

# Comparing BL and Markowitz

## Input Summary

Covariance Matrix 2	0,0019	0,0003	0,0006
	0,0003	0,0011	0,0002
	0,0006	0,0002	0,0014

Benchmark Asset returns	0,01
	0,01
	0,01

Risk aversion 15

Tau 0,91

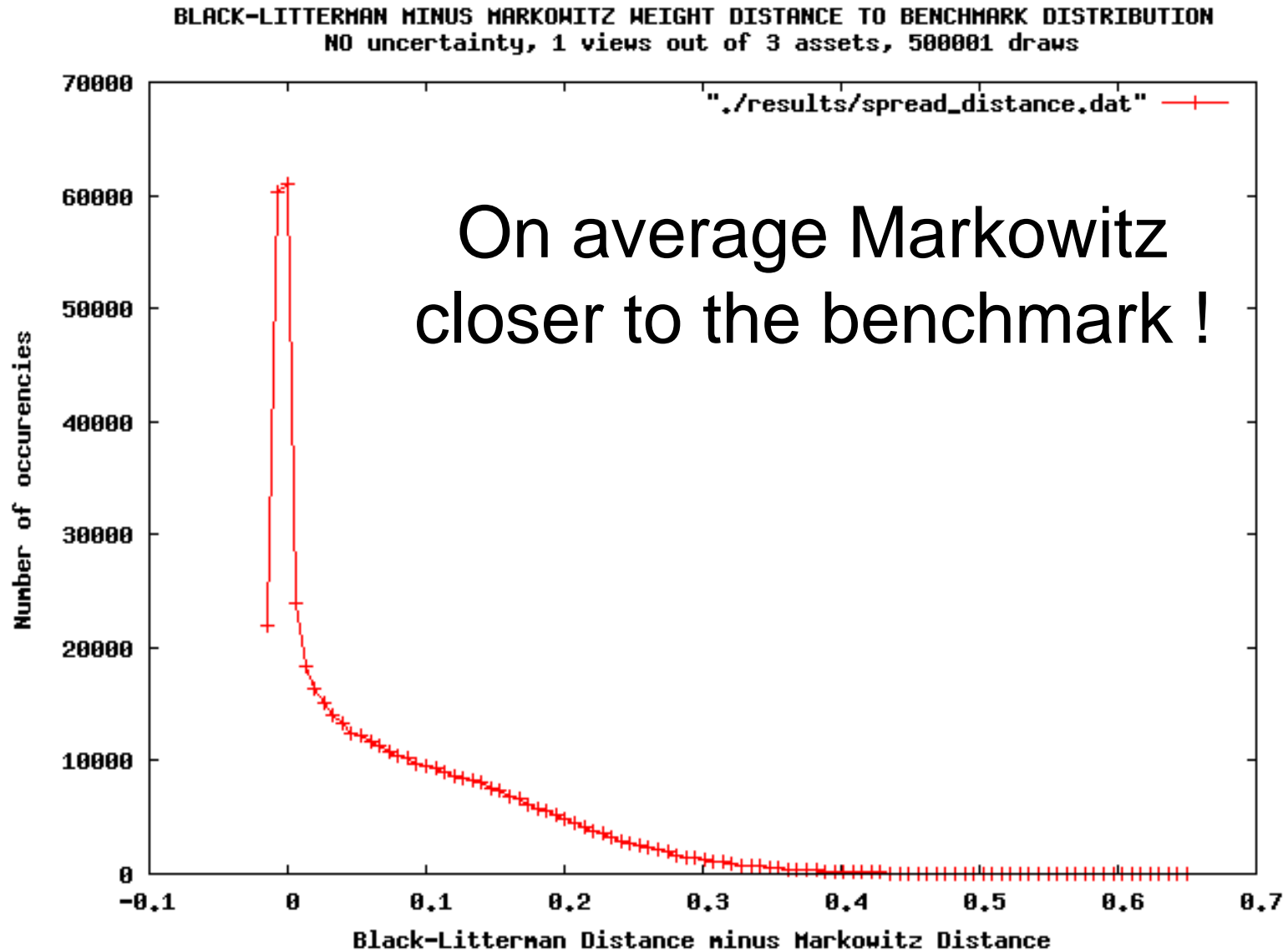
Benchmark weights	0,16666667	A
	0,5	B
	0,33333334	C
wf	0	Rf
Sum	1,00000001	

# Monte Carlo Approach

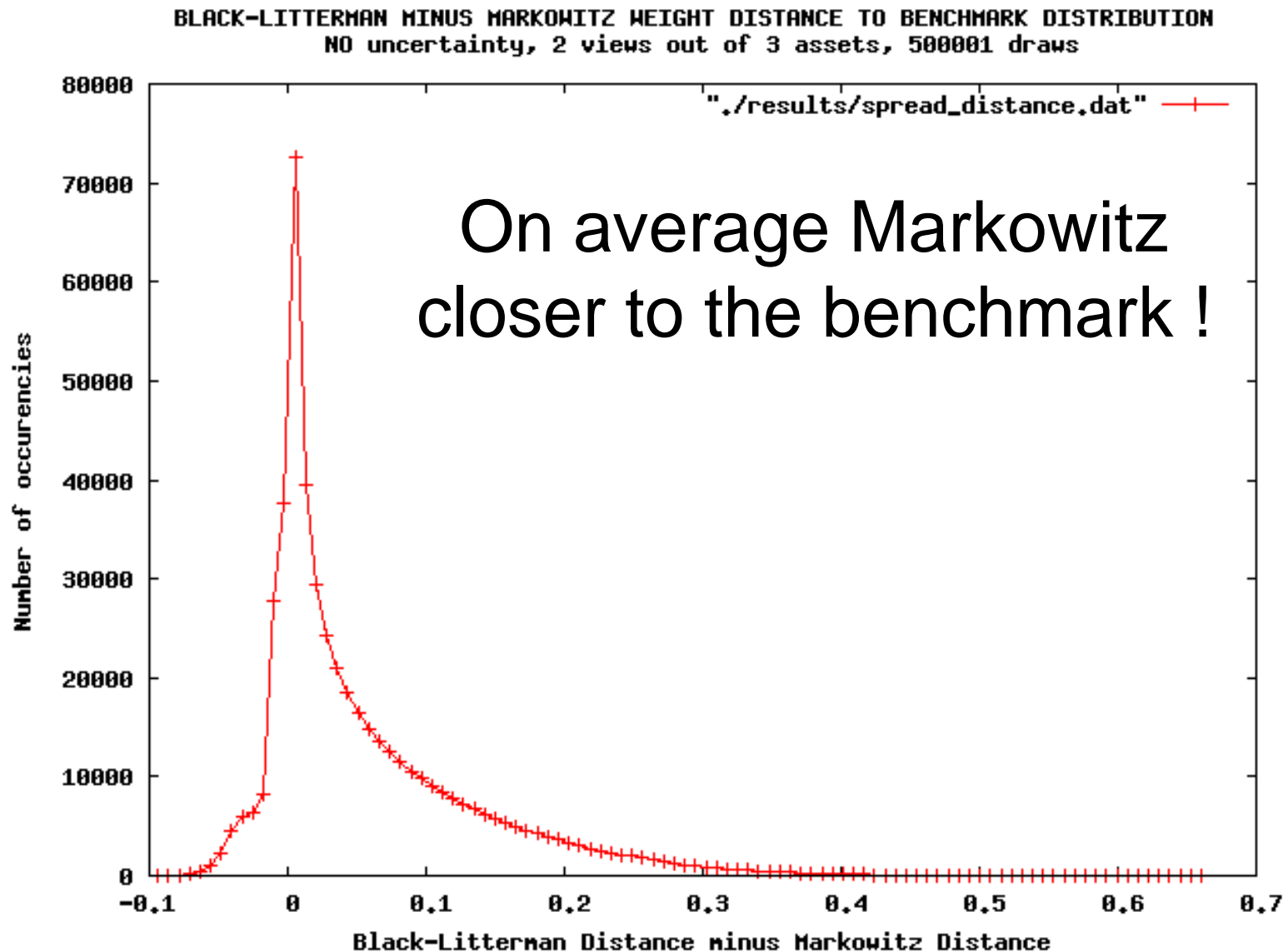
500 000 views are generated through  
random draws from normal distributions  
of mean 1% ( $\Pi$ )  
and volatilities 4.4%, 3.3% and 3.7% ( $\Sigma$ )

for A, B and C, pairs (A,B), (B,C)  
and (A,C), and triplet (A,B,C)  
with and without uncertainty

