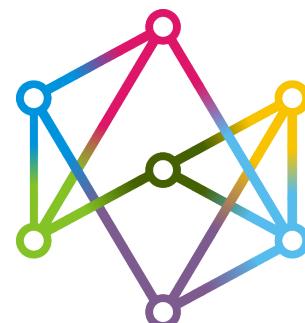


# Autonomous Online Perception and Navigation for Aerial Vehicles

Vadim Indelman



**TECHNION**  
Israel Institute  
of Technology



Israel Robotics Meetup

**ANPL**  
Autonomous Navigation and  
Perception Lab

September 25, 2019

# Introduction

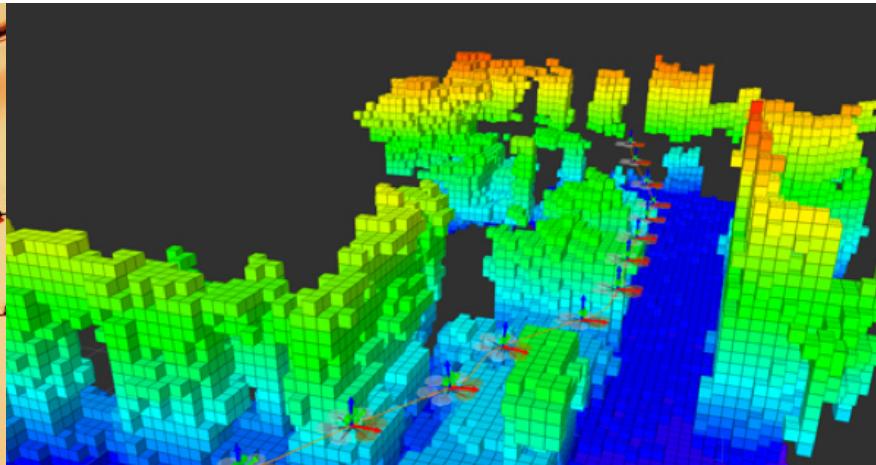
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- Autonomous operation in complex, uncertain and ambiguous scenarios
  - **Independent** of infrastructure and prior information
  - Within **static and dynamic** environments

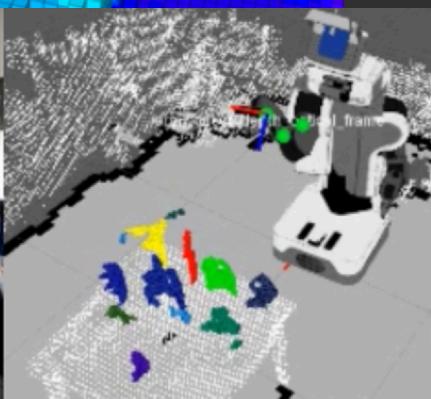
Urban environments



Indoor environments



Amazon Prime Air

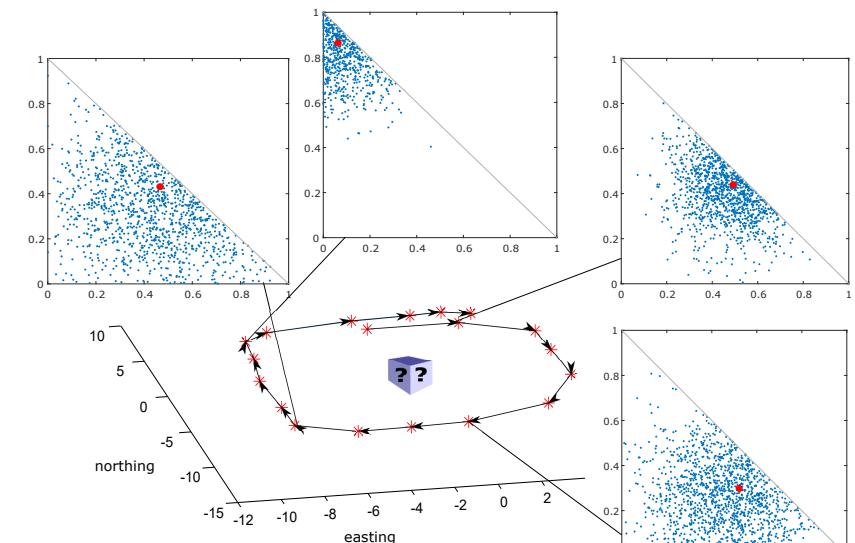
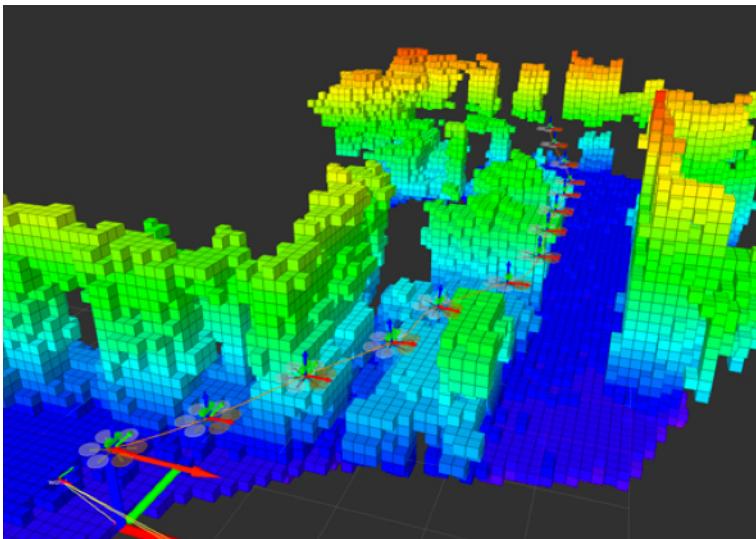
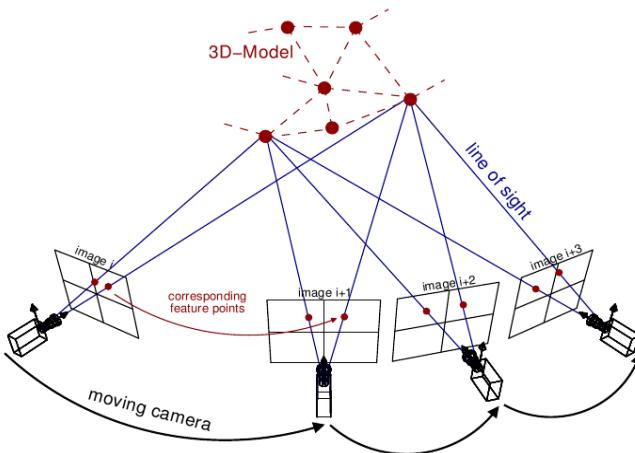


# Introduction

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Key required capabilities:

- **Perception and Inference:** Where am I? What is the surrounding environment?
- **Planning Under Uncertainty & Active Perception:** Decide next action(s) given partial, noisy data

