

# Measurement Simplification in $\rho$ -POMDP with Performance Guarantees

MSc Seminar

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# Outline

- Background
- Approach
  - Reward Bounds
  - Observation Space Partitioning
  - Computational Complexity
  - Gaussian Beliefs
- Results
  - Bounds Analysis
  - Simulation
- Recap

# Motivation

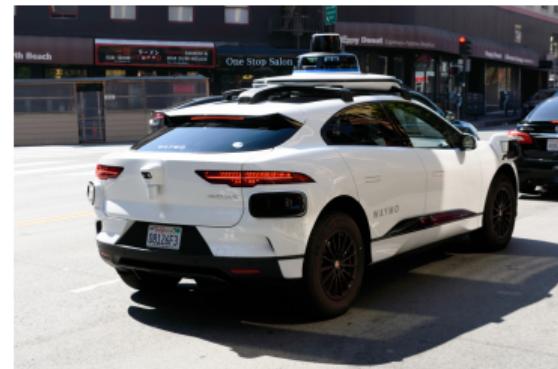
## Decision Making Under Uncertainty



(a) Informative Planning



(b) Autonomous Agents



(c) Reinforcement Learning

# Partially Observable Markov Decision Process

A POMDP formally:  $(\mathcal{X}, \mathcal{A}, \mathcal{Z}, T, O, R)$

- state, action and observation spaces
- transition and observation models
- reward function

# Partially Observable Markov Decision Process

- Markovian transition model, i.e.  $T(X, a, X') = \mathbb{P}(X'|X, a)$
- Each measurement is conditionally independent given the state, i.e.  $O(X, z) = \mathbb{P}(z|X)$
- The reward is a function of the state

# Partially Observable Markov Decision Process

The true state is unknown

- The agent only observes the environment through noisy measurements
- It must maintain a probability distribution over the true state
- $b_k \triangleq b[X_k] = \mathbb{P}(X_k | z_{0:k}, a_{0:k-1}) \triangleq \mathbb{P}(X_k | h_k)$

# POMDP - computational complexity

- Curse of dimensionality
- Curse of history

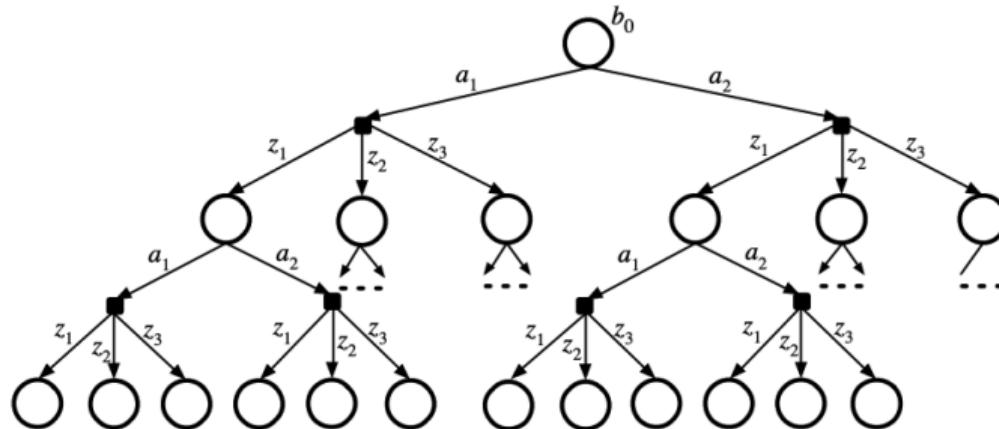
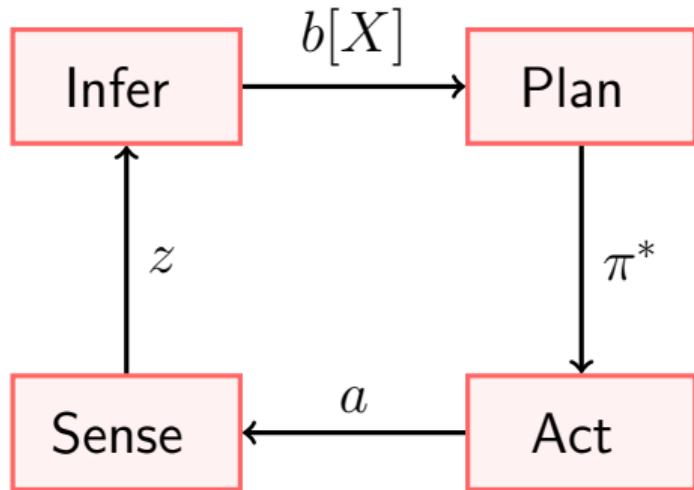
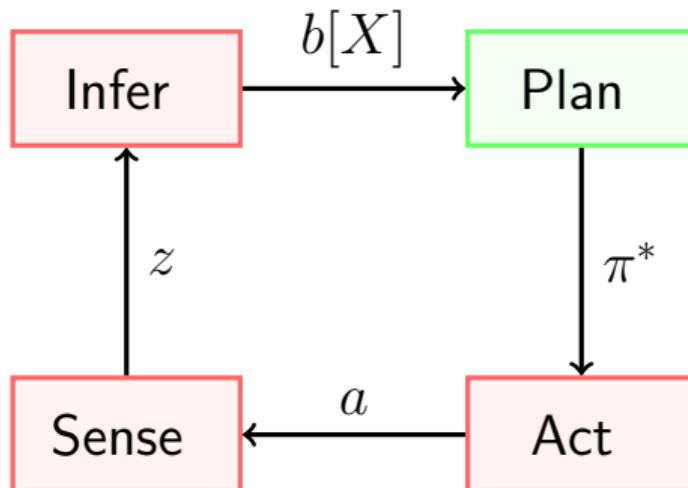


Figure: DESPOT Ye et al 2007

# Plan-act-sense-infer



# Plan-act-sense-infer



# Plan

What is a policy?

- Maps belief states to actions,  $\pi : \mathcal{B} \mapsto A$
- For some finite planning horizon  $\ell$ , the *value* of a policy  $\pi$ :

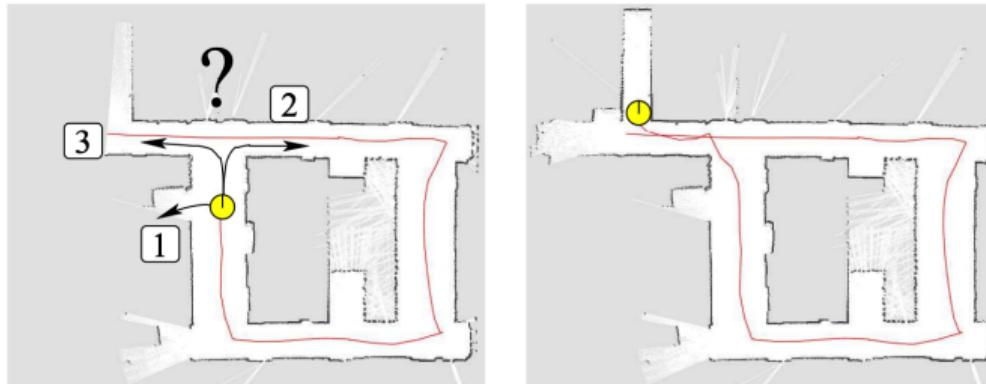
$$V^\pi(b_k) = R(b_k, \pi_k(b_k)) + \mathbb{E}_{z_{k+1:k+\ell}} \left[ \sum_{i=k+1}^{k+\ell} R(b_i, \pi_i(b_i)) \right]$$

# Plan

- Solving a POMDP is equivalent to finding the optimal policy  $\pi^*$  such that the value function is maximized.
- Can replace the optimal policy with the optimal action sequence (open loop)

# $\rho$ -POMDP

- Reasoning about uncertainty is key for planning, AI, Machine Learning
- Quantifying uncertainty allows us to identify actions that reduce it