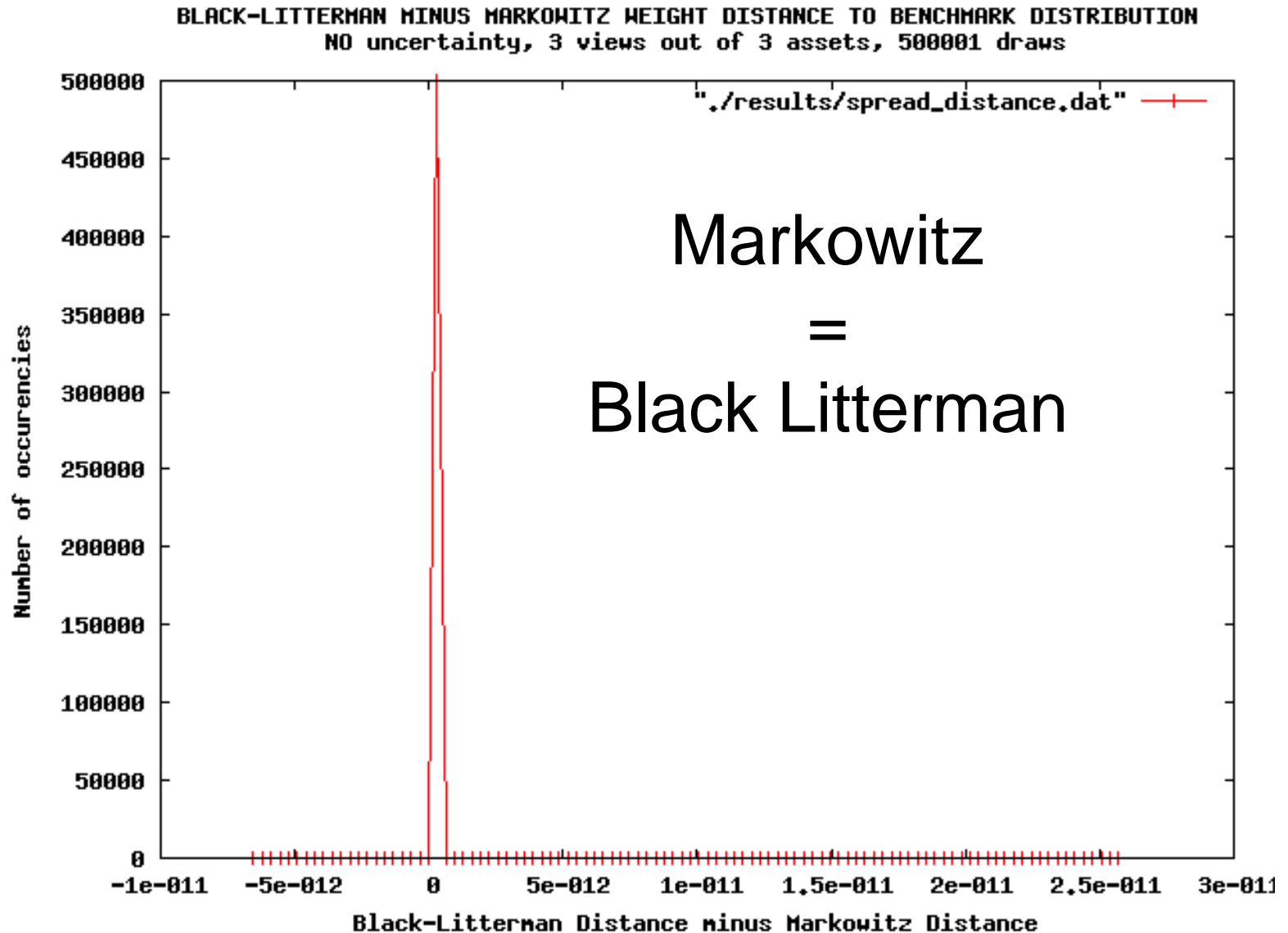
# Monte Carlo Approach



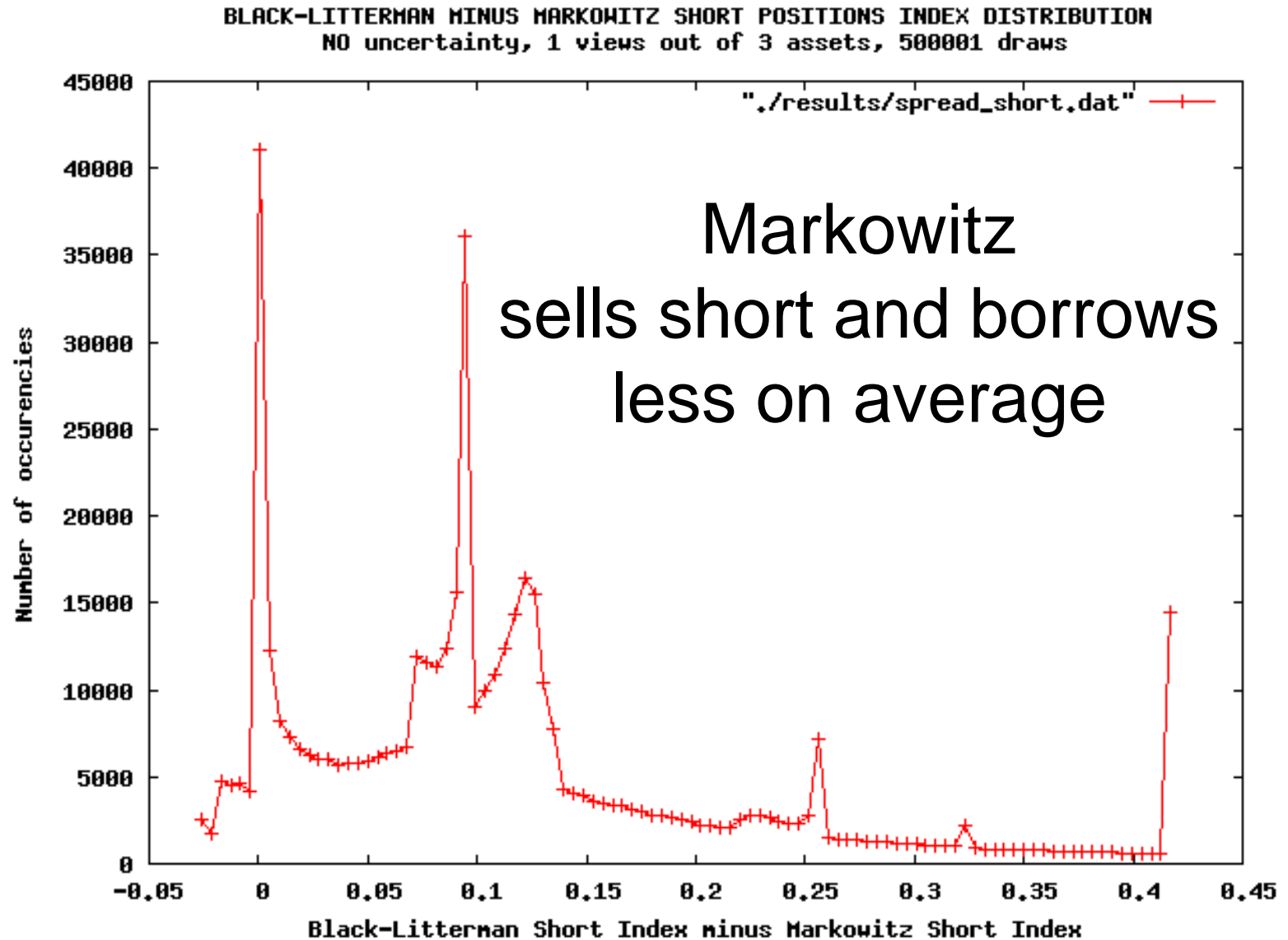
# Monte Carlo Approach



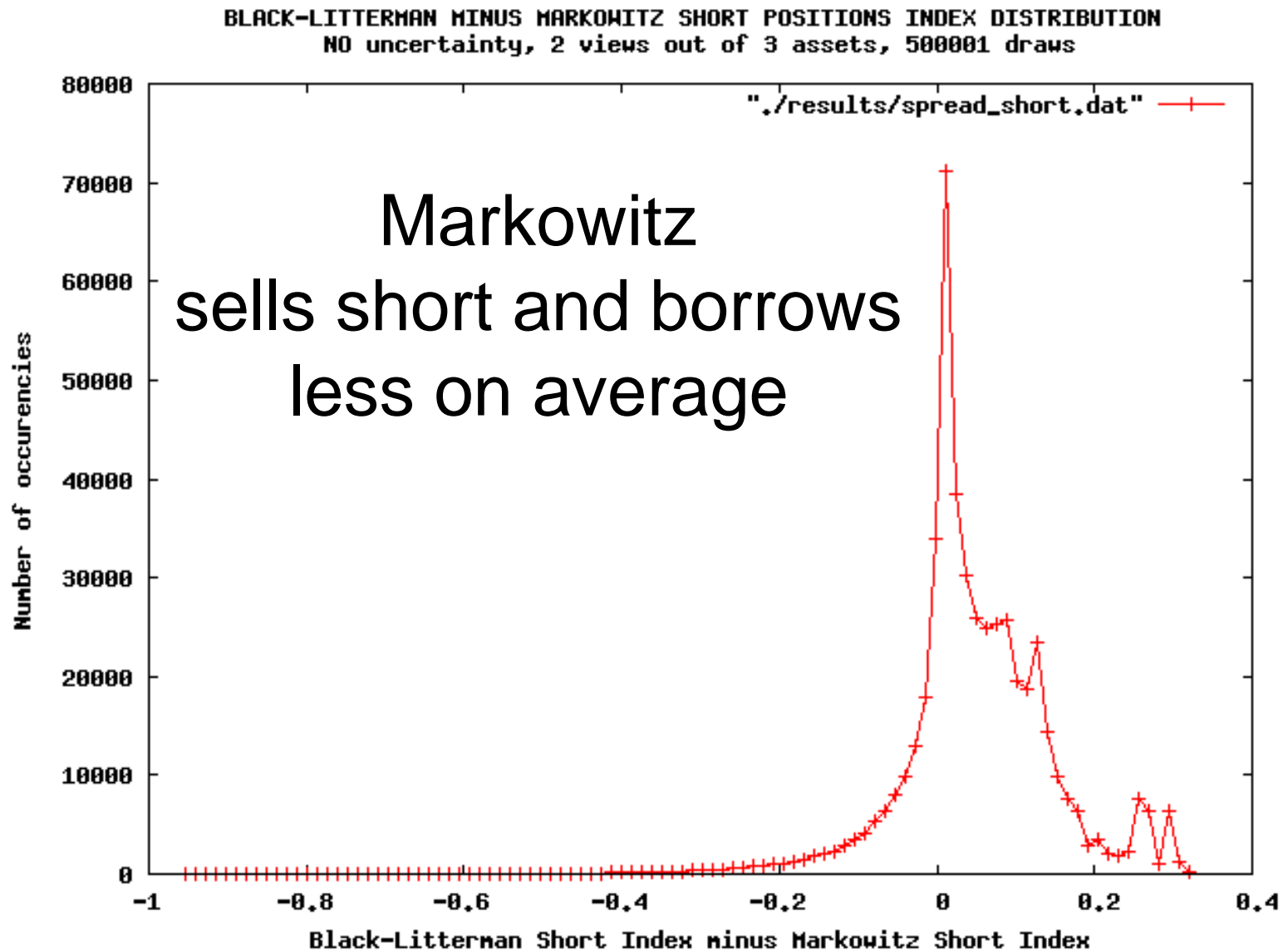
# Monte Carlo Approach



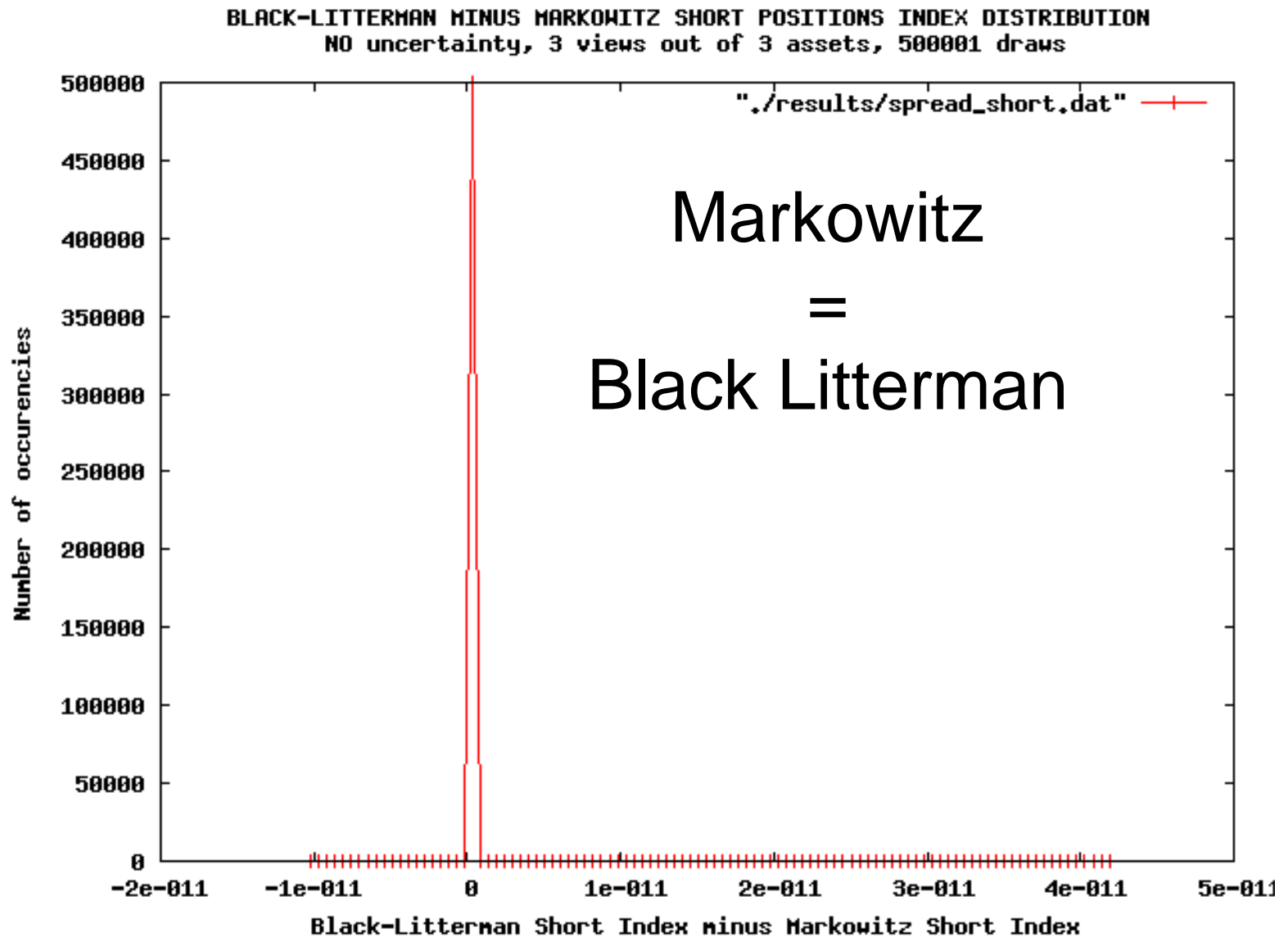