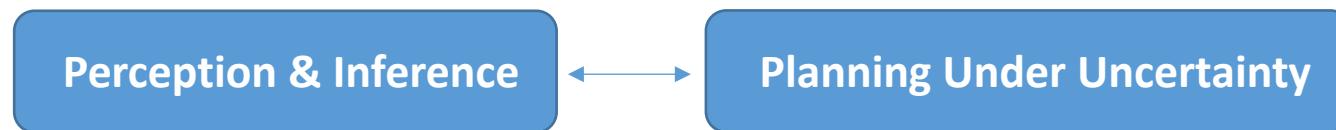


# Introduction

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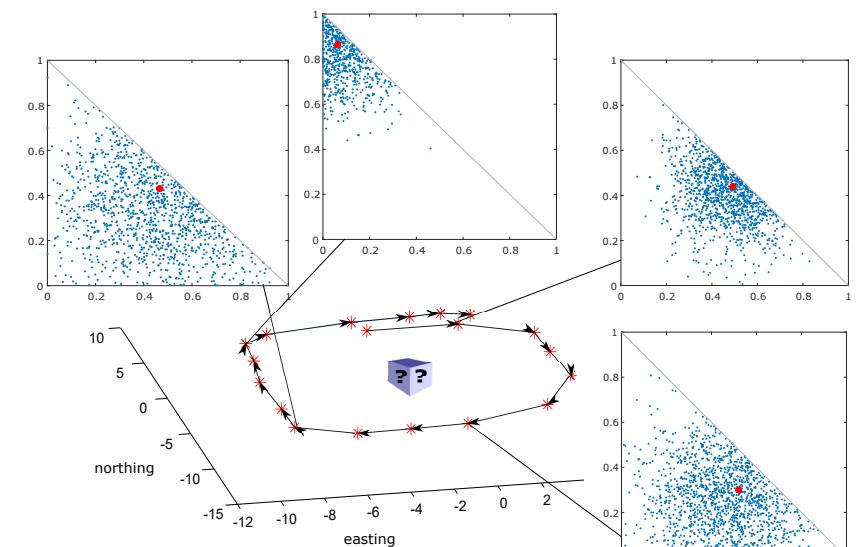
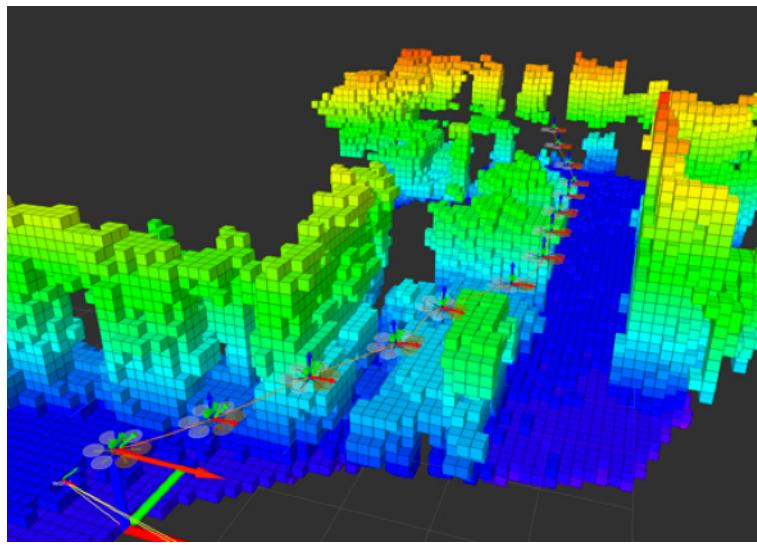
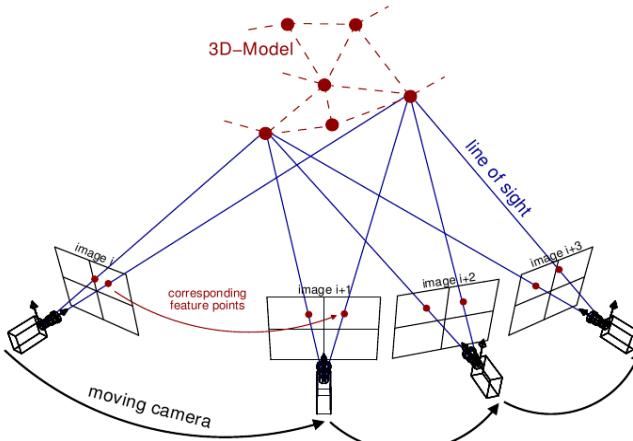
- Tight coupling with perception & inference
- Related problems: autonomous navigation, active SLAM, informative planning/sensing, etc.



## Perception & Inference

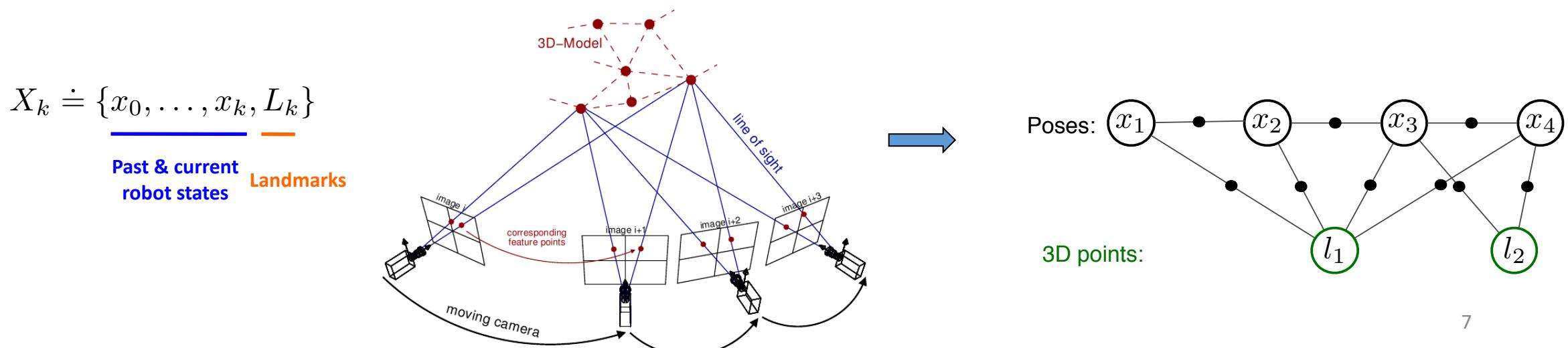
# Perception and Inference

- Key questions (given data obtained thus far):
  - Where am I?
  - What is the surrounding environment? (aspects: geometric/semantic; static/dynamic)
- What if neither is known?
  - Need to infer both robot pose and observed structure
  - **Robotics:** simultaneous localization and mapping (SLAM)
  - **Computer vision:** structure from motion, bundle adjustment



# Perception and Inference

- State/variables at time k:  $X_k \in \mathbb{R}^n$
- Posterior belief at time k:  $b[X_k] \doteq \mathbb{P}(X_k \mid u_{0:k-1}, z_{1:k})$   
 $\doteq H_k$  (history)
- Can be represented with graphical models, e.g. a factor graph
- Computationally-efficient maximum a posteriori inference e.g. [Kaess et al. 2012]



# Incremental Light Bundle Adjustment

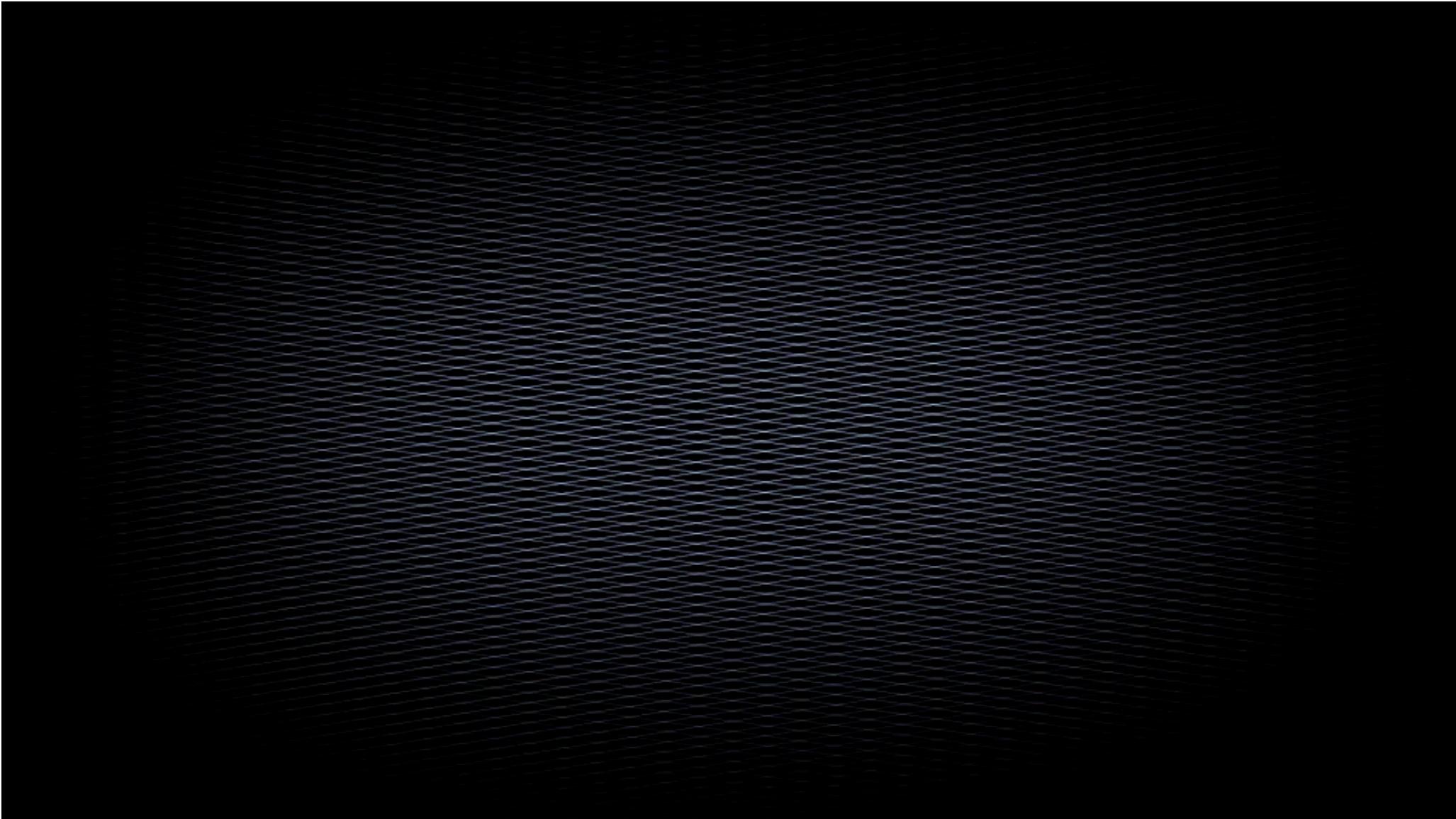
[Indelman, Richards, Dellaert, BMVC '12]

