Mission 4: Curve Introduction

Start date: 2 September 2017 Due: 5 September 2017, 23:59

Readings:

• Textbook Sections 1.1.5 to 1.1.8

Drawing Curves

A curve is a basic drawing element. Complex pictures can be obtained by drawing multiple curves. A curve is a unary function which takes one real argument within the unit interval [0,1] and returns a point (a pair of real numbers).

Intuitively, the real argument to a curve can be thought of as time, and the point returned by the curve can be thought of as the position of the pen at the time indicated by the argument. We represent curves by functions of Source type Curve, where

```
Curve: Number -> Point
```

and Point is some representation of pairs of Numbers. If C is a curve, then the starting point of the curve is always C(0), and the ending point is always C(1).

To work with Points, we need a *constructor*, make_point, which constructs Points from Numbers, and selectors, x_of and y_of, for getting the x and y coordinates of a Point. We require only that the constructors and selectors obey the rules

```
}
var unit_line = unit_line_at(0);
```

Drawing Functions

In the previous section we introduced the concept of curve as the basic drawing unit. However, in order to actually draw a curve on the window, you will need a drawing function. It is not required that you understand the implementation of the drawing functions, but you should know how to use them in order to visualize and test your solutions.

When you begin your mission, you should see an empty Canvas.

In the Interpreter, type:

```
(draw_connected(200))(unit_circle);
(draw_connected_squeezed_to_window(200))(unit_circle);
```

After the first draw statement, you will see a quarter circle, and after the second, a full circle. Note that all Curve functions accepted by the draw methods are of the form defined above:

```
Curve: Number -> Point
```

The 200 in draw_connected refers to the number of points to draw on the screen. Since 1/200 = 0.005, unit_circle will be called for values of t = 0, 0.005, 0.01, 0.015, 0.02, etc. until t = 1. draw_connected will then join two adjacent points returned by unit_circle to draw a connected Curve. If you want to draw the points without connecting them, use draw_points_on. The following is an example of how to use draw_points_on:

```
(draw points on(200))(unit circle);
```

Note that the origin of the drawing window is at the bottom-left. Moving right along the drawing window increases the value of the

x-axis until the x-coordinate equals 1. Likewise moving up along the window increases the value of the y-axis until the y-coordinate equals 1. This is why draw_connected shows only a quadrant of the unit_circle, since for some values of t, the x- and y-coordinates are outside the range [0, 1]. For example, try:

```
unit circle(0.5);
```

The y-coordinate of -1.0 is outside the range [0, 1] and hence cannot be displayed. Another function, draw_connected_squeezed_to_window, takes care of this by scaling and translating the Curve as required so that all points fall in the range [0, 1] for both axes.

More on Drawing Curves

Now that you have learnt the basics on how to visualise curves on the window, Grandmaster Martin would like you to take your drawing skills to the next level. There are other drawing

functions, listed as follows:

- 1. draw_points_on
- 2. draw_connected
- 3. draw_points_squeezed_to_window
- 4. draw_connected_squeezed_to_window

The differences between these functions are suggested by their names. They are used in a similar way. For example, to draw the pre-defined curve unit_circle on the window using 200 points, you may call:

```
(draw_points_on(200))(unit_circle);
In order to draw a connected curve, you may use:
  (draw_connected(200))(unit_circle);
If you want to make the curve fit in the current window, you may use:
  (draw_connected_squeezed_to_window(200))(unit_circle);
```

Note that the more points you use, the more accurately the curve will be drawn.

This mission has **three** tasks. **Link to template.** Fill up your answers on the template for submission. Also ensure that you using the curve tab on the top-right hand corner. Fill up your answers on the template for submission. Also ensure that you using the curve tab on the top_right hand corner.

Please stick to the old playground at http://128.199.210.247/playground for now.

Task 1:

};

}

Recall the definition of unit_line_at:
function unit_line_at(y){
 return function(t){

return make point(t, y);

1. What is the type of unit line at?

Hint: The format for expressing a type and an example is shown below:

```
<function> : <argument-type>[, ...] -> <return-type>
make point : (Number, Number) -> Point
```

- 2. Define a function vertical_line which takes two arguments, a point and a length, and returns a vertical line of that length beginning at that point. Note that the line should be drawn upwards (i.e., towards the positive-y direction) from the point.
- 3. What is the type of vertical line?

4. Using draw_connected and your function vertical_line with suitable arguments, draw a vertical line in the drawing window which is centered horizontally and vertically and has half the length of the sides of the drawing window.

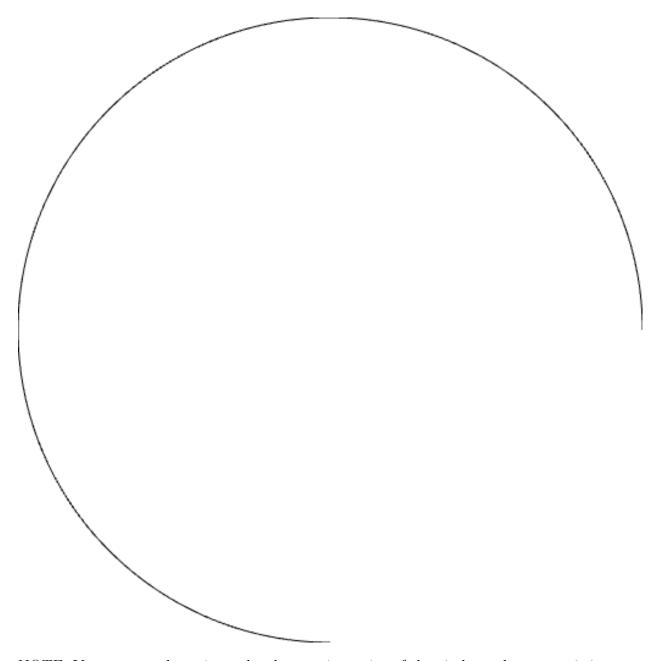
Task 2:

Define a function three_quarters that takes in a point as a parameter and returns a curve that is a 3/4 circle, i.e. three_quarters :(Point) -> Curve

Only the bottom-right quadrant of the circle will have no points. An example is shown below.

Applying draw_connected_squeezed_to_window(200) to three_quarters at some point make point(0.5, 0.25) as follows:

(draw_connected_squeezed_to_window(200))(three_quarters(make_point(0.5, 0.25))); returns the following:



NOTE: You can use the point to be the starting point of the circle or the center, it is up to you. Just make sure when you draw it using draw_connected_squeezed_to_window we get the correct shape. Make use of the trigonometric functions and mathematical constants from the available math library. See Source Week 4 for more details.

Task 3:

Now that we have successfully created a 3/4 circle, define a function s_generator that takes in a point and returns a curve creating an S shape, i.e. s_generator: Point -> Curve. An example is shown below. Also note that the radius of each half of the S is 1 and you do not need to reuse the three_quarters function for this task.

Applying draw_connected_squeezed_to_window(200) to s_generator at some point make point(0.5, 0.25) as follows:

// (draw_connected_squeezed_to_window(200))(s_generator(make_point(0.5, 0.25)));

returns the following:

HINT: You can divide the problem into the 2 halves and find a way to connect the two together. Also note that you would have to draw the S in a continuous manner so you don't have jagged edges when drawing the connected version of the curve.

Submission

IMPORTANT: Make sure that everything for your programs to work is on the left hand side (Editor) and not in the Side Content! This is because only the programs in the Editor are preserved when opening the url you have emailed to us.