# Monte Carlo Approach



# Monte Carlo Approach



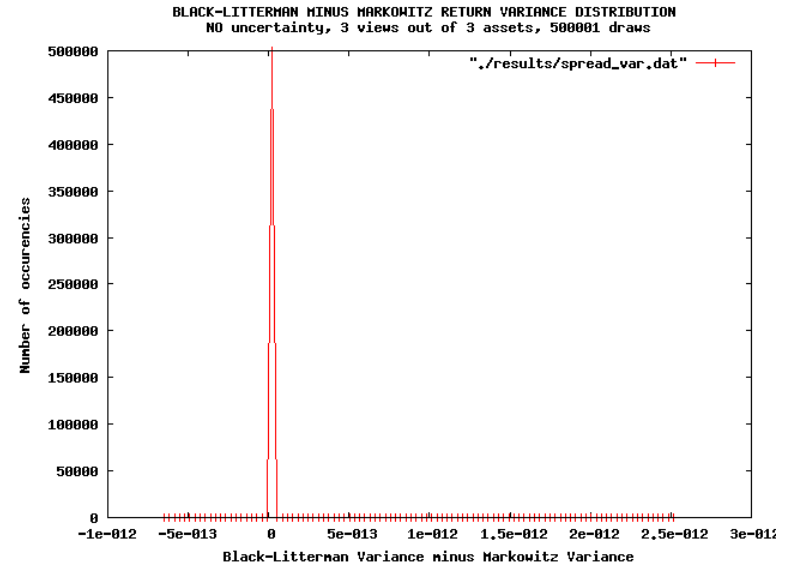
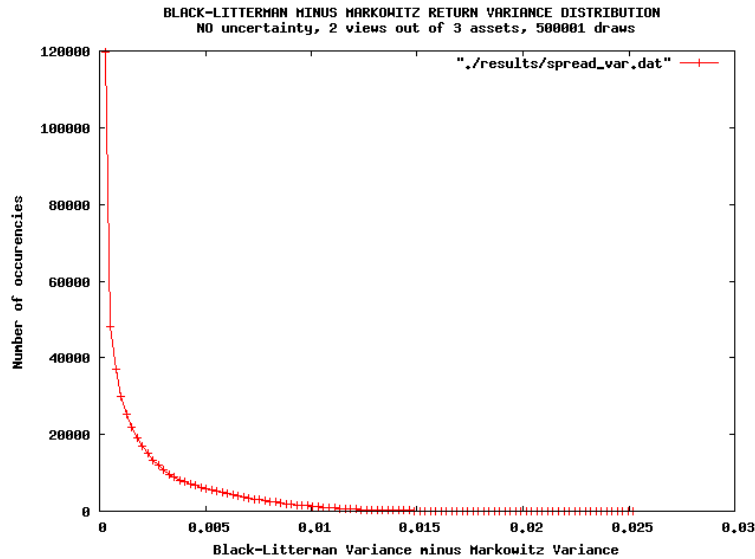
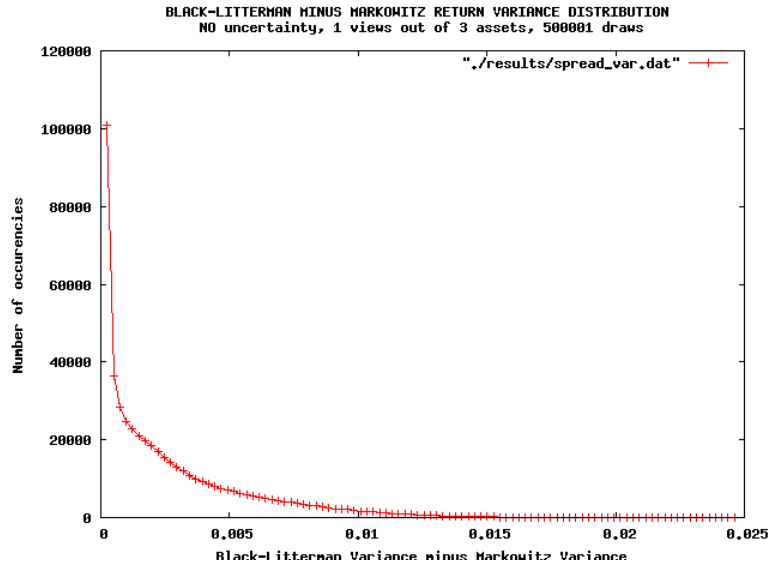
# Monte Carlo Approach