**Key idea:** (algebraically) eliminate 3D landmarks



# RGBD Mapping

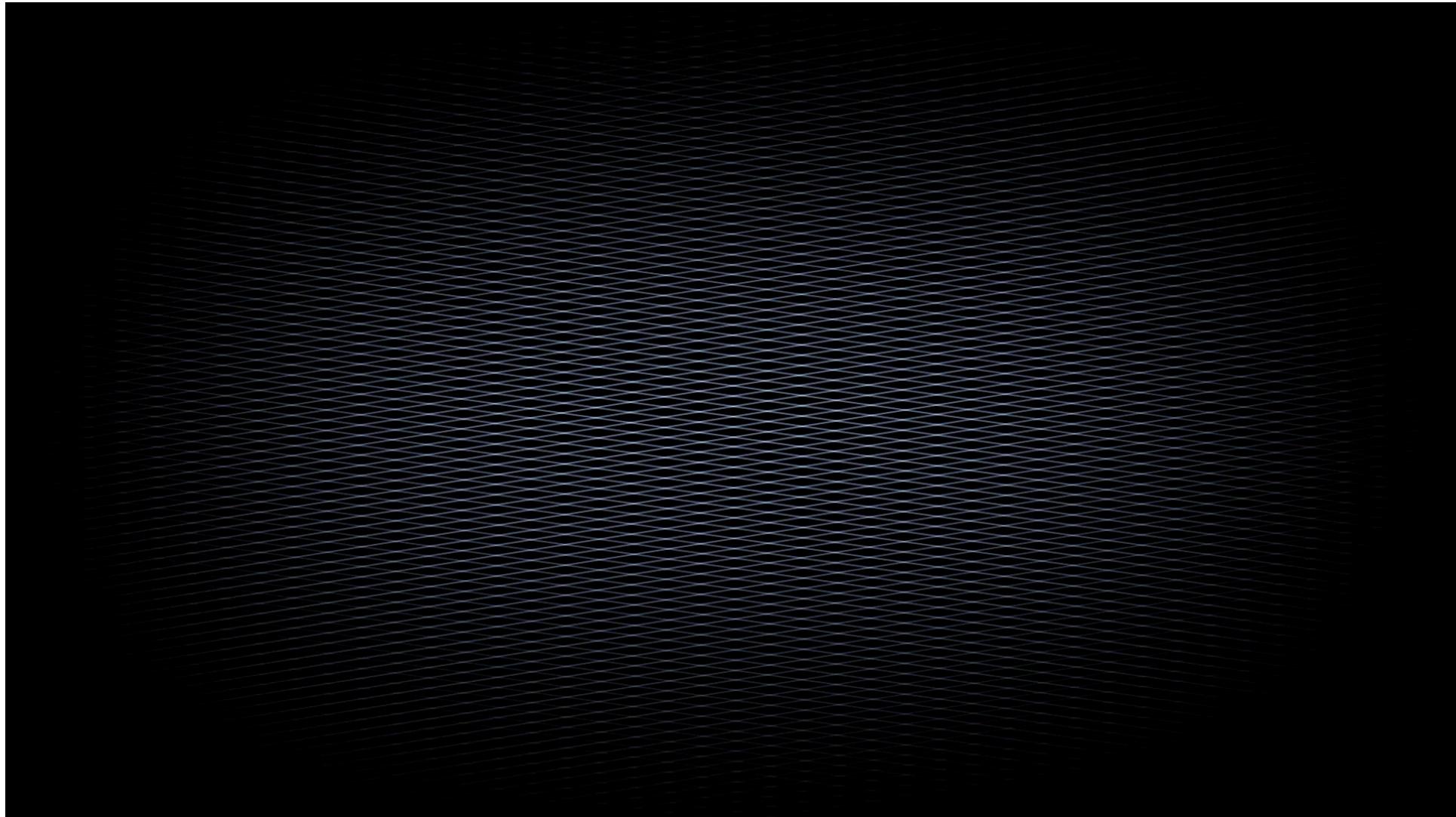
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# Collaborative Multi-Robot SLAM (2 Quads)

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**Key capability:** improve performance by **sharing information** between robots and formulating **multi-robot constraints**



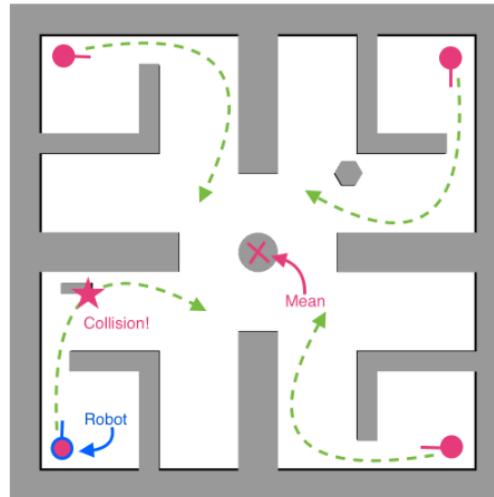
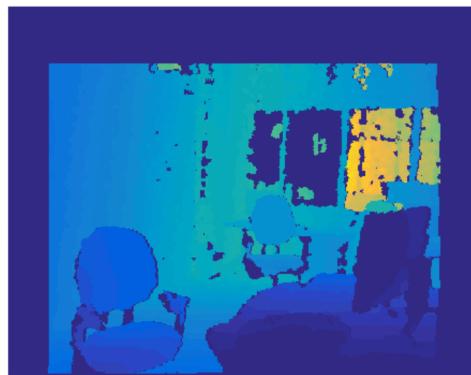
# Ambiguous Environments