Stachniss et al. RSS'05

# $\rho$ -POMDP

- Extends the POMDP model to include belief dependent rewards
- $R(b, \pi(b)) \triangleq -\mathcal{H}(X) \equiv \mathbb{E}_{X \sim b} (\log b[X])$
- If both  $X, Z$ , are treated as random variables, the expected reward becomes the conditional entropy of these random variables

# $\rho$ -POMDP

- $\mathbb{E}_Z[R(b)] = -\mathcal{H}(X \mid Z) = -\mathbb{E}_Z[\mathcal{H}(X \mid Z = z)]$
- The expected reward at each  $i$ th look ahead step:  
$$\mathbb{E}_{Z_{k+1:i}}[R(b_i, a_{i-1})] = -\mathcal{H}(X_i \mid Z_{k+1:i})$$
- Future observations are drawn from the distribution  
 $\mathbb{P}(Z_{k+1:i} \mid b_k, \pi)$  and  $i \in [k + 1, k + \ell]$

# Related Work

- POMDP online solvers
  - ▶ Sunberg and Kochenderfer - ICAPS'18
  - ▶ Ye et al. - JAIR'17
- Simplification in inference
  - ▶ Khosoussi et al. - WAFR'20
  - ▶ Zhang and Vela - CCVP'15
  - ▶ Carlevaris-Bianco, Kaess and Eustice - TRO'14
- Simplification in planning
  - ▶ Zhitnikov and Indelman - AI'22
  - ▶ Elimelech and Indelman - IJRR'22

# Contributions

- Novel observation space partitioning
- Analytical bounds on the expected reward, as function of partitioned space, that hold for all families of belief distributions.
- Partition tree that allows greater efficiency as we go down its hierarchy.
- Bounds that are adaptive and converge to the original solution.
- Hierarchy of efficient implementations for Gaussian beliefs

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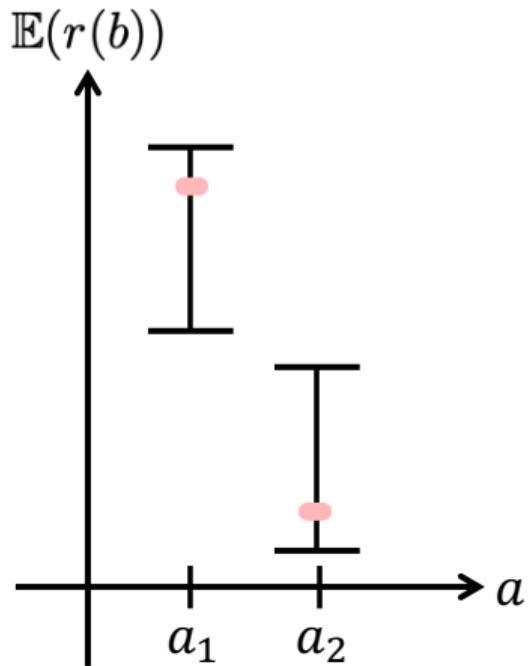
# Approach - simplification

- To choose the optimal action from a pool of candidate actions - need to evaluate the reward function for each action.
- Instead, one can evaluate bounds on the expected reward function as a proxy

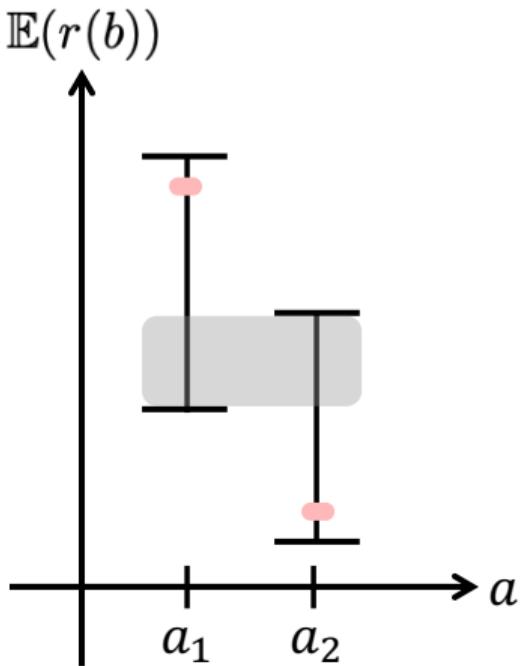
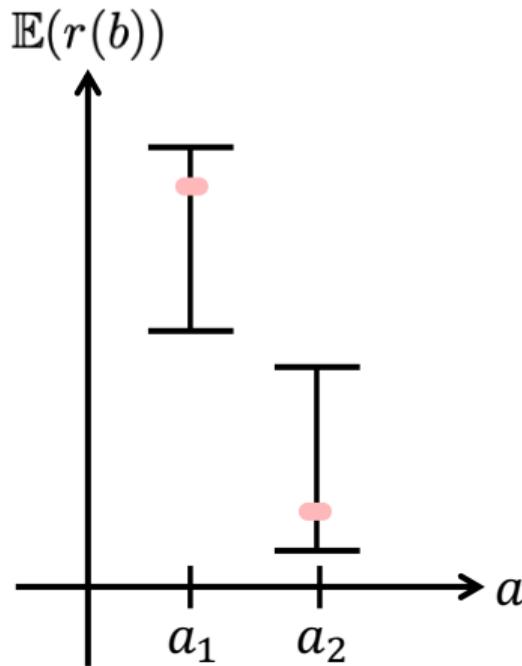
$$\mathcal{LB}_i \leq \mathbb{E}_{Z_{k:i}}(R(b_i)) \leq \mathcal{UB}_i$$

$$\sum_{i=k+1}^{k+\ell} \mathcal{LB}_i \leq J(b_k, a_{k:k+\ell-1}) \leq \sum_{i=k+1}^{k+\ell} \mathcal{UB}_i$$

# Approach - reward bounds



# Approach - reward bounds overlap



# Multivariate Observation Space

- Consider a multivariate random variable  $Z \in \mathcal{Z}$ , that represents future observations:

$$Z = (Z^1, Z^2, \dots, Z^m)$$

- $Z^i$  is a random variable defined by a given sensing modality, and  $m$  is the number of such random variables

# Multivariate Observation Space

For example, raw measurement of an image sensor

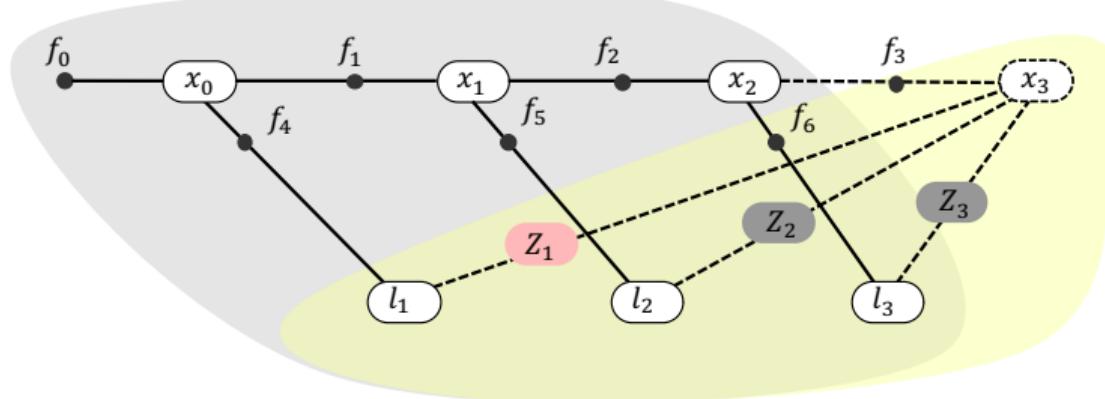


157	153	174	168	160	152	129	161	172	161	155	156
155	182	163	74	75	62	33	17	110	210	180	154
180	180	50	14	34	6	10	33	48	106	159	181
206	109	5	124	181	111	120	204	166	15	56	180
194	68	137	251	237	239	239	228	227	87	71	201
172	106	207	233	233	214	220	239	228	98	74	206
188	88	179	209	185	215	211	158	139	75	20	169
189	97	165	84	10	168	134	11	31	62	22	148
199	168	191	193	158	227	178	143	182	106	36	190
205	174	155	252	236	231	149	178	228	43	95	234
190	216	116	149	236	187	85	150	79	38	218	241
190	224	147	108	227	210	127	102	36	101	255	224
190	214	173	66	103	143	95	50	2	109	249	215
187	196	236	75	1	81	47	0	6	217	255	211
183	202	237	145	0	0	12	108	200	138	243	236
195	206	123	207	177	121	123	200	175	13	96	218