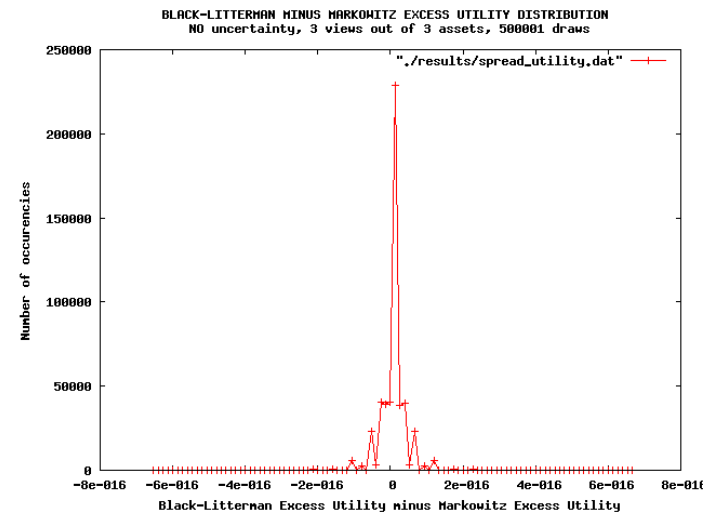
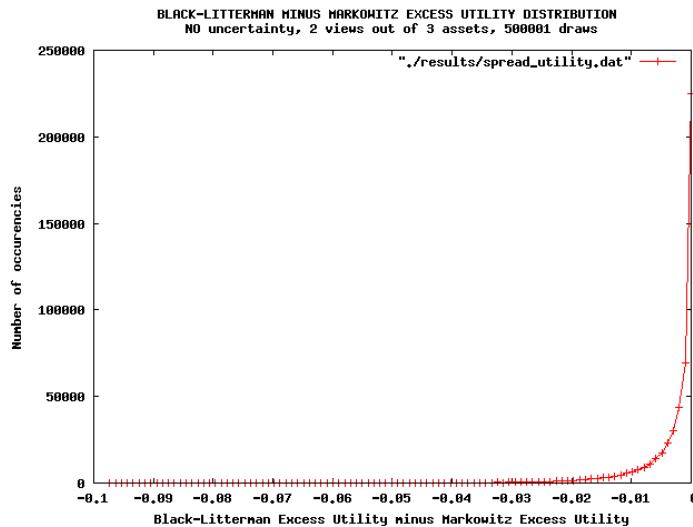
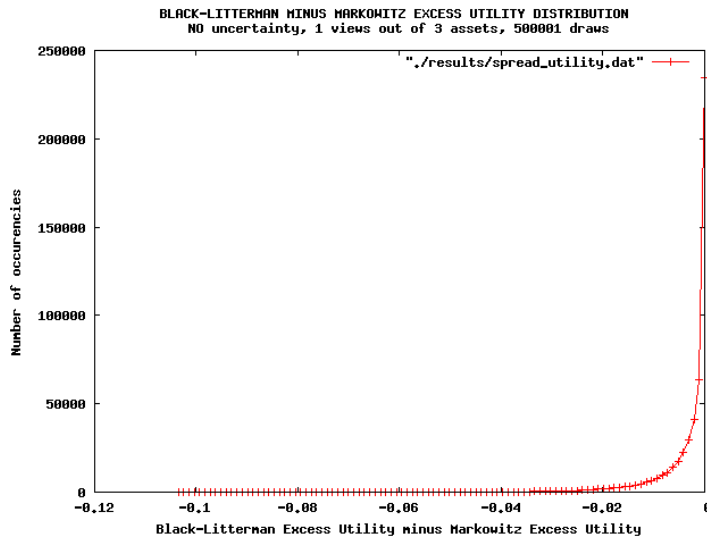
# Monte Carlo Approach

Return variance:  
Markowitz  
dominates  
Black-Litterman



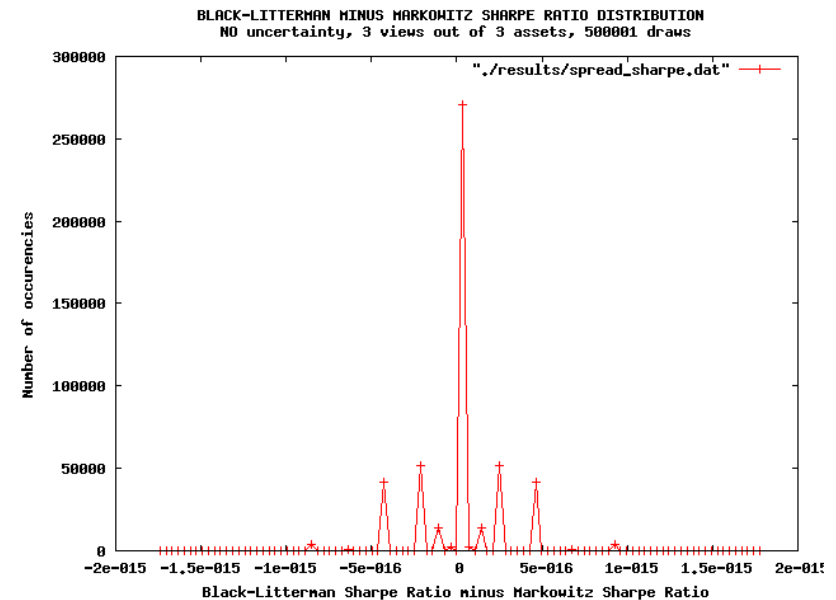
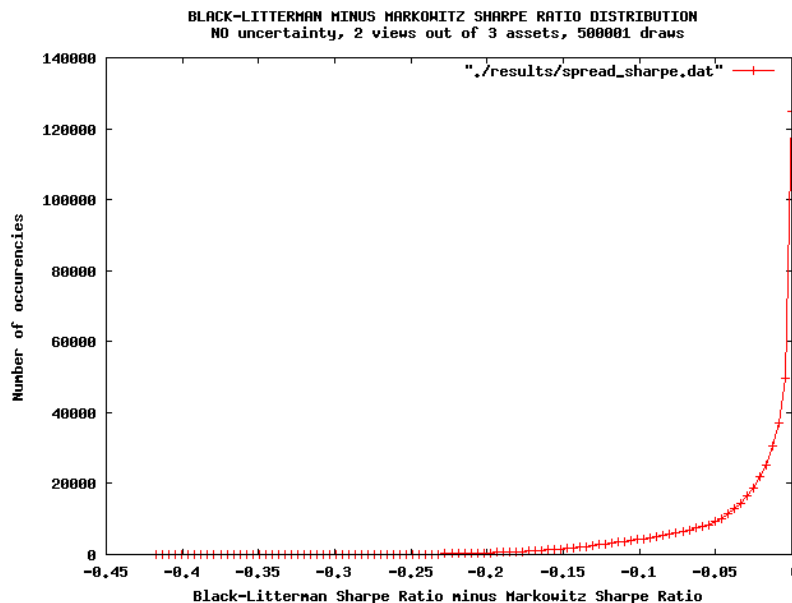
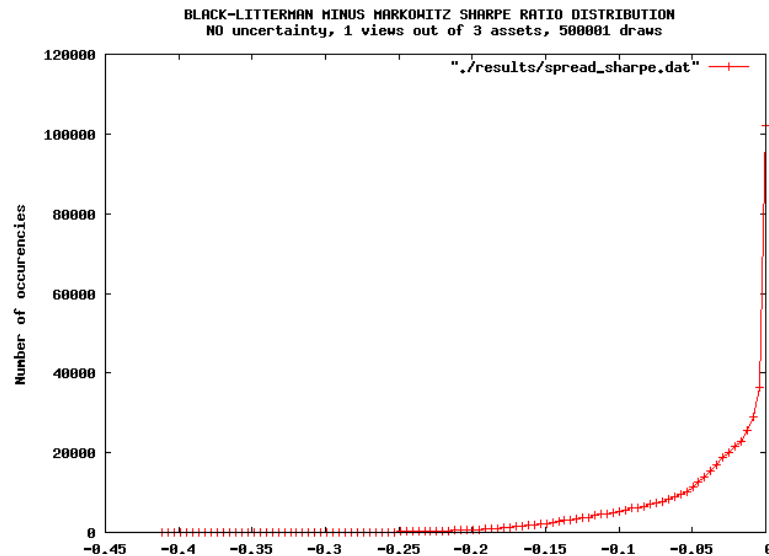
# Monte Carlo Approach

Utility:  
Markowitz  
dominates  
Black-Litterman



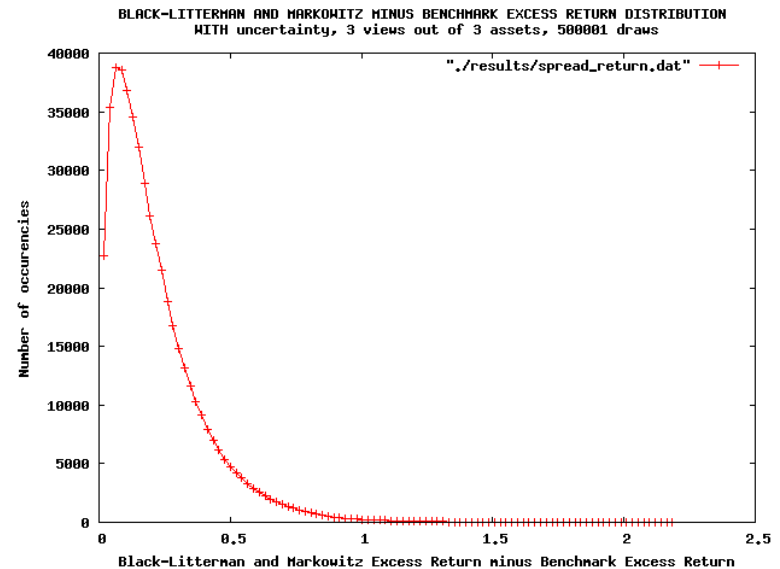
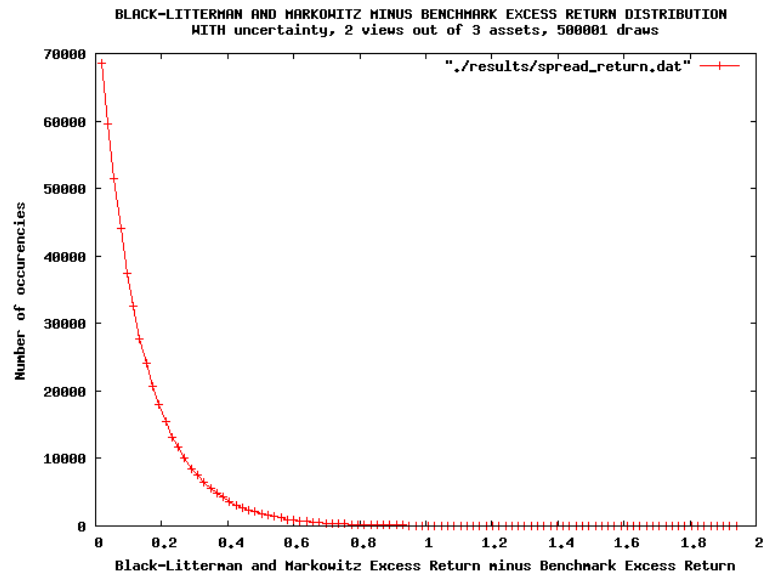
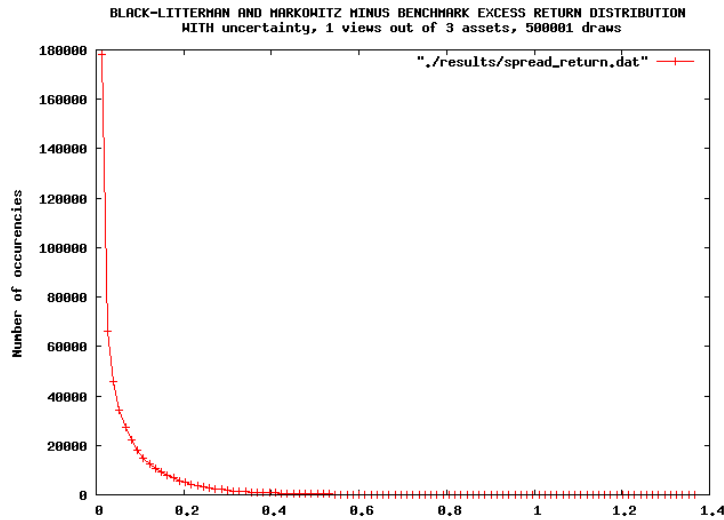
# Monte Carlo Approach