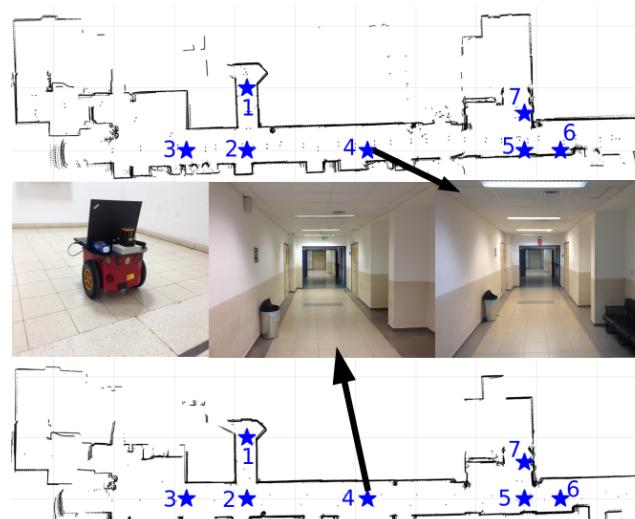
Angeli et al., TRO'08



Mu et al., IROS'16



Agarwal et al., arXiv 2015



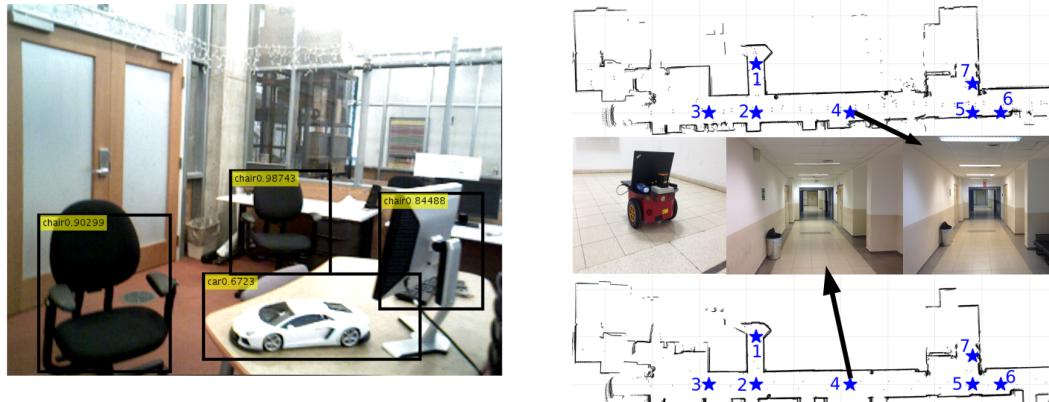
Pathak, Thomas, Indelman, IJRR 2018

Israel Robotics Meetup, September 2019

# Ambiguous Environments

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- Ambiguity can be due to (combination of):
  - Perceptually aliased scenes (two similar objects)
  - Limited/imperfect sensing (limited sensing range)



- Data association and SLAM/localization are inherently coupled
- Can we incorporate these aspects within **inference** and **decision making?**

# Robust Perception – Ambiguous Scenarios

[Indelman, et al., CSM'16]

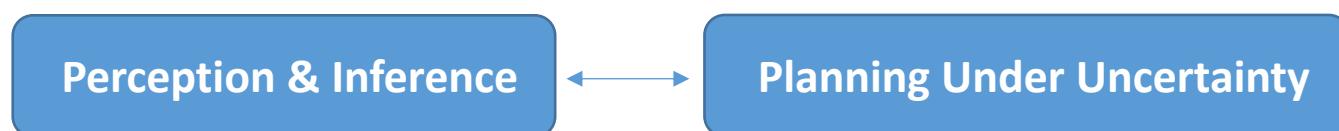
- Multi-robot collaborative localization and mapping – **distributed, online**
- **Robust perception** (cope with perceptual aliasing)

Distributed Real-time Cooperative Localization and Mapping  
using an Uncertainty-Aware Expectation Maximization Approach

Jing Dong, Erik Nelson, Vadim Indelman,  
Nathan Michael, Frank Dellaert



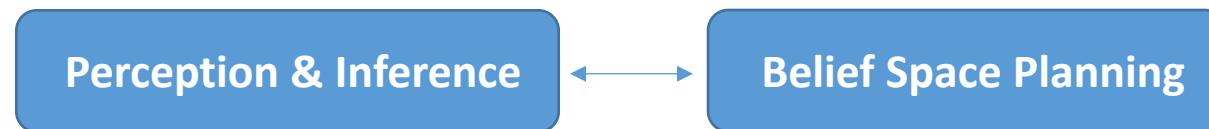
# Autonomous Perception (Planning Under Uncertainty, Belief Space Planning)



# Belief Space Planning (BSP)

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- Given partial and uncertain knowledge, determine: Next actions, given a task
- Tight coupling with perception & inference



- Related problems: autonomous navigation, active SLAM, informative planning/sensing, etc.

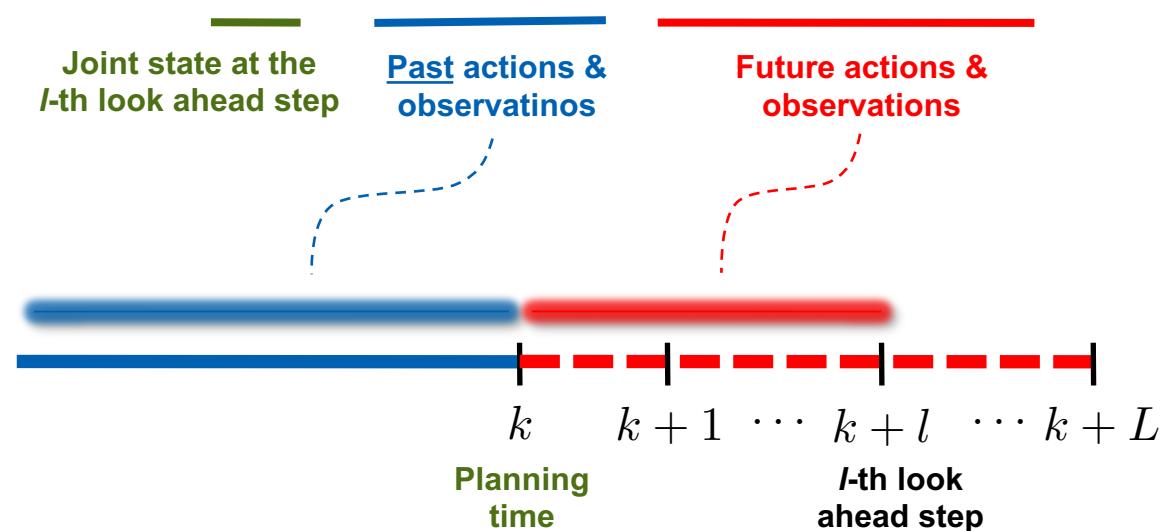


# Belief Space Planning (BSP)

- Objective function ( $u \doteq u_{k:k+L-1}$ ):

$$J(u) \doteq \mathbb{E} \left[ \sum_{l=1}^L c(b[X_{k+l}], u_{k+l-1}) \right]$$

- Belief at the  $l$ -th look-ahead step:  $b[X_{k+l}] \doteq \mathbb{P}(X_{k+l} \mid u_{0:k-1}, z_{0:k}, u_{k:k+l-1}, z_{k+1:k+l})$



- Optimal (non-myopic) actions/control:

$$u^* = \arg \min_u J(u)$$

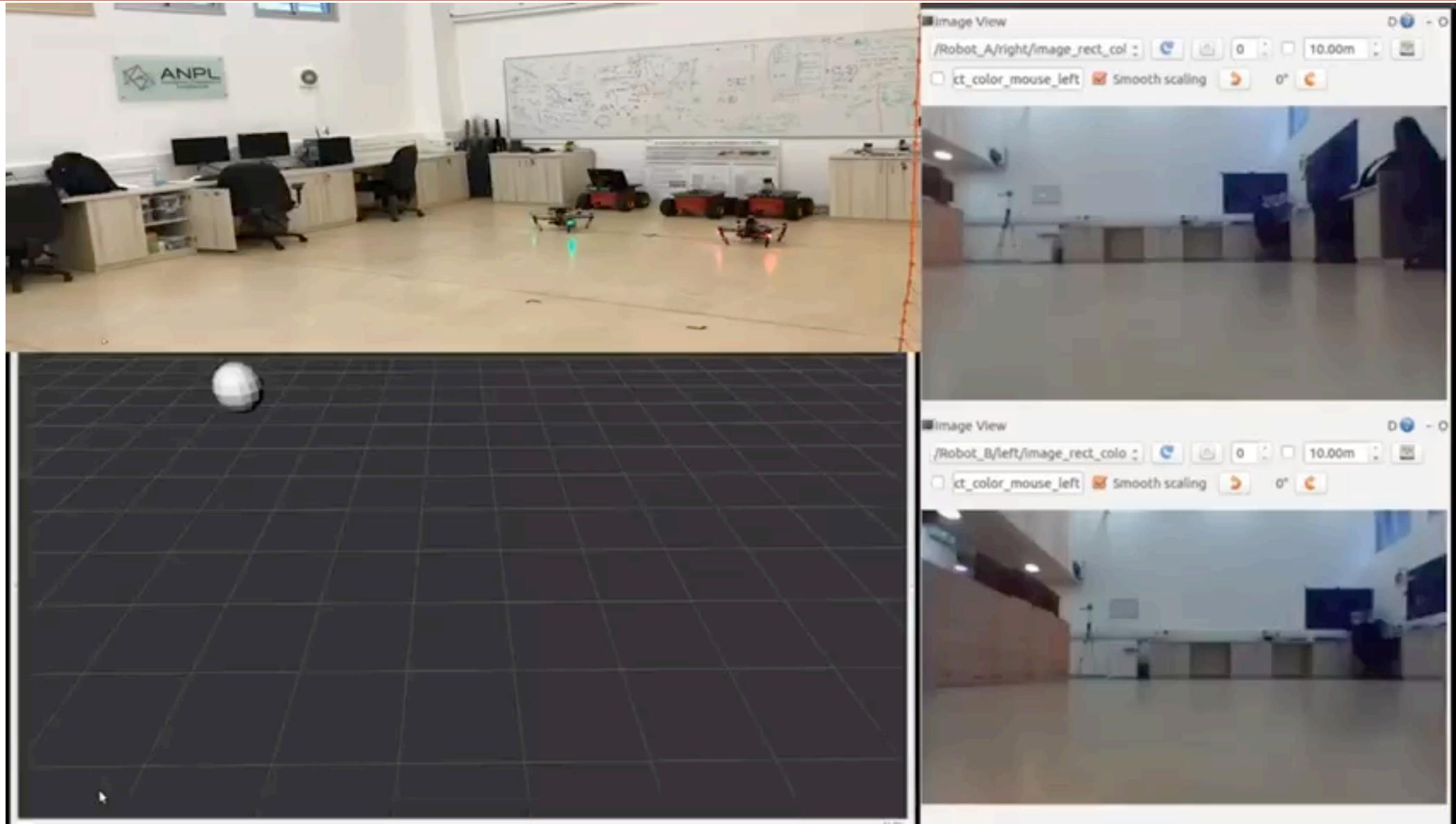
# Belief Space Planning (BSP)