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# Multivariate Observation Space

Or a factor graph



# Partitioning of Multivariate Observation Space

- Consider the partitioning  $Z^s \in \mathcal{Z}^s$  and  $Z^{\bar{s}} \in \mathcal{Z}^{\bar{s}}$ , such that:

$$Z^s = \{Z^1, Z^2, \dots, Z^n\}$$

$$Z^{\bar{s}} = \{Z^{n+1}, Z^{n+2}, \dots, Z^m\}$$

- $\mathcal{Z} = \mathcal{Z}^s \oplus \mathcal{Z}^{\bar{s}}$  (addition of subspaces)

# Partitioning of Multivariate Observation Space

But why is this a good idea?

- Apply partitioning to a raw image measurement of size  $20 \times 20$  binary pixels.
- Each pixel is represented by a random variable  $Z^{x,y} \in \{0, 1\}$ , and  $Z \in \mathcal{Z} \subseteq (\mathbb{F}_2)^{400}$ .

# Partitioning of Multivariate Observation Space

But why is this a good idea?

- Consider all of the different permutations for each pixel,  $2^{400}$  in total, which defines  $|\mathcal{Z}|$ .
- If we partition  $Z^s \triangleq \{Z^{x,y} \mid y \leq 10\}$  and  $Z^{\bar{s}} \triangleq \{Z^{x,y} \mid y > 10\}$ , we need only to consider  $2^{200}$  permutations for each random variable.
- $2^{201}$  vs  $2^{400}$

# The Big Picture

- Planning involves thinking about future observations (and actions), and evaluating a reward function
- This process is computationally expensive
- Partitioning the observation space makes this less expensive

# Bounds on Expected Reward

$$\mathcal{LB} \leq \mathcal{H}(X|Z) \leq \mathcal{UB}$$

$$\mathcal{LB} \triangleq \mathcal{H}(Z^s \mid X) + \mathcal{H}(Z^{\bar{s}}|X) - \mathcal{H}(Z^s) - \mathcal{H}(Z^{\bar{s}}) + \mathcal{H}(X)$$

$$\mathcal{UB} \triangleq \mathcal{H}(Z^s|X) + \mathcal{H}(X) - \mathcal{H}(Z^s)$$

# Bounds on Expected Reward

## Lemma 1

*The conditional Entropy can be factorized as*

$$\mathcal{H}(X|Z) = \mathcal{H}(Z|X) + \mathcal{H}(X) - \mathcal{H}(Z)$$

# Bounds on Expected Reward

## Theorem 1

*The conditional Entropy can be bounded from above by*

$$\mathcal{H}(X|Z) \leq \mathcal{UB} \triangleq \mathcal{H}(Z^s|X) + \mathcal{H}(X) - \mathcal{H}(Z^s)$$

## Proof.

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## Proof.

- $\mathcal{H}(X|Z^s) - \mathcal{H}(X|Z) = \mathcal{I}(X|Z^s; Z \setminus Z^s)$

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# Bounds on Expected Reward

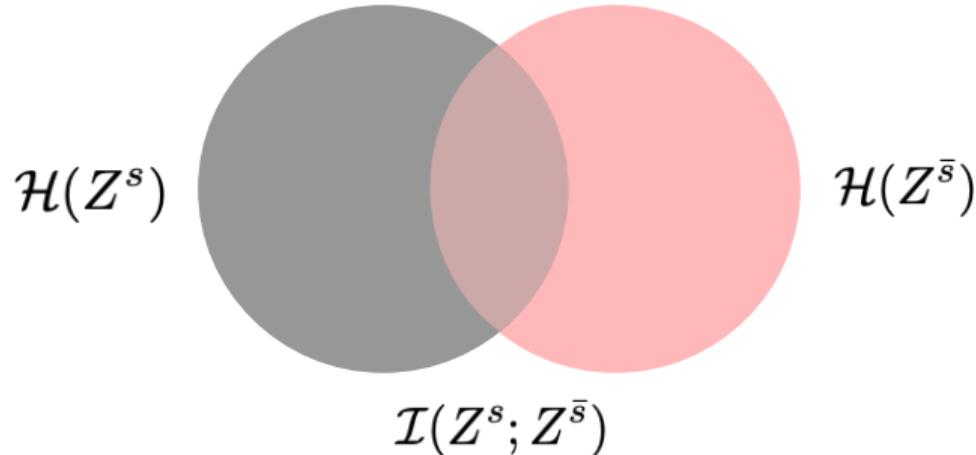
## Lemma 2

*Given two sets of expected measurements  $(Z^s, Z^{\bar{s}})$ , the conditional Entropy can be factorized as*

$$\mathcal{H}(X|Z) = \mathcal{H}(Z^s|X) + \mathcal{H}(Z^{\bar{s}}|X) - \mathcal{H}(Z^s, Z^{\bar{s}}) + \mathcal{H}(X)$$

# Bounds on Expected Reward

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# Bounds on Expected Reward

## Theorem 2

*The conditional Entropy can be bounded from below by:*

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- Plug-in to lemma 3

# Bounds on Expected Reward

$$\mathcal{LB} \leq \mathcal{H}(X|Z) \leq \mathcal{UB}$$

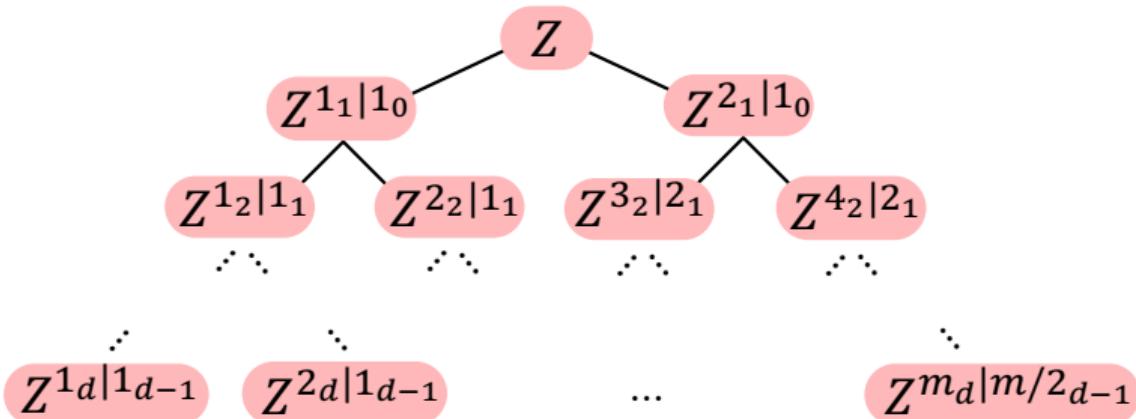
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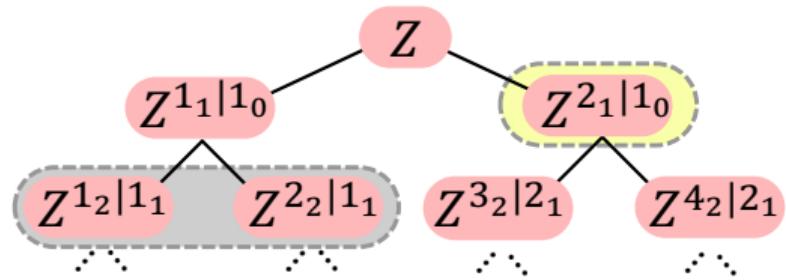
# Hierarchical Partitioning

Can we simplify further?