Sharpe ratio:  
Markowitz  
dominates  
Black-Litterman

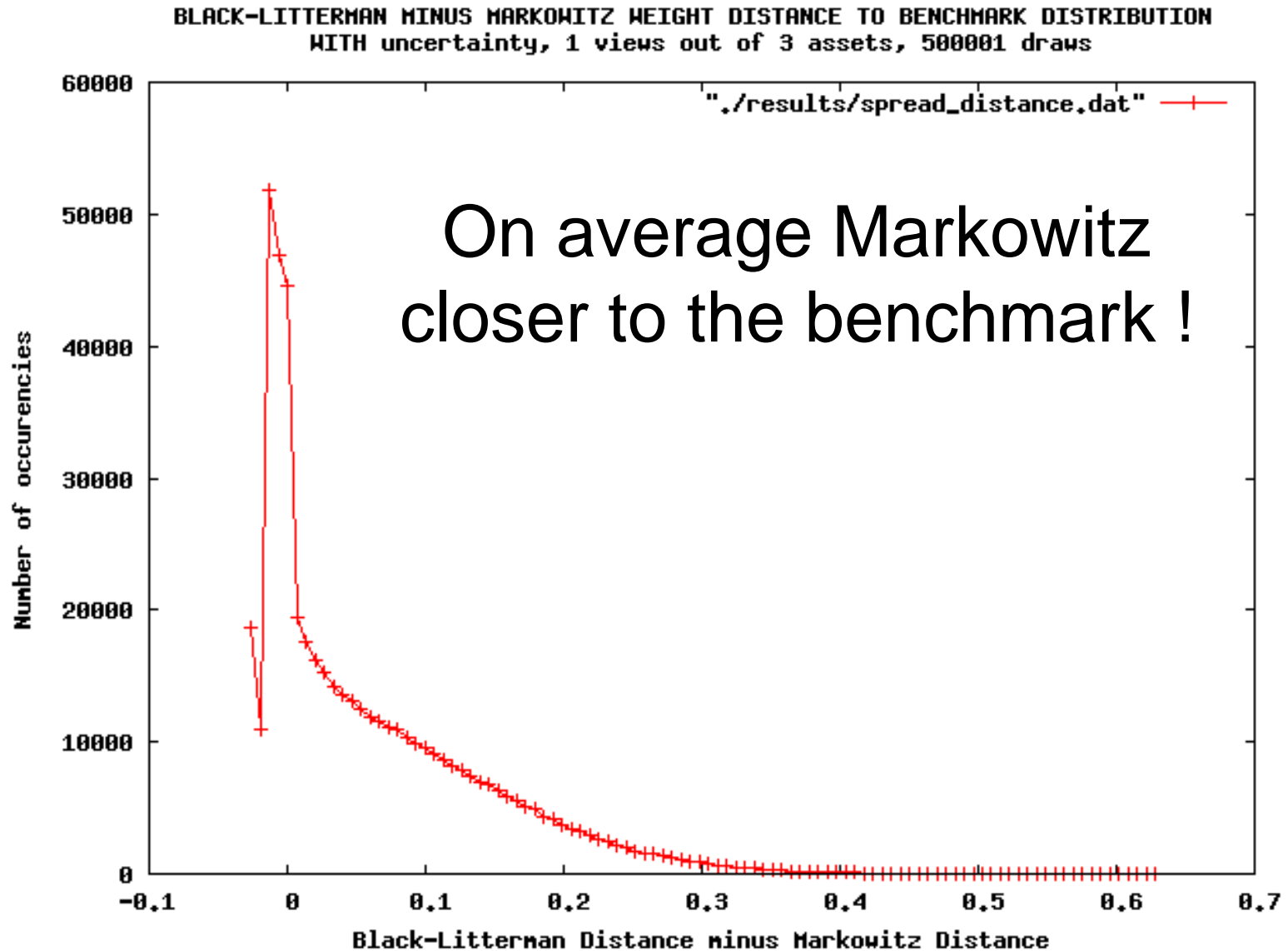


# Monte Carlo Approach

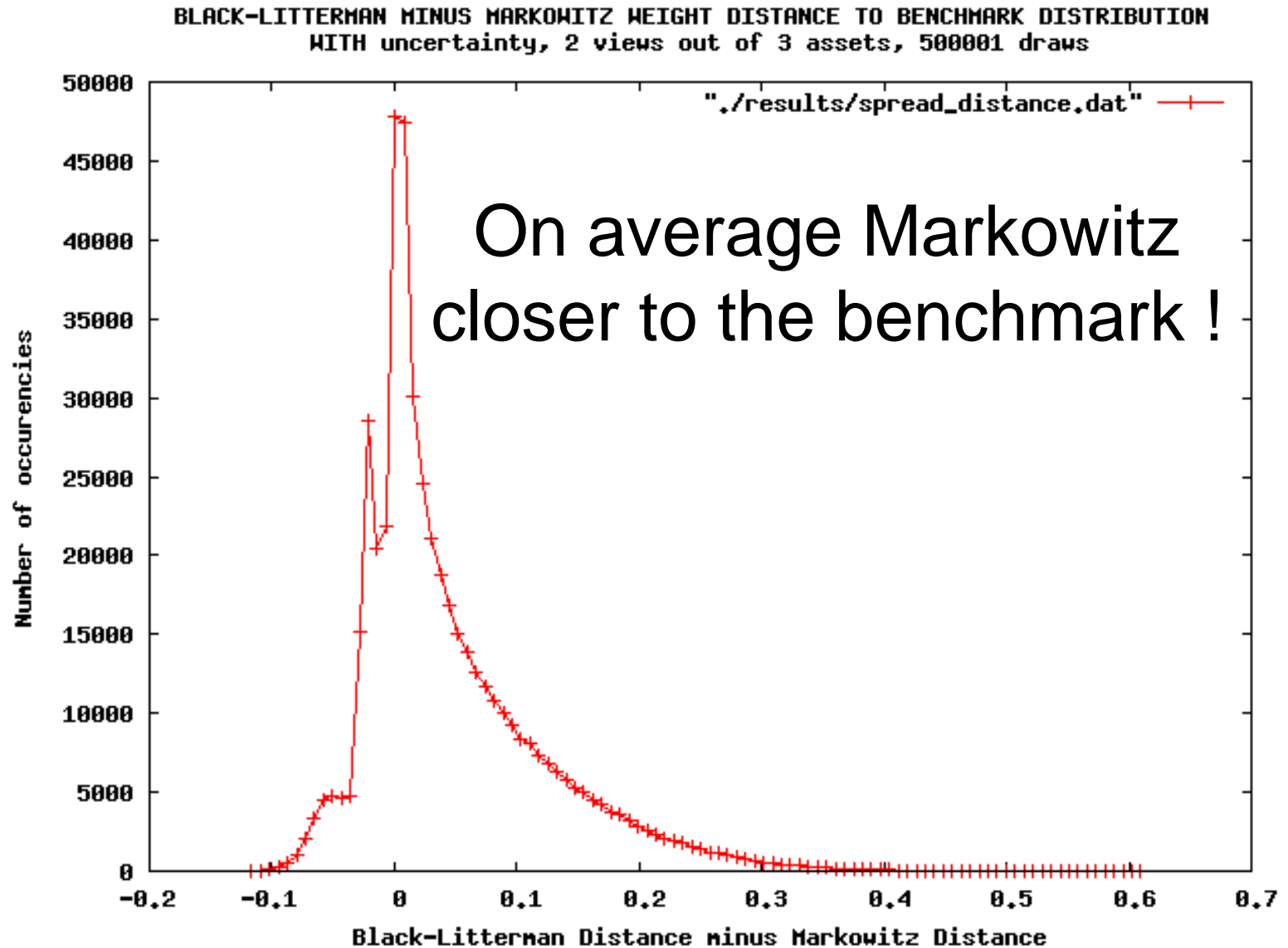
Now with uncertainty in  
views:  
Same dominance