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$$J(u) \doteq \mathbb{E} \left[ \sum_{l=1}^L c(b[X_{k+l}], u_{k+l-1}) \right]$$

- Finding an optimal solution is generally **computationally intractable**
- Our focus - want to:
  - Act autonomously, online, while accounting for different sources of uncertainty and ambiguity
  - Reliably operate in uncertain, perceptually aliased environments/scenarios

# Collaborative SLAM & BSP on Quads



# Belief Space Planning (BSP)

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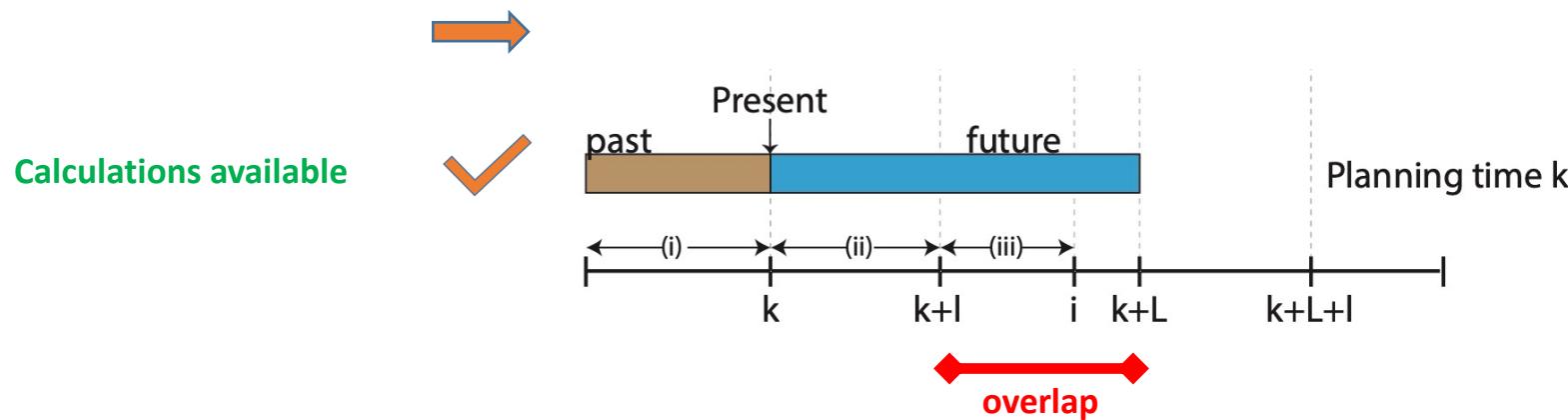
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# Incremental Belief Space Planning

[Farhi and Indelman, ICRA'19]

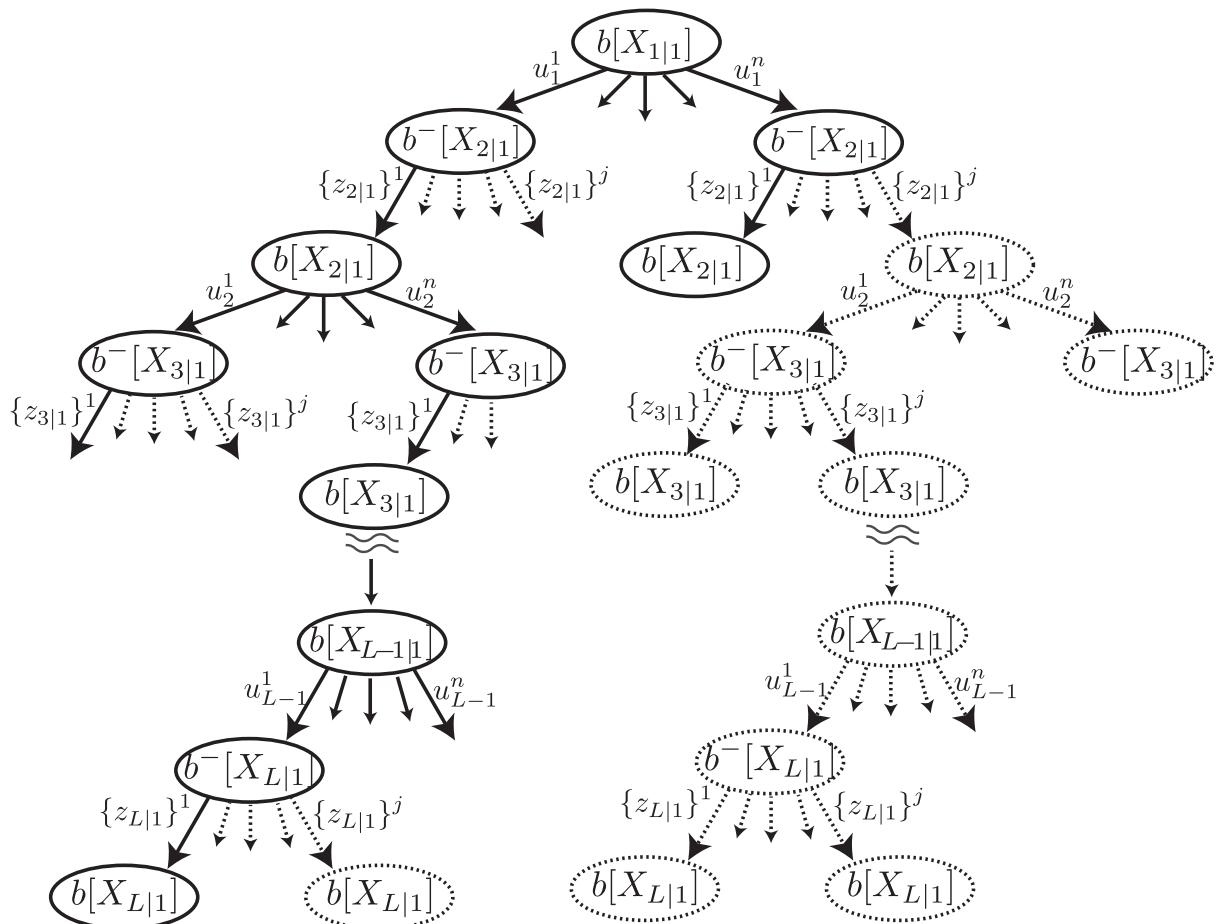
- Key idea:
  - Re-use calculations across successive planning sessions
  - Instead of calculating each planning session from scratch (state of the art)