- Unique encoding denoted as  $Z^{n_i|m_j}$ ,  $n$  is the node number at the  $i$ th partitioning level,  $m$  is the node number at the parent partitioning level  $j$



# Bounds with Hierarchical Partitioning



# Computational Complexity

## Lemma 2

*Given two sets of expected measurements  $(Z^s, Z^{\bar{s}})$ , the conditional Entropy can be factorized as*

$$\mathcal{H}(X|Z) = \mathcal{H}(Z^s|X) + \mathcal{H}(Z^{\bar{s}}|X) - \mathcal{H}(Z^s, Z^{\bar{s}}) + \mathcal{H}(X)$$

# Computational Complexity

- Baseline Expected Reward

$$\mathcal{H}(X|Z)$$

Using lemma 2:

$$\mathcal{H}(Z^s|X), \mathcal{H}(Z^{\bar{s}}|X), \mathcal{H}(X), \mathcal{H}(Z^s, Z^{\bar{s}})$$

# Computational Complexity

- Baseline Expected Reward

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- Expected Reward Bounds

$$\mathcal{H}(Z^s|X), \mathcal{H}(Z^{\bar{s}}|X), \mathcal{H}(Z^{\bar{s}}), \mathcal{H}(Z^s), \mathcal{H}(X)$$

# Computational Complexity

- Baseline Expected Reward

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- Expected Reward Bounds

$$\mathcal{H}(Z^s|X), \mathcal{H}(Z^{\bar{s}}|X), \mathcal{H}(Z^{\bar{s}}), \mathcal{H}(Z^s), \mathcal{H}(X)$$

# Computational Complexity

$$\mathcal{H}(Z^s, Z^{\bar{s}}) \text{ vs. } \mathcal{H}(Z^{\bar{s}}), \mathcal{H}(Z^s)$$

- $\mathcal{H}(Z^s, Z^{\bar{s}}) = - \int_{Z^s} \int_{Z^{\bar{s}}} \mathbb{P}(Z^s, Z^{\bar{s}}) \log \mathbb{P}(Z^s, Z^{\bar{s}}) dZ^s dZ^{\bar{s}}$
- $\mathcal{H}(Z^s) = - \int_{Z^s} \mathbb{P}(Z^s) \log \mathbb{P}(Z^s) dZ^s$
- $\mathcal{H}(Z^{\bar{s}}) = - \int_{Z^{\bar{s}}} \mathbb{P}(Z^{\bar{s}}) \log \mathbb{P}(Z^{\bar{s}}) dZ^{\bar{s}}$

# Computational Complexity

$$\mathcal{H}(Z^s, Z^{\bar{s}}) \text{ vs. } \mathcal{H}(Z^{\bar{s}}), \mathcal{H}(Z^s)$$

- $O(|\mathcal{Z}^s||\mathcal{Z}^{\bar{s}}|)$
- $O(|\mathcal{Z}^s| + |\mathcal{Z}^{\bar{s}}|)$
- Same logic applies to the hierarchical partitions

# Gaussian Belief - preliminaries

$b[X] \sim \mathcal{N}(\mu, \Sigma)$ , with mean  $\mu \in \mathbb{R}^N$  and covariance matrix  $\Sigma \in \mathbb{R}^{N \times N}$

- $\Sigma_{k+1}^{-1} = \Lambda_{k+1}$
  - $\Lambda_{k+i} \triangleq \Lambda_k^{\text{Aug}} + A_{k+1:k+i}^T \cdot A_{k+1:k+i}$

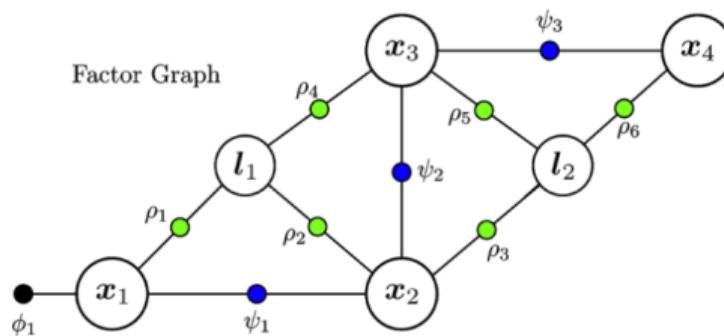


Figure: Caesar.jl'21

$$A = \begin{bmatrix} l_1 & l_2 & x_1 & x_2 & x_3 & x_4 \\ X & & X & & & \\ X & & & X & & \\ X & & & & X & \\ & X & & X & & \\ & X & & & X & \\ & X & & & & X \\ A = & & X & & X & \\ & & X & X & X & \\ & & & X & X & X \\ & & & & X & X \end{bmatrix} \begin{array}{l} \rho_1 \\ \rho_2 \\ \rho_4 \\ \rho_3 \\ \rho_5 \\ \rho_6 \\ \phi_1 \\ \psi_1 \\ \psi_2 \\ \psi_3 \end{array}$$

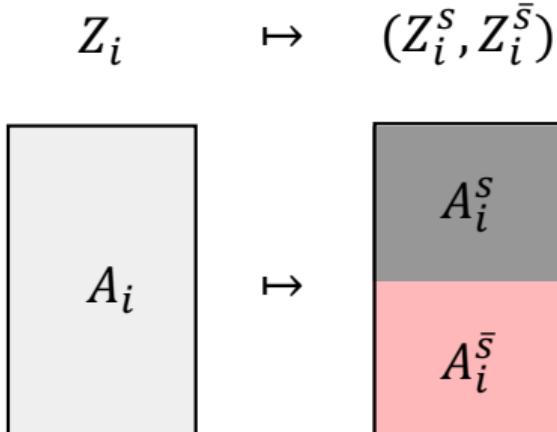
# Gaussian Belief - preliminaries

$$b[X] \sim \mathcal{N}(\mu, \Sigma)$$

- $\mathcal{H}(X_{k+1}) = \frac{1}{2}(N \ln(2\pi e) - \ln |\Lambda_{k+1}|)$
- $\mathbb{E}_{Z_{k+1:i}} [\mathcal{H}(X_i|h_i)] = C - \frac{1}{2} \mathbb{E}_{Z_{k+1:i}} [\ln |\Lambda_k^{\text{Aug}} + A_i(z)^T A_i(z)|]$
- $C = N \ln(2\pi e)$

# Partitioning of Gaussian Belief

- $\Lambda_i = \Lambda_k^{\text{Aug}} + A_i^T A_i$
- Observation partitioning corresponds to splitting the Jacobian into blocks



# Gaussian Bounds

$$f(\Lambda, A) \triangleq |\Lambda + A^T A|$$

$$\mathcal{LB} = C - \frac{1}{2} \mathbb{E}_{Z_{k+1:i}} \left[ \ln \frac{f\left(\Lambda_k^{\text{AUG}-}, A_i^s\right) \cdot f\left(\Lambda_k^{\text{AUG}-}, A_i^{\bar{s}}\right)}{|\Lambda_k^{\text{AUG}-}|} \right]$$

$$\mathcal{UB} = C - \frac{1}{2} \mathbb{E}_{Z_{k+1:i}} \left[ \ln f\left(\Lambda_k^{\text{AUG}-}, A_i^s\right) \right]$$

# Estimation of Expected Entropy

Assumption - the measurement Jacobian is not a function of  $Z$

$$\mathcal{H}(X_i|Z_{k+1:i}) = C - \frac{1}{2}(\ln f(\Lambda_k^{\text{AUG}-}, A_i)) \rightarrow$$

$$\mathcal{LB} = C - \frac{1}{2}\ln \frac{f(\Lambda_k^{\text{AUG}-}, A_i^s) \cdot f(\Lambda_k^{\text{AUG}-}, A_i^{\bar{s}})}{|\Lambda_k^{\text{AUG}-}|}$$

$$\mathcal{UB} = C - \frac{1}{2}\ln f(\Lambda_k^{\text{AUG}-}, A_i^s)$$

# Methods for Determinant Calculation

Need to evaluate  $f(\Lambda_k^{\text{AUG}-}, A_i^s), f(\Lambda_k^{\text{AUG}-}, A_i^{\bar{s}})$

- Baseline:

$$|\Lambda + A^T A|$$

- Square root form:

$$|R^T R|$$

- rAMDL:

$$|\Lambda| \cdot |I_m + A\Lambda^{-1}A^T|$$

# rAMDL

- Apply Matrix Determinant lemma to posterior Information matrix (Kopitkov and Indelman - IJRR'17)
- Baseline is  $O(N^3)$  while rAMDL is  $O(m^3)$ , Partitioning the measurements reduces  $m$ .