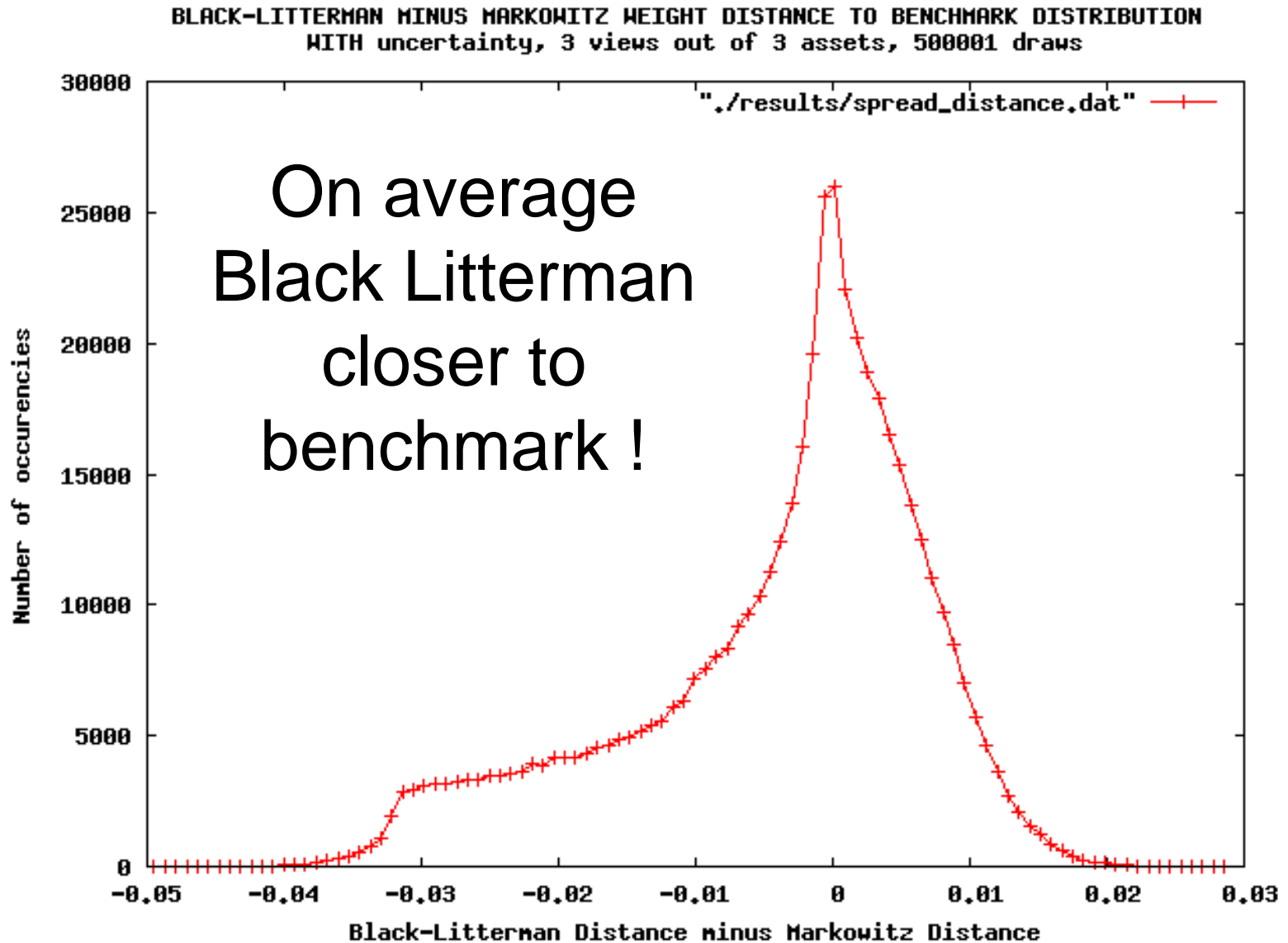
# Monte Carlo Approach



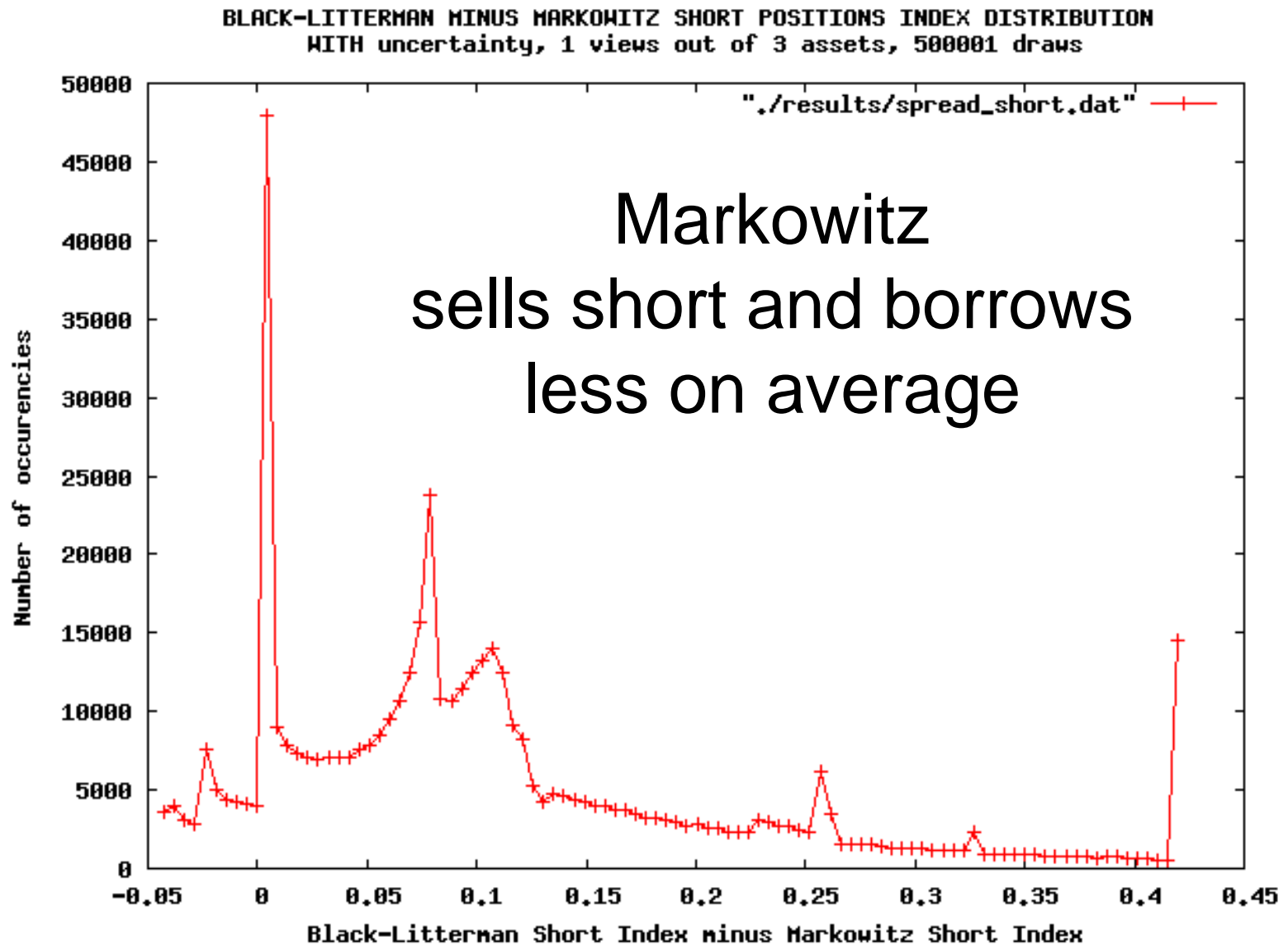
# Monte Carlo Approach



# Monte Carlo Approach

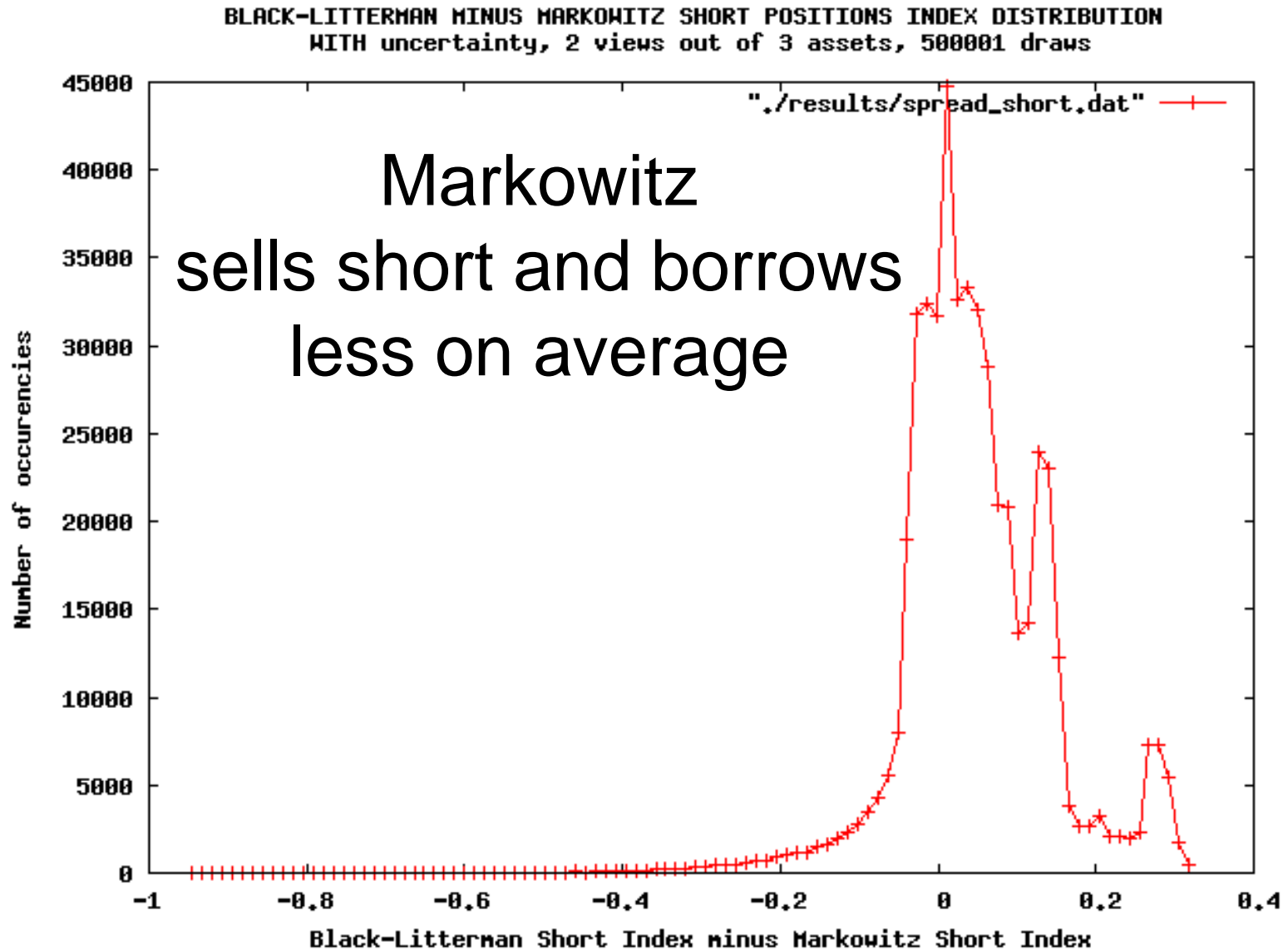


