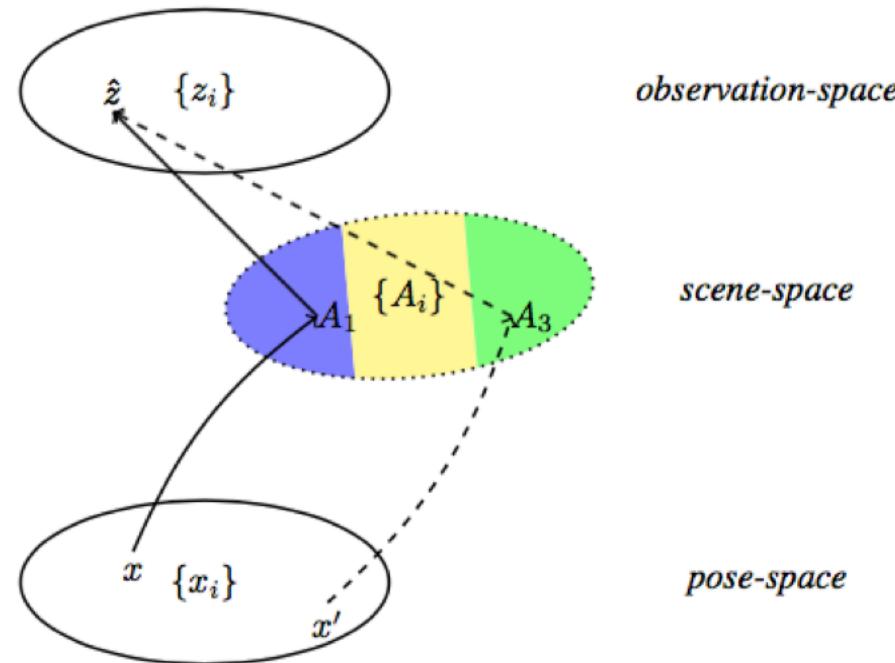
- Intuition

Perceptually aliased scenes



Active Robust Perception

- In presence of perceptual aliasing, the **same observation** could be obtained from **different poses** viewing **different scenes**



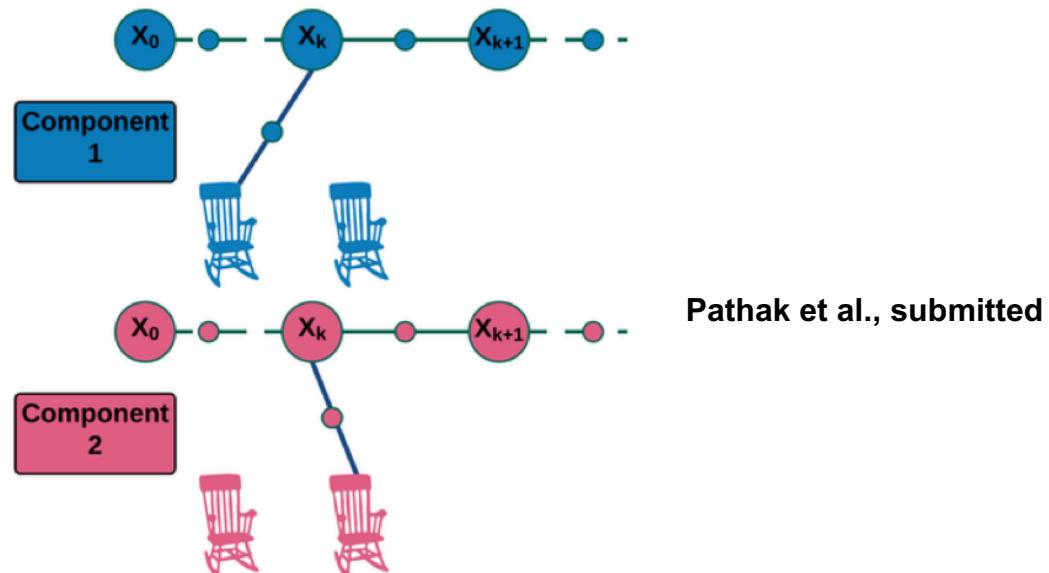
How to capture this fact within belief space planning?