# rAMDL + Bounds

- Applying rAMDL to the determinants required for  $\mathcal{LB}, \mathcal{UB}$ :

$$|\Lambda_k^{\text{AUG}-} + (A_i^s)^T A_i^s|$$

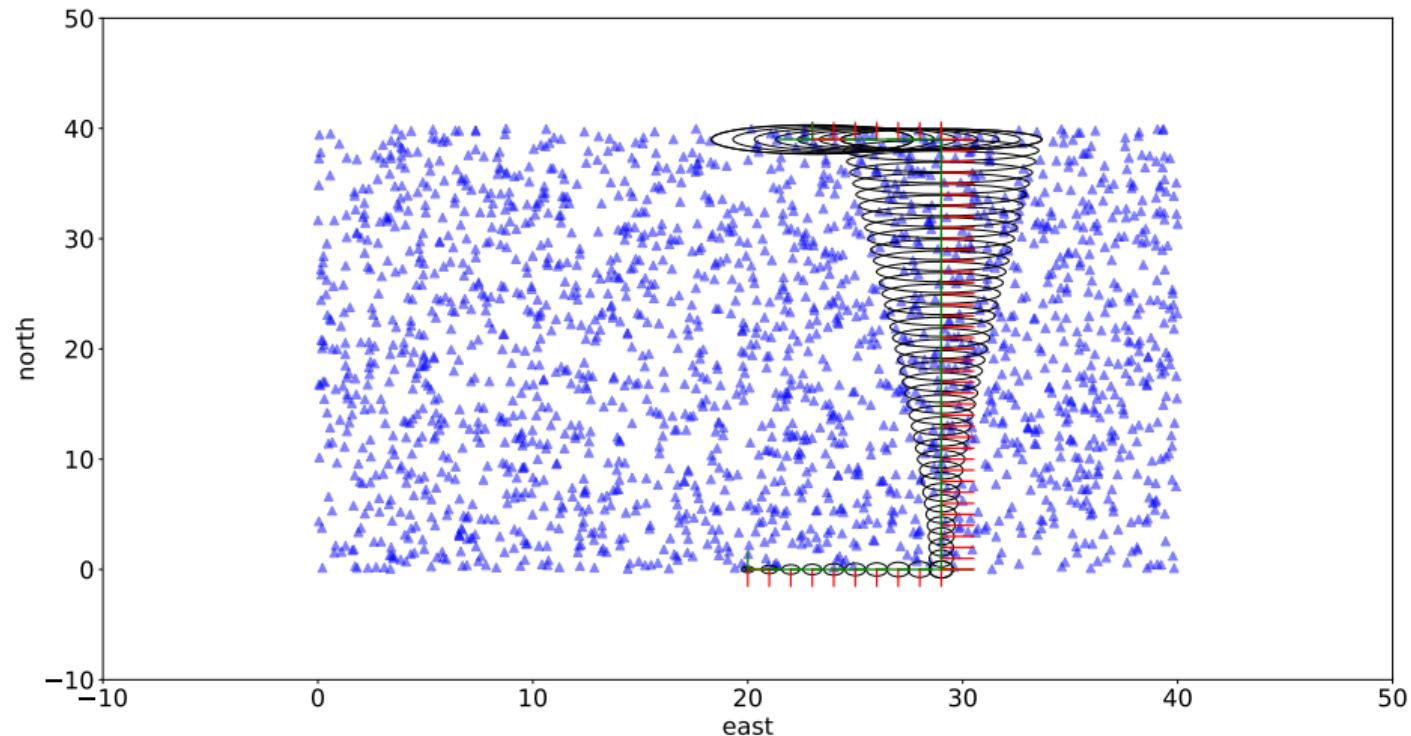
$$|\Lambda_k^{\text{AUG}-} + (A_i^{\bar{s}})^T A_i^{\bar{s}}|$$

- When  $s = \bar{s} \rightarrow |\Lambda_k^{\text{AUG}-} + (A_i^s)^T A_i^s| = O\left(\frac{m^3}{8}\right)$

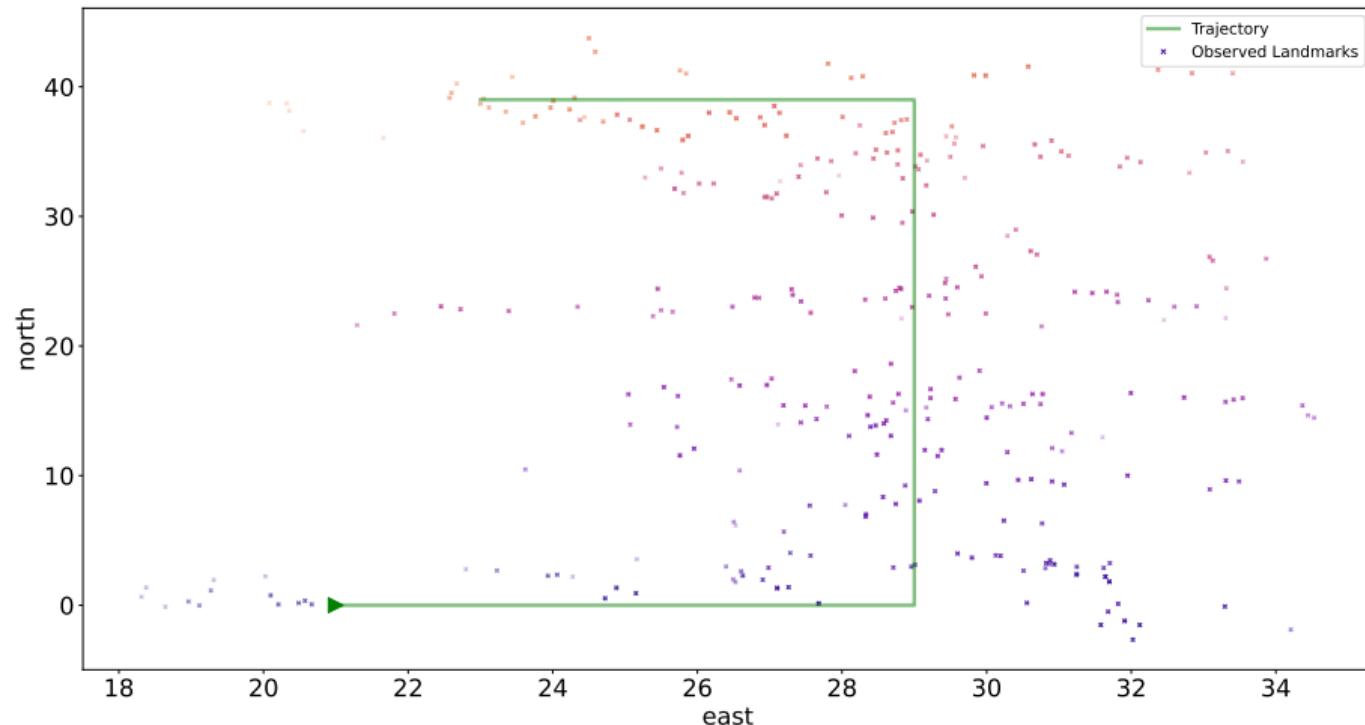
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  - Bounds Analysis
  - Simulation
- Recap