# Monte Carlo Approach

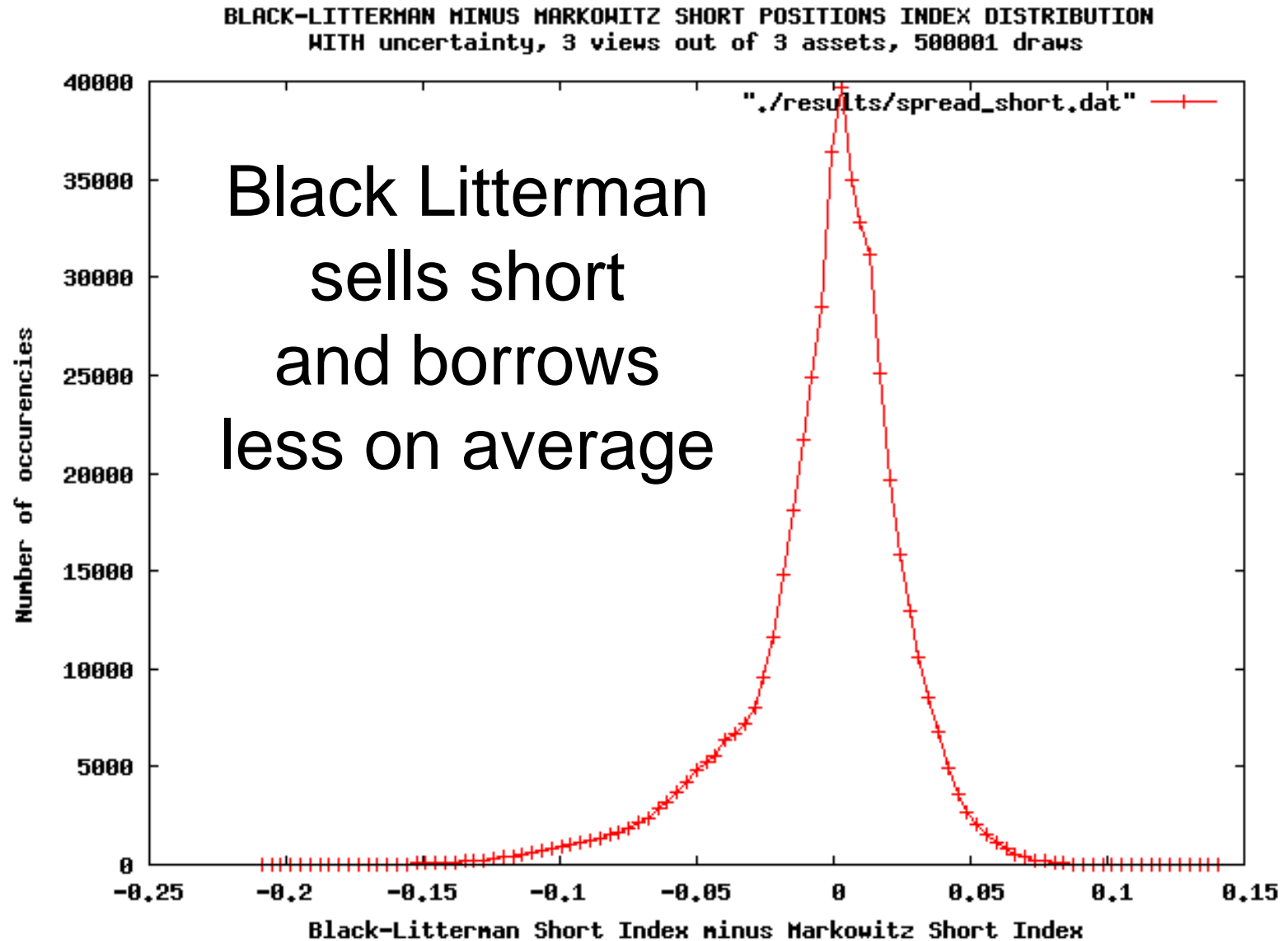




# Monte Carlo Approach

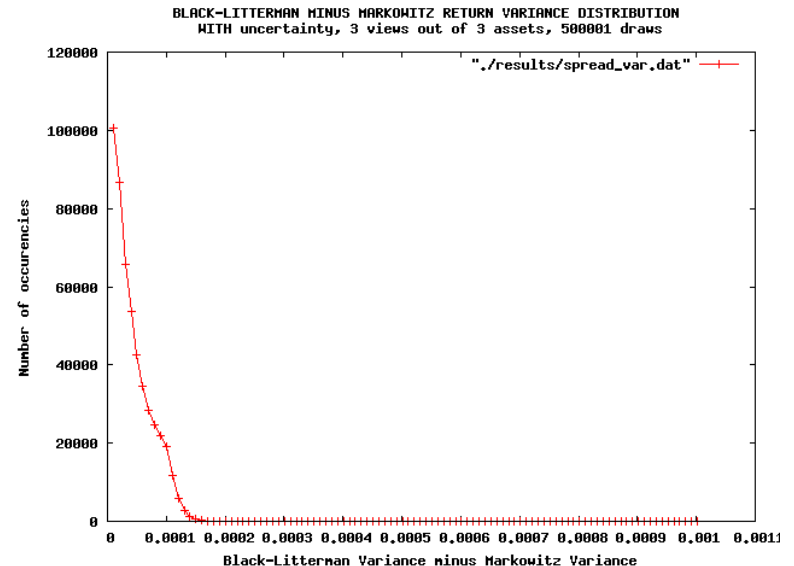
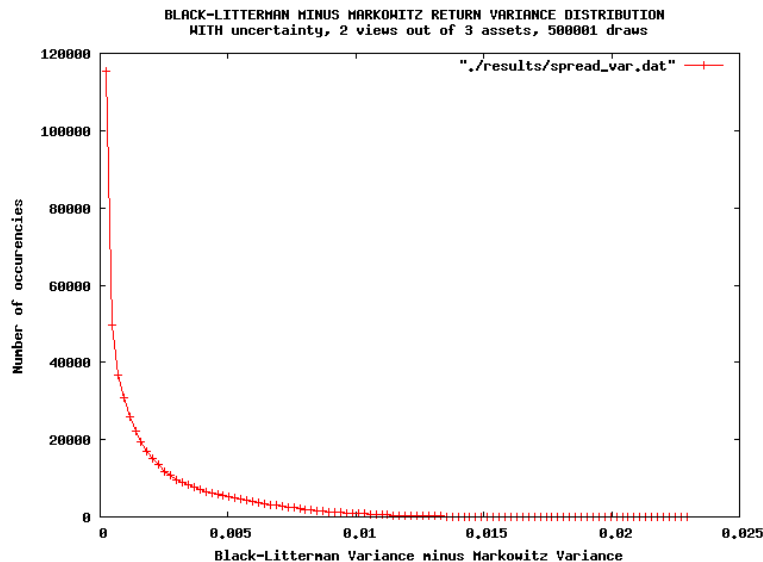
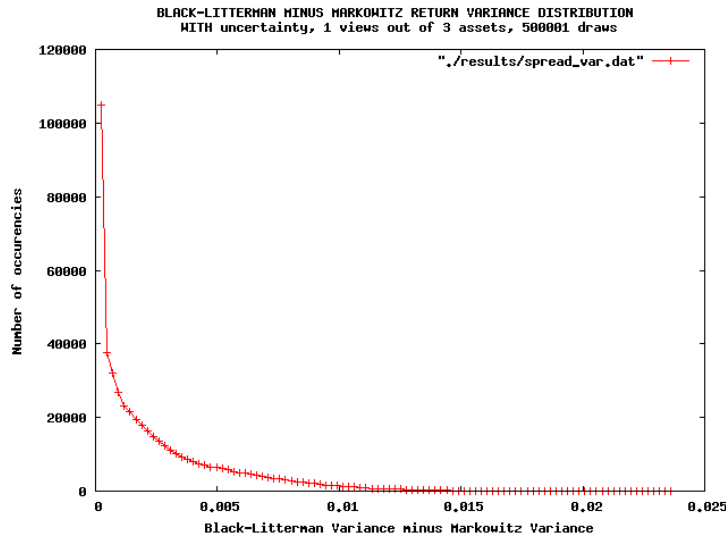