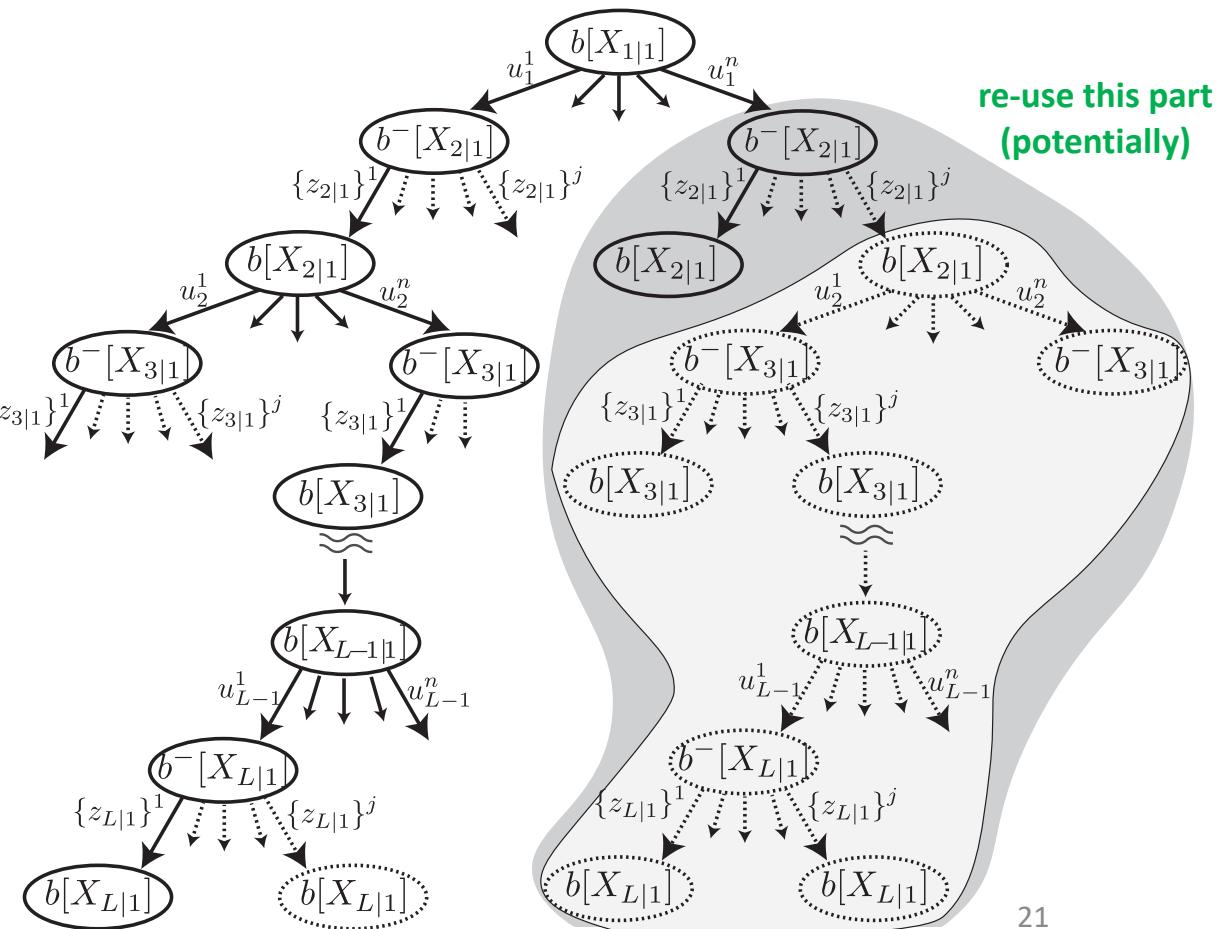
# Incremental Belief Space Planning

[Farhi and Indelman, ICRA'19]

Planning time  $k = 1$



Planning time  $k = 2$

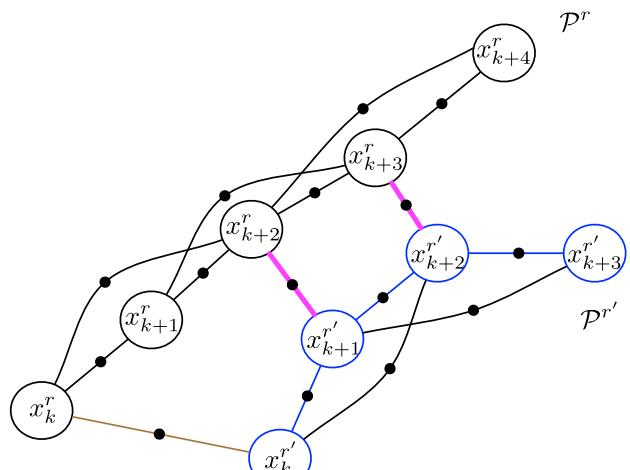


# Topological Belief Space Planning (t-BSP)

[Kitanov and Indelman, ICRA'18, arXiv'19]

- Key idea:

- Design a metric of factor graph topology that is strongly correlated with entropy
- Determine best action using that topological metric (instead of entropy)
- **Does not require explicit inference, nor partial state covariance recovery**



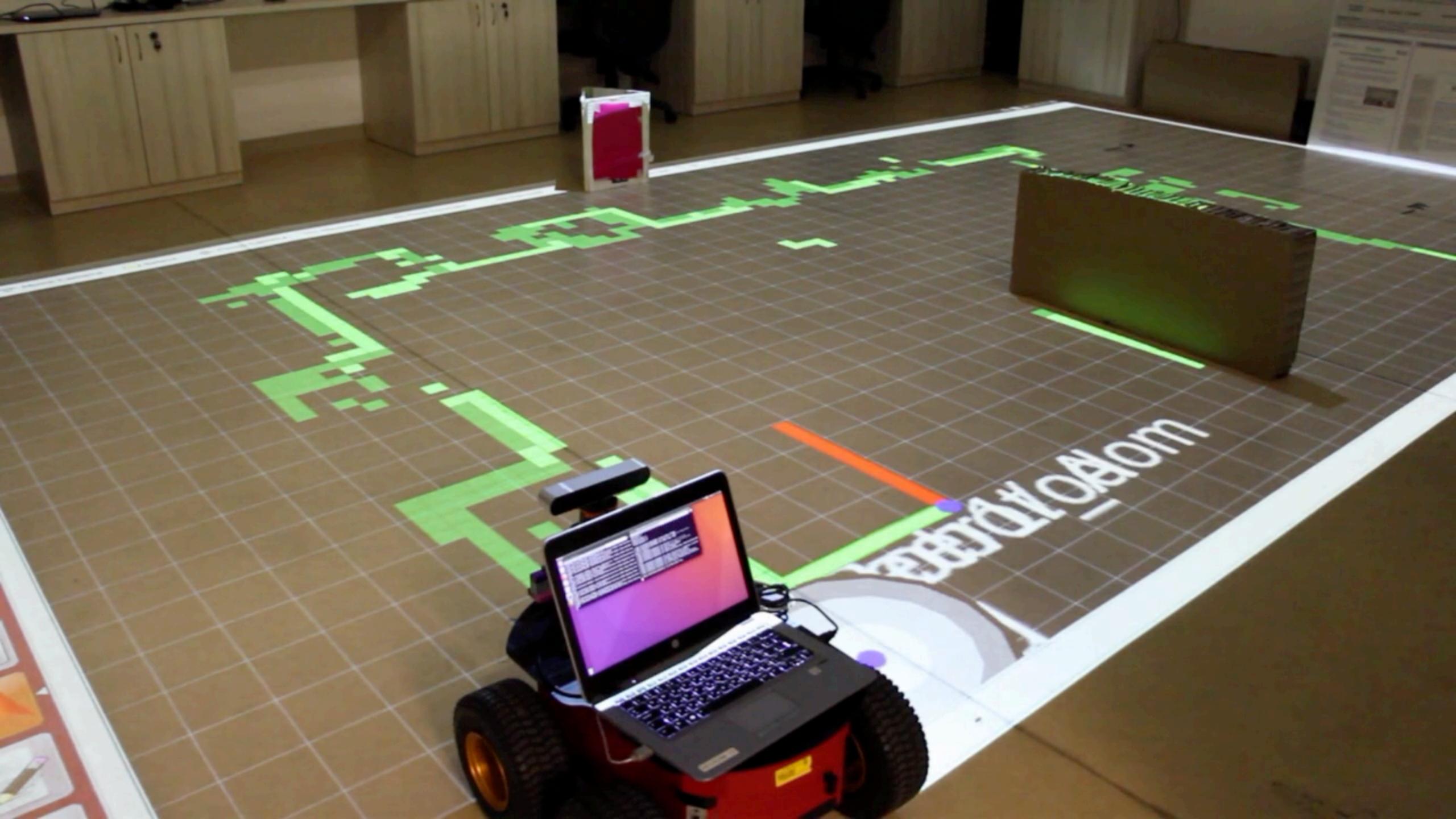
Factor graph for a 2-robot scenario,  
considering some specific candidate actions