Active Robust Perception

- Belief is represented by a Gaussian Mixture Model (GMM)

$$b[X_k] = \mathbb{P}(X_k | \mathcal{H}_k) = \sum_{j=1}^{M_k} \xi_k^j \mathbb{P}(X_k | \mathcal{H}_k, \gamma = j)$$

Weight Conditional Gaussian,
 represented by a factor graph



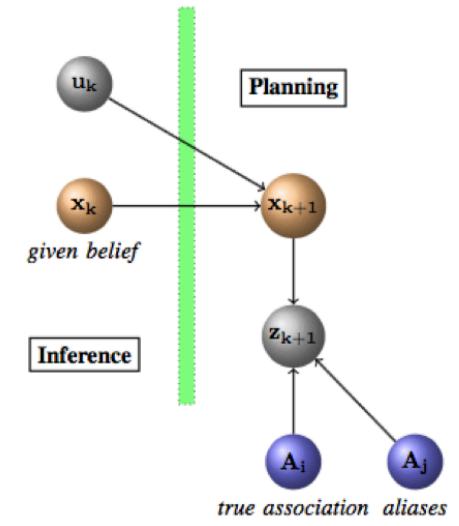
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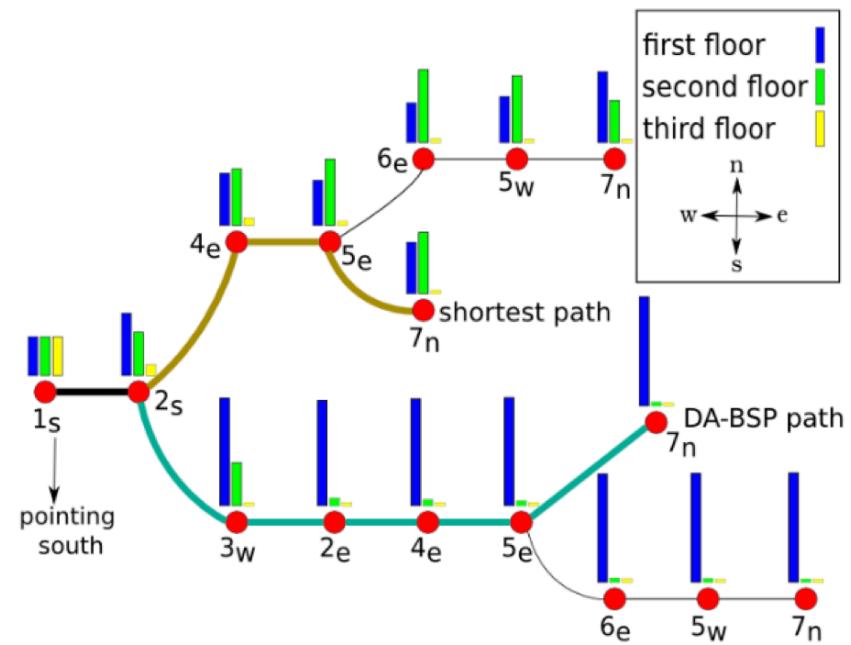
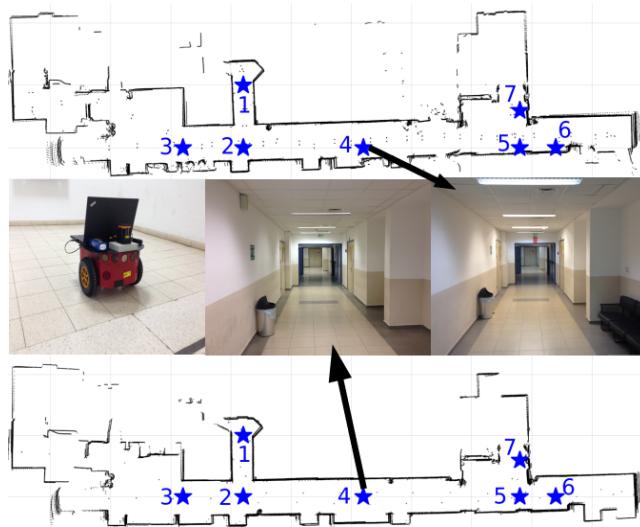
Weight Conditional Gaussian,
 represented by a factor graph

- Main idea:** Reason how GMM belief will evolve for different candidate actions
- Number of modes can go down, and go up (!)



Active Robust Perception

- Multi-floor aliased environment, kidnapped robot problem



Pathak et al., arXiv 2016

Summary

- Autonomous Navigation and Perception
 - Collaborative multi-robot inference
 - Robustness to ambiguity and perceptual aliasing
 - Active robust perception via belief space planning