# Monte Carlo Approach

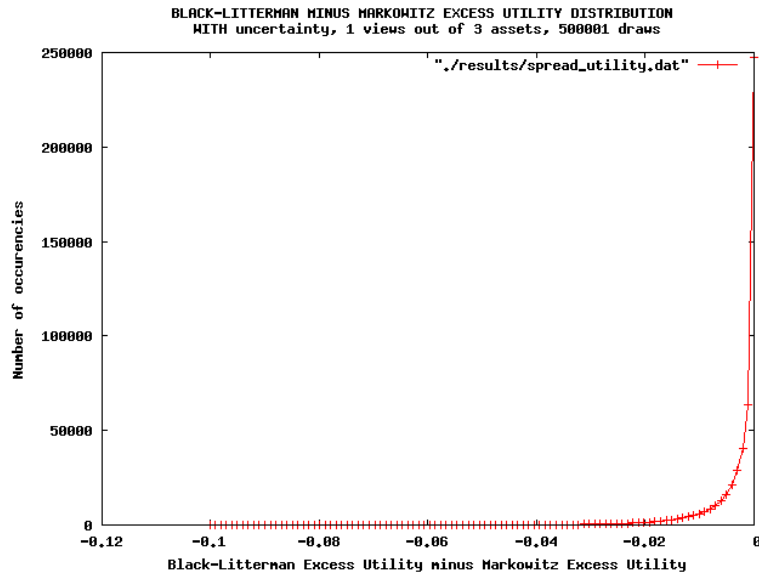


# Monte Carlo Approach

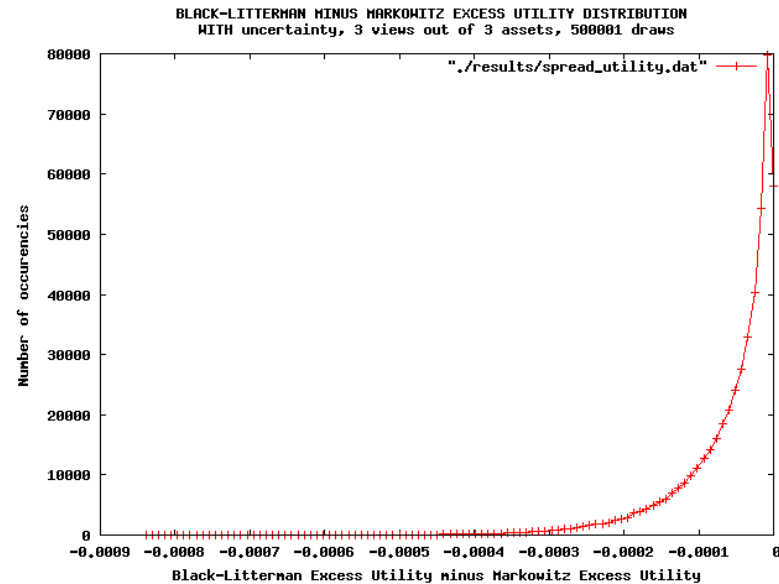
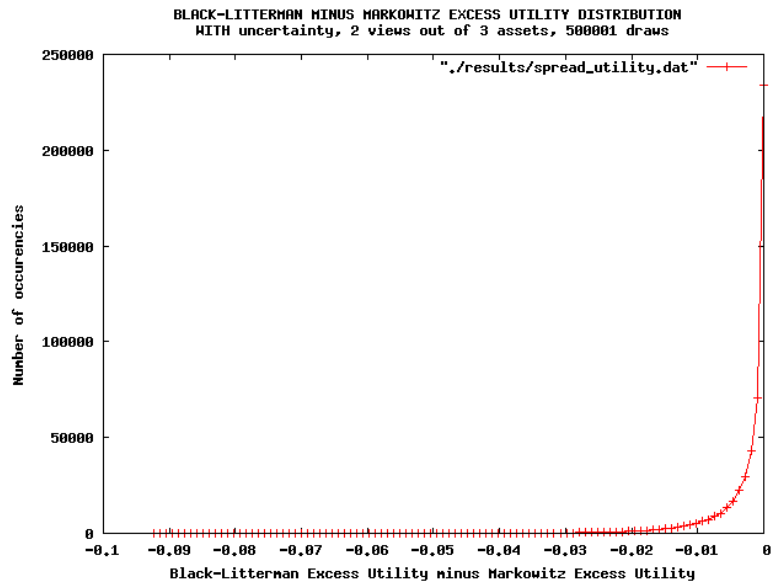
Now with uncertainty in  
views:  
Same dominance



# Monte Carlo Approach

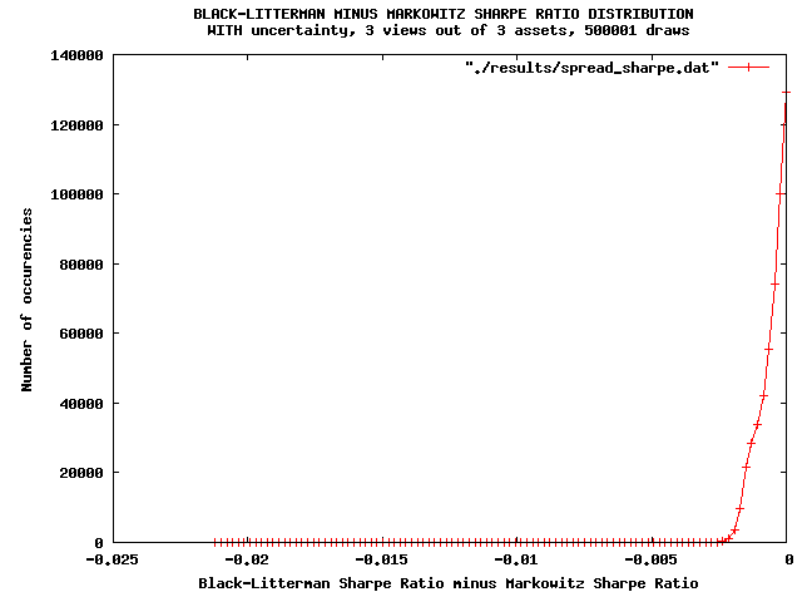
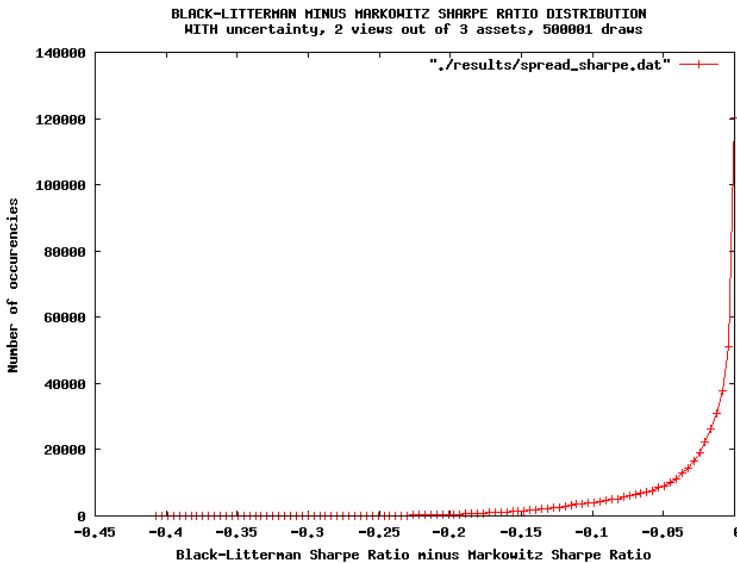
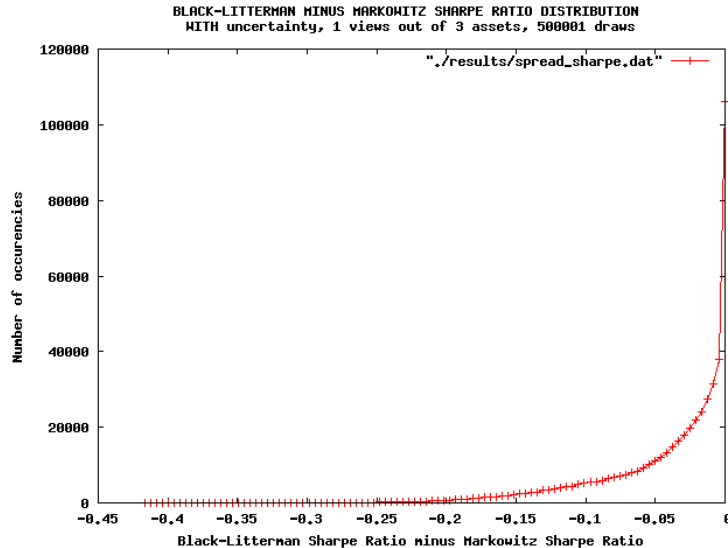


Now with uncertainty in  
views:  
Same dominance



# Monte Carlo Approach

Now with uncertainty in  
views:  
Same dominance



# Conclusion

- **Big surprise:** on average Black Litterman beaten by Markowitz from weighing stability standpoint !

despite favorable  $\delta$  (= 15)

- Has **only average modest advantage** when all assets are forecasted
- In all cases **risk, Sharpe and utility deterministic dominance by Markowitz**

# Further Research

Heuristic analysis of the performance of the  
risky component of BL solution portfolio