Corresponding topology represented  
by a graph  $G(\Gamma, E)$



topological  
metric  $s(G)$   
graph signature

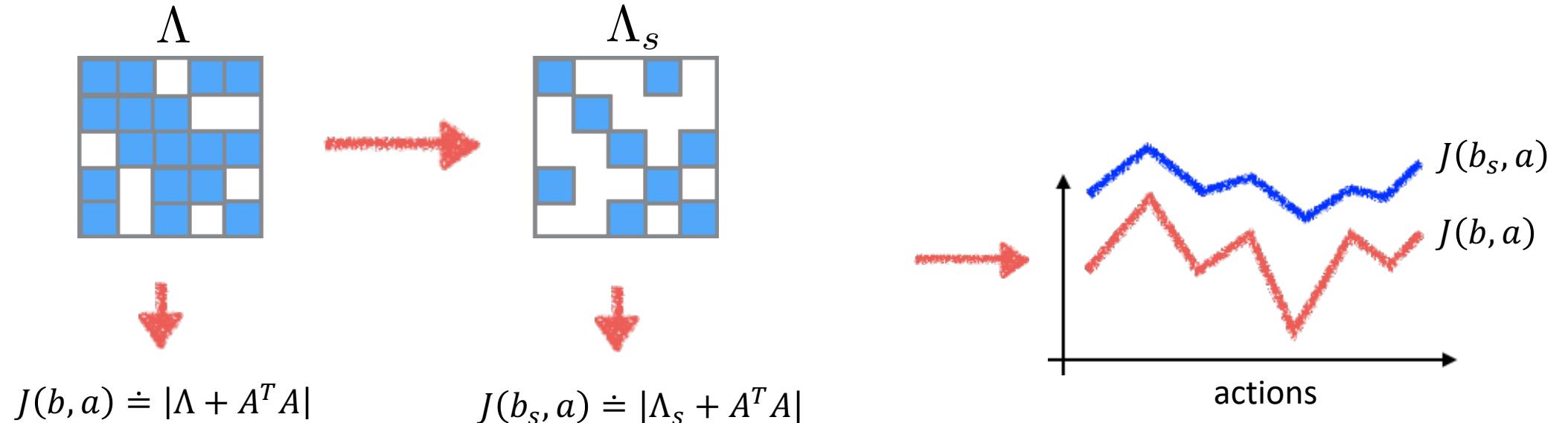




# Belief sparsification for BSP (s-BSP)

[Indelman RAL'16][Elimelech and Indelman, ICRA'17, IROS'17, ISRR'17, arXiv'19]

- Key Idea:
  - Find an appropriate **sparsified** information space (more generally, belief)
  - Perform decision making over that, rather than the original, information space

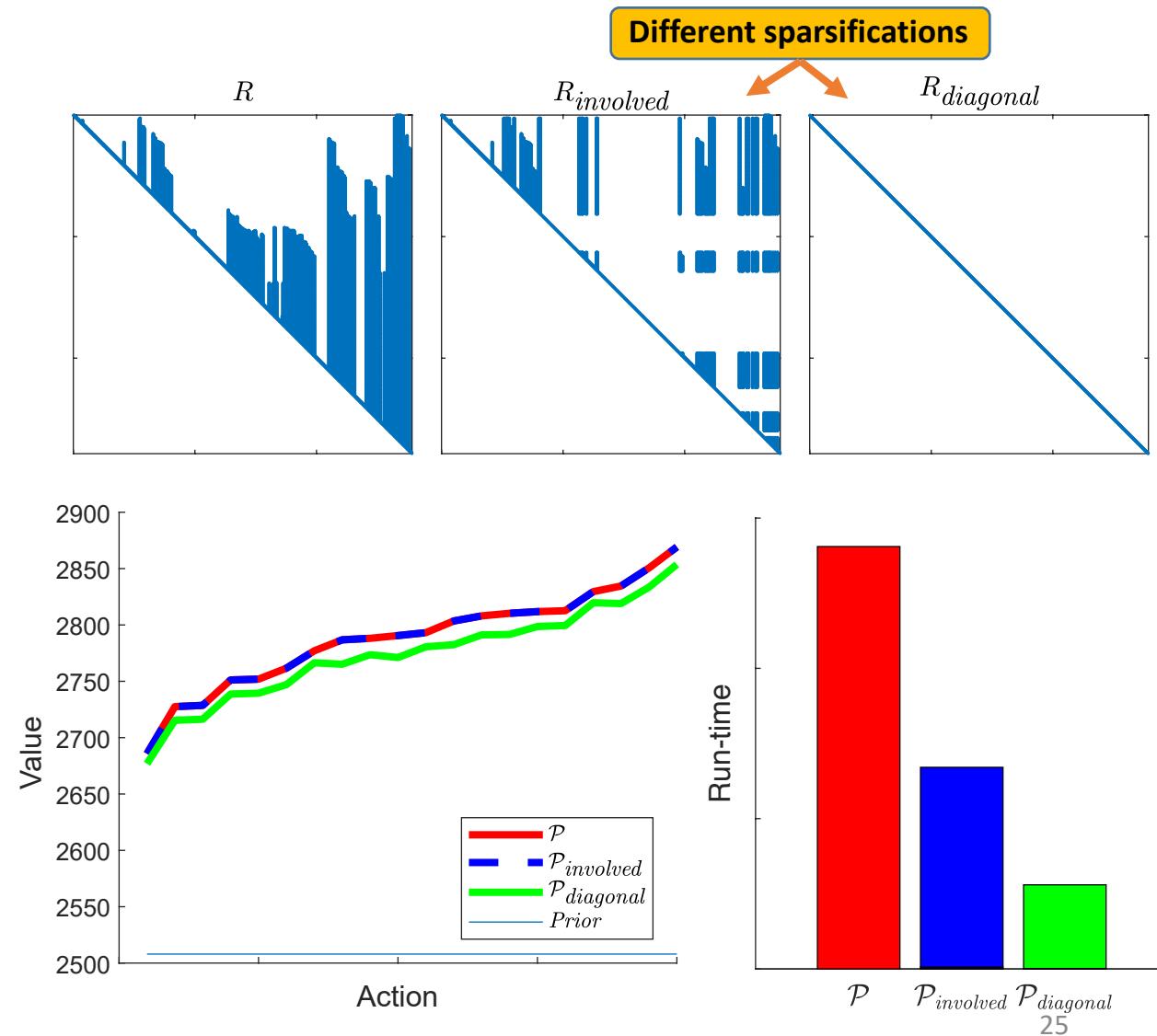
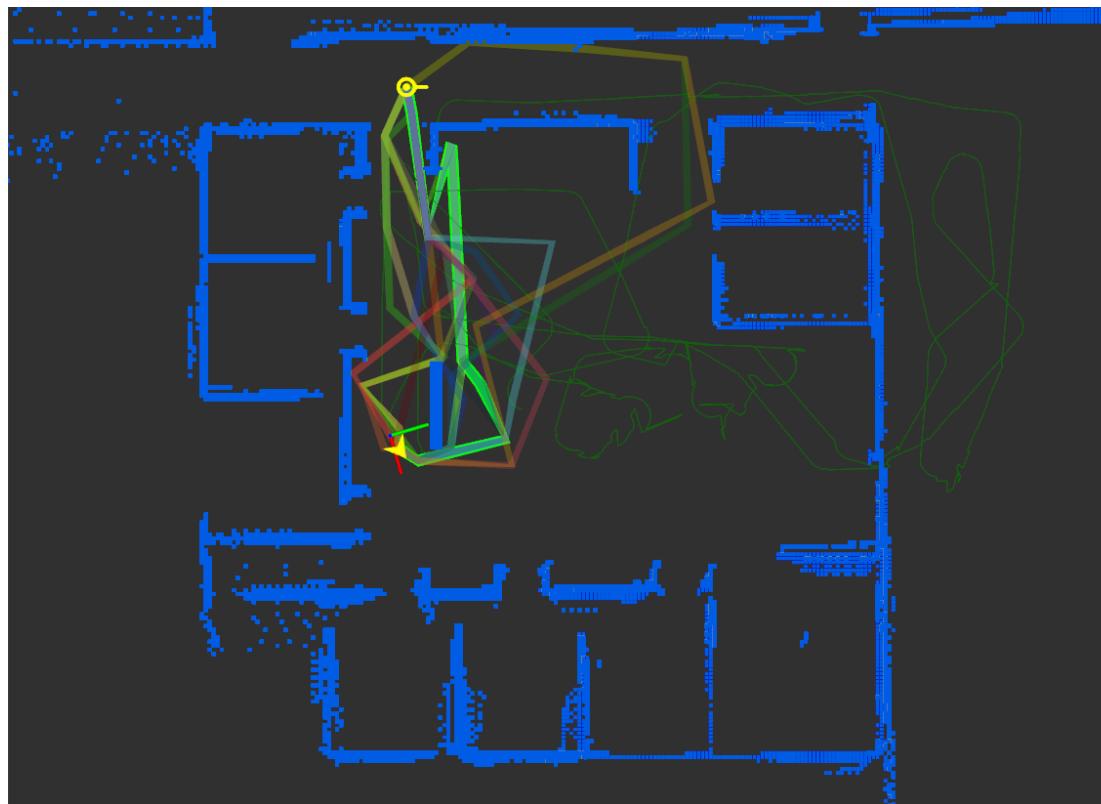