# Scenario

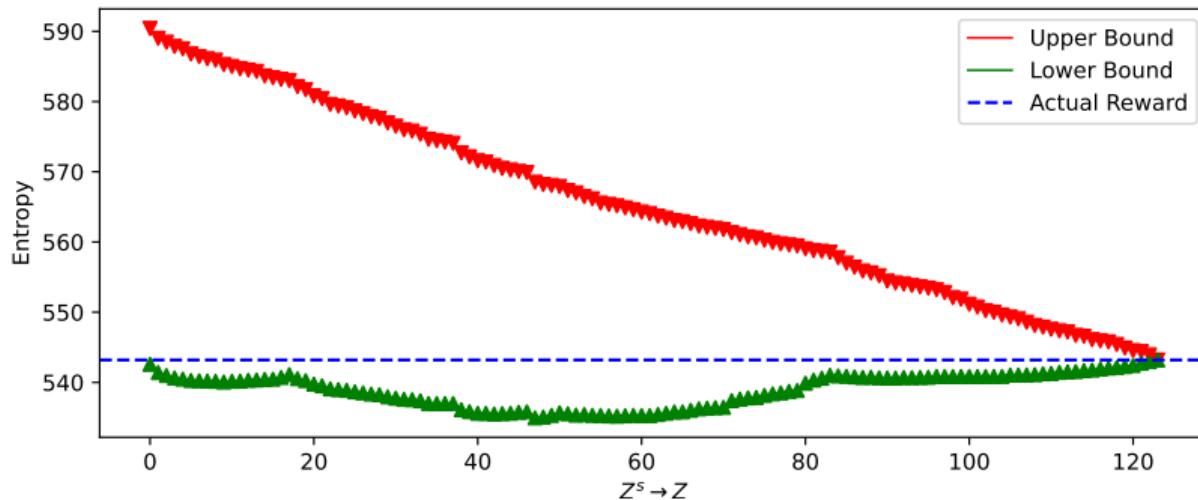


# Scenario



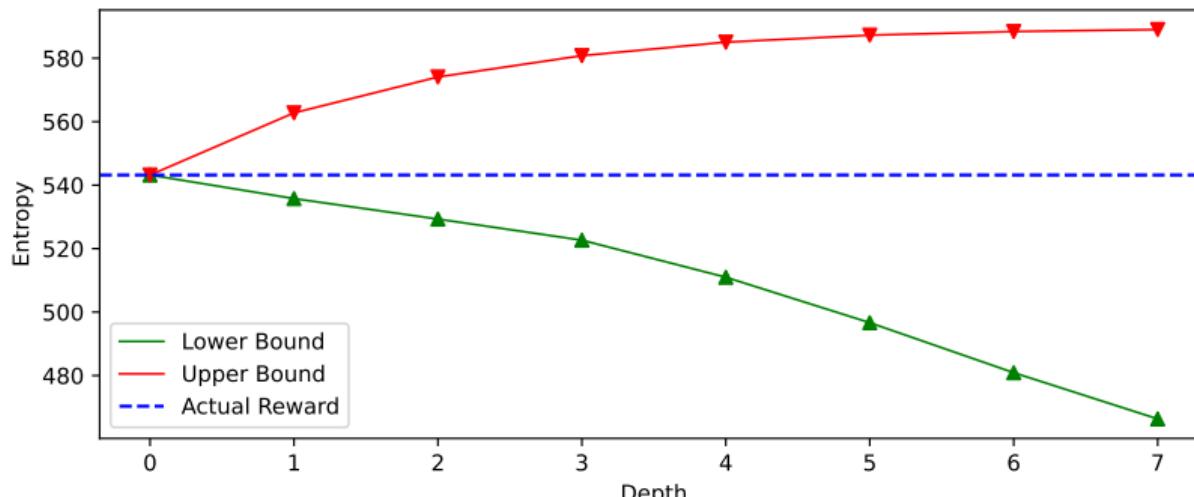
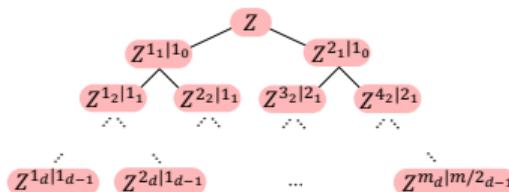
# Results - Bounds Analysis

For a specific action,  $Z^s \rightarrow Z$  while  $Z_{\bar{s}} \rightarrow \emptyset$



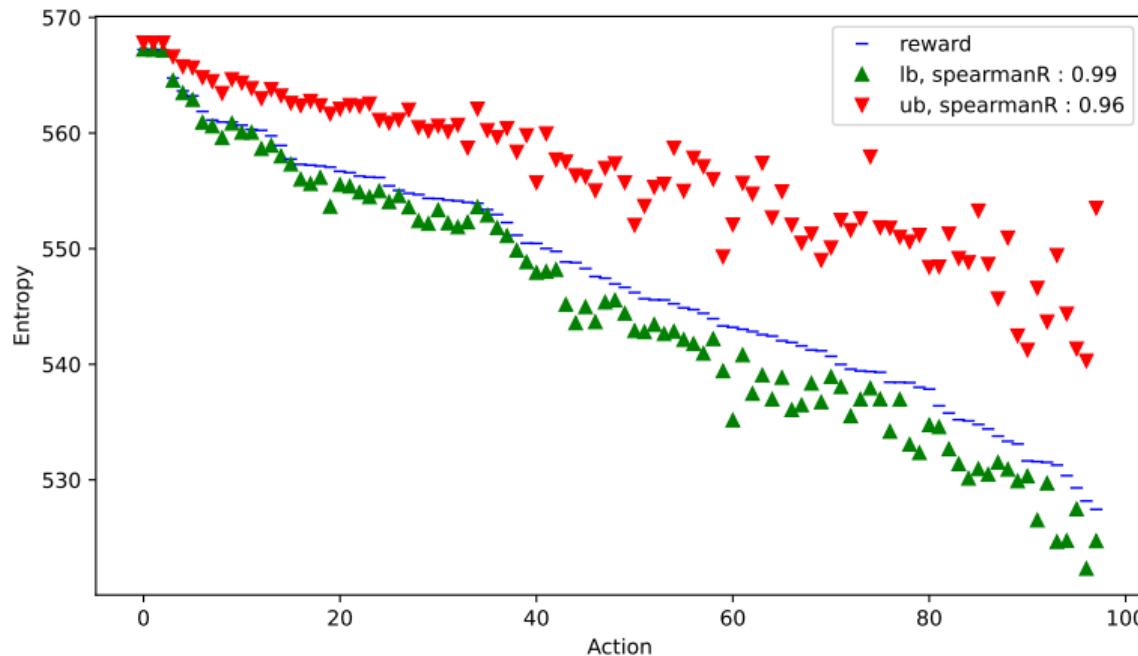
# Results - Bounds Analysis

Going down the partition tree:



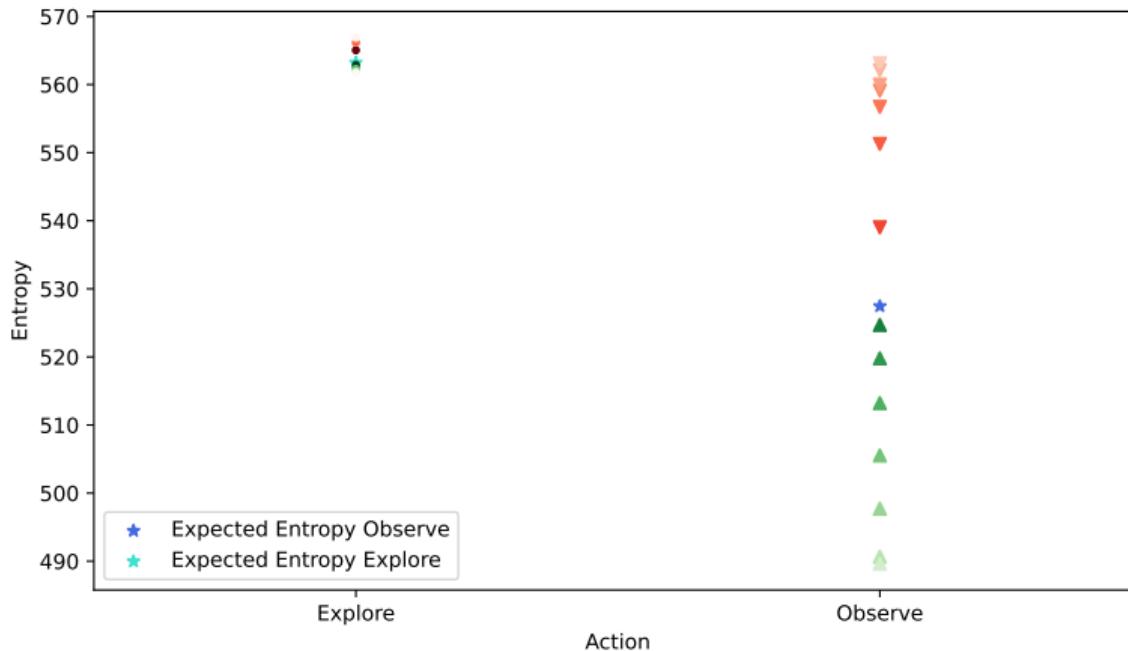
# Results - Bounds Analysis

Myopic, random actions:



# Results - Bounds Analysis

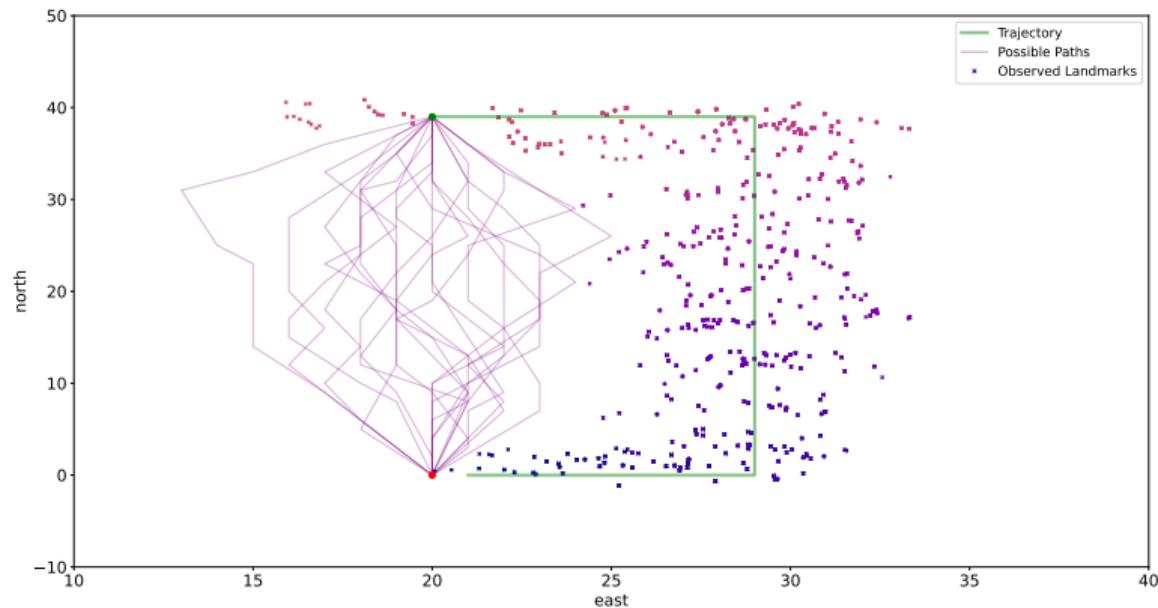
Two actions, different depths:



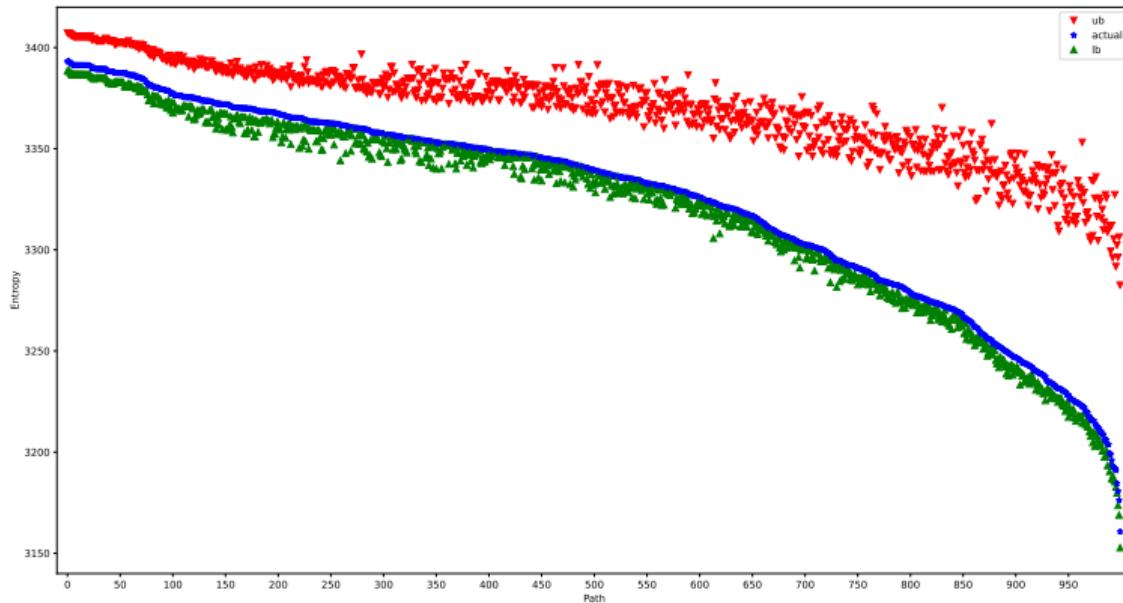
# Results - Simulation

- Scenario 1 - 1000 paths without re-planning
- Scenario 2 - 10 paths with re-planning
- Prior belief:
  - ▶ 1551 state variables
  - ▶ 6083 factors
- Scenario 3 - Real robot + visual odometry