- Do we get the same performance (decisions), i.e. is it action consistent?
- If not, can we bound the loss?

# s-BSP: Gazebo Results

[Elimelech and Indelman, arXiv'19]

Candidate actions (trajectories)



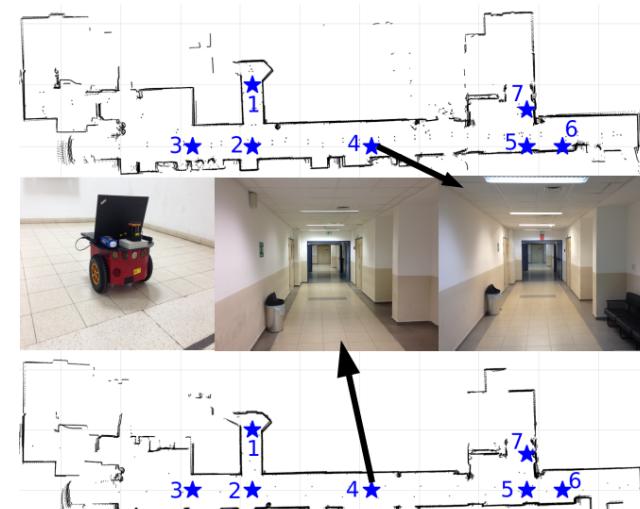
# Active Robust Perception

[Pathak, Thomas, Indelman, IJRR'18]

- What happens if the environment is **ambiguous, perceptually aliased?**
- BSP approaches typically assume data association is **given** and **perfect!** We **relax** this assumption
- Our **Data Association Aware BSP (DA-BSP)** algorithm considers both
  - **Ambiguous data association** (DA) due to perceptual aliasing, and
  - **Localization uncertainty** due to stochastic control and imperfect sensing
- Approach can be used for **active disambiguation** (for example)



Angeli et al., TRO'08



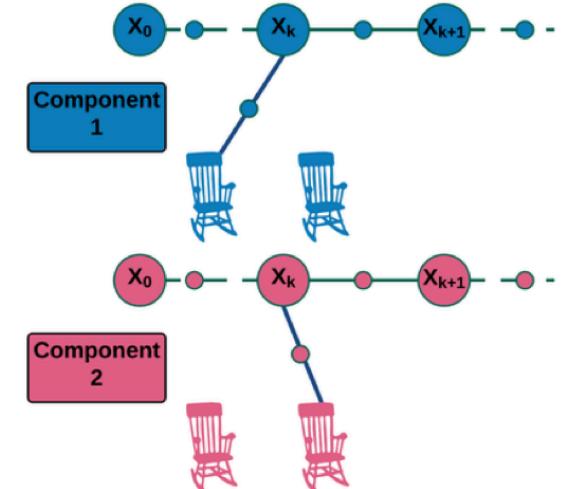
# Approach Overview

[Pathak, Thomas, Indelman, IJRR'18]

- Belief is represented by a Gaussian Mixture Model (GMM)

$$b[X_k] = \mathbb{P}(X_k | \mathcal{H}_k) = \sum_{j=1}^{M_k} \xi_k^j \mathbb{P}(X_k | \mathcal{H}_k, \gamma = j)$$

Weight    Conditional multivariate Gaussian,  
represented by a factor graph

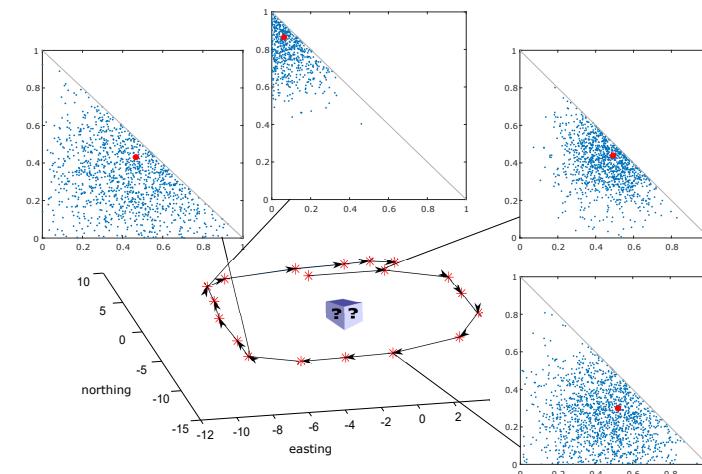
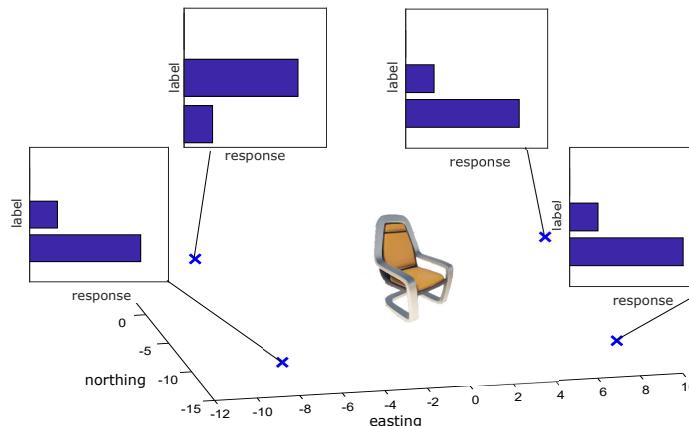


- Main idea:** Reason within BSP how a GMM belief will evolve for different candidate actions
  - Marginalize over possible data associations for future observations
  - Maintain & track data association hypotheses within inference and BSP
- Number of non-negligible modes can go down, and go up (!)

# Extension to Semantic (Active) Perception

[Feldman and Indelman, ICRA'18, ARJ'19 accepted; Tchuiev and Indelman, RAL'18; Tchuiev, Feldman and Indelman, IROS'19]

- Key challenge: operation in **perceptually aliased** environments
  - Ambiguous data association (e.g. different scenes/objects appear alike)
  - **Classification aliasing (ambiguous classification of a scene/object)**
- Ongoing work on semantic SLAM via a viewpoint-dependent classifier model
- Involves maintaining **hybrid** beliefs (continuous and discrete variables)



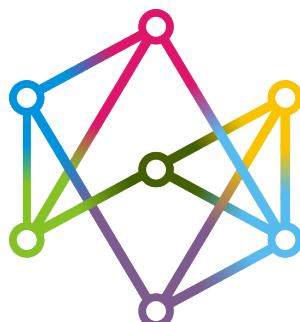
# Summary

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Autonomous Online Perception and Navigation for Aerial Vehicles

- Maintain and reason about **high-dimensional** beliefs
- Computational efficiency for online performance (both for inference & BSP)
- Robustness to ambiguous scenarios
- Collaboration between multiple (heterogenous) robots to enhance performance

More details:



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