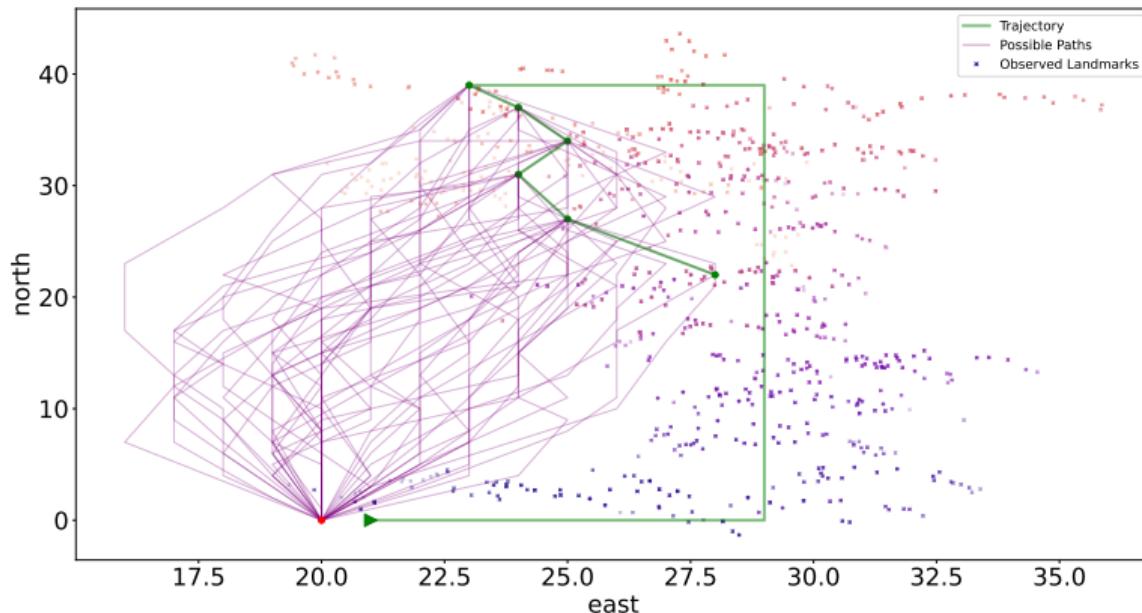
# Results - Scenario 1



# Results - Scenario 1



# Results - Scenario 2



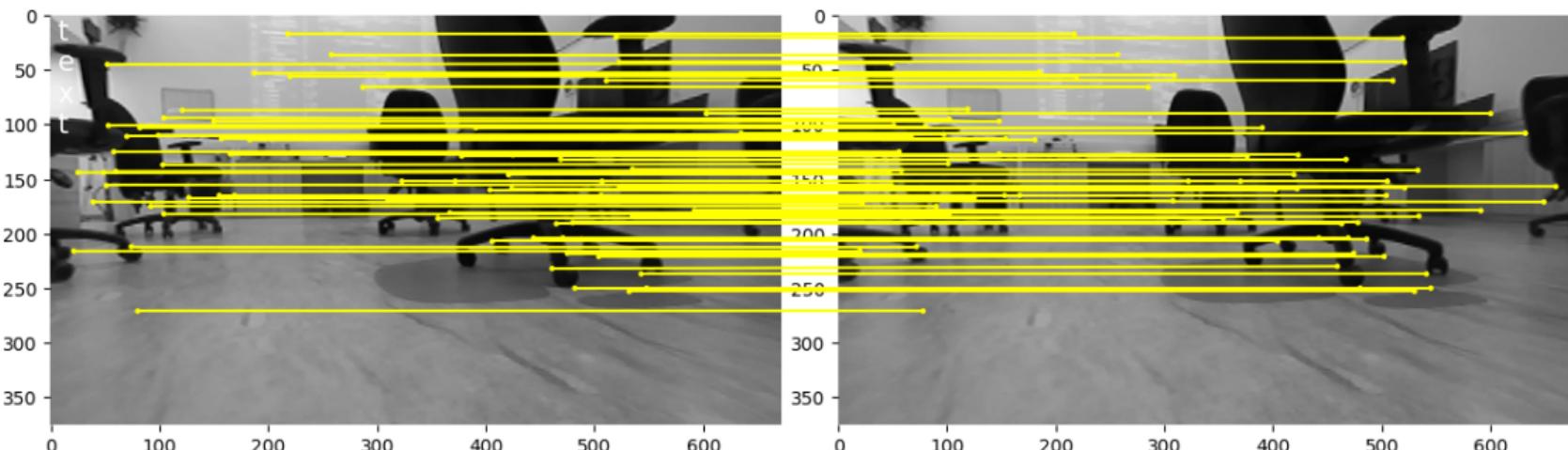
# Results - run time

Scenario	Method	Planning time [sec]
1	rAMDL	11.521
	MP	<b>6.888</b>
2	rAMDL	26.569
	MP	<b>9.737</b>

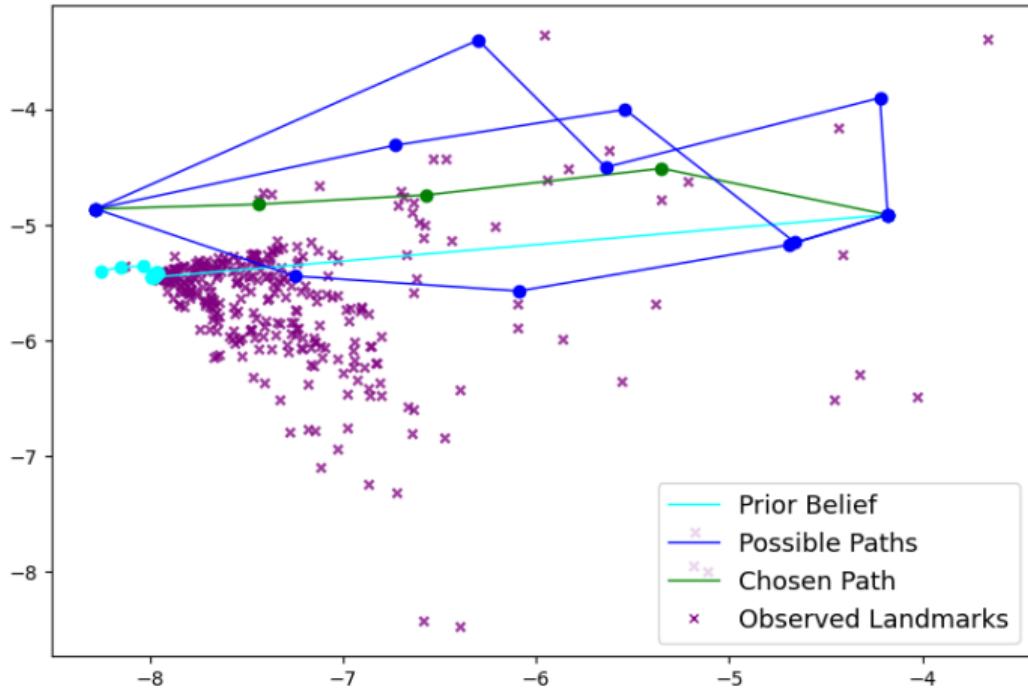
Table: Total planning time in seconds (lower is better)

# Results - Visual Odometry

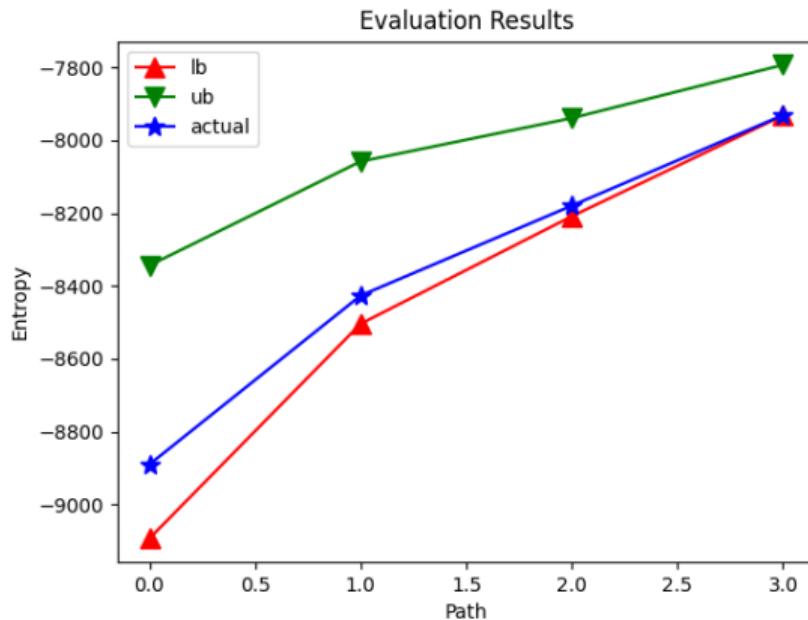
RoboMaster + ZED



# Results - Visual Odometry



# Results - Visual Odometry



# Conclusions

- We introduced a novel concept - observation space partitioning
- We proposed a simplified method to solving the POMDP planning problem using this concept
- We presented both theoretical and empirical studies of this method
  - both showing performance gains
- Multiple future research directions

# Questions

